

Attacks on Lattice Crypto

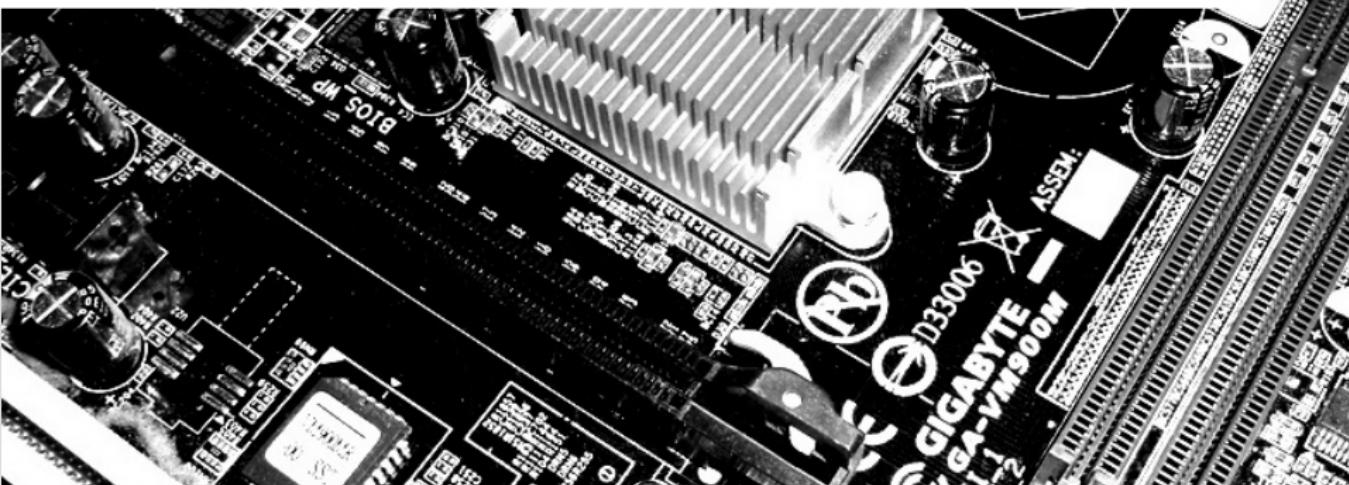
December 7th, 2016

FluxFingers

Workgroup Symmetric Cryptography

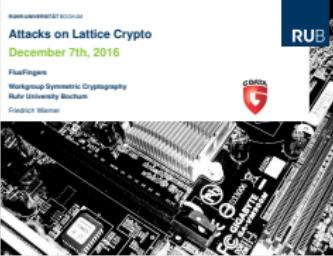
Ruhr University Bochum

Friedrich Wiemer



2016-12-07

Attacks on Lattice Crypto



Why is Lattice Based Crypto important?

Or interesting? Or...? Buzzword Bingo.



Some facts

- It is a Post-Quantum secure Cryptosystem (PQC)

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Attacks on Lattice Crypto

└ Why is Lattice Crypto important, interesting,...

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Encryption, Signatures, even Hash Functions!

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 - Fully Homomorphic Encryption (FHE),
 - Multi-linear Maps,
 - Identity-based Encryption (IBE),
 - ...

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Why is Lattice Based Crypto important?

Is everything done?



Fully Homomorphic Encryption



GF(＼_(＼＼)＼＼)
@hdevalence

Follow

Kirchner/Fouque: our attack lets us do FHE faster by just breaking the crypto & decrypting eprint.iacr.org/2016/717.pdf

The parameters proposed for schemes using similar overstretched NTRU assumption, such as in homomorphic encryption [8, 31, 17, 18, 16, 12, 32, 20] or in private information retrieval [19], are also broken in practical time using LLL. For example, we recovered a decryption key of the FHE described in [17] in only 10 hours. For comparison, they evaluated AES in 29 h: that means that we can more efficiently than the FHE evalution, recover the secret, perform the AES evaluation, and then re-encrypt the result! A decryption key was recovered for [20] in 4 h. Other instanciations such as [11, 29] are harder, but within range of practical cryptanalysis, using BKZ with moderate block-size [13].

RETWEETS
33
LIKES
34



5:37 AM - 23 Jul 2016

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Why is Lattice Based Crypto important?
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Fully Homomorphic Encryption

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RETWEETS 33 LIKES 34

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The new cool kid in town.



What is this Hype?

- “Lattice based Crypto is one of the most promising PQC candidates blablabla” (almost every paper on lattices)

Attacks on Lattice Crypto

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Everything was fine. And then Shor entered the stage...

