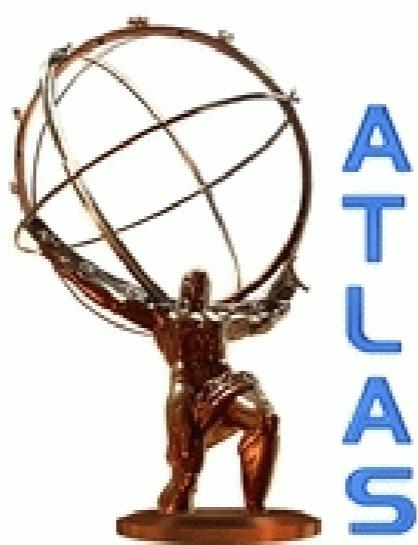


A Search for 2nd-generation Leptoquarks in $p\bar{p}$ Collisions at $\sqrt{s} = 7 \text{ TeV}$ with the ATLAS Detector

Burton DeWilde
Dissertation Defense
20 June 2012



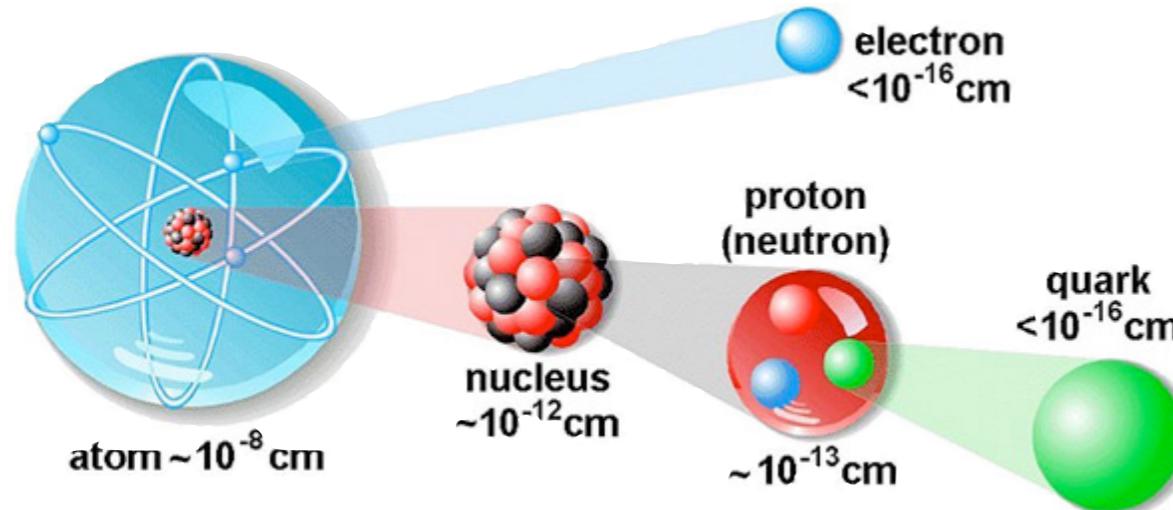
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- **Introduction**
 - Standard Model
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 - Large Hadron Collider
 - ATLAS detector
- **Event Simulation and Reconstruction**
- **A Leptoquark Search**
 - physics object and event selection
 - backgrounds and control regions
 - multivariate discriminant
 - limit-setting and results
 - future outlook
- **Conclusion**

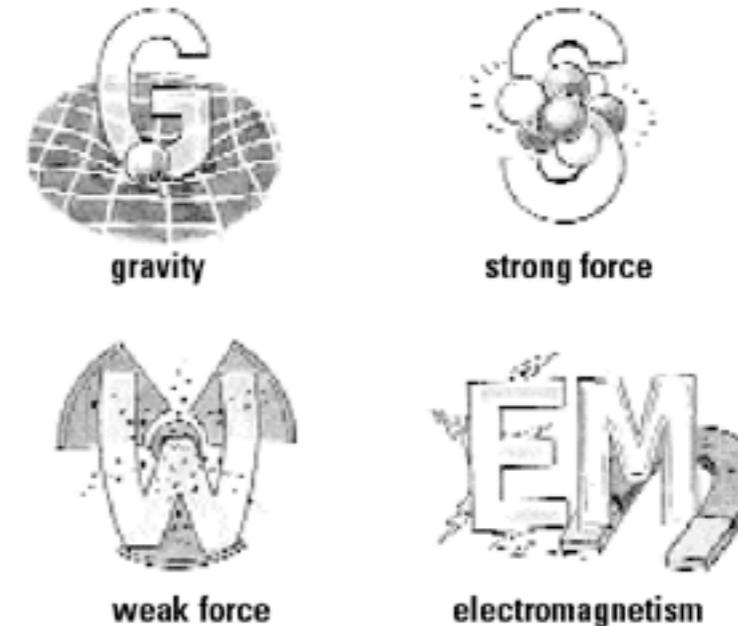


Particle Physics

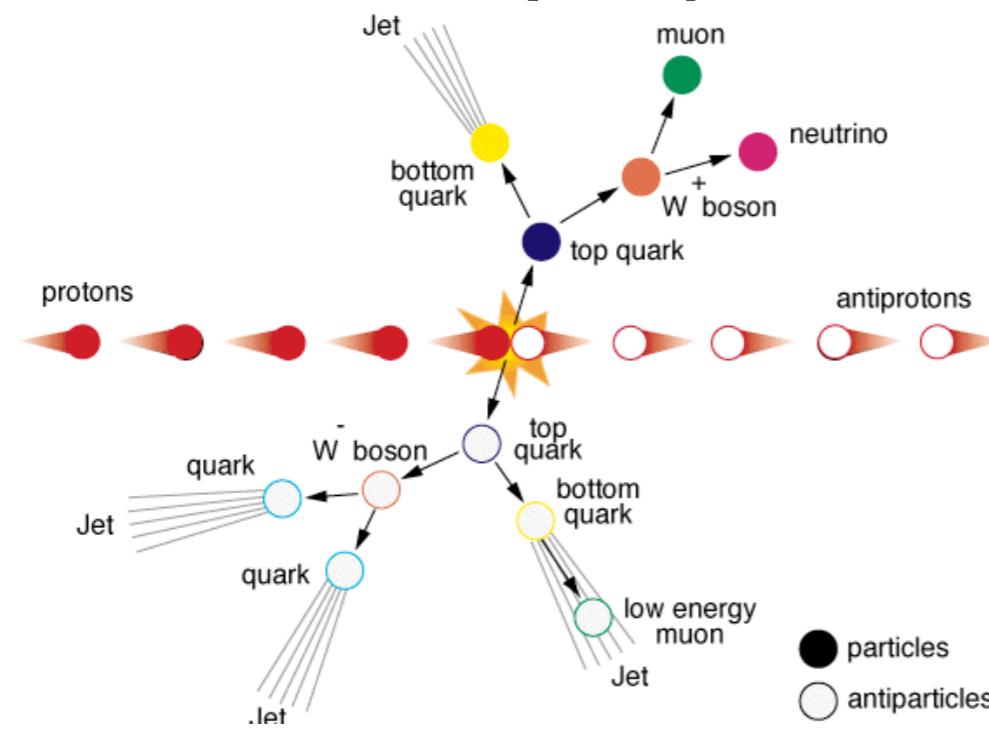
Study of fundamental particles of matter...



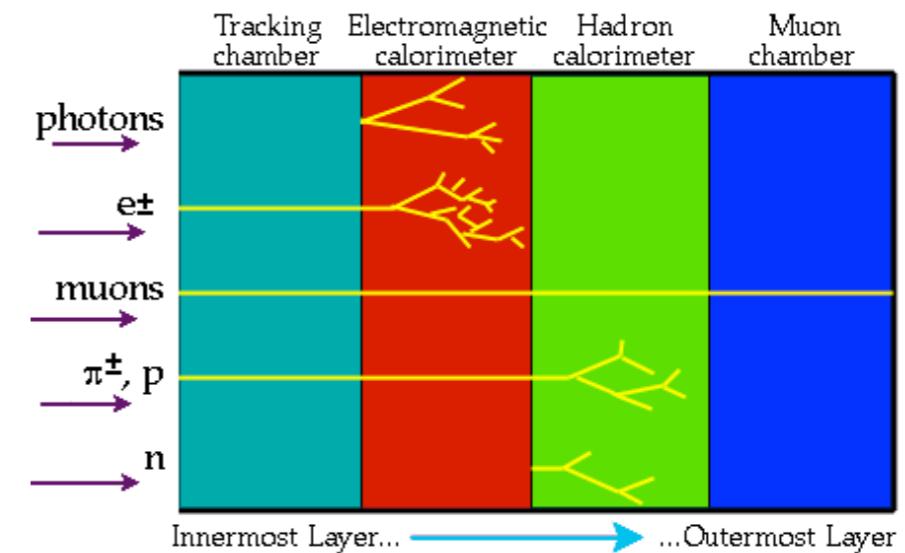
... and their interactions...



... through particle scattering
and decay experiments...



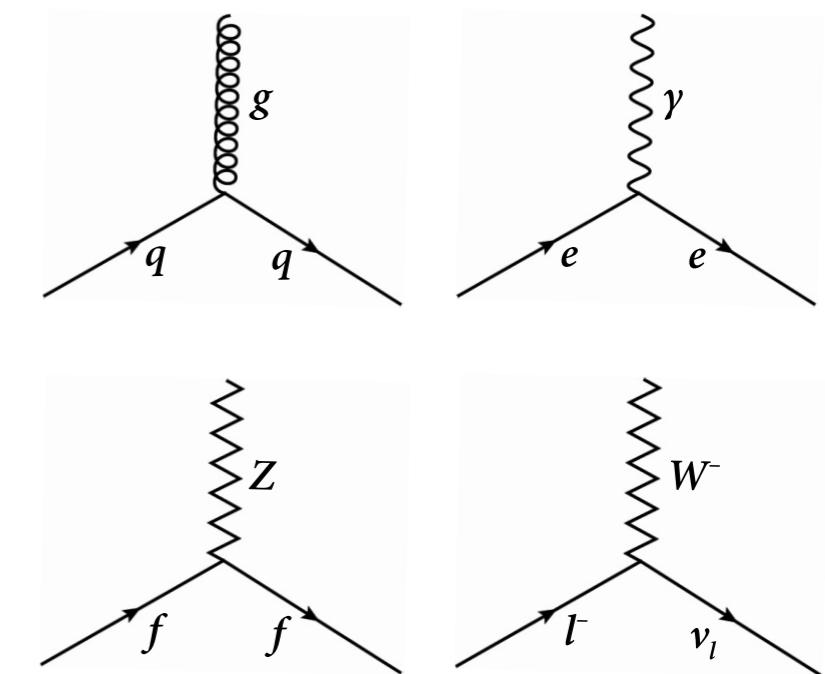
... recorded by particle detectors.



Standard Model (SM)

- Quantum Field Theory describing strong, weak, and electromagnetic interactions of elementary particles of matter
- Particles: quarks and leptons (spin-1/2 fermions), force mediators (spin-1 bosons)
 - spin, mass, electric charge, ...
 - three like generations
 - anti-particle for each
- Interactions via boson exchange: strong (gluons), weak (W^\pm , Z), electromagnetic (γ)
- Incomplete theory
 - no gravity, dark matter/energy
 - many free parameters, unanswered questions, ...

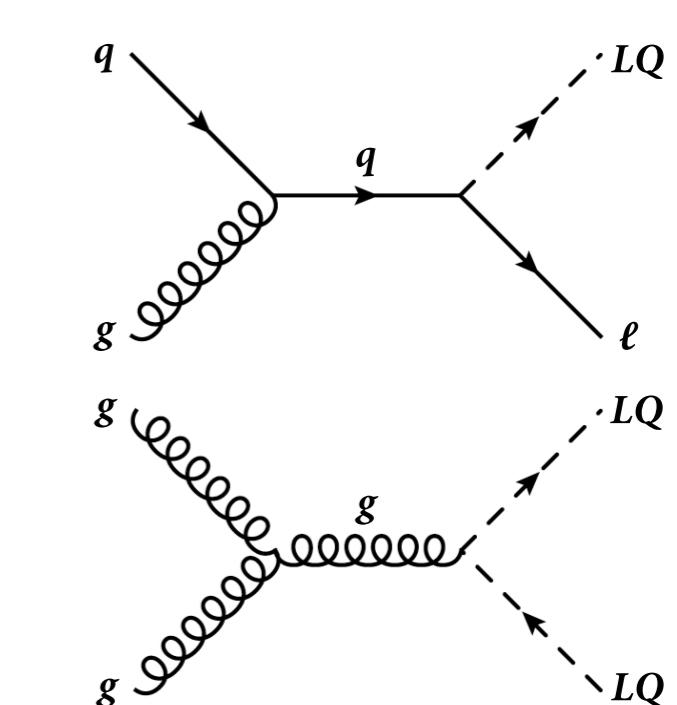
quarks	u	c	t	g	force mediators
leptons	d	s	b	W^\pm	
	ν_e	ν_μ	ν_τ	Z	
	e	μ	τ	γ	
	1	2	3	H	



Leptoquarks (LQs)

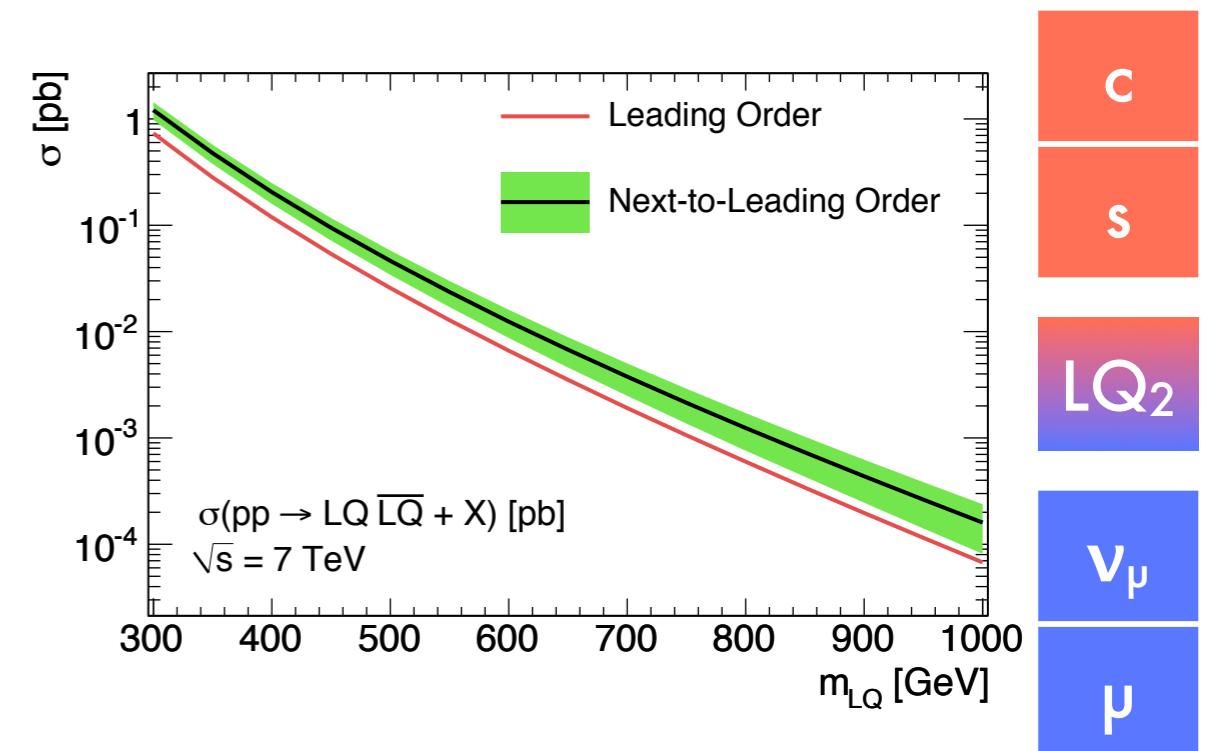
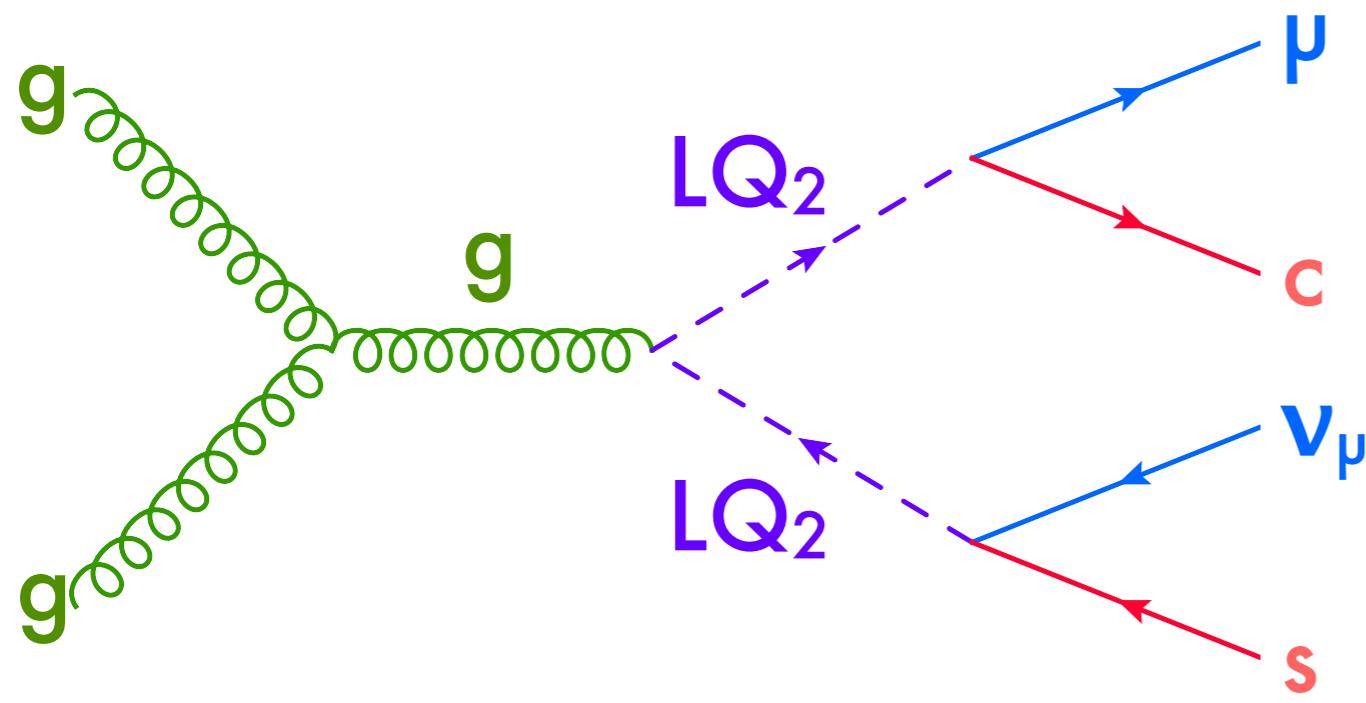
- Apparent symmetry between quarks and leptons, suggestive of fundamental relation
- Many “Beyond the SM” theories allow new interactions between quarks and leptons
- Leptoquarks: hypothetical bosons with lepton and baryon number, electric and color charge
 - scalar (spin-0) or vector (spin-1)
 - couple directly to lepton-quark pairs, strength λ_{lq}
- Experimental constraints => three generations, conserve L and B numbers
- Single- or pair-production at LHC: gluon fusion dominant, plus quark annihilation

