ECGR 5103 Homework6

April 28, 2023

1 ECGR Homework 6

[]: !pip install torch torchvision

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Set everything up:

```
!pip install d2l==1.0.0a1.post0
!pip install matplotlib_inline
Looking in indexes: https://pypi.org/simple, https://us-python.pkg.dev/colab-
wheels/public/simple/
Requirement already satisfied: torch in /usr/local/lib/python3.9/dist-packages
(2.0.0+cu118)
Requirement already satisfied: torchvision in /usr/local/lib/python3.9/dist-
packages (0.15.1+cu118)
Requirement already satisfied: jinja2 in /usr/local/lib/python3.9/dist-packages
(from torch) (3.1.2)
Requirement already satisfied: typing-extensions in
/usr/local/lib/python3.9/dist-packages (from torch) (4.5.0)
Requirement already satisfied: sympy in /usr/local/lib/python3.9/dist-packages
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Requirement already satisfied: filelock in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: requests in /usr/local/lib/python3.9/dist-
packages (from torchvision) (2.27.1)
Requirement already satisfied: pillow!=8.3.*,>=5.3.0 in
/usr/local/lib/python3.9/dist-packages (from torchvision) (8.4.0)
Requirement already satisfied: numpy in /usr/local/lib/python3.9/dist-packages
(from torchvision) (1.22.4)
Requirement already satisfied: MarkupSafe>=2.0 in /usr/local/lib/python3.9/dist-
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packages (from jinja2->torch) (2.1.2)
Requirement already satisfied: certifi>=2017.4.17 in
/usr/local/lib/python3.9/dist-packages (from requests->torchvision) (2022.12.7)
Requirement already satisfied: charset-normalizer~=2.0.0 in
/usr/local/lib/python3.9/dist-packages (from requests->torchvision) (2.0.12)
Requirement already satisfied: idna<4,>=2.5 in /usr/local/lib/python3.9/dist-
packages (from requests->torchvision) (3.4)
Requirement already satisfied: urllib3<1.27,>=1.21.1 in
/usr/local/lib/python3.9/dist-packages (from requests->torchvision) (1.26.15)
Requirement already satisfied: mpmath>=0.19 in /usr/local/lib/python3.9/dist-
packages (from sympy->torch) (1.3.0)
Looking in indexes: https://pypi.org/simple, https://us-python.pkg.dev/colab-
wheels/public/simple/
Collecting d21==1.0.0a1.post0
  Downloading d21-1.0.0a1.post0-py3-none-any.whl (93 kB)
                           93.0/93.0 kB
11.9 MB/s eta 0:00:00
Requirement already satisfied: matplotlib in
/usr/local/lib/python3.9/dist-packages (from d2l==1.0.0a1.post0) (3.7.1)
Requirement already satisfied: pandas in /usr/local/lib/python3.9/dist-packages
(from d2l==1.0.0a1.post0) (1.5.3)
Requirement already satisfied: matplotlib-inline in
/usr/local/lib/python3.9/dist-packages (from d2l==1.0.0a1.post0) (0.1.6)
Collecting jupyter
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Requirement already satisfied: gym in /usr/local/lib/python3.9/dist-packages
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Requirement already satisfied: numpy in /usr/local/lib/python3.9/dist-packages
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Requirement already satisfied: gym-notices>=0.0.4 in
/usr/local/lib/python3.9/dist-packages (from gym->d2l==1.0.0a1.post0) (0.0.8)
Requirement already satisfied: importlib-metadata>=4.8.0 in
/usr/local/lib/python3.9/dist-packages (from gym->d2l==1.0.0a1.post0) (6.6.0)
Requirement already satisfied: cloudpickle>=1.2.0 in
/usr/local/lib/python3.9/dist-packages (from gym->d2l==1.0.0a1.post0) (2.2.1)
Requirement already satisfied: ipykernel in /usr/local/lib/python3.9/dist-
packages (from jupyter->d2l==1.0.0a1.post0) (5.5.6)
Requirement already satisfied: ipywidgets in /usr/local/lib/python3.9/dist-
packages (from jupyter->d2l==1.0.0a1.post0) (7.7.1)
Requirement already satisfied: jupyter-console in /usr/local/lib/python3.9/dist-
packages (from jupyter->d2l==1.0.0a1.post0) (6.1.0)
Requirement already satisfied: nbconvert in /usr/local/lib/python3.9/dist-
packages (from jupyter->d2l==1.0.0a1.post0) (6.5.4)
Collecting qtconsole
  Downloading qtconsole-5.4.2-py3-none-any.whl (121 kB)
                          121.2/121.2 kB
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Requirement already satisfied: notebook in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: pyparsing>=2.3.1 in
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(3.0.9)
Requirement already satisfied: pillow>=6.2.0 in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: packaging>=20.0 in /usr/local/lib/python3.9/dist-
packages (from matplotlib->d2l==1.0.0a1.post0) (23.1)