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A cryptographic thriller



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A cryptographic thriller



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A cryptographic thriller

- ... and published an efficient CVP quantum algorithm [ES16]
- for one day the cryptographic community was shocked!



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- but still, Google stopped its PQ key exchange experiment with New Hope [Gooa]



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Enough motivation!

How does Lattice Crypto work?

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Attacks on Lattice Crypto

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How does Lattice Crypto work?

How does Lattice Based Crypto work?

Wait! Lattice, wtf?



Definition:

A lattice L is an discrete, additive, abelian subgroup of \mathbb{R}^n .

Attacks on Lattice Crypto

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Definition:

Let $b_1, b_2, \dots, b_d \in \mathbb{R}^n$, $d \leq n$ linear independent. Then the set

$$L = \left\{ v \in \mathbb{R}^n \mid v = \sum_{i=1}^d a_i b_i, a_i \in \mathbb{Z} \right\}$$

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Hey! You promised, this will be easy!

Lattice, dt.: Gitter



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Attacks on Lattice Crypto

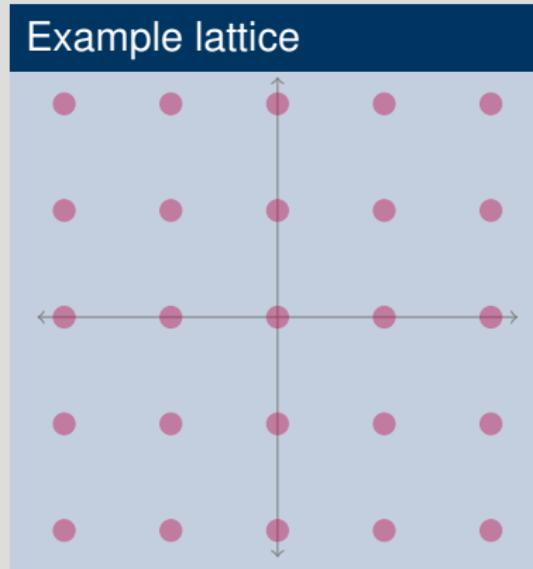
- └ How does Lattice Crypto work?

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Hey! You promised, this will be easy!

OK, OK, we can say it easier: \mathbb{Z}^2 is a Lattice



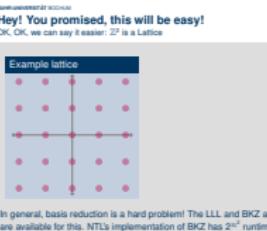
In general, basis reduction is a hard problem! The LLL and BKZ algorithm are available for this. NTL's implementation of BKZ has 2^{n^2} runtime.