quarks	u	c	t
	d	s	b
	LQ ₁	LQ ₂	LQ ₃
leptons	v _e	v _μ	v _τ
	e	μ	τ
	1	2	3

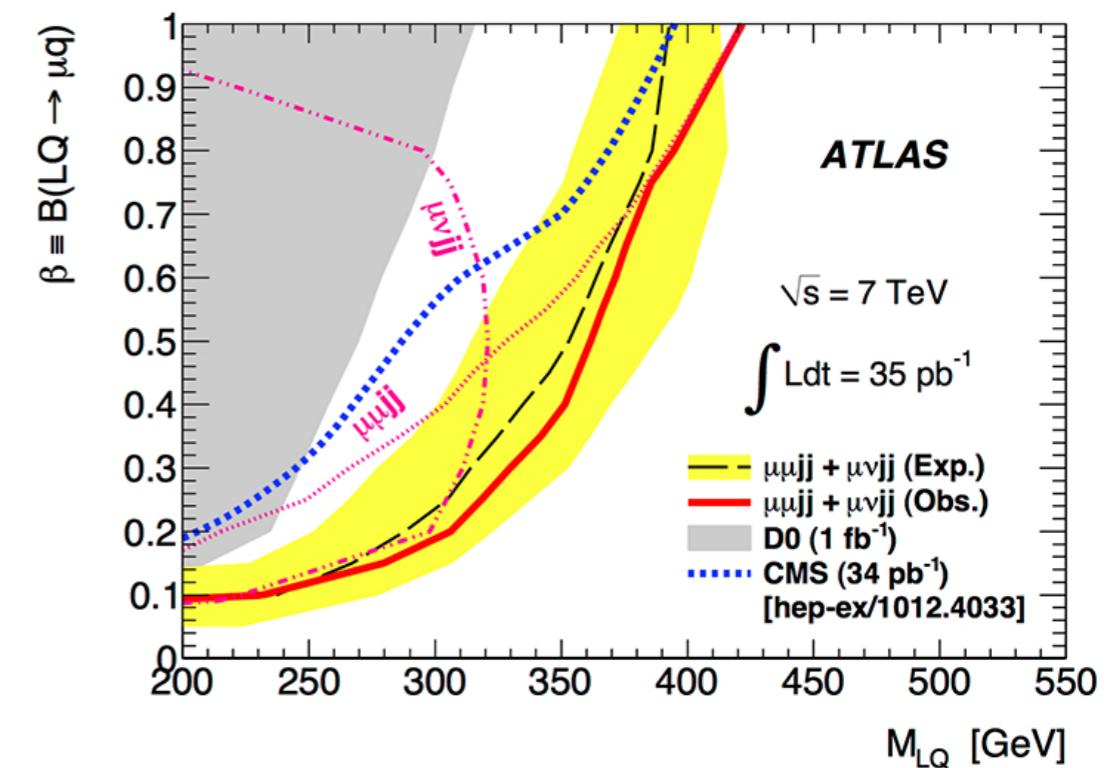


LQ Searches

- Scalar, pair-produced
 - large, model-independent cross section σ_{LQ} dependent “only” on m_{LQ}
- Three final states: $llqq$, $lvqq$, $vvqq$
 - branching ratio of LQ to a quark and a charged lepton $\beta = BR(LQ \rightarrow lq)$
- My search: 2nd-generation, μvqq (maximal at $\beta = 0.5$)

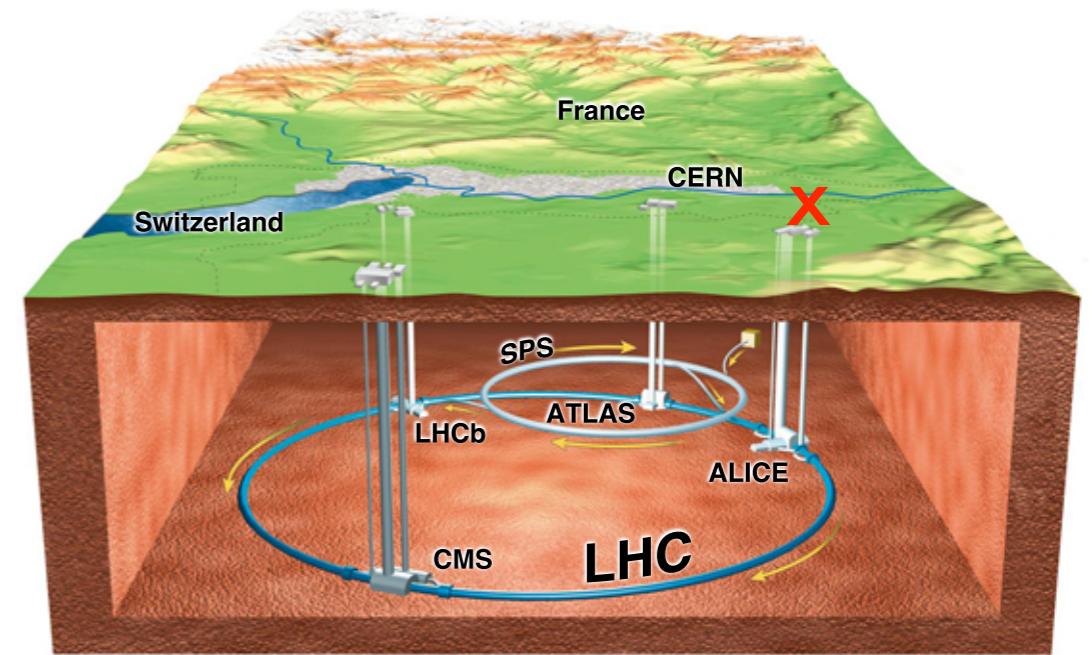


existing experimental limits:

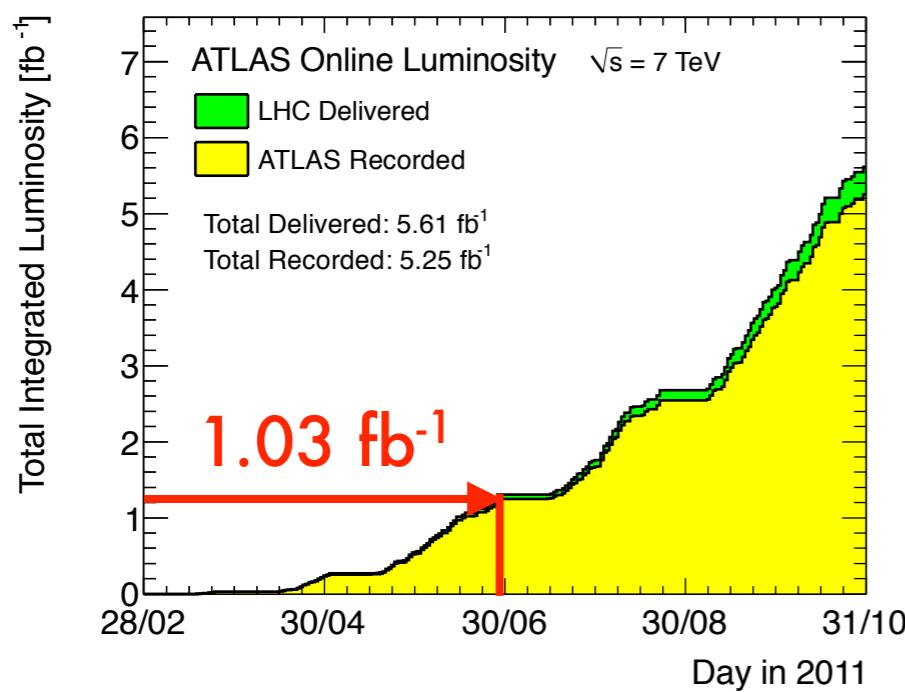
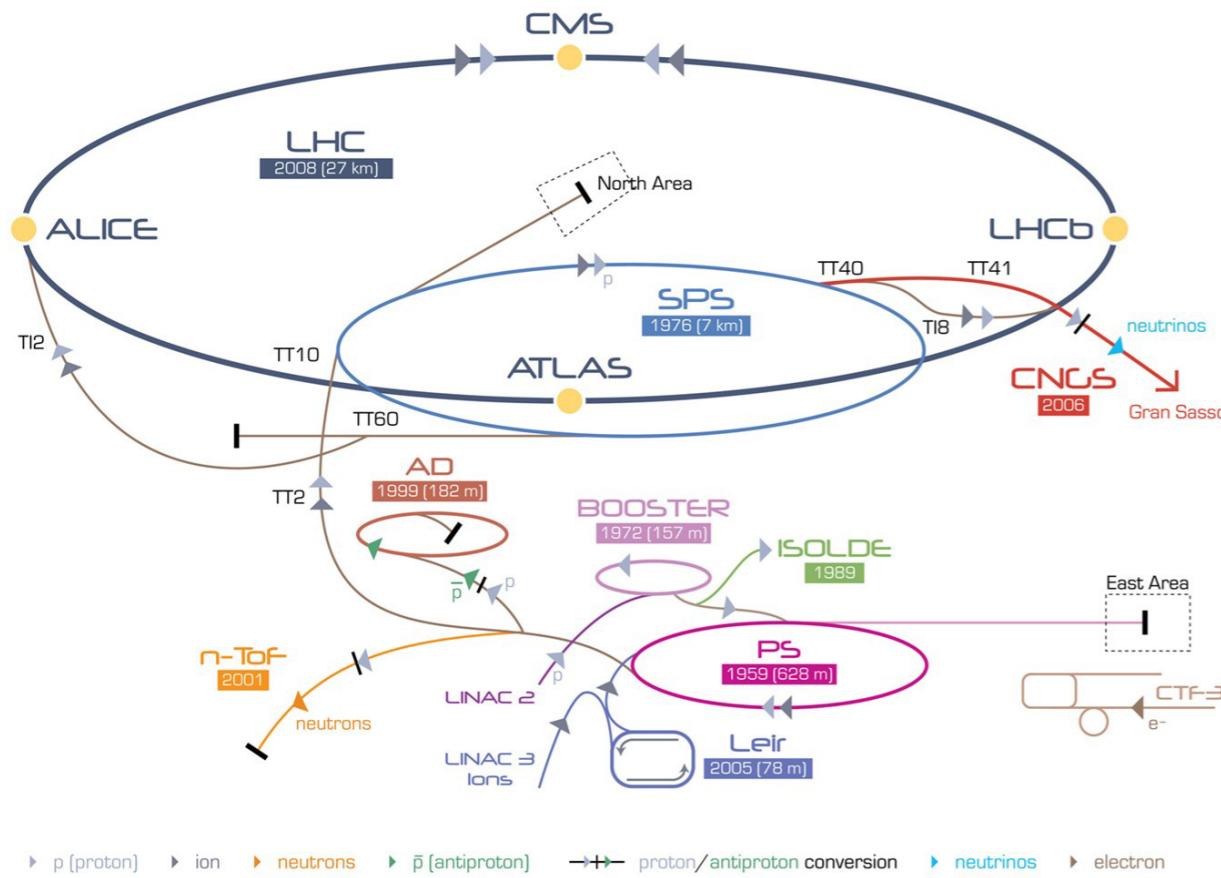


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Large Hadron Collider (LHC)



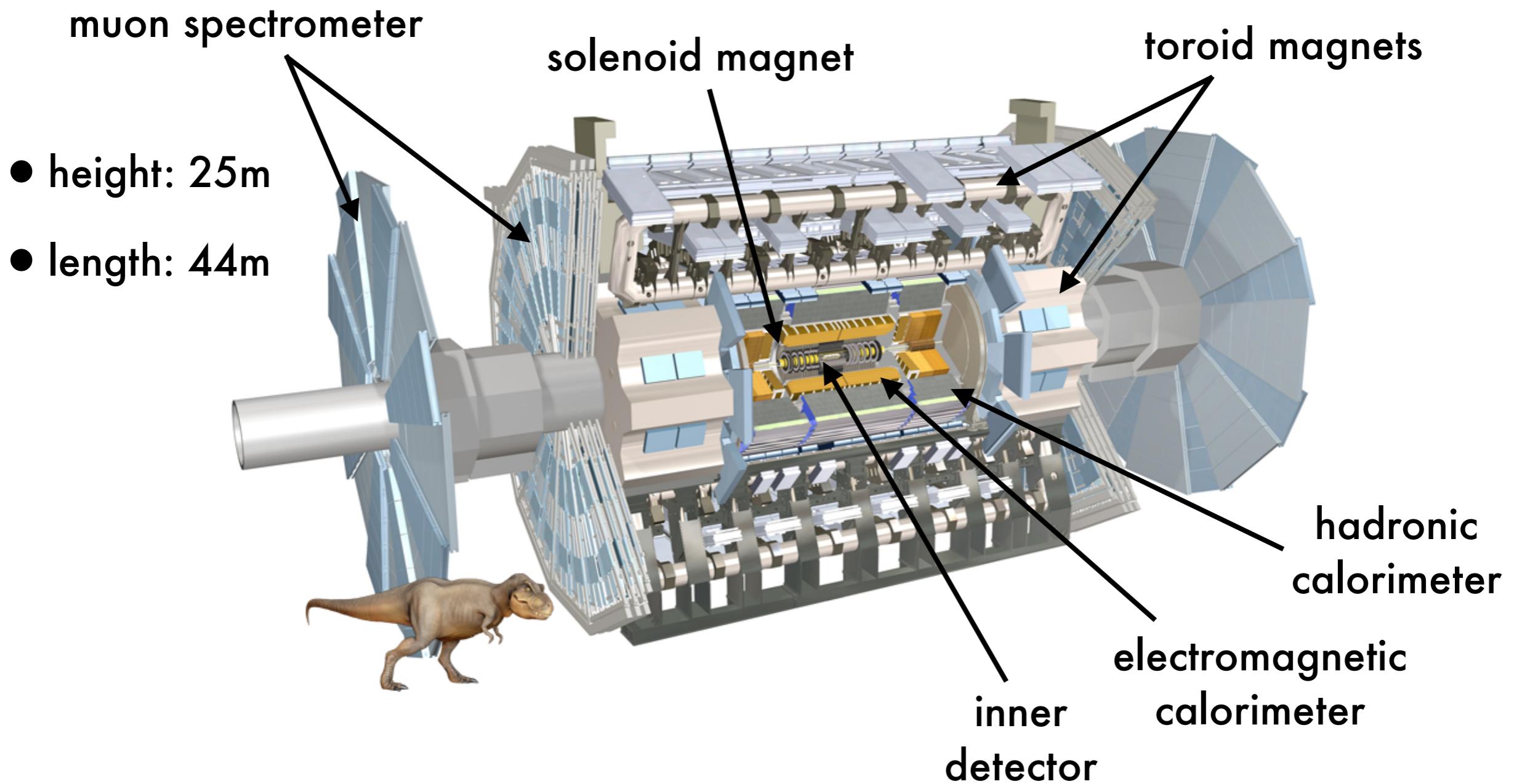
- Last, largest, most powerful link in CERN accelerator complex
- 27 km ring, accelerates then collides protons at $\sqrt{s} = 7 \text{ TeV}$
- protons grouped into bunches into beams, cross at four points on ring
- high energy => small distances, massive particles
- high luminosity => high rate of interactions, many events
- Number of $L\bar{Q}LQ \rightarrow \mu\nu qq$ events:

$$\begin{aligned}
 N_{\text{evts}} &= \sigma_{LQ} \times L_{\text{int}} \times 2\beta(1-\beta) \\
 &= 0.0124 \text{ pb} \times 1035 \text{ pb}^{-1} \times 0.5 \\
 &\approx 6.4
 \end{aligned}$$