Requirement already satisfied: cycler>=0.10 in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: contourpy>=1.0.1 in
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Requirement already satisfied: fonttools>=4.22.0 in
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Requirement already satisfied: python-dateutil>=2.7 in
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Requirement already satisfied: traitlets in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: pytz>=2020.1 in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: urllib3<1.27,>=1.21.1 in
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Requirement already satisfied: idna<4,>=2.5 in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: certifi>=2017.4.17 in
/usr/local/lib/python3.9/dist-packages (from requests->d2l==1.0.0a1.post0)
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Requirement already satisfied: zipp>=0.5 in /usr/local/lib/python3.9/dist-
packages (from importlib-metadata>=4.8.0->gym->d2l==1.0.0a1.post0) (3.15.0)
Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.9/dist-
packages (from python-dateutil>=2.7->matplotlib->d2l==1.0.0a1.post0) (1.16.0)
Requirement already satisfied: jupyter-client in /usr/local/lib/python3.9/dist-
packages (from ipykernel->jupyter->d2l==1.0.0a1.post0) (6.1.12)
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Requirement already satisfied: tornado>=4.2 in /usr/local/lib/python3.9/dist-
packages (from ipykernel->jupyter->d2l==1.0.0a1.post0) (6.2)
Requirement already satisfied: ipython-genutils in
/usr/local/lib/python3.9/dist-packages (from
ipykernel->jupyter->d2l==1.0.0a1.post0) (0.2.0)
Requirement already satisfied: ipython>=5.0.0 in /usr/local/lib/python3.9/dist-
packages (from ipykernel->jupyter->d2l==1.0.0a1.post0) (7.34.0)
Requirement already satisfied: widgetsnbextension~=3.6.0 in
/usr/local/lib/python3.9/dist-packages (from
ipywidgets->jupyter->d2l==1.0.0a1.post0) (3.6.4)
Requirement already satisfied: jupyterlab-widgets>=1.0.0 in
/usr/local/lib/python3.9/dist-packages (from
ipywidgets->jupyter->d2l==1.0.0a1.post0) (3.0.7)
Requirement already satisfied: pygments in /usr/local/lib/python3.9/dist-
packages (from jupyter-console->jupyter->d2l==1.0.0a1.post0) (2.14.0)
Requirement already satisfied: prompt-toolkit!=3.0.0,!=3.0.1,<3.1.0,>=2.0.0 in
/usr/local/lib/python3.9/dist-packages (from jupyter-
console->jupyter->d2l==1.0.0a1.post0) (3.0.38)
Requirement already satisfied: tinycss2 in /usr/local/lib/python3.9/dist-
packages (from nbconvert->jupyter->d2l==1.0.0a1.post0) (1.2.1)
Requirement already satisfied: lxml in /usr/local/lib/python3.9/dist-packages
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nbconvert->jupyter->d2l==1.0.0a1.post0) (0.4)
Requirement already satisfied: mistune<2,>=0.8.1 in
/usr/local/lib/python3.9/dist-packages (from
nbconvert->jupyter->d2l==1.0.0a1.post0) (0.8.4)
Requirement already satisfied: jinja2>=3.0 in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: nbformat>=5.1 in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: pandocfilters>=1.4.1 in
/usr/local/lib/python3.9/dist-packages (from
nbconvert->jupyter->d2l==1.0.0a1.post0) (1.5.0)
Requirement already satisfied: beautifulsoup4 in /usr/local/lib/python3.9/dist-
packages (from nbconvert->jupyter->d2l==1.0.0a1.post0) (4.11.2)
Requirement already satisfied: defusedxml in /usr/local/lib/python3.9/dist-
packages (from nbconvert->jupyter->d2l==1.0.0a1.post0) (0.7.1)
Requirement already satisfied: bleach in /usr/local/lib/python3.9/dist-packages
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Requirement already satisfied: jupyter-core>=4.7 in
/usr/local/lib/python3.9/dist-packages (from
nbconvert->jupyter->d2l==1.0.0a1.post0) (5.3.0)
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Requirement already satisfied: jupyterlab-pygments in
/usr/local/lib/python3.9/dist-packages (from
nbconvert->jupyter->d2l==1.0.0a1.post0) (0.2.2)
Requirement already satisfied: prometheus-client in
/usr/local/lib/python3.9/dist-packages (from
notebook->jupyter->d2l==1.0.0a1.post0) (0.16.0)
Requirement already satisfied: pyzmq>=17 in /usr/local/lib/python3.9/dist-
packages (from notebook->jupyter->d2l==1.0.0a1.post0) (23.2.1)
Requirement already satisfied: nest-asyncio>=1.5 in
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notebook->jupyter->d2l==1.0.0a1.post0) (1.5.6)
Requirement already satisfied: terminado>=0.8.3 in
/usr/local/lib/python3.9/dist-packages (from
notebook->jupyter->d2l==1.0.0a1.post0) (0.17.1)