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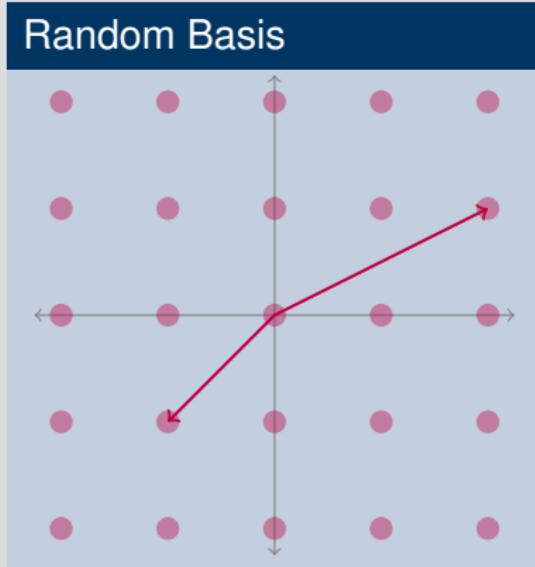
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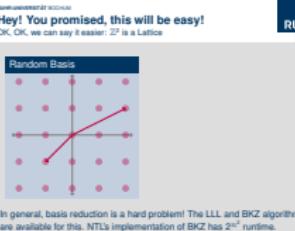
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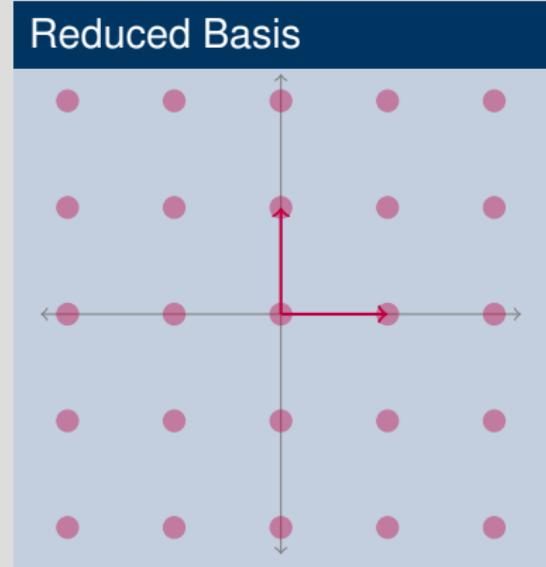
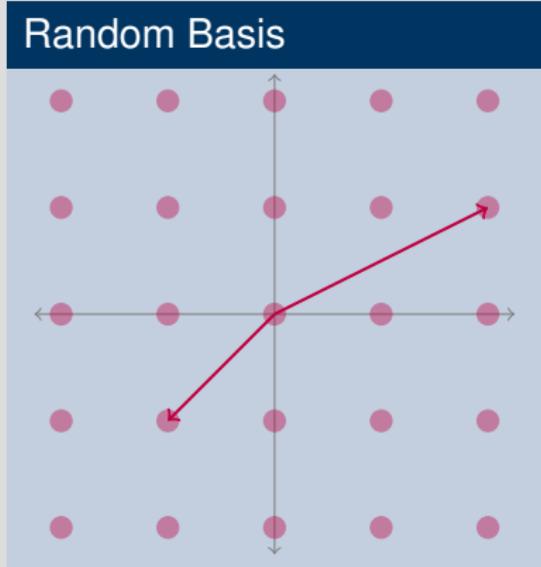
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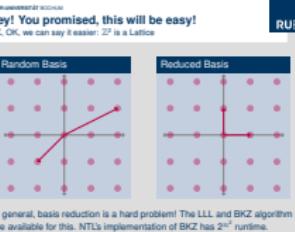
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Hard Problems in Lattices...

...are what we need for crypto.

Shortest Vector Problem (SVP)

Given a lattice L , what is the shortest vector $v \in L \setminus \{0\}$?

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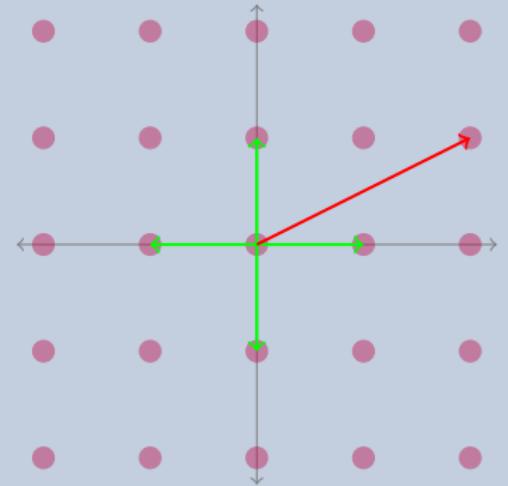
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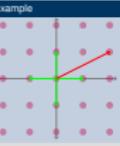
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Example



