

Fraud detection using Cost Sensitive methods

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Fraud - the crime of getting money by deceiving people.

Examples of frauds:

- Using a stolen credit card
- Overstating the cost of compensation
- Reporting event which never happened
- ...

Fraud detection techniques:

- Probability models
- Anomaly detection
- Data mining
- Expert rules systems
- Pattern recognition
- Machine learning

Problems which occurs during modeling:

- Insufficient standard metrics
- Highly imbalanced dataset (class disproportion up to 1:1000)
- Labels distortions

Classification of methodology for classification problems

Standard methodology for classification problem:

- Standard models:
 - Logistic regression
 - Decision Tree
 - Random Forest
 - XGBoost
- Standard metrics:
 - Accuracy
 - Precision
 - Recall
 - F1 Score

Confusion matrix

		Prediction	
		Fraud	Non-Fraud
True	Fraud	TP	FN
	Non-Fraud	FP	TN

$$\text{Accuracy} = \frac{TP + TN}{TP + FP + FN + TN}$$

$$\text{Precision} = \frac{TP}{TP + FP}$$

$$\text{Recall} = \frac{TP}{TP + FN}$$

$$\text{F1 Score} = 2 \cdot \frac{\text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}}$$

Cost Sensitive Methodology:

- Cost dependent classification:
 - Threshold optimization
 - Bayesian Minimum Risk
- Cost sensitive training:
 - Cost Sensitive Logistic Regression
 - Cost Sensitive Decision Tree
- Cost sensitive metrics
 - Total cost
 - Savings

Cost matrix

		Prediction	
		Fraud	Non-Fraud
True	Fraud	C_{TP_i}	C_{FN_i}
	Non-Fraud	C_{FP_i}	C_{TN_i}

$$\text{Cost}(f(\mathbf{x}_i^*)) = y_i(c_i C_{TP_i} + (1 - c_i) C_{FN_i}) + (1 - y_i)(c_i C_{FP_i} + (1 - c_i) C_{TN_i})$$

- $\mathbf{x}_i^* = [\mathbf{x}_i, C_{TP_i}, C_{FP_i}, C_{FN_i}, C_{TN_i}]$ - features vector for i-th observation extended by classification cost
- C_i - classification cost for i-th observation
- $f(\cdot)$ - predictive model
- y_i - true label for i-th observation
- c_i - prediction for i-th observation

Cost Sensitive metrics

Cost sensitive metrics:

$$\text{Total cost}(f(\mathbf{S})) = \sum_{i=1}^N \text{Cost}(f(\mathbf{x}_i^*))$$

$$\text{Savings} = \frac{\text{Cost}_I(\mathbf{S}) - \text{Cost}(f(\mathbf{S}))}{\text{Cost}_I(\mathbf{S})}$$

- \mathbf{S} - data set
- $\text{Cost}_I = \min\{\text{Cost}(f_0(\mathbf{S})), \text{Cost}(f_1(\mathbf{S}))\}$
- $f_a(\mathbf{S}) = \mathbf{a}$ where $a \in \{0, 1\}$

Cost Sensitive Modeling

Threshold Optimization

We are looking for threshold th such that

$$\arg \min_{th \in [0,1]} \text{Total cost}(\mathbf{C}, \mathbf{P})$$

Where

- $\mathbf{C} = (c_i)_{i=1}^n$ - vector of true labels
- $\mathbf{P} = (p_i > th)_{i=1}^n$ - vector of binary outcomes

Bayesian Minimum Risk

Risk associated with predictions:

$$R(p_f|x) = L(p_f|y_f)P(p_f|x) + L(p_f|y_l)P(y_l|x)$$

$$R(p_l|x) = L(p_l|y_l)P(p_l|x) + L(p_l|y_f)P(y_f|x)$$

Classification threshold:

$$R(p_f|x) \leq R(p_l|x)$$

Where:

- $P(p_f|x)$, $P(p_l|x)$ - estimated probability of fraud/legitimate transaction
- $L(p_i|y_j)$ and $i, j \in \{l, f\}$ - loss function