Requirement already satisfied: argon2-cffi in /usr/local/lib/python3.9/dist-
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Requirement already satisfied: Send2Trash>=1.8.0 in
/usr/local/lib/python3.9/dist-packages (from
notebook->jupyter->d2l==1.0.0a1.post0) (1.8.0)
Collecting qtpy>=2.0.1
 Downloading QtPy-2.3.1-py3-none-any.whl (84 kB)
                           84.9/84.9 kB
12.6 MB/s eta 0:00:00
Requirement already satisfied: setuptools>=18.5 in
/usr/local/lib/python3.9/dist-packages (from
ipython>=5.0.0->ipykernel->jupyter->d2l==1.0.0a1.post0) (67.7.2)
Requirement already satisfied: pexpect>4.3 in /usr/local/lib/python3.9/dist-
packages (from ipython>=5.0.0->ipykernel->jupyter->d2l==1.0.0a1.post0) (4.8.0)
Requirement already satisfied: pickleshare in /usr/local/lib/python3.9/dist-
packages (from ipython>=5.0.0->ipykernel->jupyter->d2l==1.0.0a1.post0) (0.7.5)
Requirement already satisfied: decorator in /usr/local/lib/python3.9/dist-
packages (from ipython>=5.0.0->ipykernel->jupyter->d2l==1.0.0a1.post0) (4.4.2)
Requirement already satisfied: backcall in /usr/local/lib/python3.9/dist-
packages (from ipython>=5.0.0->ipykernel->jupyter->d2l==1.0.0a1.post0) (0.2.0)
Collecting jedi>=0.16
 Downloading jedi-0.18.2-py2.py3-none-any.whl (1.6 MB)
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Requirement already satisfied: platformdirs>=2.5 in
/usr/local/lib/python3.9/dist-packages (from jupyter-
core>=4.7->nbconvert->jupyter->d2l==1.0.0a1.post0) (3.2.0)
Requirement already satisfied: jsonschema>=2.6 in /usr/local/lib/python3.9/dist-
packages (from nbformat>=5.1->nbconvert->jupyter->d2l==1.0.0a1.post0) (4.3.3)
Requirement already satisfied: fastjsonschema in /usr/local/lib/python3.9/dist-
packages (from nbformat>=5.1->nbconvert->jupyter->d2l==1.0.0a1.post0) (2.16.3)
Requirement already satisfied: wcwidth in /usr/local/lib/python3.9/dist-packages
(from prompt-toolkit!=3.0.0,!=3.0.1,<3.1.0,>=2.0.0->jupyter-
console->jupyter->d2l==1.0.0a1.post0) (0.2.6)
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Requirement already satisfied: ptyprocess in /usr/local/lib/python3.9/dist-
    packages (from terminado>=0.8.3->notebook->jupyter->d2l==1.0.0a1.post0) (0.7.0)
    Requirement already satisfied: argon2-cffi-bindings in
    /usr/local/lib/python3.9/dist-packages (from
    argon2-cffi->notebook->jupyter->d2l==1.0.0a1.post0) (21.2.0)
    Requirement already satisfied: soupsieve>1.2 in /usr/local/lib/python3.9/dist-
    packages (from beautifulsoup4->nbconvert->jupyter->d2l==1.0.0a1.post0) (2.4.1)
    Requirement already satisfied: webencodings in /usr/local/lib/python3.9/dist-
    packages (from bleach->nbconvert->jupyter->d2l==1.0.0a1.post0) (0.5.1)
    Requirement already satisfied: parso<0.9.0,>=0.8.0 in
    /usr/local/lib/python3.9/dist-packages (from
    jedi>=0.16->ipython>=5.0.0->ipykernel->jupyter->d2l==1.0.0a1.post0) (0.8.3)
    Requirement already satisfied: attrs>=17.4.0 in /usr/local/lib/python3.9/dist-
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    jsonschema>=2.6->nbformat>=5.1->nbconvert->jupyter->d2l==1.0.0a1.post0) (23.1.0)
    Requirement already satisfied: pyrsistent!=0.17.0,!=0.17.1,!=0.17.2,>=0.14.0 in
    /usr/local/lib/python3.9/dist-packages (from
    jsonschema \ge 2.6 - nbformat \ge 5.1 - nbconvert - jupyter - >d2l == 1.0.0a1.post0) (0.19.3)
    Requirement already satisfied: cffi>=1.0.1 in /usr/local/lib/python3.9/dist-
    packages (from argon2-cffi-
    bindings->argon2-cffi->notebook->jupyter->d2l==1.0.0a1.post0) (1.15.1)
    Requirement already satisfied: pycparser in /usr/local/lib/python3.9/dist-
    packages (from cffi>=1.0.1->argon2-cffi-
    bindings->argon2-cffi->notebook->jupyter->d2l==1.0.0a1.post0) (2.21)
    Installing collected packages: qtpy, jedi, qtconsole, jupyter, d21
    Successfully installed d21-1.0.0a1.post0 jedi-0.18.2 jupyter-1.0.0
    qtconsole-5.4.2 qtpy-2.3.1
    Looking in indexes: https://pypi.org/simple, https://us-python.pkg.dev/colab-
    wheels/public/simple/
    Requirement already satisfied: matplotlib_inline in
    /usr/local/lib/python3.9/dist-packages (0.1.6)
    Requirement already satisfied: traitlets in /usr/local/lib/python3.9/dist-
    packages (from matplotlib_inline) (5.7.1)
[]: %matplotlib inline
     import time
     import math
     import torch
     import torchvision
     from torchvision import transforms
     from d21 import torch as d21
     from torch import nn
     import torch.nn.functional as F
     d2l.use_svg_display()
```

