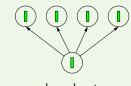




Scientific Computing

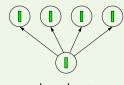
Parallele Algorithmen

Collective Communication

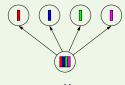


broadcast

Collective Communication

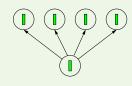


broadcast

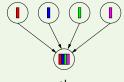


scatter

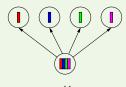
Collective Communication



broadcast

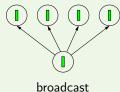


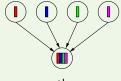
gather



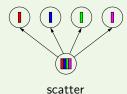
scatter

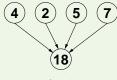
Collective Communication





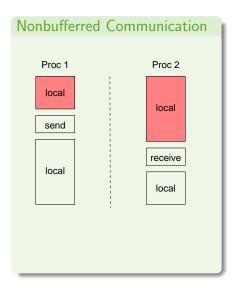
gather

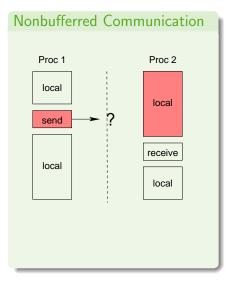




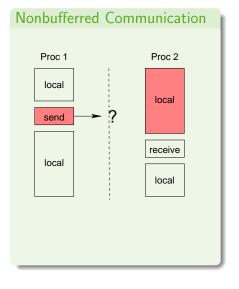
reduction

```
Point-to-Point Communication
Example 1: Hello world
char msg[20];
int myrank;
int tag = 99;
MPI_Status status;
MPI_Comm_rank( MPI_COMM_WORLD, &myrank);
if (myrank == 0) {
    strcpy( msg, "Hello world!");
   MPI_Send( msg, strlen( msg) + 1, MPI_CHAR, 1, tag, MPI_COMM_WORLD);
}
else if (myrank == 1) {
    MPI_Recv( msg, 20, MPI_CHAR, 0, tag, MPI_COMM_WORLD, &status);
   printf( "%s\n", msg);
```

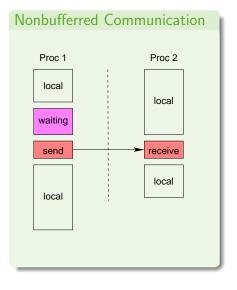




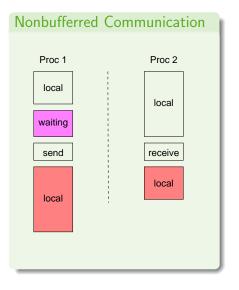
1. P1 has to wait till P2 is ready, if there is no/not enough buffer.



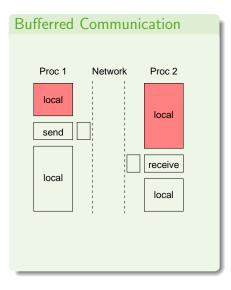
- 1. P1 has to wait till P2 is ready, if there is no/not enough buffer.
- 2. P1 will not continue, P1 is blocked.

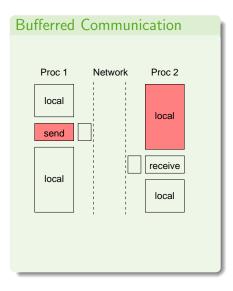


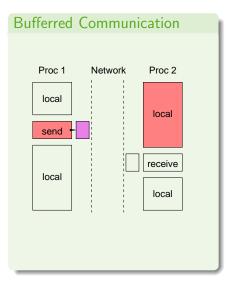
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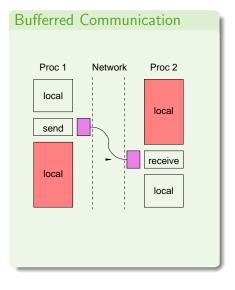
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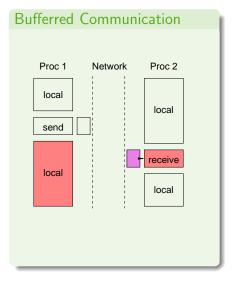




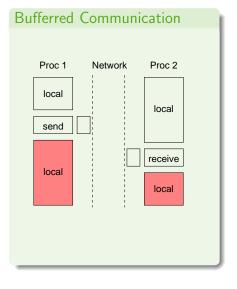
1. P1 copies data to buffer.