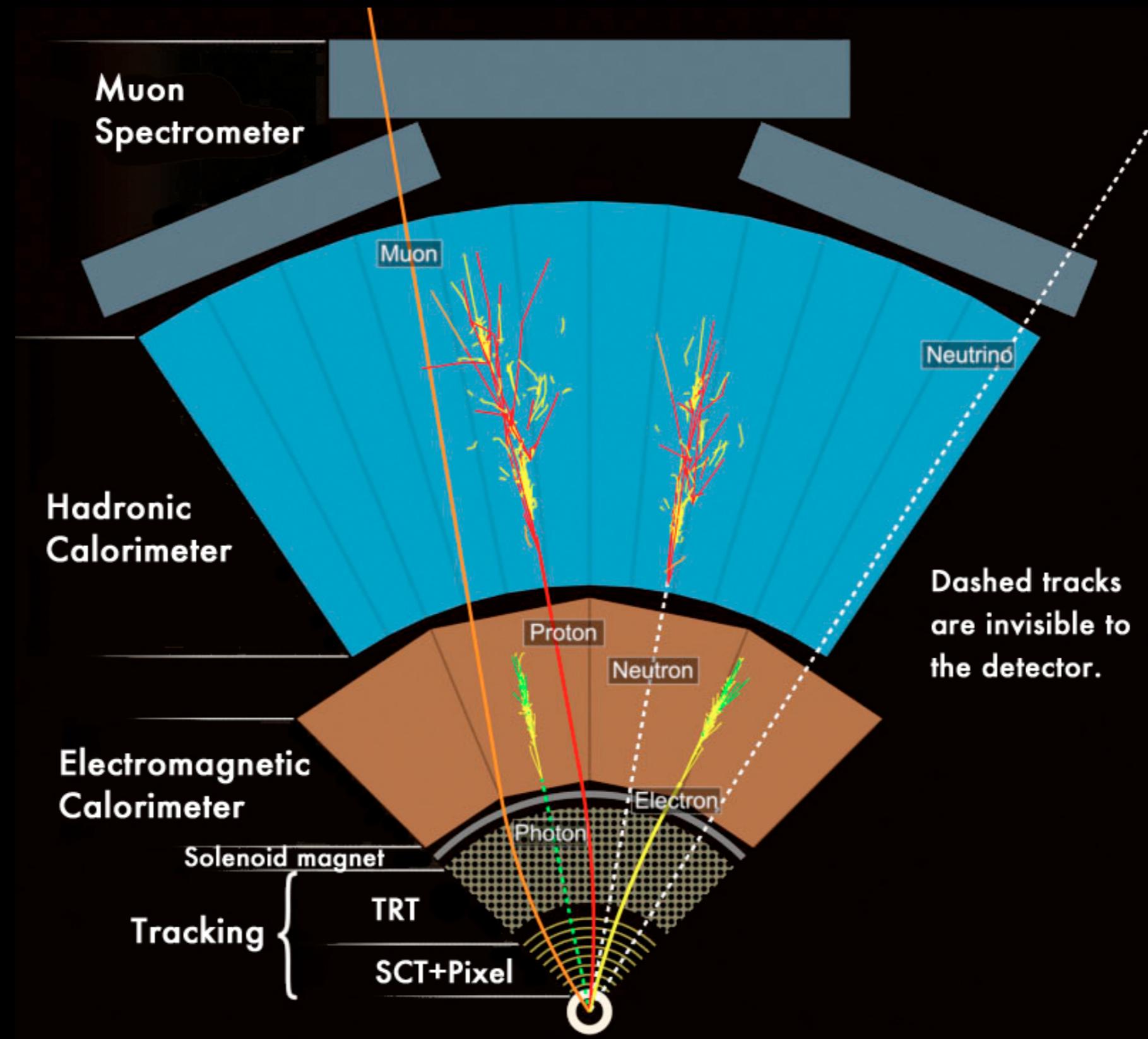
For $m_{LQ}=600 \text{ GeV}$, $\beta=0.5$

ATLAS Detector

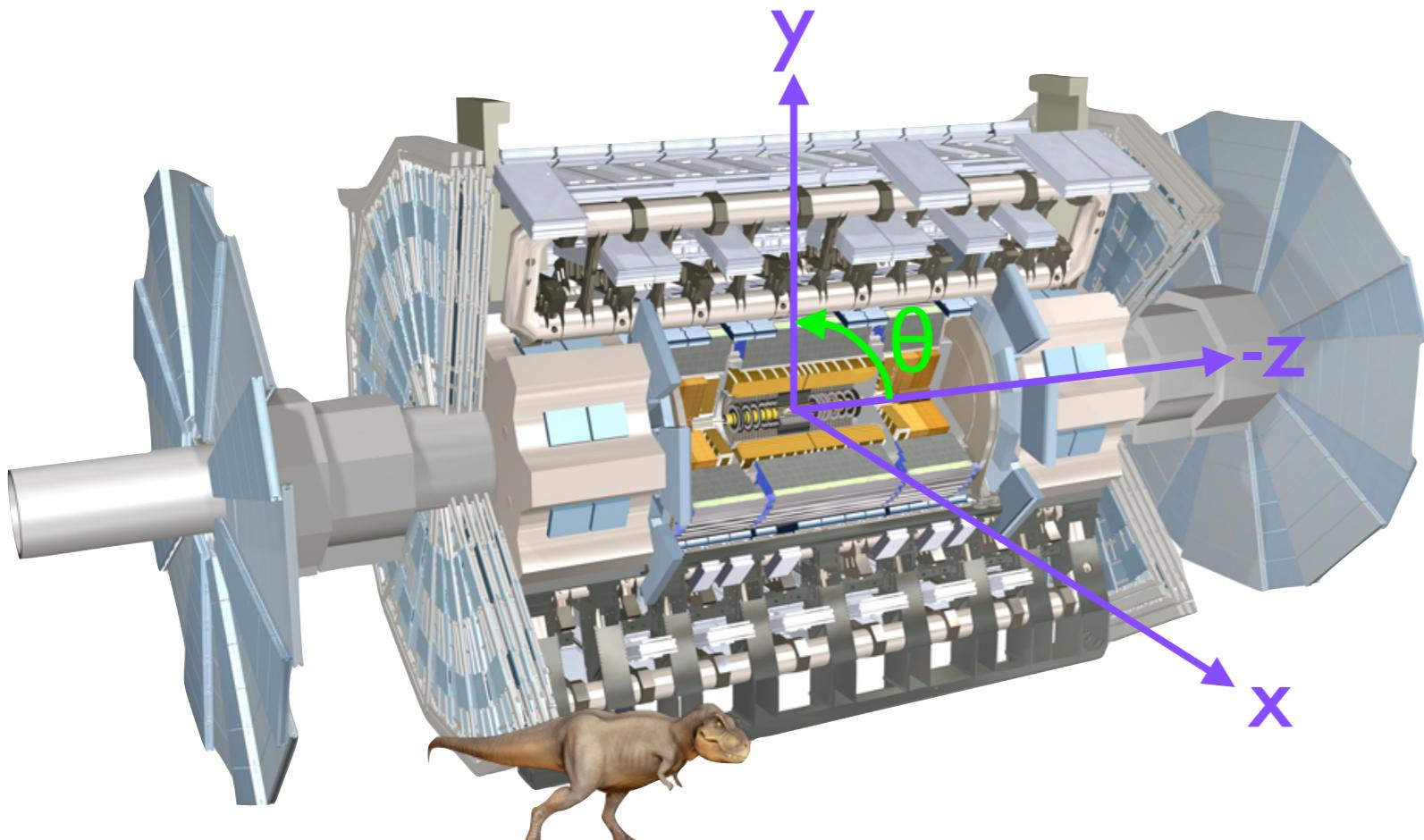
- Multi-purpose detector, forward-backward symmetric cylindrical geometry, nearly 4π coverage in solid angle



ATLAS Detector

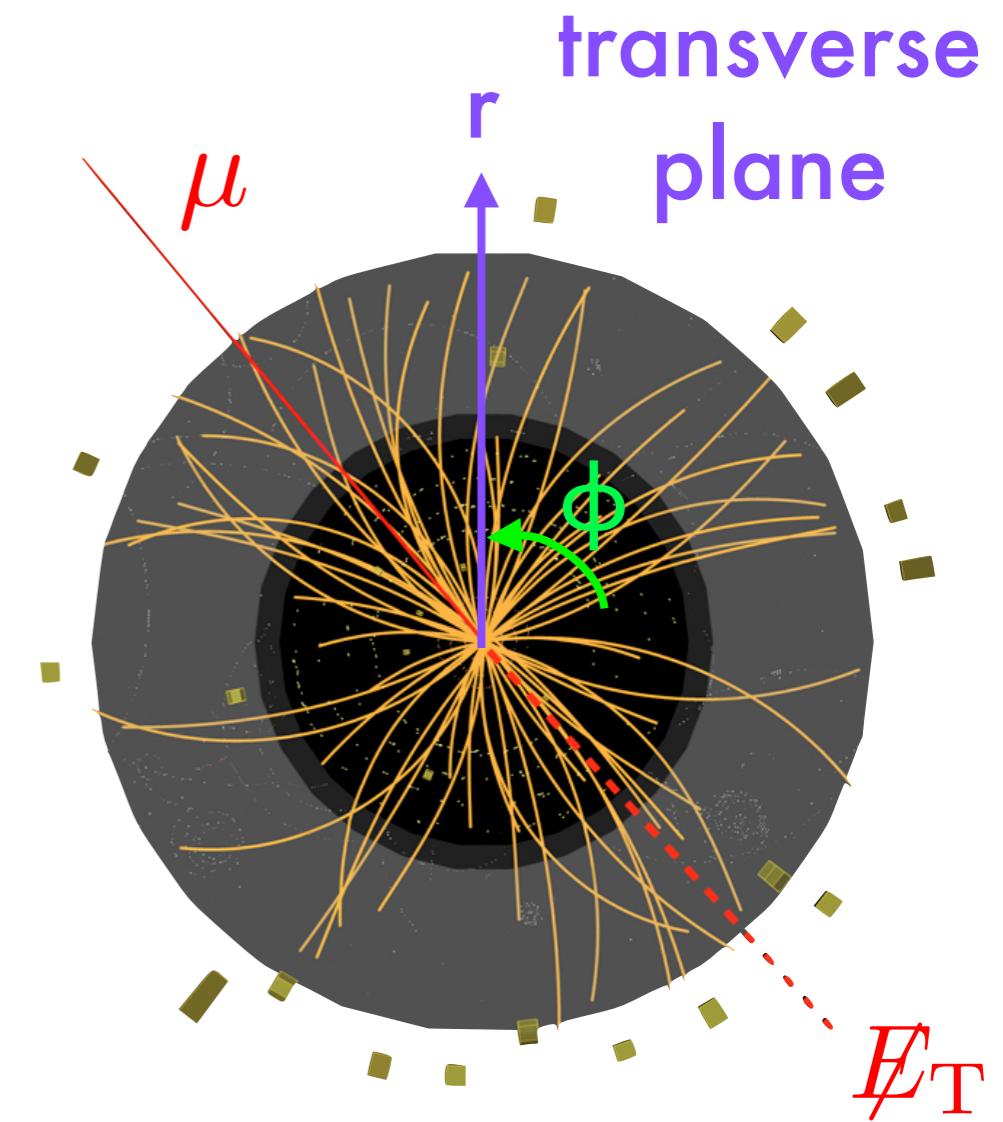


ATLAS Detector



pseudorapidity: $\eta \equiv -\ln \left(\tan \frac{\theta}{2} \right)$

angular separation: $\Delta R = \sqrt{(\Delta\phi)^2 + (\Delta\eta)^2}$



Outline

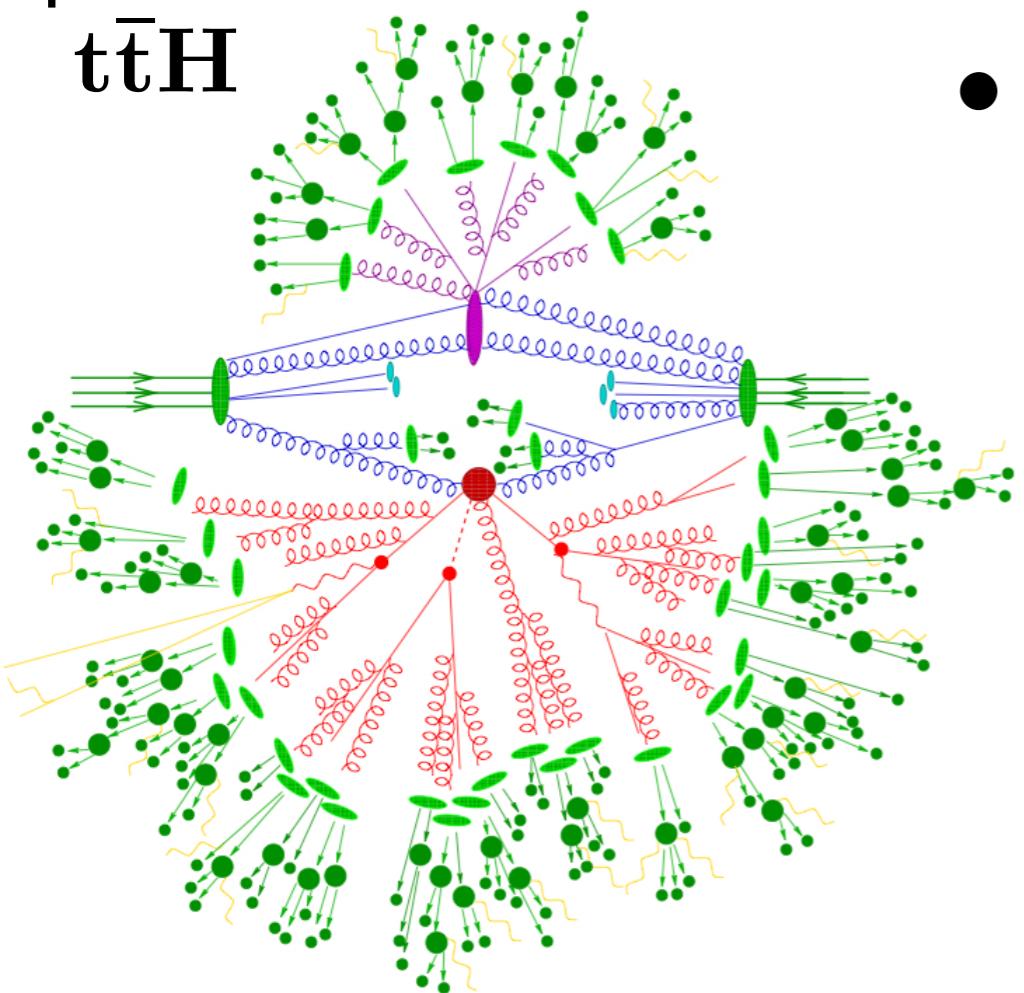
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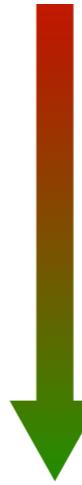


Monte Carlo (MC)

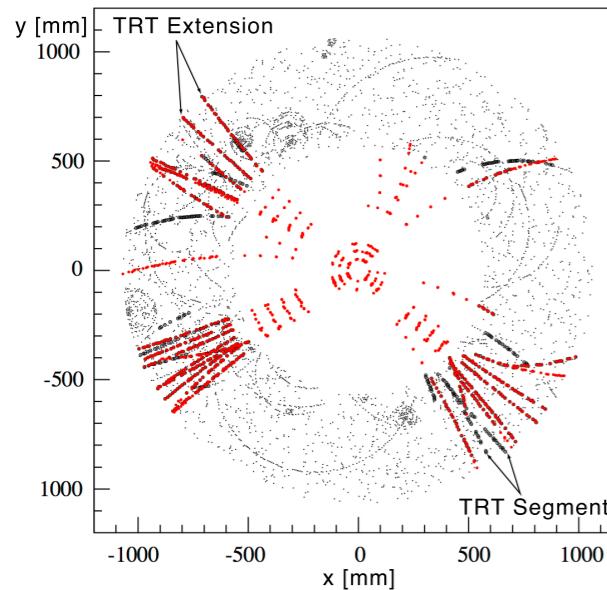
process:

$t\bar{t}H$

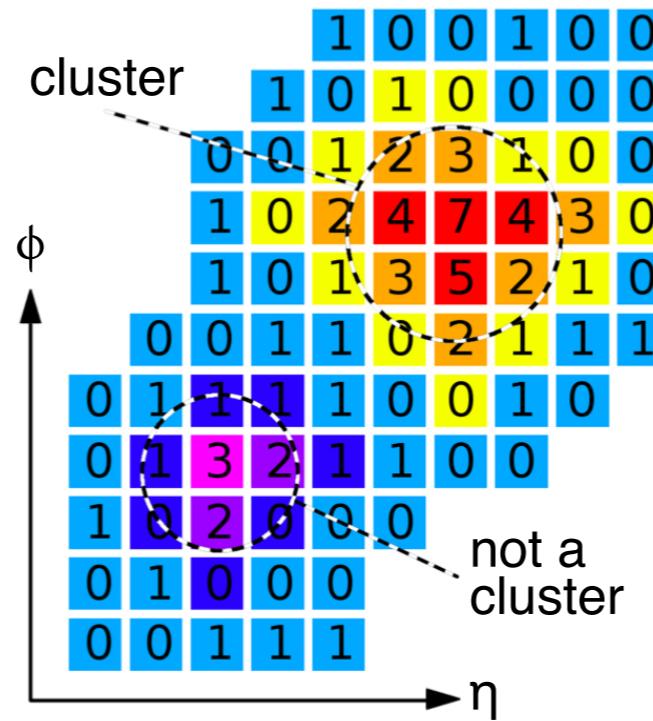
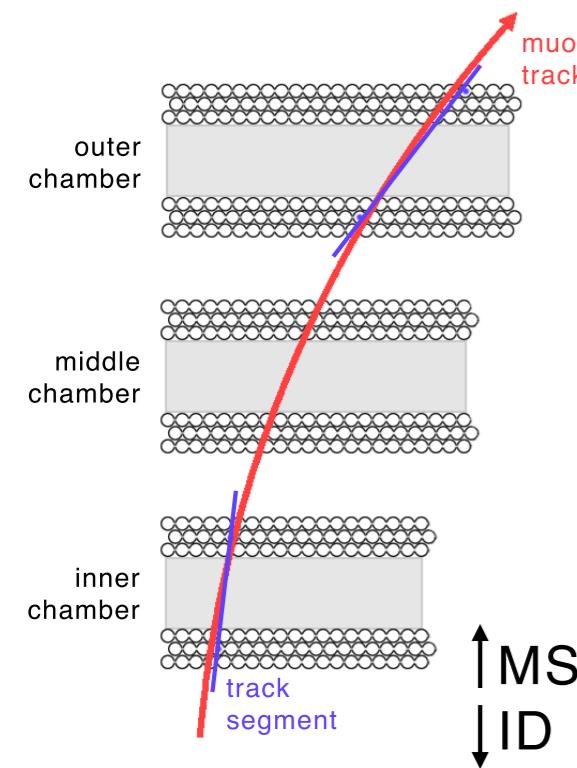
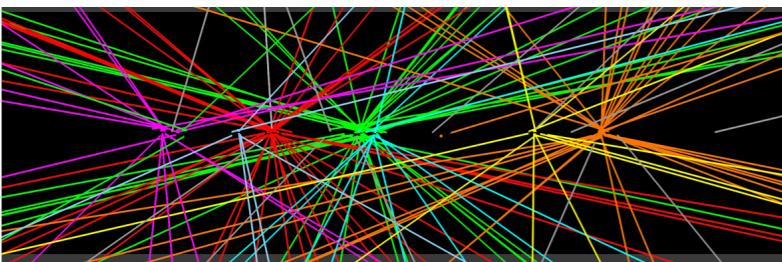


- Need predictions of both SM *background* and LQ *signal* events to compare with data
 - Given a theoretical model, event generators use Monte Carlo numerical methods to simulate each “phase” of an event:
 - hard scatter
 - parton showering
 - hadronization
 - decays
 - + underlying event
 - Result: simulated events samples as expected in Nature
 - Propagate MC particles through ATLAS simulation: interactions => measurements => reconstruction, just like data!
- 
Energy Scale
- + pile-up events from neighbor bunches

Event Reconstruction



- Pattern recognition algorithms reconstruct physics objects from raw detector data
 - **tracks:** sets of ID hits matched along trajectory of a charged particle
 - **vertices:** shared origin of neighboring tracks
 - **muons:** standalone MS track, may be statistically combined with matching ID track
 - **electrons:** ID track matched to EM energy cluster
 - **jets:** topologically related energy clusters grouped with anti- k_T algorithm ($R_c = 0.4$)
 - **MET:** negative vector sum of calorimeter E_T plus muon p_T



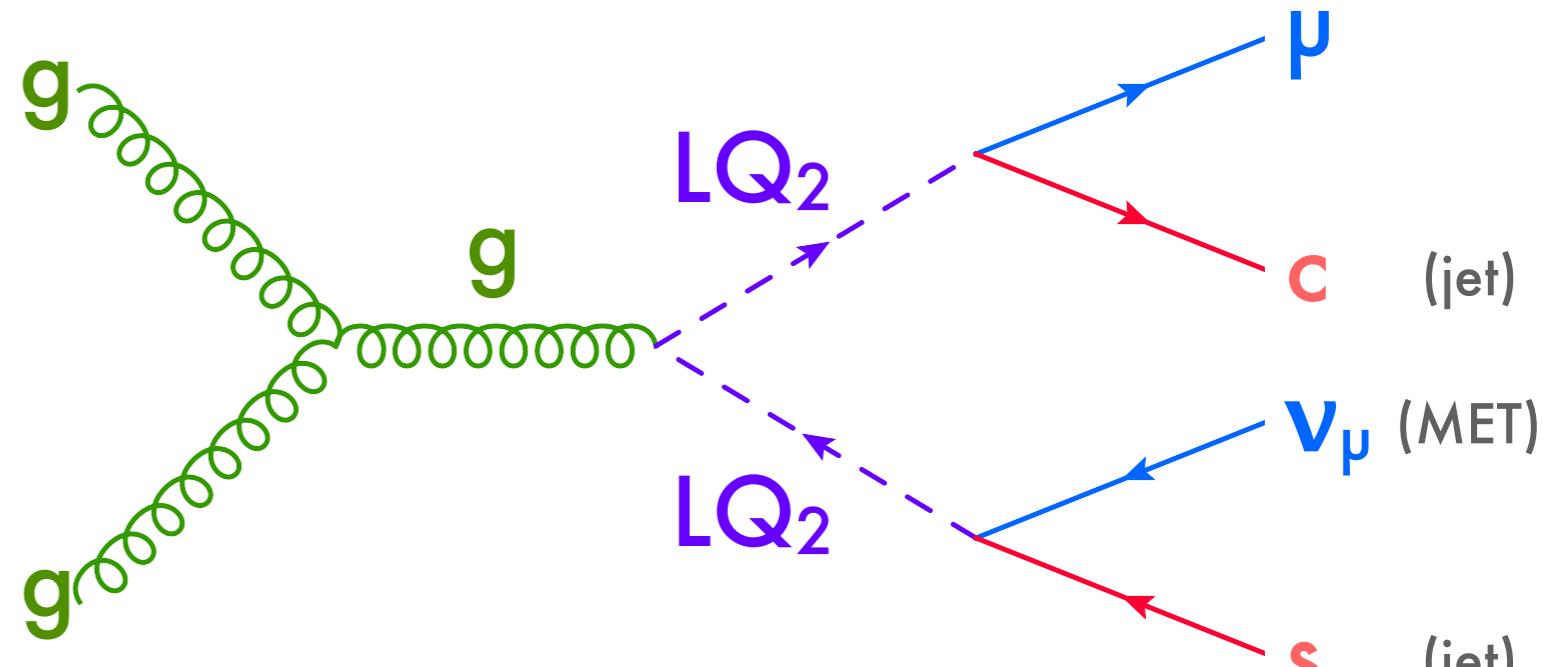
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Physics Object Selection

- Physics object and event selections based on LQ event topology
- high signal efficiency!



MUONS

ID+MS tracks combined

$$|\eta| < 2.4$$

$$p_T > 30 \text{ GeV}$$

track quality requirements

$$|d_0| < 0.1 \text{ mm}, |z_0| < 5.0 \text{ mm}$$

isolated in tracking

JETS

$$|\eta| < 2.8$$

$$p_T > 30 \text{ GeV}$$

quality requirements

$$\Delta R(\text{jet}, l) > 0.4$$

ELECTRONS (veto)

$$|\eta| < 2.47$$

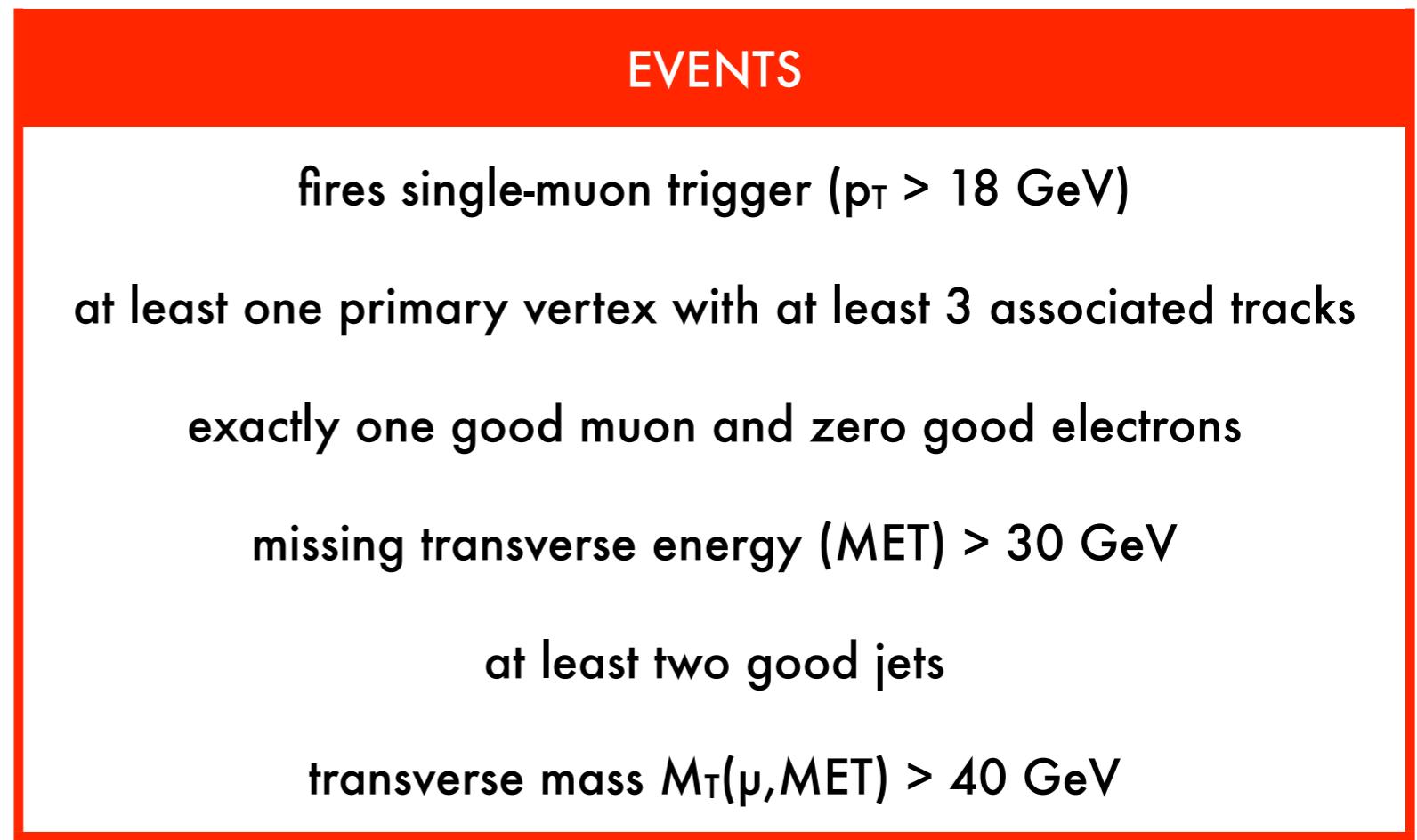
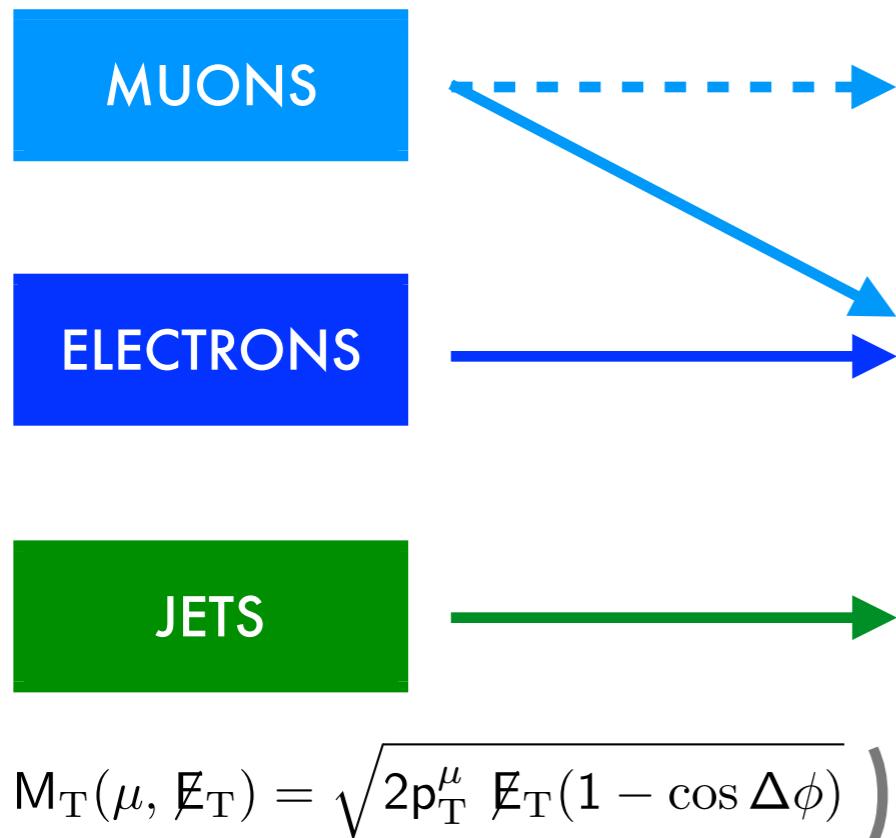
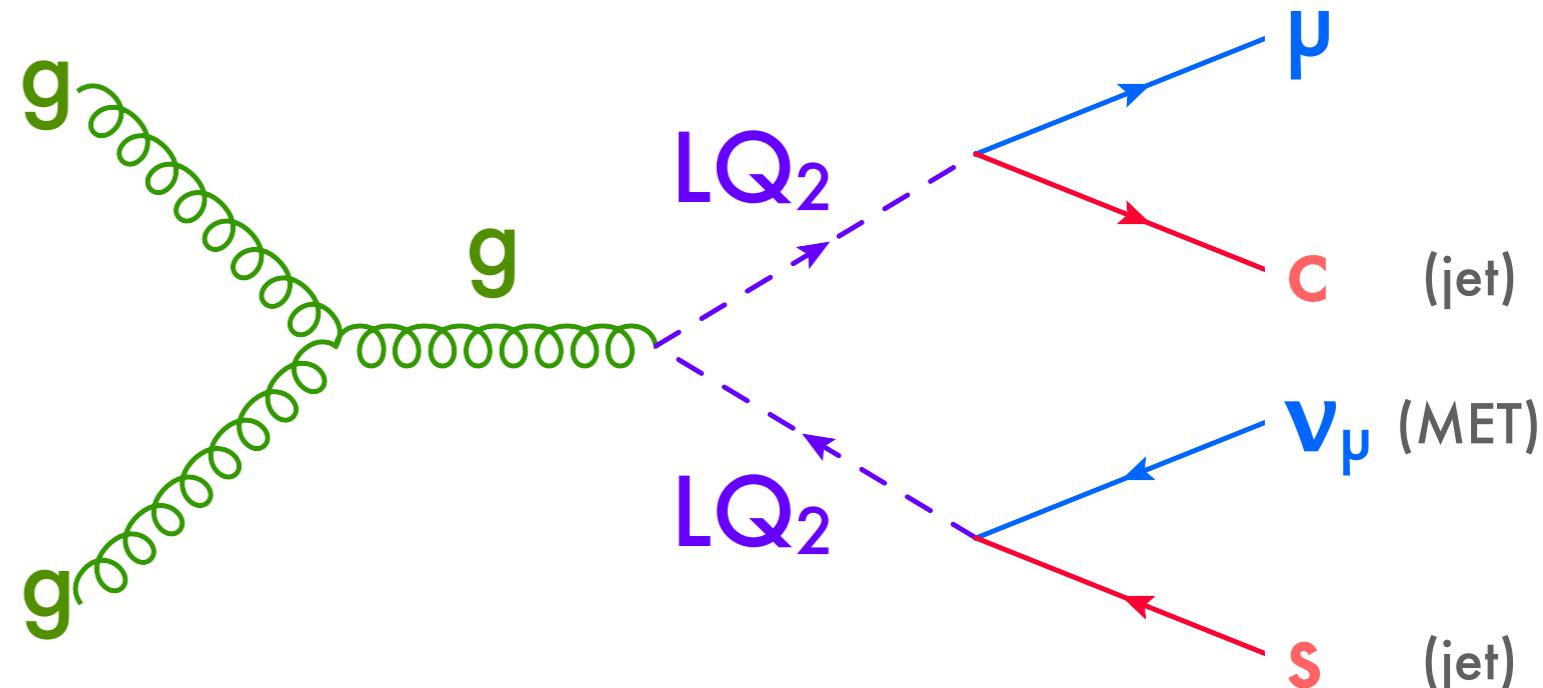
$$p_T > 20 \text{ GeV}$$