1.1 Problem 1

For the problem of Machine Translation problem: Train a deeper Transformer than what we did during the lectures. How does it affect the training speed, model complexity, and translation performance both quantitatively and qualitatively? Report and plot your results.

Normalization and other utility functions:

```
[]: class PositionWiseFFN(nn.Module):
         """The positionwise feed-forward network."""
        def __init__(self, ffn_num_hiddens, ffn_num_outputs):
             super().__init__()
             self.dense1 = nn.LazyLinear(ffn_num_hiddens)
             self.relu = nn.ReLU()
             self.dense2 = nn.LazyLinear(ffn_num_outputs)
        def forward(self, X):
             return self.dense2(self.relu(self.dense1(X)))
[]: |ffn = PositionWiseFFN(4, 8)
     ffn.eval()
     ffn(torch.ones((2, 3, 4)))[0]
    /usr/local/lib/python3.9/dist-packages/torch/nn/modules/lazy.py:180:
    UserWarning: Lazy modules are a new feature under heavy development so changes
    to the API or functionality can happen at any moment.
      warnings.warn('Lazy modules are a new feature under heavy development '
[]: tensor([[ 0.2107, -0.2126, 0.1207, -0.3937, -0.1298, -0.3482, -0.1620,
    -0.3778,
             [0.2107, -0.2126, 0.1207, -0.3937, -0.1298, -0.3482, -0.1620,
     -0.3778],
             [0.2107, -0.2126, 0.1207, -0.3937, -0.1298, -0.3482, -0.1620,
     -0.3778],
           grad_fn=<SelectBackward0>)
[]: ln = nn.LayerNorm(2)
     bn = nn.LazyBatchNorm1d()
     X = torch.tensor([[1, 2], [2, 3]], dtype=torch.float32)
     # Compute mean and variance from X in the training mode
     print('layer norm:', ln(X), '\nbatch norm:', bn(X))
    layer norm: tensor([[-1.0000, 1.0000],
            [-1.0000, 1.0000]], grad_fn=<NativeLayerNormBackward0>)
    batch norm: tensor([[-1.0000, -1.0000],
            [ 1.0000, 1.0000]], grad_fn=<NativeBatchNormBackward0>)
[]: class AddNorm(nn.Module):
         """The residual connection followed by layer normalization."""
```

```
def __init__(self, norm_shape, dropout):
             super().__init__()
             self.dropout = nn.Dropout(dropout)
             self.ln = nn.LayerNorm(norm_shape)
         def forward(self, X, Y):
             return self.ln(self.dropout(Y) + X)
[]: add_norm = AddNorm(4, 0.5)
     shape = (2, 3, 4)
     d21.check_shape(add_norm(torch.ones(shape), torch.ones(shape)), shape)
    The encoder:
[]: class TransformerEncoderBlock(nn.Module):
         """The Transformer encoder block."""
         def __init__(self, num_hiddens, ffn_num_hiddens, num_heads, dropout,
                      use_bias=False):
             super().__init__()
             self.attention = d21.MultiHeadAttention(num_hiddens, num_heads,
                                                      dropout, use_bias)
             self.addnorm1 = AddNorm(num_hiddens, dropout)
             self.ffn = PositionWiseFFN(ffn_num_hiddens, num_hiddens)
             self.addnorm2 = AddNorm(num hiddens, dropout)
         def forward(self, X, valid lens):
             Y = self.addnorm1(X, self.attention(X, X, X, valid_lens))
             return self.addnorm2(Y, self.ffn(Y))
[]: X = \text{torch.ones}((2, 100, 24))
     valid_lens = torch.tensor([3, 2])
     encoder_blk = TransformerEncoderBlock(24, 48, 8, 0.5)
     encoder blk.eval()
     d2l.check_shape(encoder_blk(X, valid_lens), X.shape)
[]: class TransformerEncoder(d21.Encoder):
         """The Transformer encoder."""
         def __init__(self, vocab_size, num_hiddens, ffn_num_hiddens,
                      num_heads, num_blks, dropout, use_bias=False):
             super().__init__()
             self.num_hiddens = num_hiddens
             self.embedding = nn.Embedding(vocab_size, num_hiddens)
             self.pos encoding = d21.PositionalEncoding(num hiddens, dropout)
```

self.blks.add_module("block"+str(i), TransformerEncoderBlock(

num_hiddens, ffn_num_hiddens, num_heads, dropout, use_bias))

self.blks = nn.Sequential()
for i in range(num_blks):

```
def forward(self, X, valid_lens):
    # Since positional encoding values are between -1 and 1, the embedding
    # values are multiplied by the square root of the embedding dimension
    # to rescale before they are summed up
    X = self.pos_encoding(self.embedding(X) * math.sqrt(self.num_hiddens))
    self.attention_weights = [None] * len(self.blks)
    for i, blk in enumerate(self.blks):
        X = blk(X, valid_lens)
        self.attention_weights[
            i] = blk.attention.attention_weights
        return X
```