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2016-12-07 Attacks on Lattice Crypto
└ How does Lattice Crypto work?
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Closest Vector Problem (CVP)
Given a lattice L and a target $t \notin L$,
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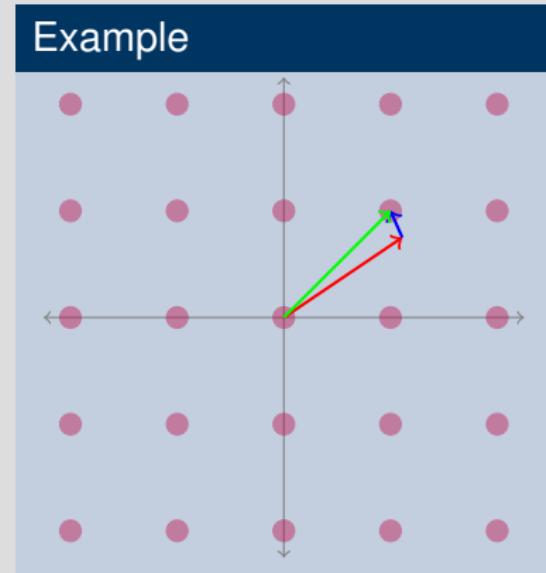
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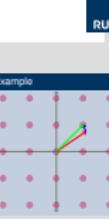
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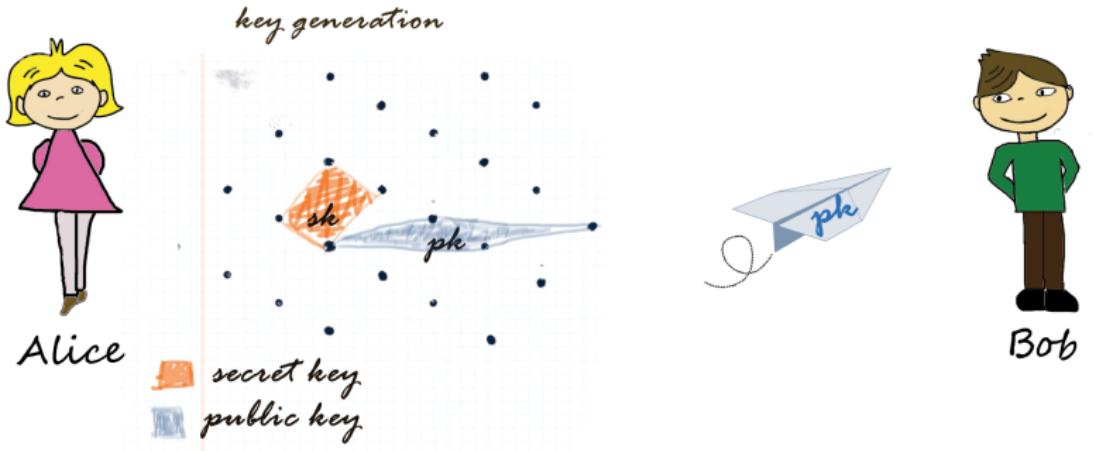
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Lattice Based Crypto

Learning With Errors – or: the equivalent to textbook RSA

Key Generation¹



¹Thanks to Elena for the nice pictures.

Attacks on Lattice Crypto

- └ How does Lattice Crypto work?
- └ Lattice Based Crypto

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Lattice Based Crypto
Learning With Errors – or: the equivalent to textbook RSA
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Key Generation¹

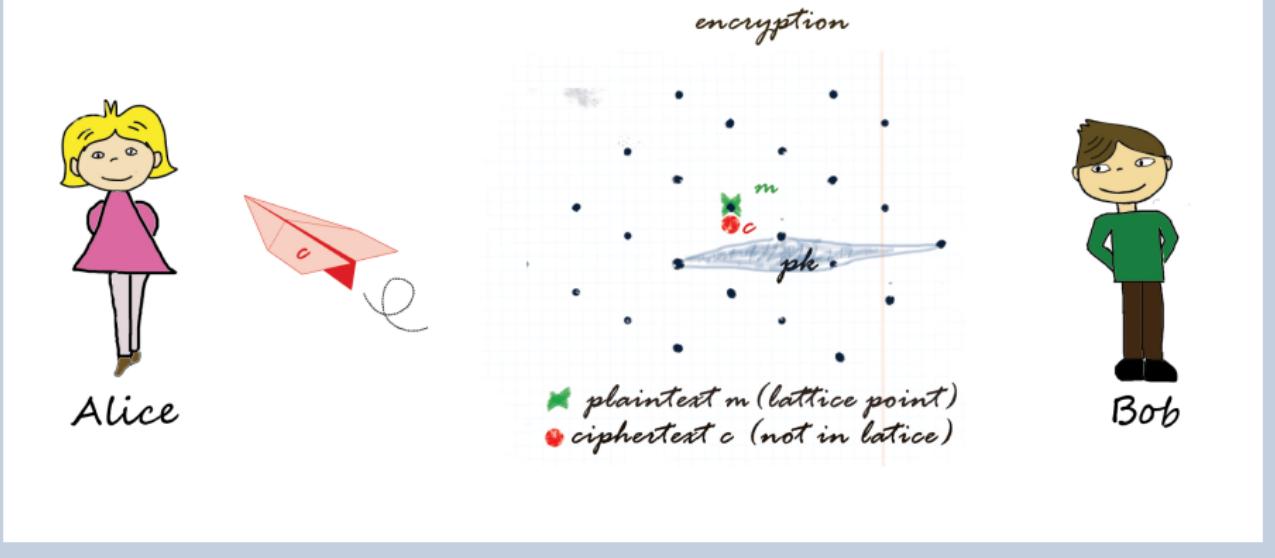
Alice secret key public key Bob

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Lattice Based Crypto

Learning With Errors – or: the equivalent to textbook RSA

Encryption



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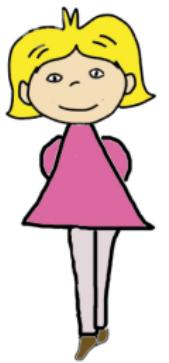
- Attacks on Lattice Crypto
 - └ How does Lattice Crypto work?
 - └ Lattice Based Crypto