- 1. P1 copies data to buffer.
- 2. P1 continues.



- 1. P1 copies data to buffer.
- 2. P1 continues.
- 3. P2 will continue work after receiving data.



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 - architecture.
 - operating system,
 - MPI implementation.

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Problem: How large is the system buffer?

- Programs may fail due to system buffer exhaustion.
- ► Too bad: system buffer size depends on
 - architecture.
 - operating system,
 - MPI implementation.
- Portability of code restricted.

What makes a Message?

Message Envelope Data Source
Destination
Tag
Communicator
Data

MPI_Send

```
int MPI_Send( void *buffer,
                                      /* address of send buffer
                                                                      */
              int count.
                                      /* number of entries in buffer
                                                                     */
                                                                      */
              MPI_Datatype datatype, /* datatype of entry
              int destination
                                     /* rank of destination
                                                                      */
                                                                      */
                                     /* message tag
              int tag,
              MPI_Comm communicator /* communicator
                                                                      */
```

- Standard blocking send operation.
- Assembles message envelope.
- ▶ Sends message to destination.
- May return as soon as message is handed over to 'system' (buffered communication).
- May wait for corresponding receive operation (unbuffered communication).
- ▶ Buffering behaviour is implementation-dependent.
- ▶ No synchronization with receiver (guaranteed).

```
MPI_Recv
```

```
int MPI_Recv(void *buffer,
                                   /* OUT : address of receive buffer */
             int count,
                                   /* IN : maximum number of entries */
             MPI_Datatype datatype, /* IN
                                           : datatype of entry
                                                                       */
                                   /* IN
                                           : rank of source
             int source
                                                                       */
                                    /* IN
                                                                       */
             int tag,
                                           : message tag
             MPI_Comm communicator, /* IN
                                           : communicator
                                                                       */
             MPI_Status *status /* OUT : return status
                                                                       */
```

- Standard blocking receive operation.
- ▶ Receives message from source with tag.
- ► Disassembles message envelope.
- Stores message data in buffer.
- Returns not before message is received.
- Returns additional status data structure.

Receiving messages from any source?
Use wildcard source specification MPI_ANY_SOURCE.

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- Receiving messages with any tag?
 Use wildcard tag specification MPI_ANY_TAG
- Message buffer larger than message? Don't worry, superfluous buffer fields remain untouched.
- Message buffer smaller than message?
 Message is truncated, no buffer overflow.
 MPI_Recv returns error code MPI_ERR_TRUNCATE.

Deadlock I

٦	Гime	Process A	Process B
	1	MPI_Send to B, tag $= 0$	local work
	2	MPI_Send to B, $tag=1$	local work
	3	local work	MPI_Recv from A, tag $=1$
	4	local work	MPI_Recv from A, tag $= 0$

Deadlock I

Time	Process A	Process B
1	MPI_Send to B, tag $= 0$	local work
2	MPI_Send to B, tag $= 1$	local work
3	local work	<code>MPI_Recv</code> from A, tag $=1$
4	local work	MPI_Recv from A, tag $= 0$

► The program will deadlock, if system provides no buffer.

Deadlock I

Time	Process A	Process B
1	MPI_Send to B, tag $= 0$	local work
2	MPI_Send to B, tag $=1$	local work
3	local work	MPI_Recv from A, tag $=1$
4	local work	$ exttt{MPI_Recv from A, tag} = 0$

- ▶ The program will deadlock, if system provides no buffer.
- ▶ Process A is not able to send message with tag=0.

