ISy
E6739 Homework 1

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2-19

a)

$$A' = 3, 5, 6, 8$$

b)

$$A \cap B = 1, 2$$

c)

$$(A\cap B)\cup C=1,2,3,4,5$$

d)

$$(B \cup C)' = 7,8$$

e)

$$(A \cap B)' \cup C = 1, 3, 4, 5, 6, 7, 8$$

2-81

a)

$$P(A) = \frac{52^8}{62^8} = 0.2448461$$

52^8/62^8

[1] 0.2448461

b)

$$P(B) = \frac{10^8}{62^8} = 4.580011e - 7$$

10^8/62^8

[1] 4.580011e-07

c)

$$P(B \ge 1) = 1 - P(A) = 0.7551539$$

1 - 52^8/62^8

[1] 0.7551539

d)

$$P(B=2) = \frac{\binom{8}{6} \times 10^2 \times 52^6}{62^8} = 0.2535389$$

(choose(8,6)*10^2*52^6)/(62^8)

[1] 0.2535389

2-90

a)

$$P(A) = \frac{\binom{5}{1} \times 36^5}{36^6} = 5/36 \approx 0.138889$$

 $(choose(5,1)*36^5)/36^6$

[1] 0.1388889

b)

$$P(B) = \frac{\binom{5}{1} \times 36^5}{36^6} = 5/36 \approx 0.138889$$

 $(choose(5,1)*36^5)/36^6$

[1] 0.1388889

c)

$$P(A \cap B) = P(A) \cdot P(B) = \frac{25}{36^2} \approx 0.019290$$

(5/36) * (5/36)

[1] 0.01929012

d)

$$P(A \cup B) = P(A) + P(B) - P(A \cap B) = \frac{5}{36} + \frac{5}{36} - \frac{25}{36^2} = 0.258487$$

 $(5/36) + (5/36) - (25/36^2)$

[1] 0.2584877

2-141

a)

$$P(A|B') = \frac{P(A \cap B')}{P(B')} = \frac{P(A)}{1 - P(B)} = \frac{P(A)}{1 - P(B)}$$

$$P(A) = \frac{52^8}{62^8}; P(B) = \frac{10^8}{62^8}$$

$$\therefore P(A|B') = \frac{\frac{52^8}{62^8}}{1 - \frac{10^8}{62^8}} = 0.24484$$

((52^8/62^8)/(1-(10^8/62^8)))

[1] 0.2448462

b)

$$P(A'\cap B) = P(A'|B)P(B) = P(B) = \frac{10^8}{62^8} = 4.580011e - 7$$
 B is a subset of A' so $P(A'|B) = 1$

10^8/62^8

[1] 4.580011e-07

c)

Let T be passwords with exactly 2 integers and I be passwords with at least 1 integer. $P(T|I) = \frac{P(T \cap I)}{P(I)} = \frac{P(T)}{P(I)}$ Since P(T) is a subset of P(I), $\frac{P(T \cap I)}{P(I)} = \frac{P(T)}{P(I)}$

From 2-81 part d, P(T) = 0.2535From 2-81 part c, P(I) = 0.7551 $\therefore P(T|I) = \frac{0.2535}{0.7551} = 0.3357$

0.2535/0.7551

[1] 0.3357171

2-179

a)

$$P(F|S) = 0.6; P(F|V) = 0.04 \\ P(F) = P(F|S)P(S) + P(F|V)P(V) = 0.6 \times 0.2 + 0.04 \times 0.8 = 0.152$$

0.6*0.2 + 0.8*0.04

[1] 0.152

b)

$$P(S|F) = \frac{P(F|S)P(S)}{P(F)} = \frac{0.6 \times 0.2}{0.152} = 0.78947$$

(0.6*0.2)/0.152

[1] 0.7894737

c)

$$P(V|F') = \frac{P(F'|V)P(V)}{P(F')} = \frac{0.96 \times 0.8}{1-0.152} = 0.90566$$

(0.96*0.8)/(1-0.152)

[1] 0.9056604

$\mathbf{Q2}$

$$\binom{13}{1}\binom{4}{3}\binom{12}{2}\binom{4}{1}\binom{4}{1}=54,912$$

 $\verb|choose(13,1)| * \verb|choose(4,3)*| choose(12,2)*| choose(4,1)^2|$

[1] 54912