A screenshot of a presentation slide titled "Encryption". The slide features two cartoon characters, Alice and Bob, and a 2D grid representing a lattice. A green dot labeled "plaintext m (lattice point)" and a red dot labeled "ciphertext c (not in lattice)" are shown. A blue shaded region labeled "pk" represents the public key. The slide is part of a larger presentation titled "Attacks on Lattice Crypto" and includes the subtitle "Learning With Errors – or: the equivalent to textbook RSA". The RUB logo is visible in the top right corner.

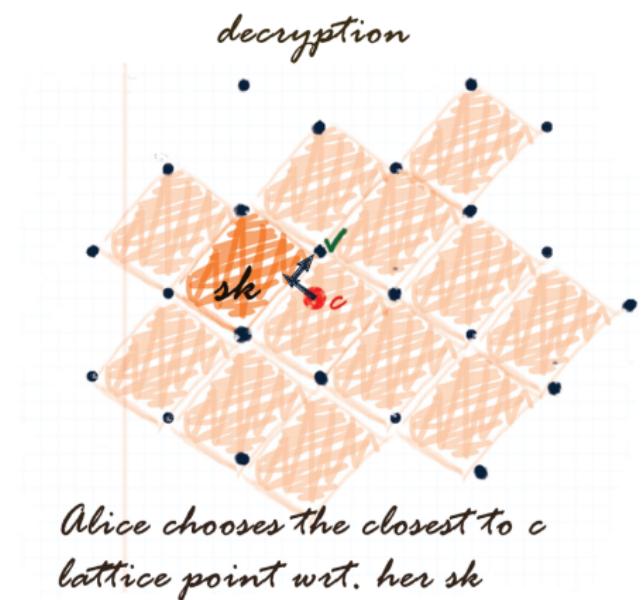
Lattice Based Crypto

Learning With Errors – or: the equivalent to textbook RSA

Decryption



Alice



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- Attacks on Lattice Crypto
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Lattice Based Crypto
Learning With Errors – or: the equivalent to textbook RSA

Decryption

Alice chooses the closest to c lattice point wrt. her sh

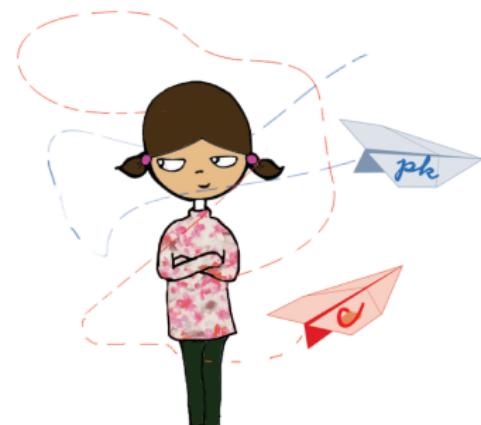
In practice most efficient strategy is Babai's Nearest Plane [Bab86], improved by Lindner and Peikert [LP11] and Gama *et al.* [GNR10].

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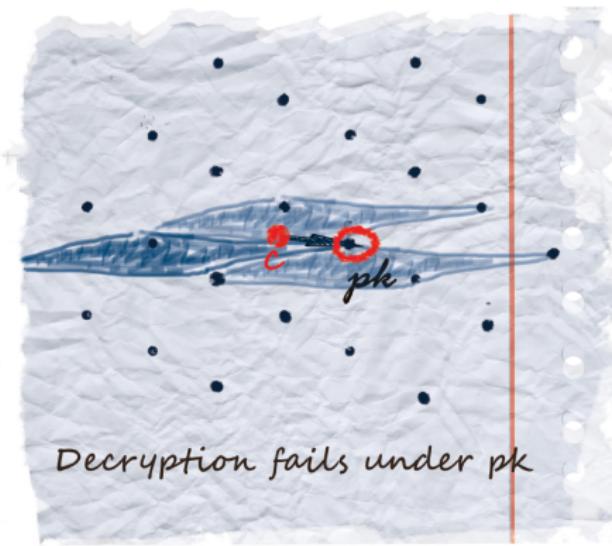
Attacks on Lattice Crypto
└ Attacks on Lattice Based Crypto
 └ Attack Algorithm

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Attack



Eve



Decryption fails under pk

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- Attacks on Lattice Crypto
 - Attacks on Lattice Based Crypto
 - Nearest Plane

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Nearest Plane
or BDD Enumeration

RUB

Attack

A small version of the Eve illustration from the main slide, showing her standing next to a crumpled paper diagram of a lattice. The text "Decryption fails under pk" is visible at the bottom right of the diagram.