The decoder:

```
[]: class TransformerDecoderBlock(nn.Module):
         # The i-th block in the Transformer decoder
         def __init__(self, num_hiddens, ffn_num_hiddens, num_heads, dropout, i):
             super().__init__()
             self.i = i
             self.attention1 = d21.MultiHeadAttention(num_hiddens, num_heads,
                                                      dropout)
             self.addnorm1 = AddNorm(num_hiddens, dropout)
             self.attention2 = d21.MultiHeadAttention(num_hiddens, num_heads,
                                                      dropout)
             self.addnorm2 = AddNorm(num_hiddens, dropout)
             self.ffn = PositionWiseFFN(ffn_num_hiddens, num_hiddens)
             self.addnorm3 = AddNorm(num_hiddens, dropout)
         def forward(self, X, state):
             enc_outputs, enc_valid_lens = state[0], state[1]
             # During training, all the tokens of any output sequence are processed
             # at the same time, so state[2][self.i] is None as initialized. When
             # decoding any output sequence token by token during prediction,
             # state[2][self.i] contains representations of the decoded output at
             # the i-th block up to the current time step
             if state[2][self.i] is None:
                 key_values = X
             else:
                 key_values = torch.cat((state[2][self.i], X), dim=1)
             state[2][self.i] = key_values
             if self.training:
                 batch_size, num_steps, _ = X.shape
```

```
# Shape of dec valid lens: (batch size, num steps), where every
                 # row is [1, 2, ..., num_steps]
                 dec_valid_lens = torch.arange(
                     1, num_steps + 1, device=X.device).repeat(batch_size, 1)
             else:
                 dec_valid_lens = None
             # Self-attention
             X2 = self.attention1(X, key_values, key_values, dec_valid_lens)
             Y = self.addnorm1(X, X2)
             # Encoder-decoder attention. Shape of enc_outputs:
             # (batch_size, num_steps, num_hiddens)
             Y2 = self.attention2(Y, enc_outputs, enc_outputs, enc_valid_lens)
             Z = self.addnorm2(Y, Y2)
             return self.addnorm3(Z, self.ffn(Z)), state
[]: decoder_blk = TransformerDecoderBlock(24, 48, 8, 0.5, 0)
     X = torch.ones((2, 100, 24))
     state = [encoder_blk(X, valid_lens), valid_lens, [None]]
     d21.check_shape(decoder_blk(X, state)[0], X.shape)
[]: class TransformerDecoder(d21.AttentionDecoder):
         def __init__(self, vocab_size, num_hiddens, ffn_num_hiddens, num_heads,
                      num_blks, dropout):
             super().__init__()
             self.num_hiddens = num_hiddens
             self.num_blks = num_blks
             self.embedding = nn.Embedding(vocab_size, num_hiddens)
             self.pos_encoding = d21.PositionalEncoding(num_hiddens, dropout)
             self.blks = nn.Sequential()
             for i in range(num blks):
                 self.blks.add_module("block"+str(i), TransformerDecoderBlock(
                     num_hiddens, ffn_num_hiddens, num_heads, dropout, i))
             self.dense = nn.LazyLinear(vocab_size)
         def init_state(self, enc_outputs, enc_valid_lens):
             return [enc_outputs, enc_valid_lens, [None] * self.num_blks]
         def forward(self, X, state):
             X = self.pos_encoding(self.embedding(X) * math.sqrt(self.num_hiddens))
             self._attention_weights = [[None] * len(self.blks) for _ in range (2)]
             for i, blk in enumerate(self.blks):
                 X, state = blk(X, state)
                 # Decoder self-attention weights
                 self._attention_weights[0][
                     i] = blk.attention1.attention.attention weights
                 # Encoder-decoder attention weights
```

self._attention_weights[1][

```
i] = blk.attention2.attention.attention_weights
    return self.dense(X), state

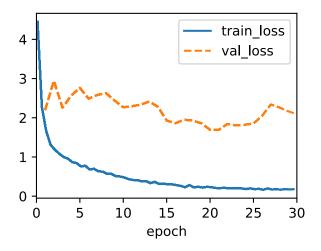
@property
def attention_weights(self):
    return self._attention_weights
```

Training:

```
[]: data = d21.MTFraEng(batch_size=128)
```

Downloading ../data/fra-eng.zip from http://d21-data.s3-accelerate.amazonaws.com/fra-eng.zip...

```
[]: trainer = d21.Trainer(max_epochs=30, gradient_clip_val=1, num_gpus=1) trainer.fit(model, data)
```



