## Index Sets for 4 Component Separation: Splits Between Consecutive Key Components

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1. TASKS = \{t \mid t \text{ is a separation task}\}
   TASKS = \{A/BCD, AB/CD, ABC/D, AB/C, A/BC, BC/D, B/CD, A/B, B/C, C/D\}
2. STATES = \{s \mid s \text{ is a state/mixture in the network}\}
   STATES = \{ABCD, ABC, BCD, AB, BC, CD, A, B, C, D\}
3. FEED = state that is the feed to the system
   FEED = \{ABCD\}
4. FS_F = \{\text{columns whose feed is the initial mixture}\}
   FS_F = \{A/BCD, AB/CD, ABC/D\}
5. TS_s = \{ \text{tasks } t \text{ that state } s \text{ is able to produce} \}
   TS_{ABCD} = \{ABC/D, AB/CD, ABC/D\}
   TS_{ABC} = \{A/BC, AB/C\}
   TS_{BCD} = \{B/CD, BC/D\}
   TS_{AB} = \{A/B\}
   TS_{BC} = \{B/C\}
   TS_{CD} = \{C/D\}
6. ST_s = \{ \text{tasks } t \text{ that are able to produce state } s \}
   ST_{ABC} = \{ABC/D\}
   ST_{BCD} = \{A/BCD\}
   ST_{AB} = \{AB/CD, AB/C\}
   ST_{BC} = \{A/BC, BC/D\}
   ST_{CD} = \{AB/CD, B/CD\}
   ST_A = \{A/BCD, A/BC, A/B\}
   ST_B = \{B/CD, A/B, B/C\}
   ST_C = \{AB/C, B/C, C/D\}
   ST_D = \{ABC/D, BC/D, C/D\}
7. PRE_i = \{ \text{tasks } t \text{ that produce final product } i \text{ through a rectifying section} \}
   PRE_A = \{A/BCD, A/BC, A/B\}
   PRE_B = \{B/CD, B/C\}
   PRE_C = \{C/D\}
8. PST_i = \{ \text{tasks } t \text{ that produce final product } i \text{ through a stripping section} \}
   PST_B = \{A/B\}
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PST_C = \{AB/C, B/C\}
    PST_D = \{ABC/D, BC/D, C/D\}
 9. COMP \{i \mid i \text{ is a component in the mixture}\}
    COMP = \{A, B, C, D\}
10. RECT_s = \{ tasks \ t \ that \ produce \ state \ s \ through \ a \ rectifying \ section \}
    RECT_{ABC} = \{ABC/D\}
    RECT_{AB} = \{AB/C, AB/CD\}
    RECT_{BC} = \{BC/D\}
    RECT_A = \{A/BCD, A/BC, A/B\}
    RECT_B = \{B/CD, B/C\}
    RECT_C = \{C/D\}
11. STRIP_s = \{ tasks \ t \ that \ produce \ state \ s \ through \ a \ stripping \ section \}
    STRIP_{BCD} = \{A/BCD\}
    STRIP_{BC} = \{A/BC\}
    STRIP_{CD} = \{AB/CD, B/CD\}
    STRIP_B = \{A/B\}
    STRIP_C = \{B/C, AB/C\}
    STRIP_D = \{ABC/D, BC/D, C/D\}
12. ISTATE = \{s \mid s \text{ is an intermediate state in the network}\}
    ISTATE = \{ABC, BCD, AB, BC, CD\}
13. IREC_s = \{ tasks \ t \ that \ produce \ an \ intermediate \ state \ s \ through \ a \ rectifying \ section \}
    IREC_{ABC} = \{ABC/D\}
    IREC_{AB} = \{AB/C, AB/CD\}
    IREC_{BC} = \{BC/D\}
14. ISTRIP_s = \{ tasks \ t \ that \ produce \ an \ intermediate \ state \ s \ through \ a \ stripping \ section \}
    ISRIP_{BCD} = \{A/BCD\}
    ISRIP_{BC} = \{A/BC\}
    ISRIP_{CD} = \{AB/CD, B/CD\}
15. LK_t = \{i \mid i \text{ is the light key component in separation task } t\}
    LK_{A/BCD} = A
    LK_{AB/CD} = B
    LK_{ABC/D} = C
    LK_{AB/C} = B
    LK_{A/BC} = A
    LK_{BC/D} = C
    LK_{B/CD} = B
    LK_{A/B} = A
    LK_{B/C} = B
    LK_{C/D} = C
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16.  $HK_t = \{i \mid i \text{ is the heavy key component in separation task } t\}$ 

$$HK_{A/BCD} = B$$

$$HK_{AB/CD} = C$$

$$HK_{ABC/D} = D$$

$$HK_{AB/C} = C$$

$$HK_{A/BC} = B$$

$$HK_{BC/D}=\mathbf{D}$$

$$HK_{B/CD} = C$$

$$HK_{A/B} = B$$

$$HK_{B/C} = C$$

$$HK_{C/D} = D$$

17.  $R = \{r \mid r \text{ is an Underwood root}\}$ 

$$R = \{r_1, r_2, r_3\}$$

note: a system with N components will have N-1 active Underwood roots

18.  $RUA_t = \{\text{active Underwood roots for task } t\}$ 

$$RUA_{A/BCD} = \{r_1, r_2, r_3\}$$

$$RUA_{AB/CD} = \{r_1, r_2, r_3\}$$

$$RUA_{ABC/D} = \{r_1, r_2, r_3\}$$

$$RUA_{AB/C} = \{r_1, r_2\}$$

$$RUA_{A/BC} = \{r_1, r_2\}$$

$$RUA_{BC/D} = \{r_2, r_3\}$$

$$RUA_{B/CD} = \{r_2, r_3\}$$

$$RUA_{A/B} = \{r_1\}$$

$$RUA_{B/C} = \{r_2\}$$

$$RUA_{C/D} = \{r_3\}$$