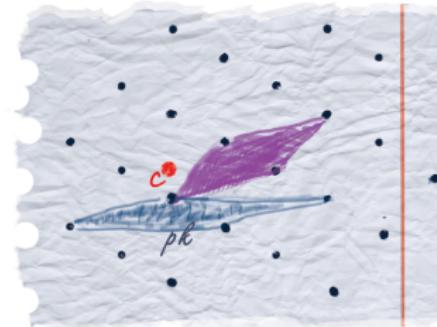
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Decryption fails under pk

Step 1: Basis Reduction



step1: Find an approximation to s_k



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- Attacks on Lattice Crypto
 - Attacks on Lattice Based Crypto
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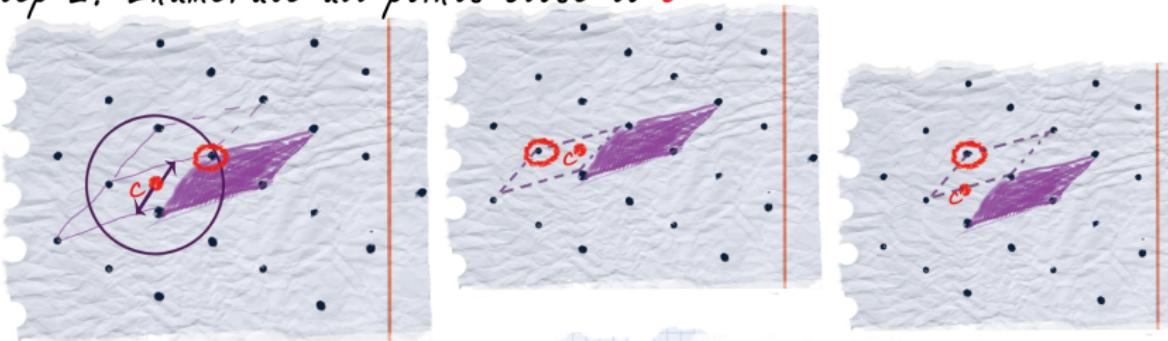
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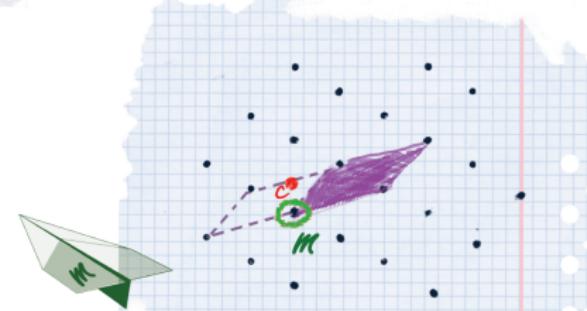
Nearest Plane or BDD Enumeration

Step 2: Enumerate Nearest Planes

step 2: Enumerate all points close to c



Eve



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 - Attacks on Lattice Based Crypto
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Nearest Plane
or BDD Enumeration

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Parallel Implementation of BDD enumeration for LWE

Finally, what we (joint work with Elena Kirshanova and Alex May) did:

Research Project

- Goal: What is the *practical* runtime of BDD enumeration?
- Build a parallel implementation of NearestPlanes.
- Test this on some large scale parallel system.
- Hopefully break some real world parameters.

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Attacks on Lattice Crypto

└ OK. And what did I do?

└ Parallel Implementation of BDD enumeration for LWE

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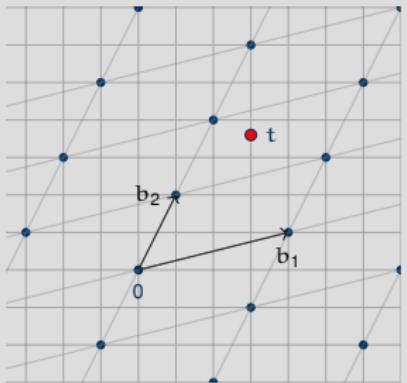
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Parallelisation of Enumeration

