

a)

$$\text{Availability} = t_{\text{up}} / t_{\text{total}}$$

A:

$$t_{\text{up}} = 60\text{min} - 3 \cdot 30\text{s} = 58.5\text{min}$$

$$t_{\text{total}} = 60\text{min}$$

$$\text{Availability} = 58.5\text{min} / 60\text{min} = 97.5\%$$

B:

$$t_{\text{up}} = 60\text{min} - 30 \cdot 3\text{s} = 58.5\text{min}$$

$$t_{\text{total}} = 60\text{min}$$

$$\text{Availability} = 58.5\text{min} / 60\text{min} = 97.5\%$$

b)

Given:

$$97.5\% \text{ availability} = 0.25\% \text{ failrate}$$

We want an availability of 99.9%, thus:

$$99.9\% \text{ availability} = 0.1\% \text{ failrate}$$

For each server, we get more and more availability:

$$(0.5\%)^n = \text{availability}_{\text{total}}$$

Where n is the number of servers.

Solving the inequation:

$$(0.5\%)^n \leq 0.1\%$$

Will resolve to the following inequation:

$$n \geq \log_{0.5\%}(0.1\%) \text{ (as a general form: } n \geq \log_{\text{given\%}}(\text{desired\%}) \text{)}$$

Solving this, tells us that we need 1.8 (2) servers to get this concrete availability.