quality requirements

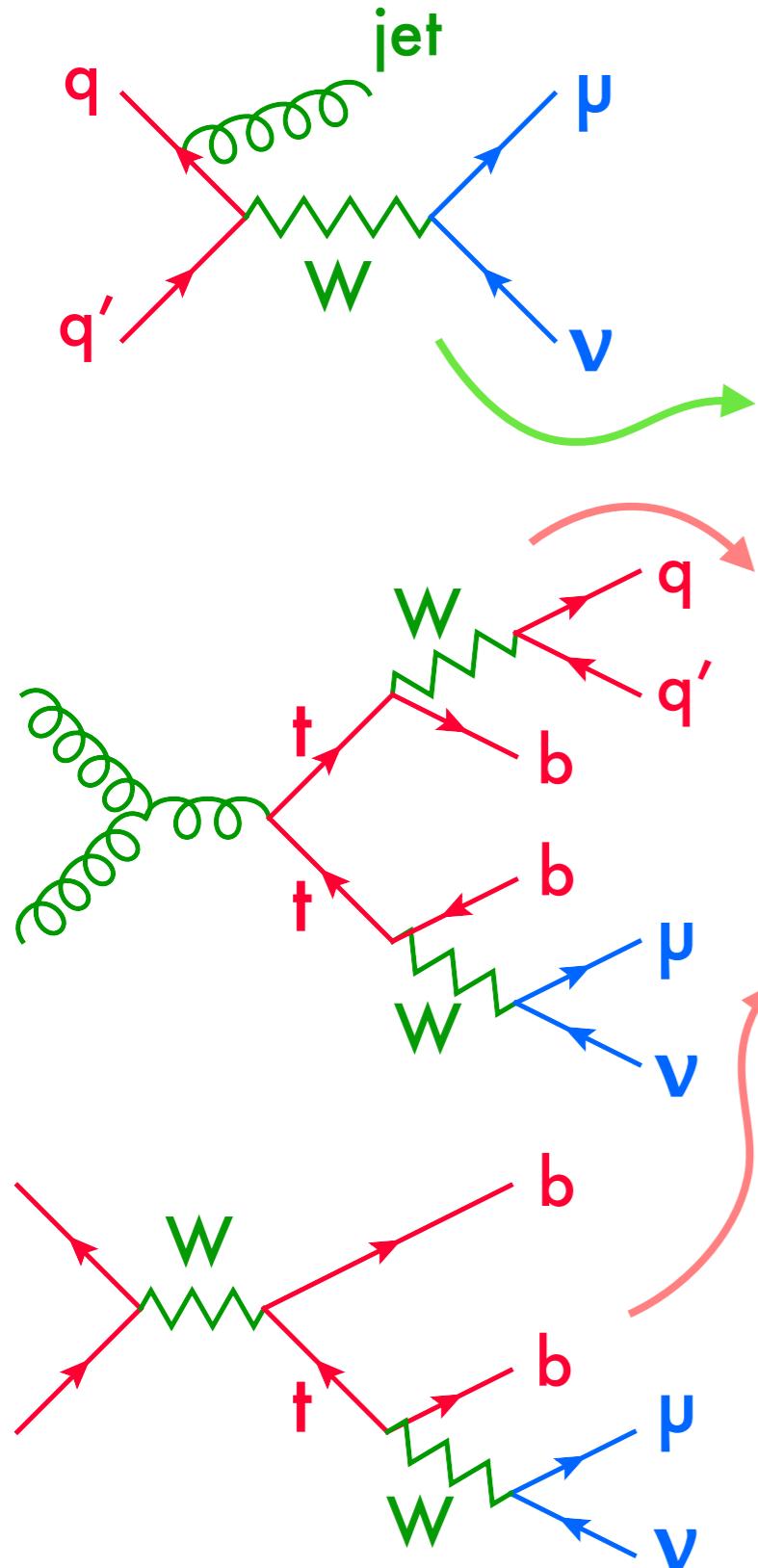
isolated in calorimeter

Event Selection

- Physics object and event selections based on LQ event topology
- high signal efficiency!



SM Backgrounds



Source	Estimation
V+jets (W+jets and Z+jets)	normalization from control region, shape from MC (Alpgen)
t-tbar	normalization from control region, shape from MC (MC@NLO)
single top	normalization and shape from MC (MC@NLO), NLO cross sections
diboson (WW, WZ, ZZ)	normalization and shape from MC (Herwig), NLO cross sections
multi-jet	normalization and shape from fully data-driven methods

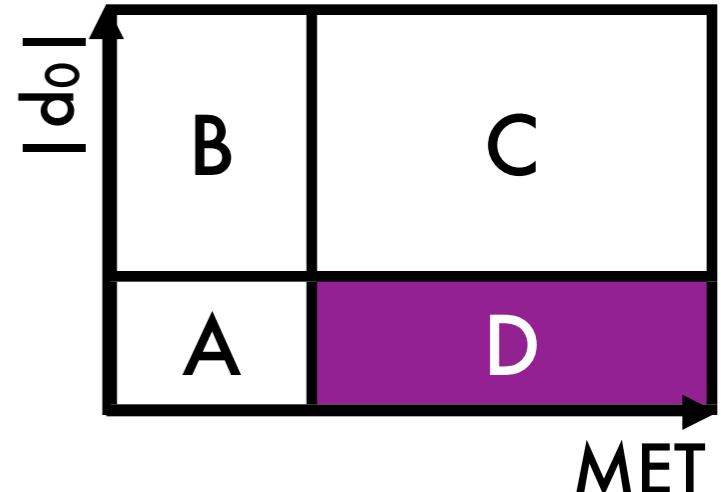
Multi-jet Estimation

● Method 1: ABCD

- MET vs muon impact parameter (nominal)
- MET vs muon track isolation (alternate)
- shape from region C, scaled to N_D

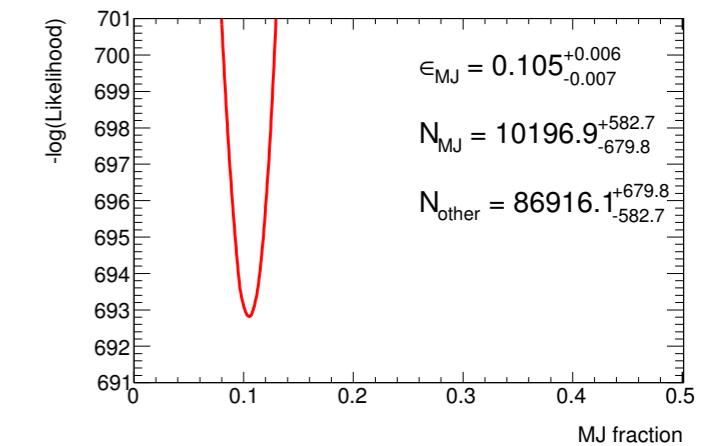
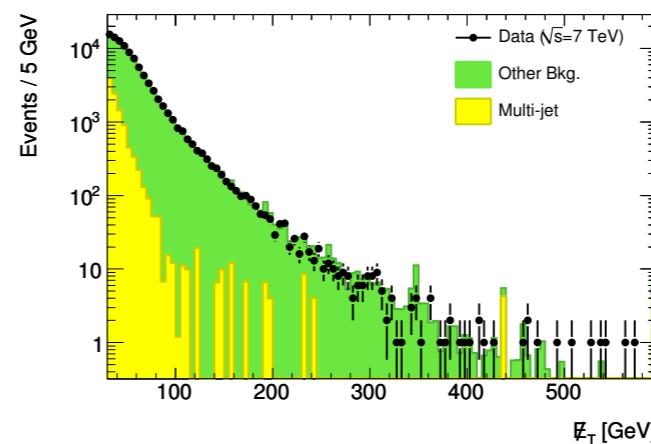
$$N_D = \frac{N_A N_C}{N_B}$$

$$h_D = h_C \cdot \left(\frac{N_D}{N_C} \right)$$



● Method 2: Fitting

- fit MET distribution of MC bkg + MJ to data
- bkg, data yields constrained to be equal
- MJ fraction as floating parameter



● Combination

- average normalizations from both methods to get nominal yields
- nominal shape from C in ABCD, alternate shape used as systematic

Control Regions (CRs)

W+jets CR

passes event selection

$M_T(\mu, \text{MET}) < 120 \text{ GeV}$

$S_T < 225 \text{ GeV}$

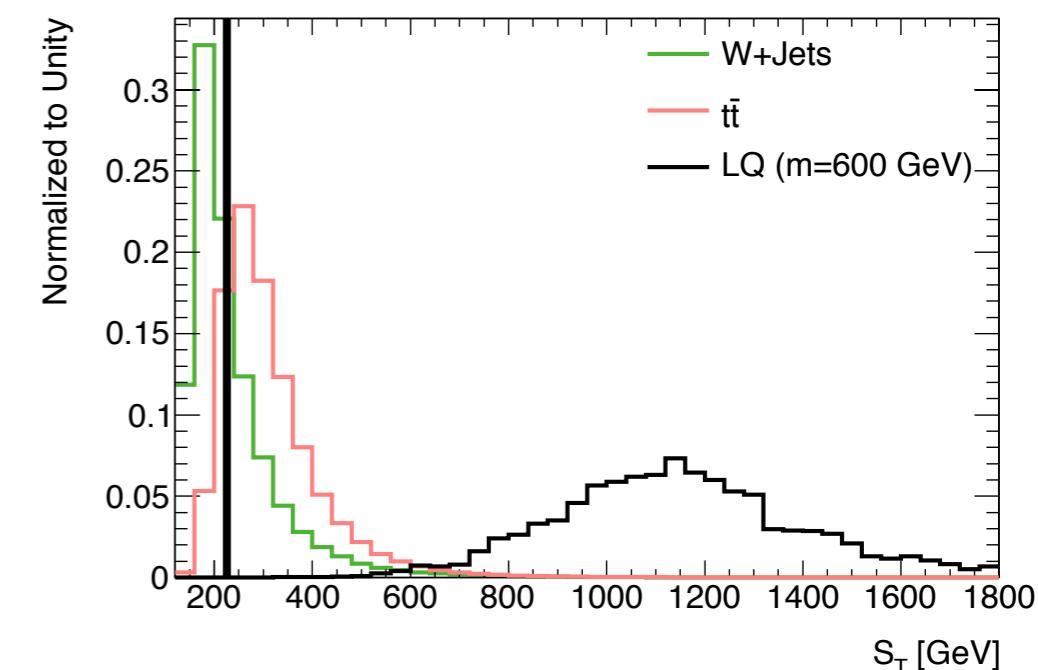
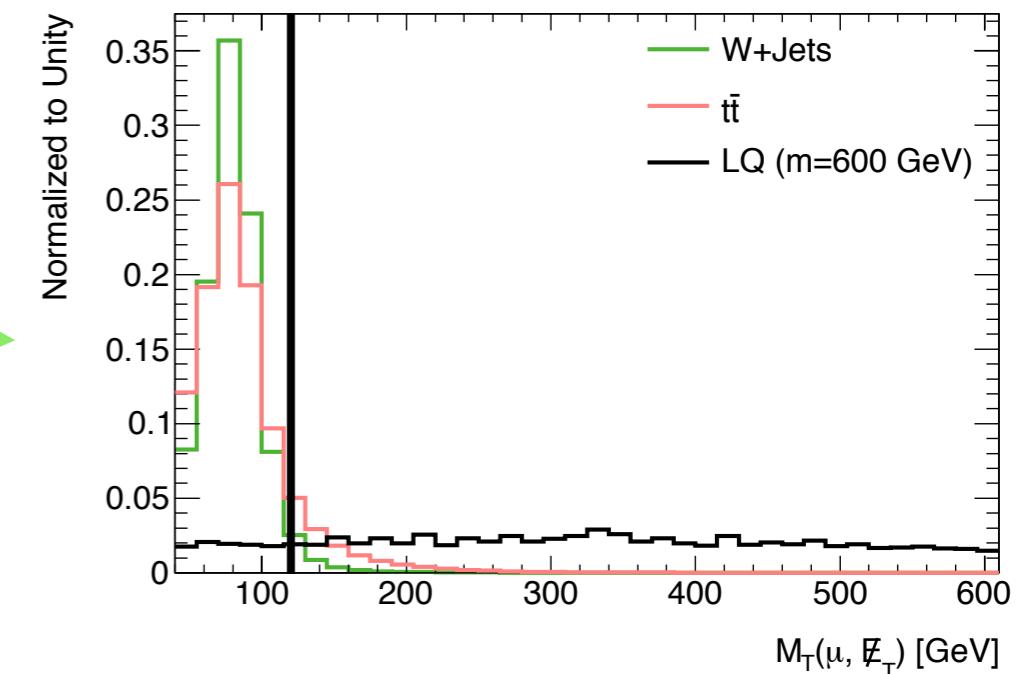
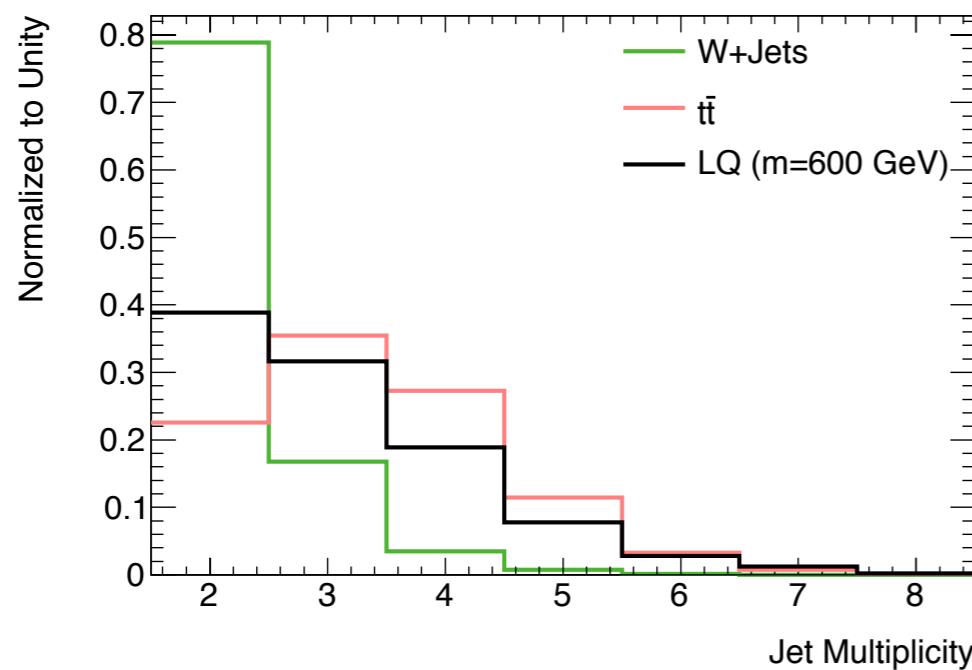
W+2jets: exactly two jets

W+3jets: at least three jets

- Defined to enhance dominant backgrounds, minimize signal; verify background modeling

$$M_T(\mu, \not{E}_T) = [2p_T^\mu \not{E}_T (1 - \cos \Delta\phi)]^{1/2}$$

$$S_T = p_T^{\text{jet}1} + p_T^{\text{jet}2} + p_T^\mu + \not{E}_T$$



Control Regions (CRs)

$t\bar{t}$ CR

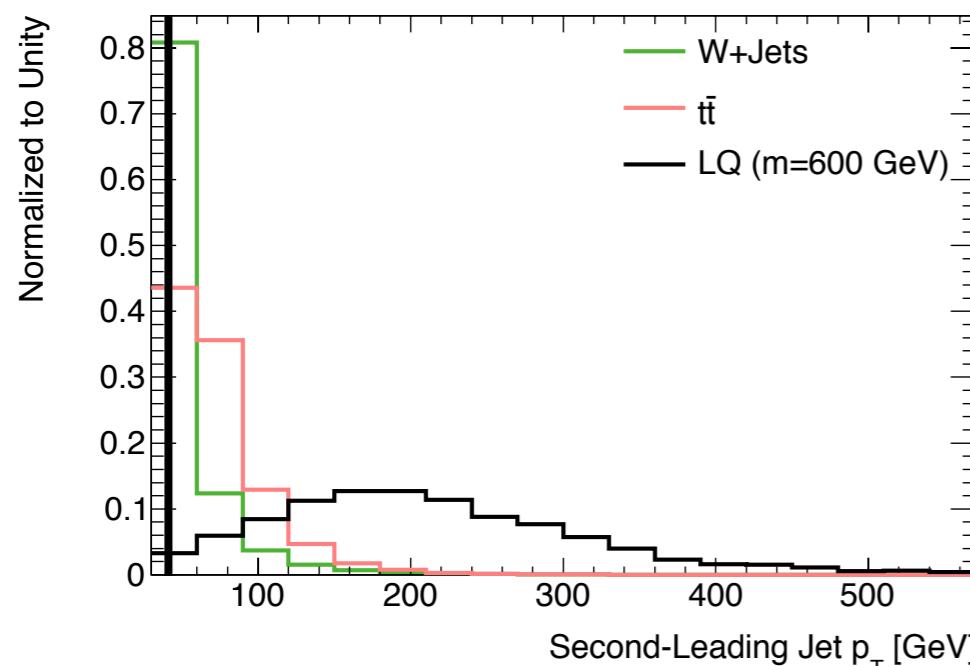
passes event selection

$M_T(\mu, \text{MET}) < 120 \text{ GeV}$

at least four jets

$p_T^{\text{jet}1} > 50 \text{ GeV}$

$p_T^{\text{jet}2} > 40 \text{ GeV}$

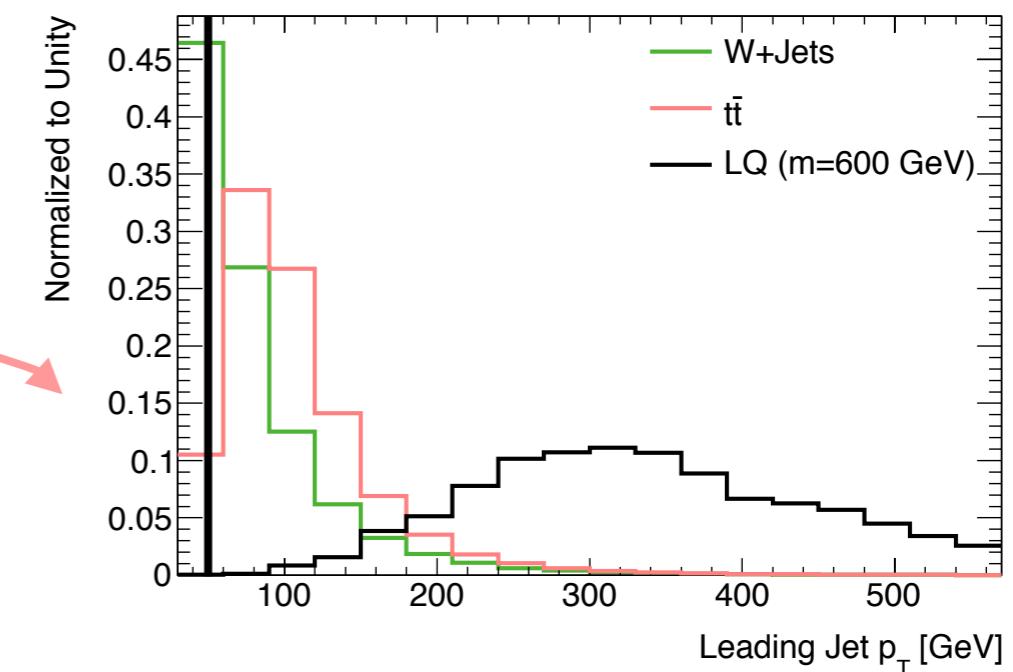


- Modify normalization with scale factors derived from simultaneous χ^2 fit to all CRs

$$\chi^2 = \sum_{\text{CR}} \left[\frac{N_i^{\text{data}} - N_i^{\text{MC}}}{\sigma_i^{\text{data}}} \right]^2,$$

$$N_i^{\text{MC}} \equiv (\text{SF}^{t\bar{t}} \times N_i^{t\bar{t}}) + (\text{SF}^V \times N_i^V) + N_i^{\text{other}}$$