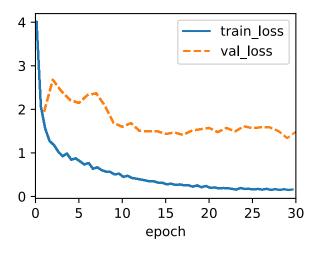
Test:

```
[]: engs = ['go .', 'i lost .', 'he\'s calm .', 'i\'m home .']
  fras = ['va !', 'j\'ai perdu .', 'il est calme .', 'je suis chez moi .']
  preds, _ = model.predict_step(
          data.build(engs, fras), d21.try_gpu(), data.num_steps)
  for en, fr, p in zip(engs, fras, preds):
          translation = []
     for token in data.tgt_vocab.to_tokens(p):
          if token == '<eos>':
               break
          translation.append(token)
     print(f'{en} => {translation}, bleu,'
               f'{d21.bleu(" ".join(translation), fr, k=2):.3f}')
```

```
go . => ['va', '!'], bleu,1.000
i lost . => ["j'ai", 'perdu', '.'], bleu,1.000
he's calm . => ['il', 'est', 'mort', '.'], bleu,0.658
i'm home . => ['je', 'suis', 'chez', 'moi', '.'], bleu,1.000
```

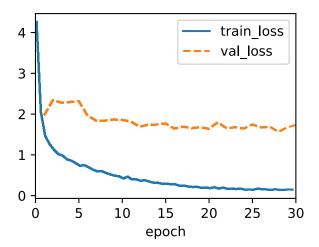
Make the network deeper (adjust the number of feed-forward layer):

```
[]: trainer = d21.Trainer(max_epochs=30, gradient_clip_val=1, num_gpus=1) trainer.fit(model, data)
```



```
Test:
```

```
[]: engs = ['go .', 'i lost .', 'he\'s calm .', 'i\'m home .']
     fras = ['va !', 'j\'ai perdu .', 'il est calme .', 'je suis chez moi .']
     preds, _ = model.predict_step(
         data build(engs, fras), d2l try_gpu(), data num_steps)
     for en, fr, p in zip(engs, fras, preds):
         translation = []
         for token in data.tgt_vocab.to_tokens(p):
             if token == '<eos>':
                 break
             translation.append(token)
         print(f'{en} => {translation}, bleu,'
               f'{d21.bleu(" ".join(translation), fr, k=2):.3f}')
    go . => ['va', '!'], bleu,1.000
    i lost . => ["j'ai", 'perdu', '.'], bleu,1.000
    he's calm . => ['<unk>', '.'], bleu,0.000
    i'm home . => ['je', 'suis', 'chez', 'moi', '.'], bleu,1.000
    Adjust the feed-forward layer even more:
[]: num_hiddens, num_blks, dropout = 256, 2, 0.2
     ffn_num_hiddens, num_heads = 256, 16
     encoder = TransformerEncoder(
         len(data.src_vocab), num_hiddens, ffn_num_hiddens, num_heads,
         num_blks, dropout)
     decoder = TransformerDecoder(
         len(data.tgt_vocab), num_hiddens, ffn_num_hiddens, num_heads,
         num blks, dropout)
     model = d21.Seq2Seq(encoder, decoder, tgt_pad=data.tgt_vocab['<pad>'],
                         lr=0.0015)
[]: trainer = d21.Trainer(max_epochs=30, gradient_clip_val=1, num_gpus=1)
     trainer.fit(model, data)
```



```
go . => ['va', '!'], bleu,1.000
i lost . => ["j'ai", 'perdu', '.'], bleu,1.000
he's calm . => ['il', 'est', 'mouillé', '.'], bleu,0.658
i'm home . => ['je', 'suis', 'chez', 'moi', '.'], bleu,1.000
```

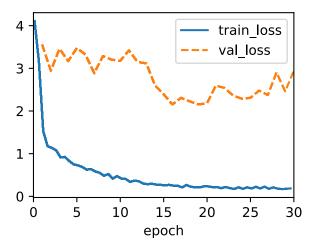
Adjust the number of hidden layers:

```
[]: num_hiddens, num_blks, dropout = 512, 2, 0.2
ffn_num_hiddens, num_heads = 64, 4

encoder = TransformerEncoder(
    len(data.src_vocab), num_hiddens, ffn_num_hiddens, num_heads,
    num_blks, dropout)
decoder = TransformerDecoder(
    len(data.tgt_vocab), num_hiddens, ffn_num_hiddens, num_heads,
    num_blks, dropout)
model = d21.Seq2Seq(encoder, decoder, tgt_pad=data.tgt_vocab['<pad>'],
```

```
lr=0.0015)
```

```
[]: trainer = d21.Trainer(max_epochs=30, gradient_clip_val=1, num_gpus=1) trainer.fit(model, data)
```

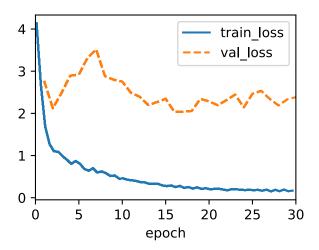


```
go . => ['va', '!'], bleu,1.000
i lost . => ["j'ai", 'perdu', '.'], bleu,1.000
he's calm . => ['il', 'est', 'mouillé', '.'], bleu,0.658
i'm home . => ['je', 'suis', 'chez', 'moi', '.'], bleu,1.000
```