Elena's explanation



Closest point search via depth-first tree-traversal:



t

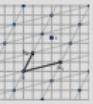
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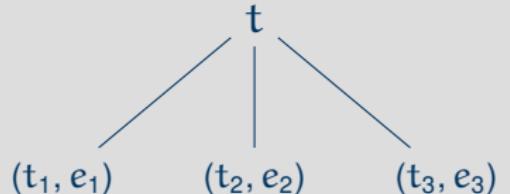
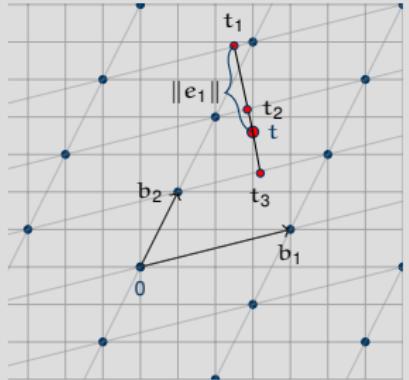
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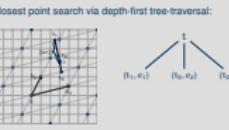


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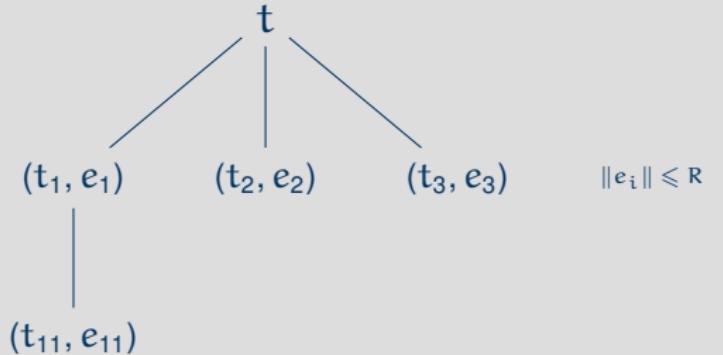
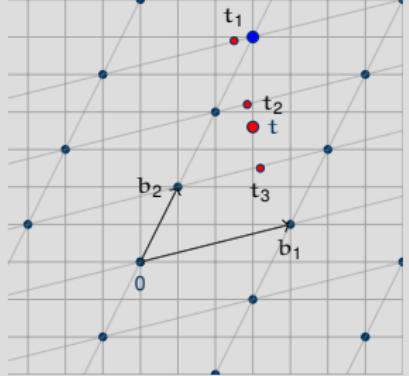
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- └ Parallelisation of Enumeration

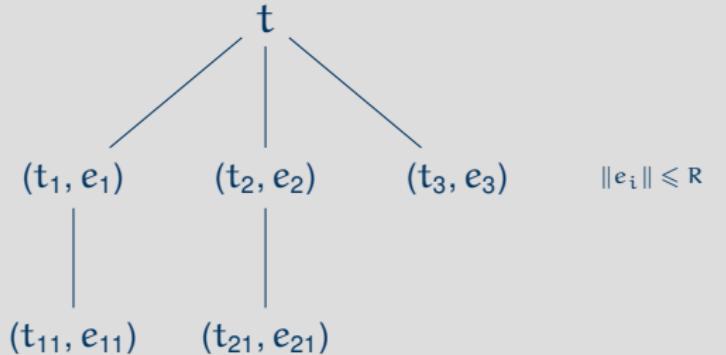
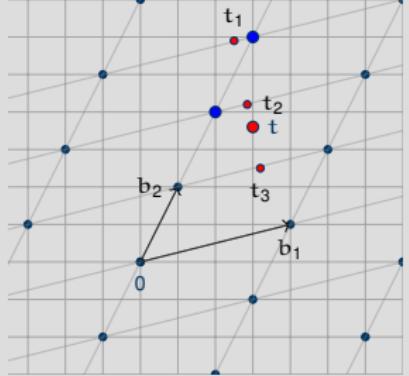
Closest point search via depth-first tree-traversal:



Parallelisation of Enumeration

Elena's explanation

Closest point search via depth-first tree-traversal:



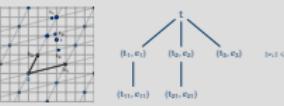
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- └ OK. And what did I do?