W+jets SF	0.911 ± 0.005
t-tbar SF	1.092 ± 0.25



	W+2jets CR	W+3jets CR	t-tbar CR
Total Bkg	45100 ± 300	8300 ± 120	7300 ± 80
Data	45213	8125	7303

Control Regions (CRs)

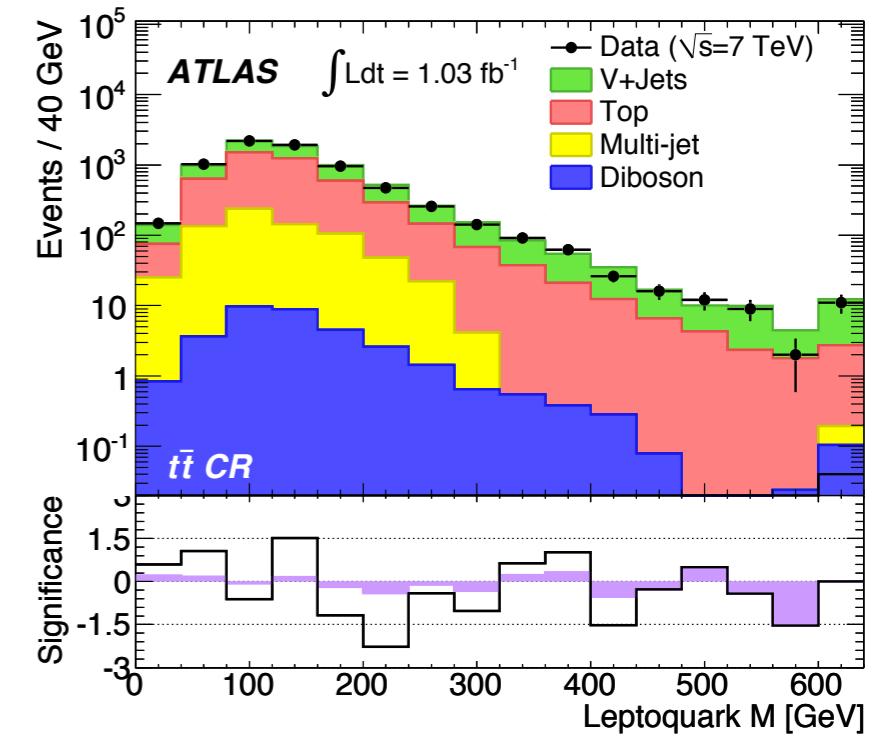
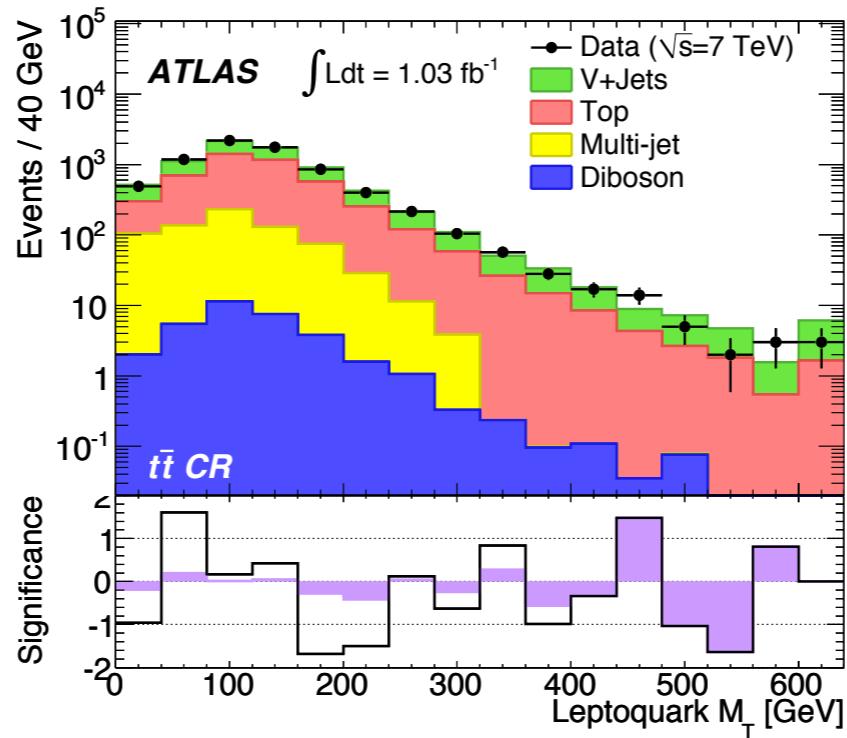
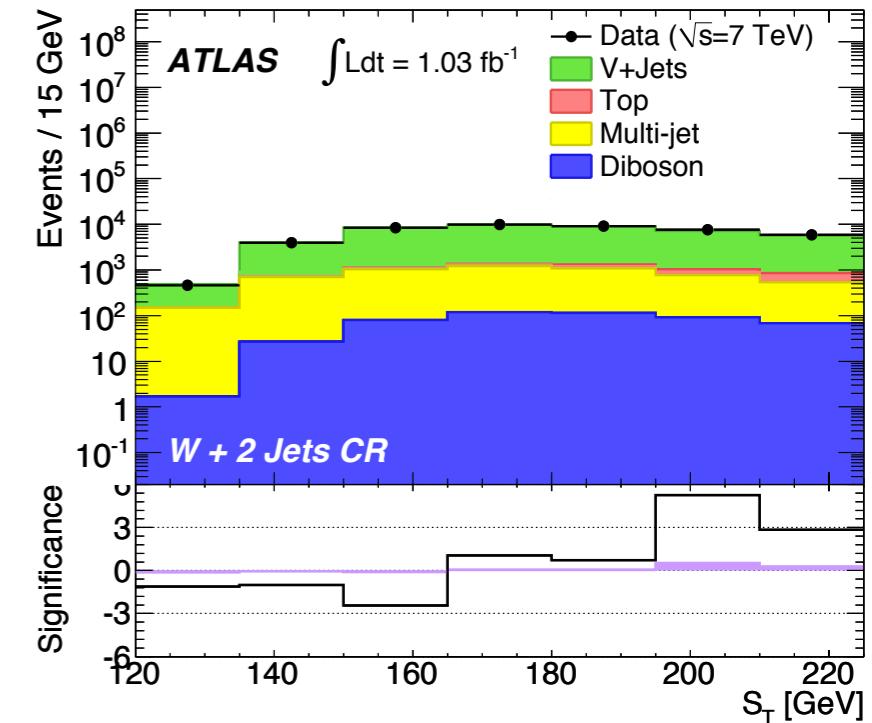
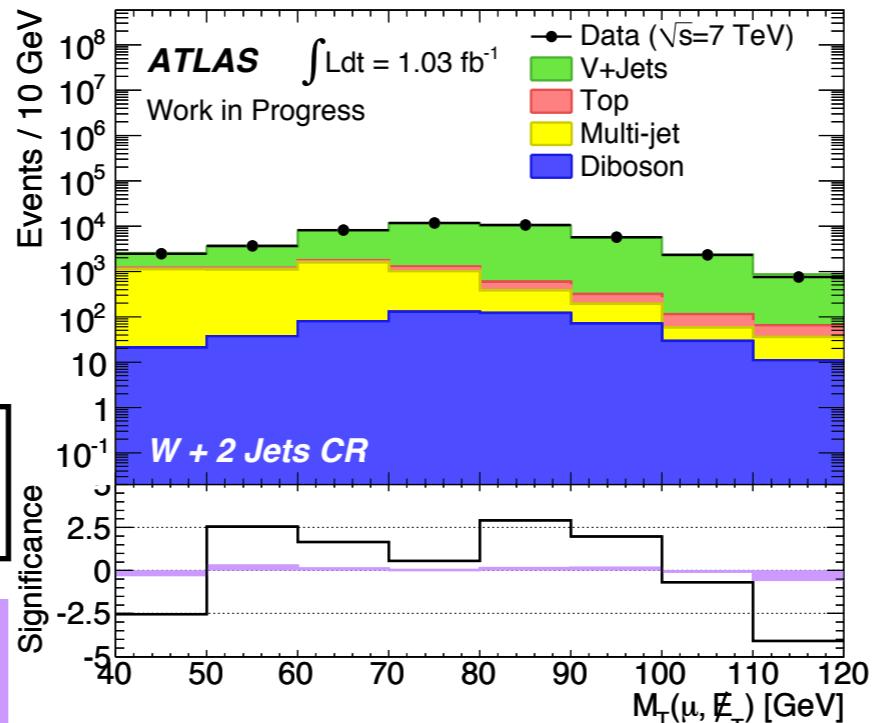
Backgrounds
well modeled!

$$\text{Significance} = \frac{(\text{data} - \text{prediction})}{\text{stat. uncert.}}$$

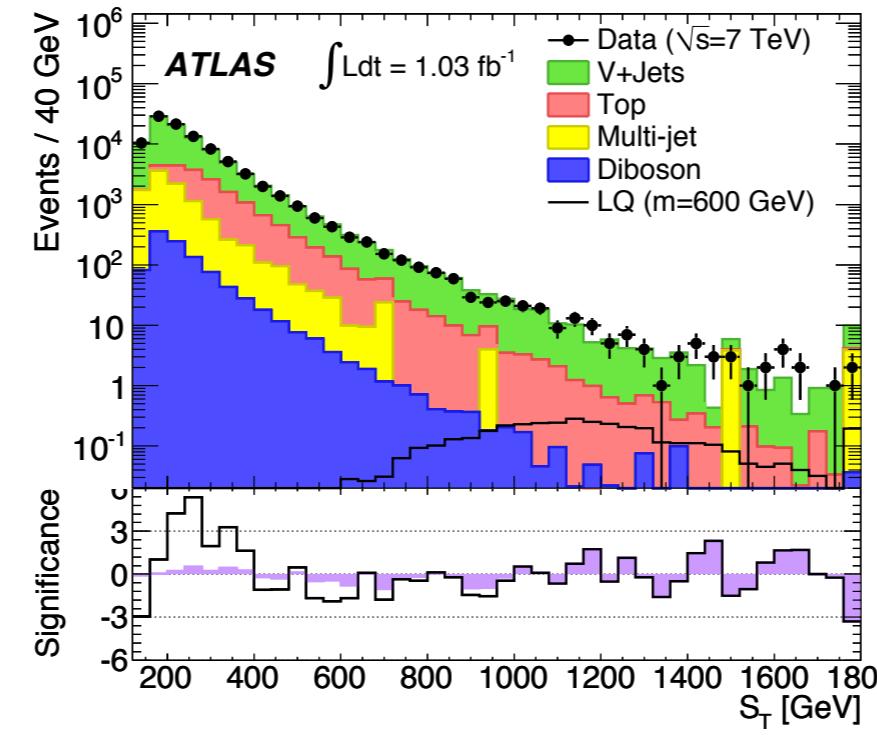
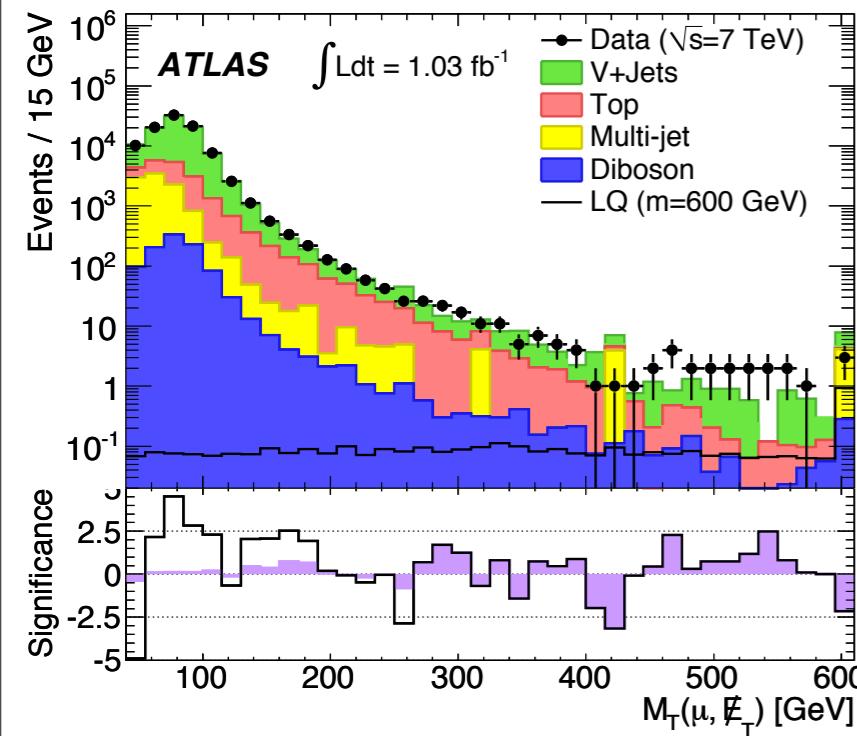
$$\text{Significance} = \frac{(\text{data} - \text{prediction})}{\text{stat. + syst.}}$$

M_T^{LQ} and M^{LQ} from MET-jet and
 μ -jet such that ΔM is minimum

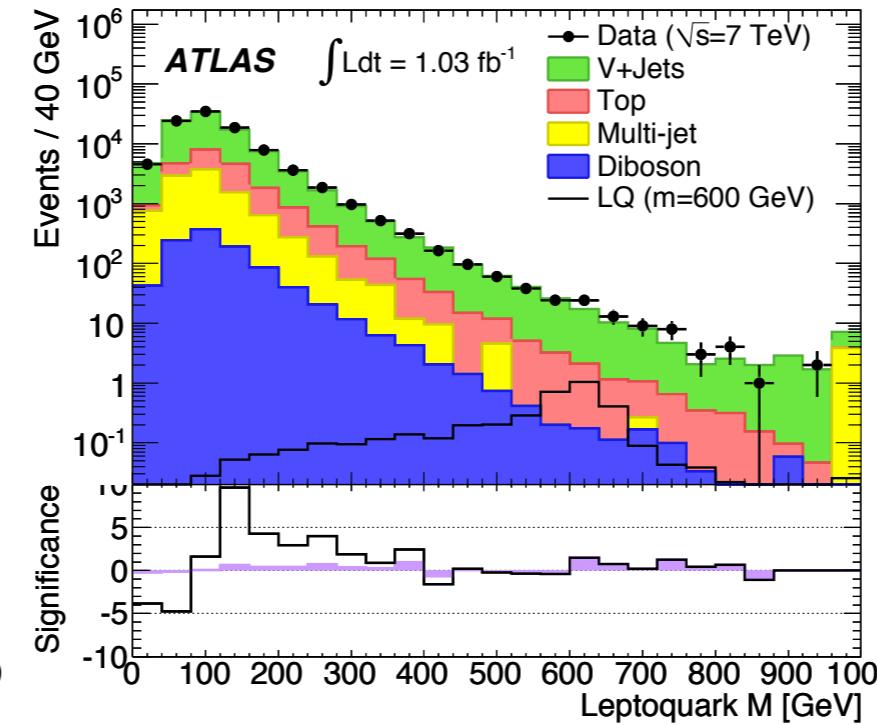
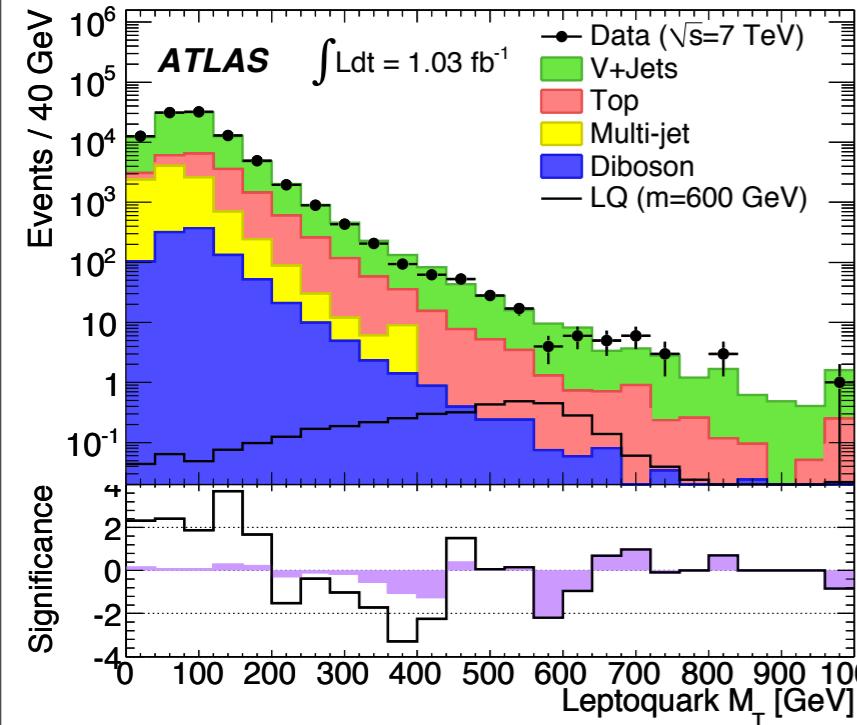
(negligible signal contribution)