Deadlock I

Time	Process A	Process B
1	MPI_Send to B, tag $= 0$	local work
2	MPI_Send to B, tag $=1$	local work
3	local work	MPI_Recv from A, tag $=1$
4	local work	MPI_Recv from A, tag $= 0$

- ▶ The program will deadlock, if system provides no buffer.
- ▶ Process A is not able to send message with tag=0.
- ▶ Process B is not able to receive message with tag=1.

Deadlock II

Time	Process A	Process B
1	MPI_Send to B	MPI_Send to A
2	MPI_Recv from B B	MPI_Recv from A

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Deadlock II

Time	Process A	Process B
1	MPI_Send to B	MPI_Send to A
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- ▶ The program will deadlock, if system provides no buffer.
- ▶ Process A and Process B are not able to send messages.

Communication with MPI

Deadlock II

Time	Process A	Process B
1	MPI_Send to B	MPI_Send to A
2	MPI_Recv from B B	MPI_Recv from A

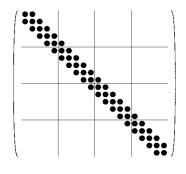
- The program will deadlock, if system provides no buffer.
- ▶ Process A and Process B are not able to send messages.
- ► Order communications in the right way!

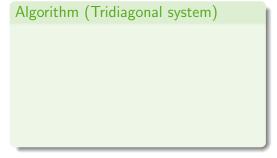
Communication with MPI

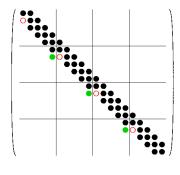
Example: Exchange of messages

```
if (myrank == 0) {
    MPI_Send( sendbuf, 20, MPI_INT, 1, tag, communicator);
    MPI_Recv( recvbuf, 20, MPI_INT, 1, tag, communicator, &status);
}
else if (myrank == 1) {
    MPI_Recv( recvbuf, 20, MPI_INT, 0, tag, communicator, &status);
    MPI_Send( sendbuf, 20, MPI_INT, 0, tag, communicator);
}
```

- ▶ This code succeeds even with no buffer space at all !!!
- ▶ Important note: Code which relies on buffering is considered unsafe !!!

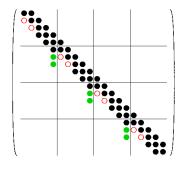






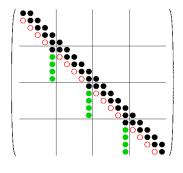
Algorithm (Tridiagonal system)

1. Eliminate in each diagonal block subdiagonal elements.



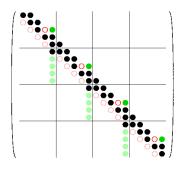
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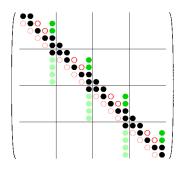


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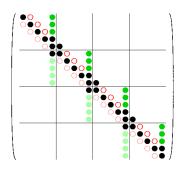
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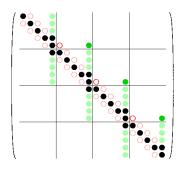
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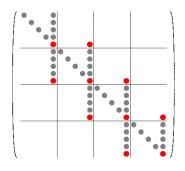
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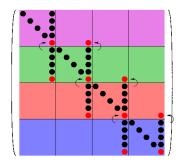
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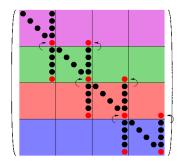
Results in a tridiagonal subsystem with unknowns x_5 , x_{10} , x_{15} , x_{20} .



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Results in a tridiagonal subsystem with unknowns x_5 , x_{10} , x_{15} , x_{20} . If data are stored rowwise only one communication to neighbouring processor neccessary.