Adjust the number of blocks:

```
[]: num_hiddens, num_blks, dropout = 256, 4, 0.2
ffn_num_hiddens, num_heads = 64, 4
encoder = TransformerEncoder(
    len(data.src_vocab), num_hiddens, ffn_num_hiddens, num_heads,
```

```
[]: trainer = d21.Trainer(max_epochs=30, gradient_clip_val=1, num_gpus=1) trainer.fit(model, data)
```



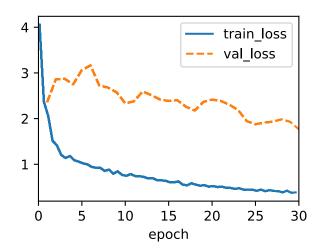
Adjust dropout:

```
go . => ['va', '!'], bleu,1.000
i lost . => ["j'ai", 'perdu', '.'], bleu,1.000
he's calm . => ['il', 'est', 'mouillé', '.'], bleu,0.658
i'm home . => ['je', 'suis', 'chez', 'moi', '.'], bleu,1.000
```

```
[]: num_hiddens, num_blks, dropout = 256, 2, 0.4
ffn_num_hiddens, num_heads = 64, 4

encoder = TransformerEncoder(
    len(data.src_vocab), num_hiddens, ffn_num_hiddens, num_heads,
    num_blks, dropout)
decoder = TransformerDecoder(
    len(data.tgt_vocab), num_hiddens, ffn_num_hiddens, num_heads,
    num_blks, dropout)
model = d21.Seq2Seq(encoder, decoder, tgt_pad=data.tgt_vocab['<pad>'],
    lr=0.0015)
```

```
[]: trainer = d21.Trainer(max_epochs=30, gradient_clip_val=1, num_gpus=1) trainer.fit(model, data)
```



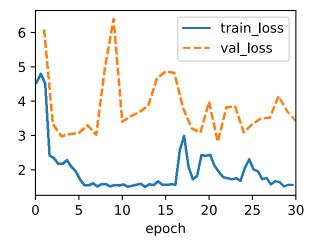
```
[]: engs = ['go .', 'i lost .', 'he\'s calm .', 'i\'m home .']
fras = ['va !', 'j\'ai perdu .', 'il est calme .', 'je suis chez moi .']
preds, _ = model.predict_step(
    data.build(engs, fras), d2l.try_gpu(), data.num_steps)
for en, fr, p in zip(engs, fras, preds):
    translation = []
    for token in data.tgt_vocab.to_tokens(p):
        if token == '<eos>':
            break
        translation.append(token)
    print(f'{en} => {translation}, bleu,'
            f'{d2l.bleu(" ".join(translation), fr, k=2):.3f}')
```

go . => ['va', 'doucement', '!'], bleu,0.000

```
i lost . => ['je', 'suis', '<unk>', 'perdu', '.'], bleu,0.447
he's calm . => ['il', 'est', 'calme', '.'], bleu,1.000
i'm home . => ['je', 'suis', 'chez', 'moi', '.'], bleu,1.000
```

Combine all together:

```
[]: trainer = d21.Trainer(max_epochs=30, gradient_clip_val=1, num_gpus=1) trainer.fit(model, data)
```



Test:

```
translation.append(token)
print(f'{en} => {translation}, bleu,'
    f'{d21.bleu(" ".join(translation), fr, k=2):.3f}')
```

```
go . => [], bleu,0.000
i lost . => [], bleu,0.000
he's calm . => [], bleu,0.000
i'm home . => [], bleu,0.000
```

2 Problem 2

For the problem of the Vision Transformer, we need, in lectures, to train a deeper Transformer with more multiheaded self-attention blocks. How does it affect the training speed, model complexity, and validation accuracy? Report and plot your results.

Embeddings:

The encoder:

```
[]: class ViTMLP(nn.Module):
    def __init__(self, mlp_num_hiddens, mlp_num_outputs, dropout=0.5):
        super().__init__()
        self.dense1 = nn.LazyLinear(mlp_num_hiddens)
        self.gelu = nn.GELU()
        self.dropout1 = nn.Dropout(dropout)
```

```
self.dense2 = nn.LazyLinear(mlp_num_outputs)
self.dropout2 = nn.Dropout(dropout)

def forward(self, x):
    return self.dropout2(self.dense2(self.dropout1(self.gelu(self.dense1(x)))))
```

```
[]: X = torch.ones((2, 100, 24))
encoder_blk = ViTBlock(24, 24, 48, 8, 0.5)
encoder_blk.eval()
d2l.check_shape(encoder_blk(X), X.shape)
```