Selected Events

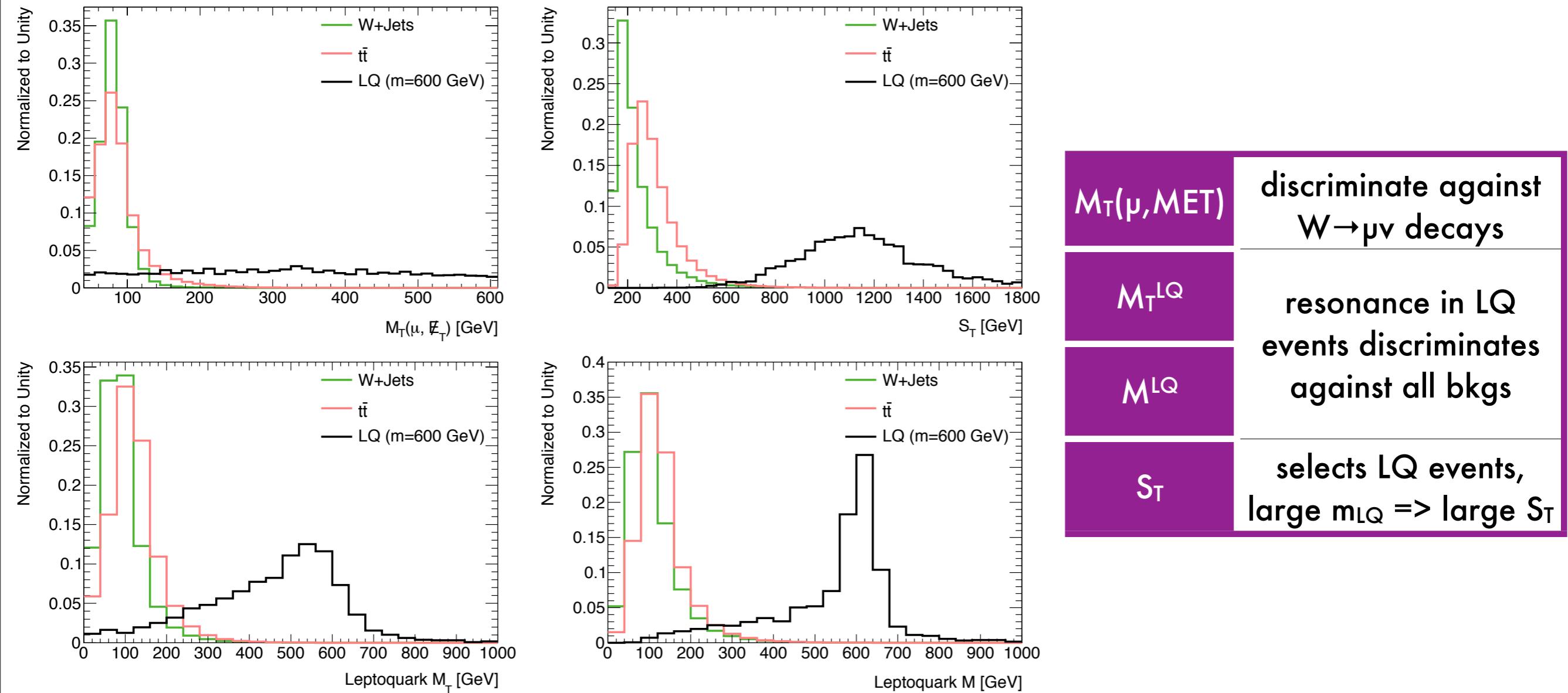


sample	yield
V+jets	74000 ± 17000
top	11600 ± 1900
multi-jet	9690 ± 230
diboson	1020 ± 180
Total Bkg	96000 ± 17000
Data	97113
LQ $\rightarrow \mu\nu jj$ ($m=600 \text{ GeV}$)	3.9 ± 0.2



(statistical + systematic uncertainties)

Multivariate Discriminant?

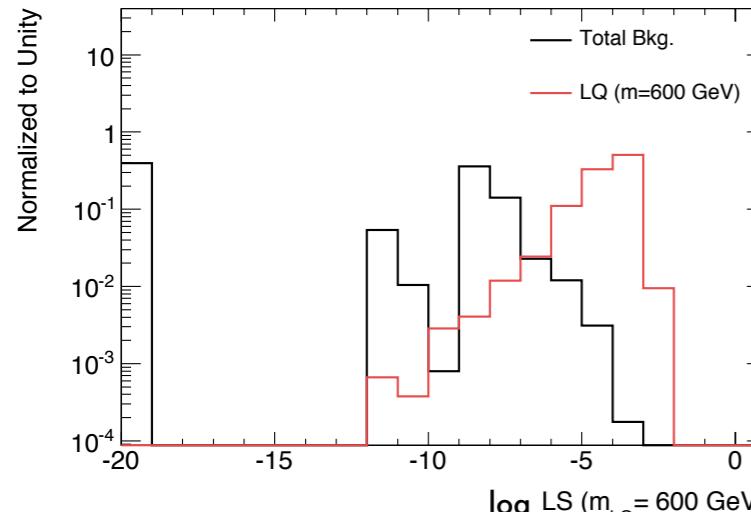


$M_T(\mu, \text{MET})$ | discriminate against $W \rightarrow \mu\nu$ decays
 M_T^{LQ} | resonance in LQ events discriminates against all bkgds
 M^{LQ} |
 S_T | selects LQ events, large $m_{\text{LQ}} \Rightarrow$ large S_T

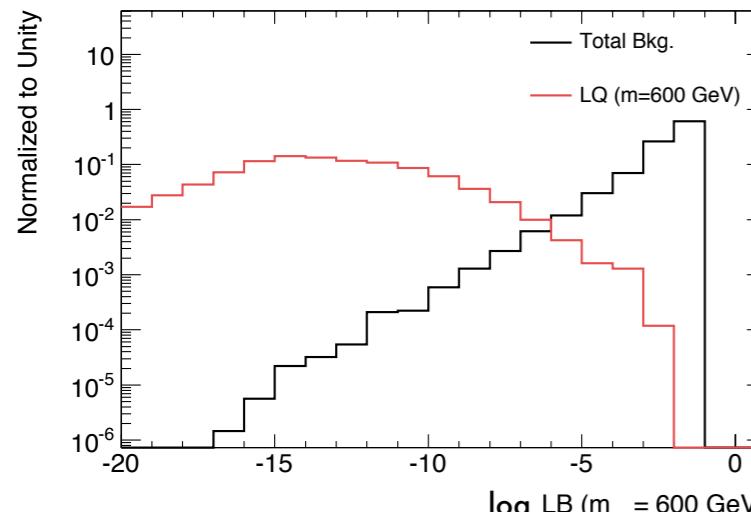
- Choose kinematic variables with strong signal-bkg discrimination
- Combine in a multivariate discriminant to test bkg-only, signal+bkg hypotheses and compute a final result

Log-likelihood Ratio (LLR)

- From PDFs for background (P_B^i) and signal (P_S^i), compute background and signal likelihoods (L_B and L_S) for each event

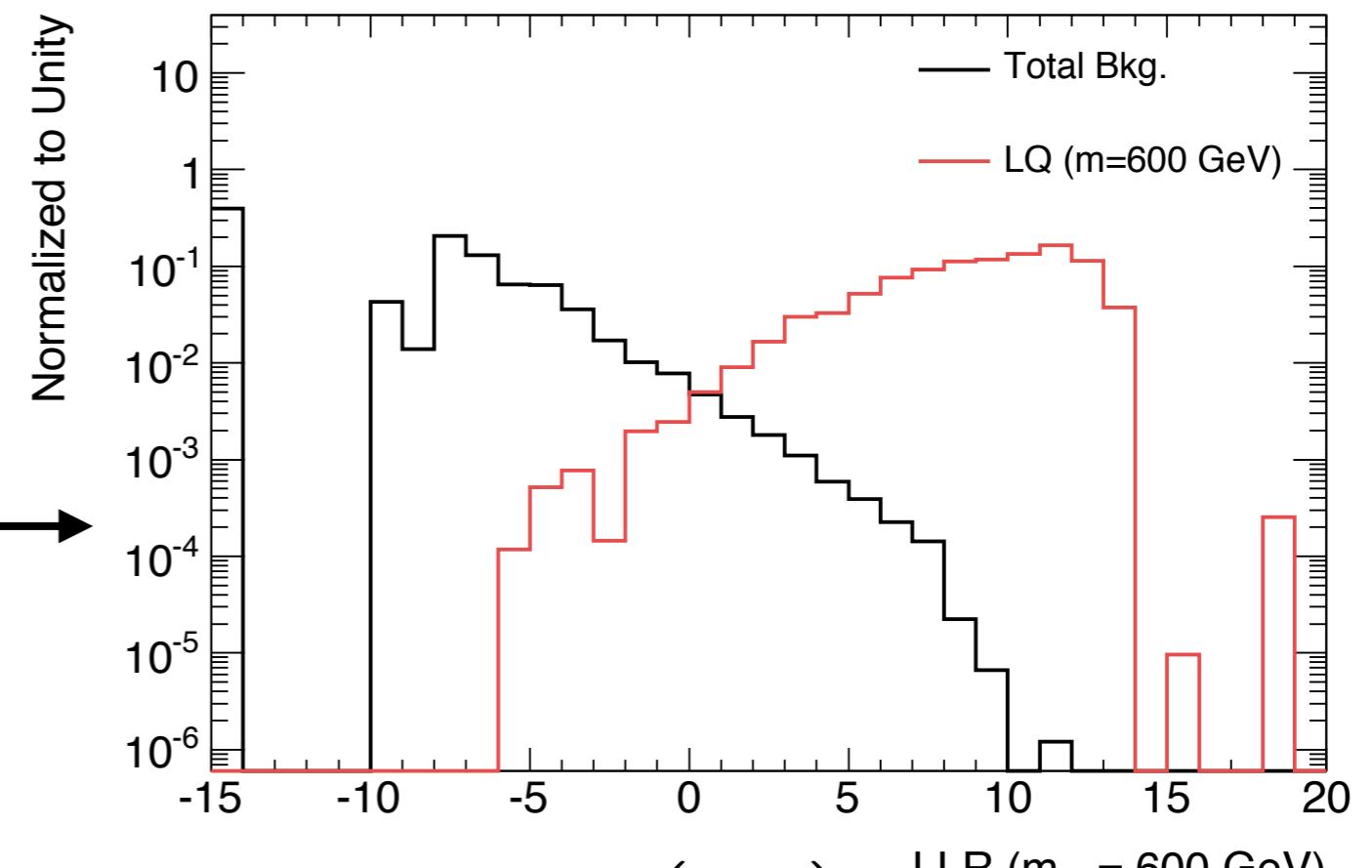


$$L_S = \prod_i P_S^i$$



$$L_B = \prod_i P_B^i$$

- Unique LLR distributions for each m_{LQ} point

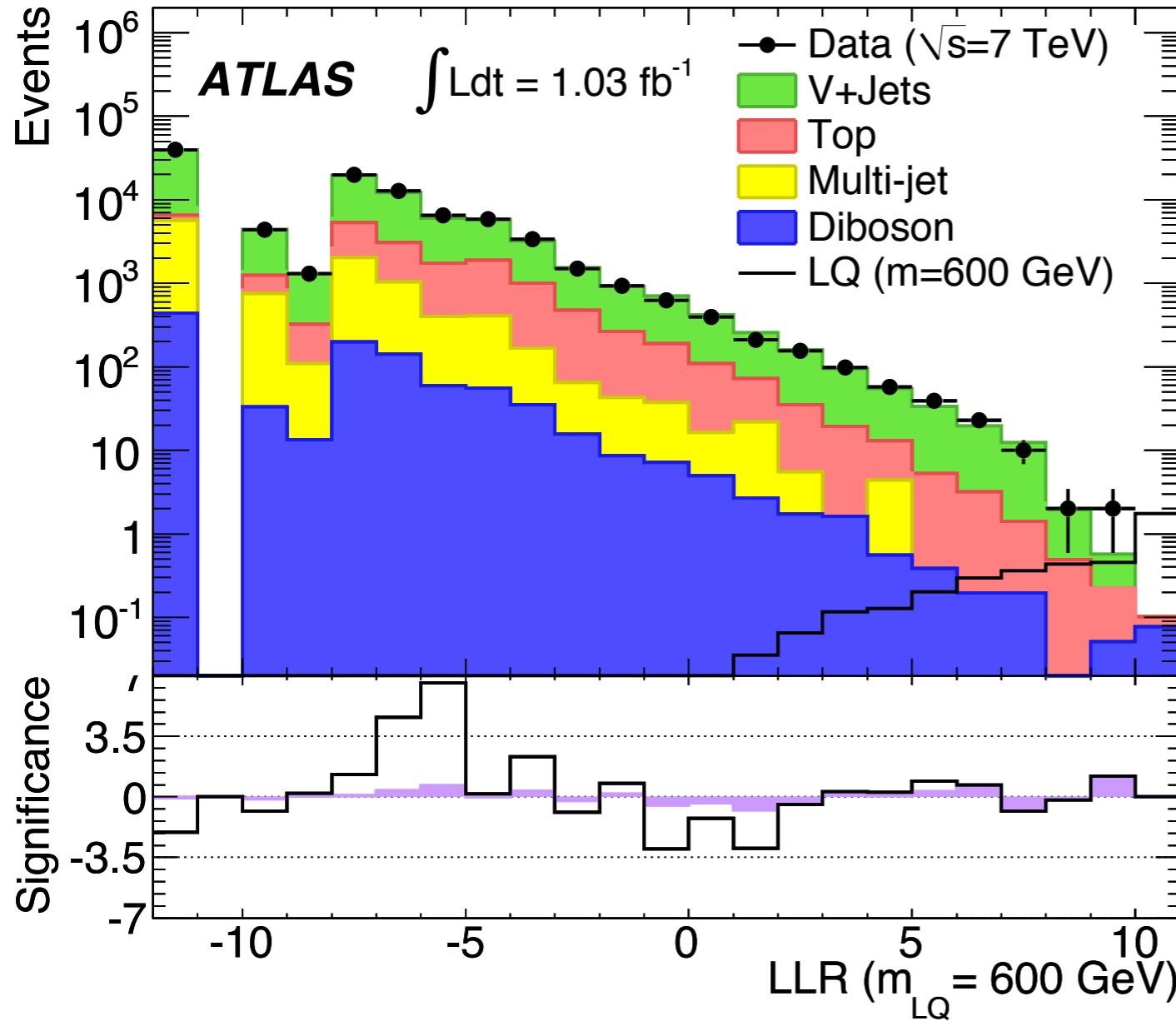


$$\text{LLR}(m_{LQ}) = \log\left(\frac{L_S}{L_B}\right)$$

Systematic Uncertainties

Source	Handling
V+jets and t-tbar modeling	use different generators, vary top mass ($m = 170, 175 \text{ GeV}$), vary ISR/FSR up and down
MC samples cross-section, normalization	use theoretical uncertainties on x-sections, account for SF variation at high/low p_T
integrated luminosity	flat 3.7% applied to single top and diboson backgrounds, plus signal
jet energy scale, jet energy resolution	vary jet energy scale $\pm 1\sigma$, smear jet energy by 1σ Gaussian
muon momentum resolution, muon reconstruction efficiency	vary muon p_T smearing $\pm 1\sigma$, vary ID efficiency event weights $\pm 1\sigma$
Multi-jet	use $\pm 1\sigma$ normalization, alternate shape
Signal PDFs	re-weight signal LLR by CTEQ errors
LLR input PDFs	statistics in LLR input PDFs propagated onward

Results



sample	yield (LLR ≥ 7)
V+jets	12.9 ± 9.9
top	1.9 ± 1.2
multi-jet	< 0.1
diboson	0.3 ± 0.1
Total Bkg	15 ± 10
Data	14
LQ $\rightarrow \mu\nu jj$ ($m=600 \text{ GeV}$)	3.2 ± 0.2

(statistical + systematic uncertainties)