- └ Parallelisation of Enumeration

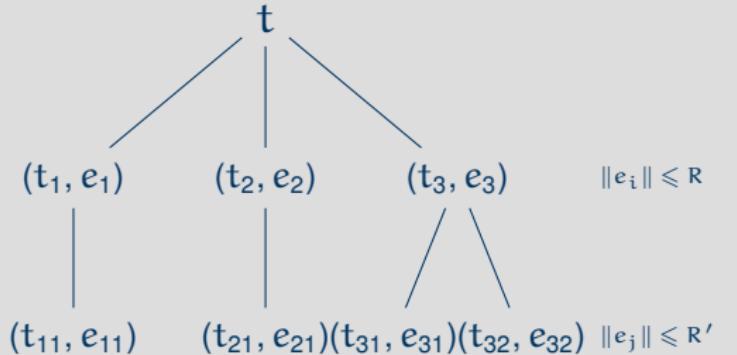
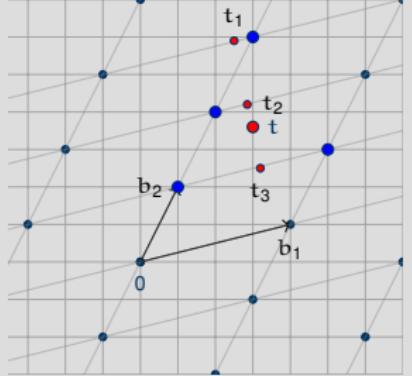
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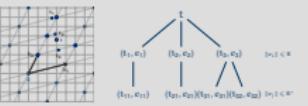
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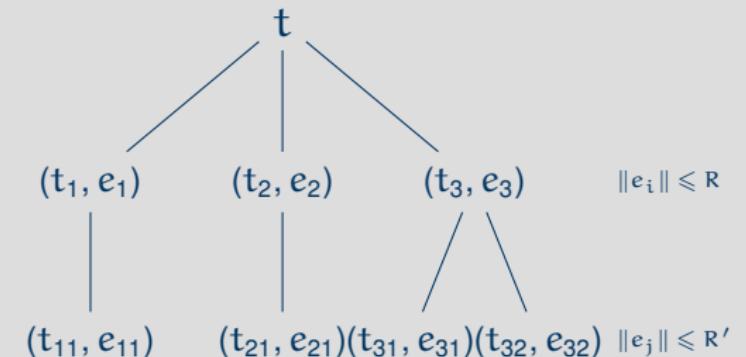
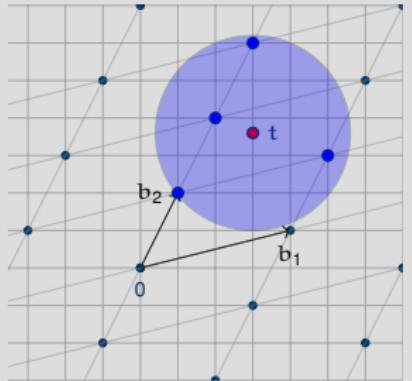
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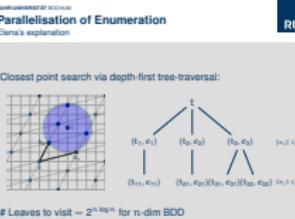
Leaves to visit = $2^{n \log n}$ for n -dim BDD

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Results



After more than one year of work, two submissions and something like over 9000 weeks of benchmarking

We ended up with:

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- an open source implementation:
<https://github.com/pfasante/cvp-enum>
- an ACNS paper [KMW16] and a Best Student Paper Award ☺
- huge table of runtimes

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Results: Numbers!



Standard LWE

LWE-parameters			BKZ-reduction	Enumeration	
n	q	$ e \leqslant$	T	# Threads	T
90	4093	10	11.3h	1	35h
90	4093	10	11.3h	10	3.6h
100	4093	10	7h	24	2.7h

To be compared with: ($n = 192, |e| < 18, q = 4093$) reaches 2^{87} -security level [LP11].

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LWE variant: Small secret

LWE-parameters			BKZ-reduction		Enumeration	
n	q	m	T	# Threads	T	
140	16411	170	12h	1	16h	
140	16411	170	12h	10	1.7h	

To be compared with: ($n = 128$, $q = 16411$, $m = 2^{28}$, $T = 13h$) for combinatorial attack on LWE [KF15].

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LWE variant: Binary matrix

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n	q	m	T	T
256	500009	440	4.5h	2min

To be compared with: Estimation by Galbraith [Gal] roughly one day.

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Questions?

Thank you for your attention!

Review

- Working as an engineer together with mathematicians can be fun
You can code, they... can do math
😊
- Even if you don't understand what you are implementing, you can get something working out of it
- Eventually you'll understand the math 🎯



Mainboard & Questionmark Images: flickr

Attacks on Lattice Crypto

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