Exact formula:

$$P(p_f|x) \geq \frac{L(p_f|y_I) - L(p_I|y_I)}{L(p_I|y_f) - L(p_f|y_f) - L(p_I|y_I) + L(p_f|y_I)}$$

After reformulation:

$$p \geq \frac{C_{FP} - C_{TN}}{C_{FN} - C_{TP} - C_{TN} + C_{FP}}$$

Cost Sensitive Logistic Regression

Formulation of standard Logistic Regression:

$$\hat{p} = P(y = 1|\mathbf{x}_i) = h_{\theta}(\mathbf{x}_i) = g\left(\sum_{j=1}^k \theta^{(j)} x_i^{(j)}\right)$$

Where loss function is defined:

$$J(\theta) = \frac{1}{N} \sum_{i=1}^N J_i(\theta)$$

Where:

- $g(z) = \frac{1}{(1 + e^{-z})}$
- $J_i(\theta) = -y_i \log(h_{\theta}(\mathbf{x}_i)) - (1 - y_i) \log(1 - h_{\theta}(\mathbf{x}_i))$

Cost Sensitive Logistic Regression

Standard costs:

$$J_i(\theta) \approx \begin{cases} 0, & \text{if } y_i \approx h_\theta(\mathbf{x}_i), \\ \infty, & \text{if } y_i \approx (1 - h_\theta(\mathbf{x}_i)). \end{cases}$$

Thus

$$C_{TP_i} = C_{TN_i} \approx 0$$

$$C_{FP_i} = C_{FN_i} \approx \infty$$

Cost Sensitive Logistic Regression

Actual costs:

$$J_i^c(\theta) = \begin{cases} C_{TP_i}, & \text{if } y_i = 1 \text{ and } h_\theta(\mathbf{x}_i) \approx 1, \\ C_{TN_i}, & \text{if } y_i = 0 \text{ and } h_\theta(\mathbf{x}_i) \approx 0, \\ C_{FP_i}, & \text{if } y_i = 0 \text{ and } h_\theta(\mathbf{x}_i) \approx 1, \\ C_{FN_i}, & \text{if } y_i = 1 \text{ and } h_\theta(\mathbf{x}_i) \approx 0. \end{cases}$$

Cost sensitive loss function:

$$J^c(\theta) = \frac{1}{N} \sum_{i=1}^N \left(y_i \left(h_\theta(\mathbf{x}_i) C_{TP_i} + (1 - h_\theta(\mathbf{x}_i)) C_{FN_i} \right) \right. \\ \left. + (1 - y_i) \left(h_\theta(\mathbf{x}_i) C_{FP_i} + (1 - h_\theta(\mathbf{x}_i)) C_{TN_i} \right) \right)$$

Cost Sensitive Decision Tree

Standard impurity measures:

- Misclassification: $I_m(\pi_1) = 1 - \max(\pi_1, 1 - \pi_1)$
- Entropy: $I_e(\pi_1) = -\pi_1 \log(\pi_1) - (1 - \pi_1) \log(1 - \pi_1)$
- Gini: $I_g(\pi_1) = 2\pi_1(1 - \pi_1)$

Cost Sensitive impurity measure:

- $I_c(\mathcal{S}) = \min \{ \text{Cost}(f_0(\mathcal{S})), \text{Cost}(f_1(\mathcal{S})) \}$

Where:

- $\pi_1 = \frac{|\mathcal{S}_1|}{|\mathcal{S}|}$ - percentage of positive class
- \mathcal{S} - set of samples

Experiment

Experiment description

Data set:

- Credit Card Fraud Detection Dataset
- 284,807 transactions with 492 frauds
- Class imbalance approx. 1:600 (0.172% fraud transactions)

Data split:

- Training: 50%
- Validation: 17%
- Test: 33%

Cost matrix for the experiment

Cost matrix:

		Prediction	
		Fraud	Non-Fraud
True	Fraud	$C_{TP_i} = C_a$	$C_{FN_i} = \text{Amt}_i$
	Non-Fraud	$C_{FP_i} = C_a$	$C_{TN_i} = 0$

- Amt_i - Value of transaction
- C_a - Administrative cost

Decision threshold for Bayesian Minimum Risk:

$$p \geq \frac{C_a}{\text{Amt}_i}$$

Results - Savings

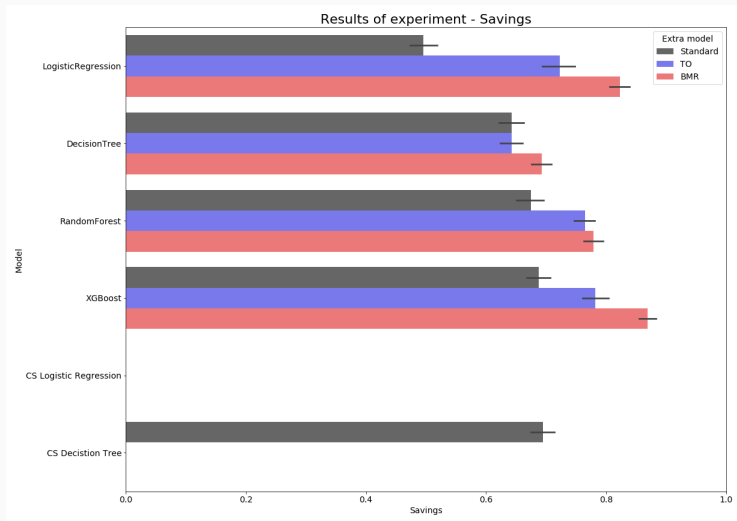


Figure 1: Results of the experiment for $C_a = 1$ and Saving metric.

Results - F1 Score

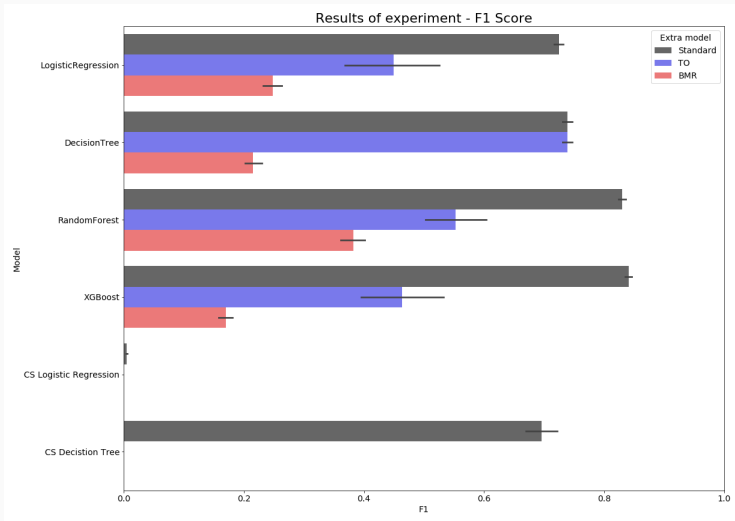


Figure 2: Results of the experiment for $C_a = 1$ and F1 Score metric.

Conclusions:

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Conclusions:

- Threshold Optimization and Bayesian Minimum Risk improves results for Savings metric,
- But unfortunately almost always worsens the results for F1 Score metric,
- And this leads to trade-off between cost and precision/recall.
- Cost Sensitive training may be good choice when Savings and F1 Score are simultaneously important.

Future work:

- Conducting the experiment in respect to different administrative cost.
- Extension of the used models with Cost Sensitive Ensembles and other boosting models (e.g. LightGMB, CatBoost).
- Extension of the experiment with under/over-sampling methods.
- Defining custom loss function (similarly to Logistic Regression) for boosting algorithms.



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Ensemble of example-dependent cost-sensitive decision trees, 2015.



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Thanks for your attention!

Questions?