Connecting everything:

```
[]: class ViT(d21.Classifier):
         """Vision Transformer."""
         def __init__(self, img_size, patch_size, num_hiddens, mlp_num_hiddens,
                      num_heads, num_blks, emb_dropout, blk_dropout, lr=0.1,
                      use_bias=False, num_classes=10):
             super().__init__()
             self.save_hyperparameters()
             self.patch embedding = PatchEmbedding(
                 img_size, patch_size, num_hiddens)
             self.cls token = nn.Parameter(torch.zeros(1, 1, num hiddens))
             num_steps = self.patch_embedding.num_patches + 1  # Add the cls token
             # Positional embeddings are learnable
             self.pos_embedding = nn.Parameter(
                 torch.randn(1, num_steps, num_hiddens))
             self.dropout = nn.Dropout(emb_dropout)
             self.blks = nn.Sequential()
             for i in range(num_blks):
                 self.blks.add_module(f"{i}", ViTBlock(
                     num_hiddens, num_hiddens, mlp_num_hiddens,
```

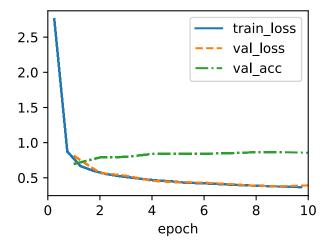
Training:

```
[]: data = d21.FashionMNIST(batch size=128, resize=(img size, img size))
    Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-
    images-idx3-ubyte.gz
    Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-
    images-idx3-ubyte.gz to ../data/FashionMNIST/raw/train-images-idx3-ubyte.gz
              | 26421880/26421880 [00:03<00:00, 8666732.59it/s]
    100%
    Extracting .../data/FashionMNIST/raw/train-images-idx3-ubyte.gz to
    ../data/FashionMNIST/raw
    Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-
    labels-idx1-ubyte.gz
    Downloading http://fashion-mnist.s3-website.eu-central-1.amazonaws.com/train-
    labels-idx1-ubyte.gz to ../data/FashionMNIST/raw/train-labels-idx1-ubyte.gz
              | 29515/29515 [00:00<00:00, 143512.00it/s]
    100%|
    Extracting ../data/FashionMNIST/raw/train-labels-idx1-ubyte.gz to
    ../data/FashionMNIST/raw
    Downloading http://fashion-mnist.s3-website.eu-
    central-1.amazonaws.com/t10k-images-idx3-ubyte.gz
    Downloading http://fashion-mnist.s3-website.eu-
    central-1.amazonaws.com/t10k-images-idx3-ubyte.gz to
    ../data/FashionMNIST/raw/t10k-images-idx3-ubyte.gz
    100%1
              4422102/4422102 [00:01<00:00, 2672794.77it/s]
    Extracting .../data/FashionMNIST/raw/t10k-images-idx3-ubyte.gz to
    ../data/FashionMNIST/raw
    Downloading http://fashion-mnist.s3-website.eu-
    central-1.amazonaws.com/t10k-labels-idx1-ubyte.gz
    Downloading http://fashion-mnist.s3-website.eu-
```

```
central-1.amazonaws.com/t10k-labels-idx1-ubyte.gz to
../data/FashionMNIST/raw/t10k-labels-idx1-ubyte.gz
100%| | 5148/5148 [00:00<00:00, 5448467.57it/s]</pre>
```

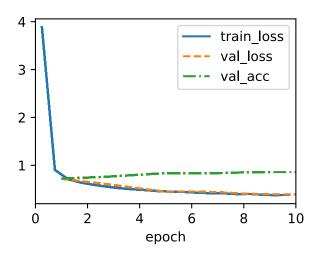
Extracting ../data/FashionMNIST/raw/t10k-labels-idx1-ubyte.gz to ../data/FashionMNIST/raw

```
[]: trainer = d21.Trainer(max_epochs=10, num_gpus=1) trainer.fit(model, data)
```



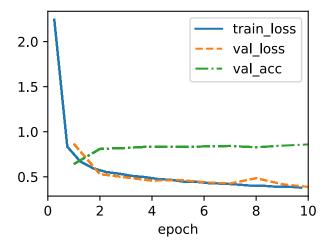
Adjust number of hiddens:

```
[]: trainer = d21.Trainer(max_epochs=10, num_gpus=1)
trainer.fit(model, data)
```



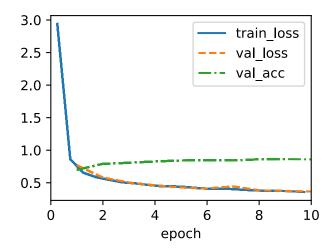
Adjust the number of MLP hiddens:

```
[]: trainer = d21.Trainer(max_epochs=10, num_gpus=1) trainer.fit(model, data)
```



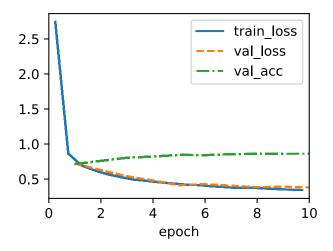
Adjust the number of heads:

```
[]: trainer = d21.Trainer(max_epochs=10, num_gpus=1)
trainer.fit(model, data)
```



Adjust the number of blocks:

```
[]: trainer = d21.Trainer(max_epochs=10, num_gpus=1) trainer.fit(model, data)
```



Combine it all together:

[]: trainer = d21.Trainer(max_epochs=10, num_gpus=1) trainer.fit(model, data)

