

# 1 Python

## 1.1 getting started with the code

**in a python script:**

Save your new python script in the folder `flow_polytopes/` at the top of it include the lines:

```
from graph_cal import *
from quiver_cal import *
```

Then use any of the functions listed below!

**in a python shell:**

navigate to the folder `flow_polytopes/`

```
>>> from graph_cal import *
>>> from quiver_cal import *
```

**Building a first quiver:**

In python, the quiver  $Q$  is represented using either a list of arrows  $[(a_i, b_i)]$  for  $a_i, b_i \in Q_0$ ,  $i = 0, \dots, |Q_1|$ . or as a numpy matrix:

$$a_{ij} = \begin{cases} 1, & \text{if head of arrow } j \text{ is vertex } i \\ -1, & \text{if tail of arrow } j \text{ is vertex } i \\ 0, & \text{otherwise} \end{cases}$$

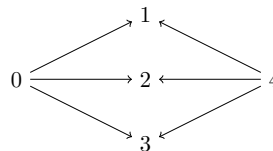
There is also functionality to go between the two representations of a quiver, as shown below.

**Example:** The code to represent the quiver shown below is given in two ways as a sample:

`sampleScript.py`:

```
from numpy import *
from graph_cal import *
from quiver_cal import *

Q_list = [(0,1),(0,2),(0,3),(4,1),(4,2),(4,3)]
Q_mat = matrix([
    [-1,-1,-1, 0, 0, 0],
    [ 1, 0, 0, 1, 0, 0],
    [ 0, 1, 0, 0, 1, 0],
    [ 0, 0, 1, 0, 0, 1],
    [ 0, 0, 0,-1,-1,-1]
])
```



## 1.2 available functions

To obtain all  $d$ -dimensional quivers:

```
Qs = all_possible_graphs(d)
```

Get the polytope associated to the quiver  $Q$ :

```
flow_polytope(Q)
```

Generate all the subquivers of  $Q$

`subquivers(Q)`

Get all subsets of the vertices of  $Q$  that are closed under arrows:

`subsets_closed(M)`

Calculates weights of the vertices that are inherited from the weights on the arrows

`theta(Q)`

Is the subquiver  $subQ$  stable?

`is_stable(Q, subQ)`