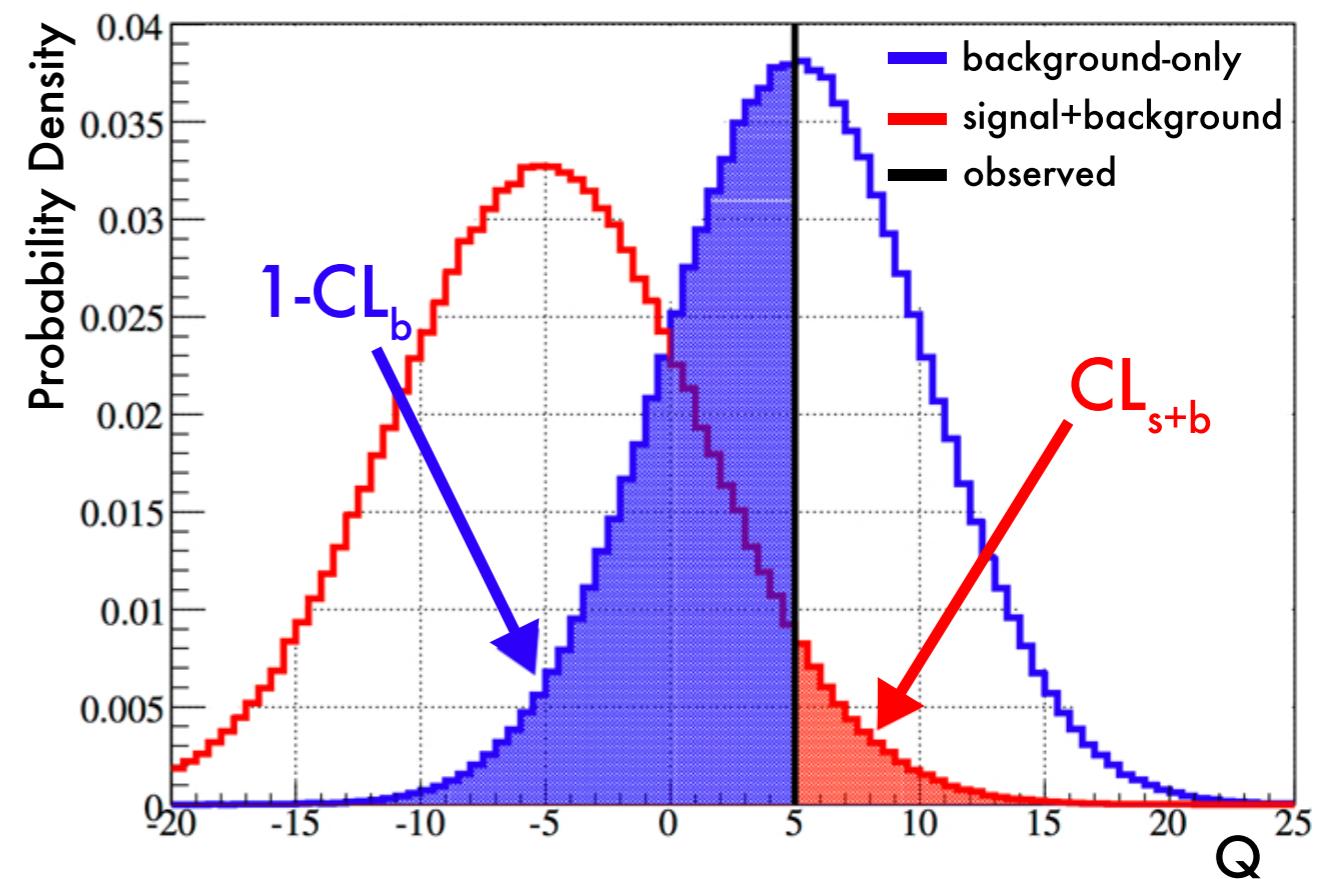
Data in good agreement with SM background expectation!
No evidence for LQ production...

Limit-Setting

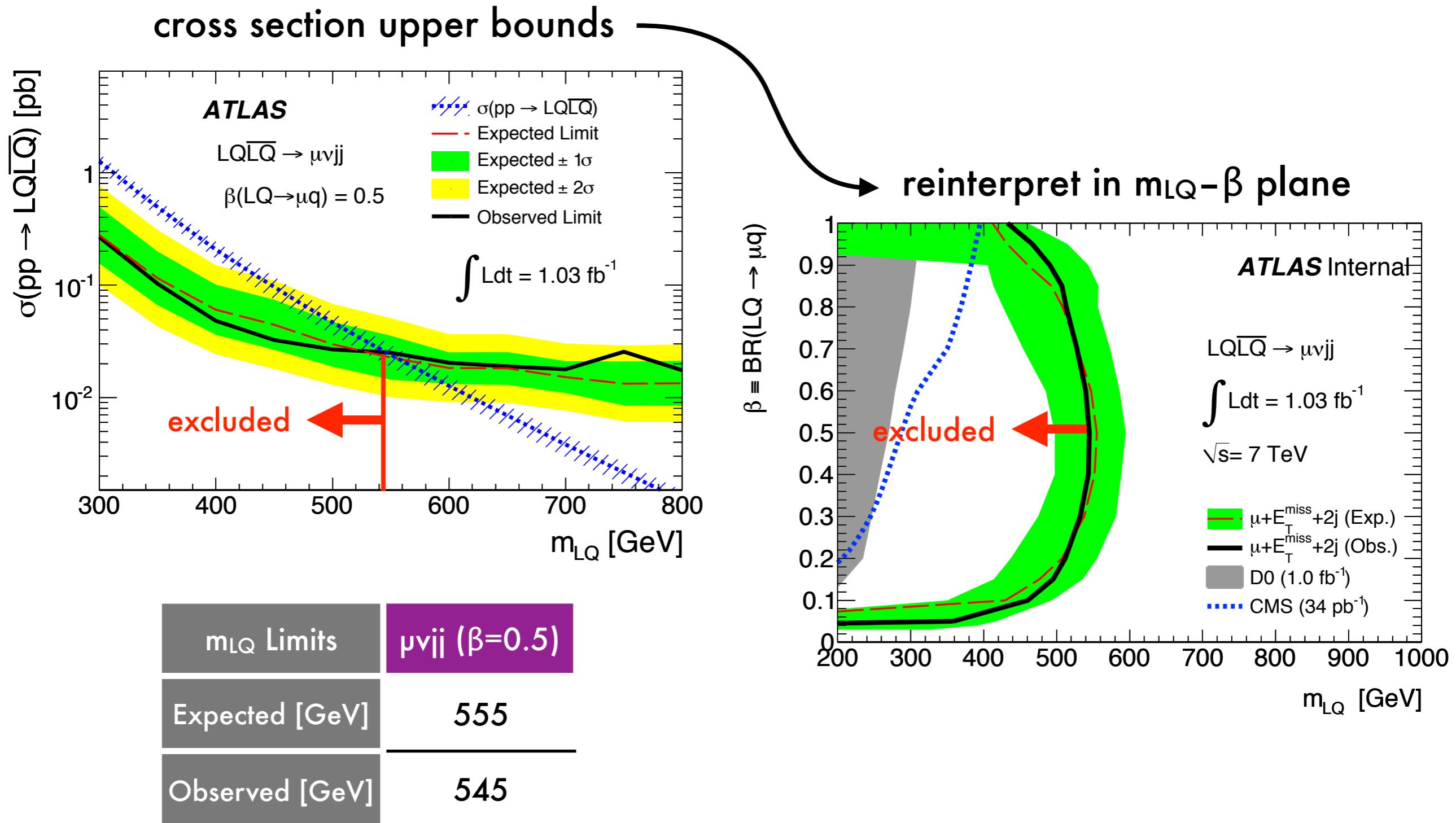
- Want to quantify agreement between experimental outcome and two hypotheses: background-only (H_0) and signal+background (H_1)
 - Counting experiment test statistic: $Q(x) = \frac{\mathcal{L}(x|H_1)}{\mathcal{L}(x|H_0)} = \frac{(s+b)^x e^{-(s+b)}/x!}{(b)^x e^{-(b)}/x!} \rightarrow -2 \ln(Q)$
 - perform many pseudo-experiments
 - systematic uncertainties as “nuisance parameters”
 - generalizes to multiple channels, discriminant bins:
 - Compute confidence levels CL_{s+b} (CL_b): probability for H_1 (H_0) to produce an outcome more background-like than observation in data
 - Modified Frequentist: $CL_s \equiv \frac{CL_{s+b}}{CL_b}$
- exclude H_1 at 95% CL
if $1 - CL_s \geq 0.95$

$$x = \text{data}, b = \text{background}, s = \text{signal yields}$$

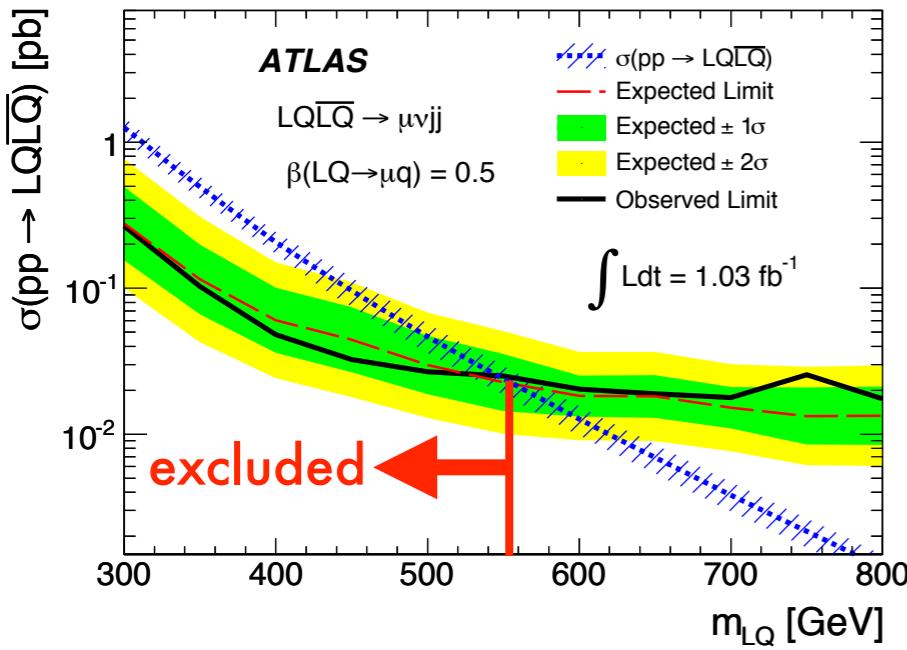
$$Q(\vec{x}) = \prod_i \prod_j^{\text{chans bins}} Q_{ij}(x_{ij})$$



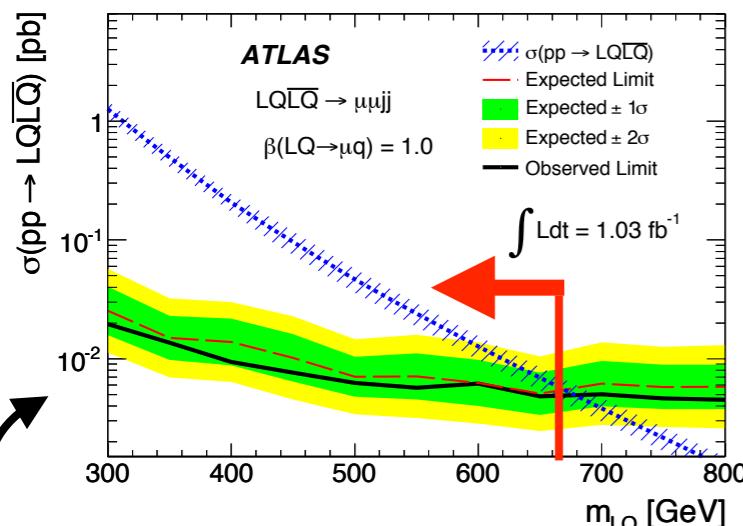
Final Limits



Final Limits

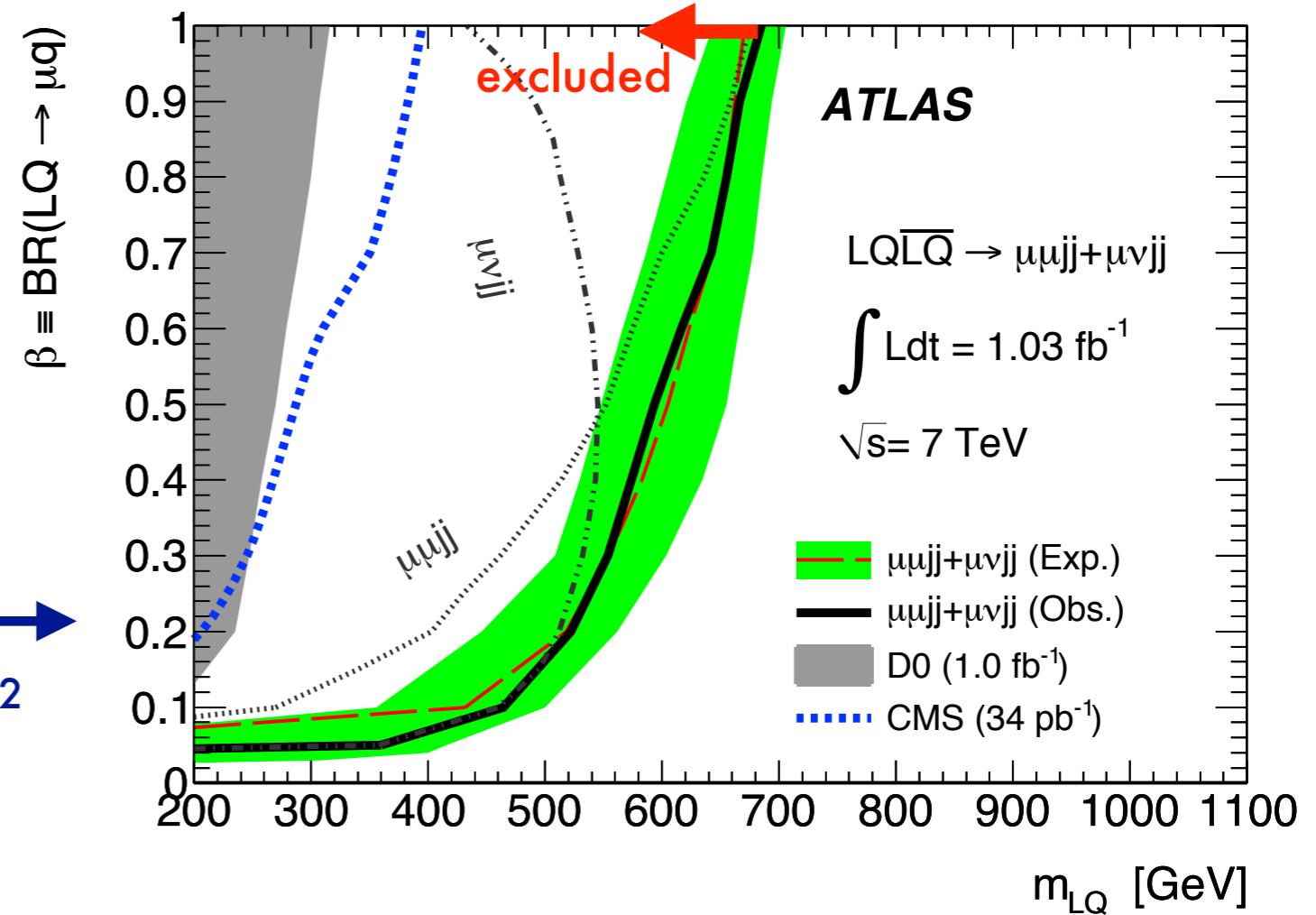


cross section upper bounds



complementary search in $\mu\mu jj$ final state

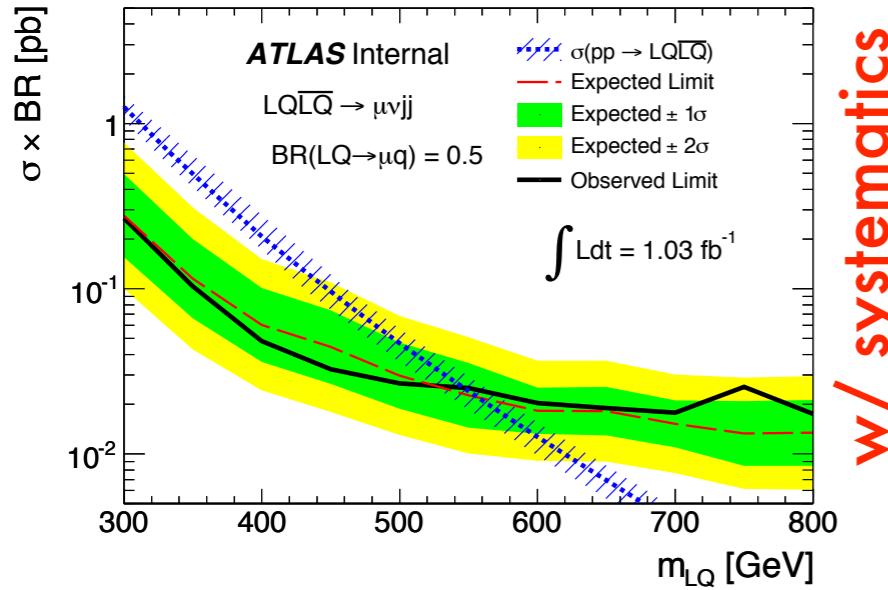
combine, reinterpret limits in $m_{LQ}-\beta$ plane



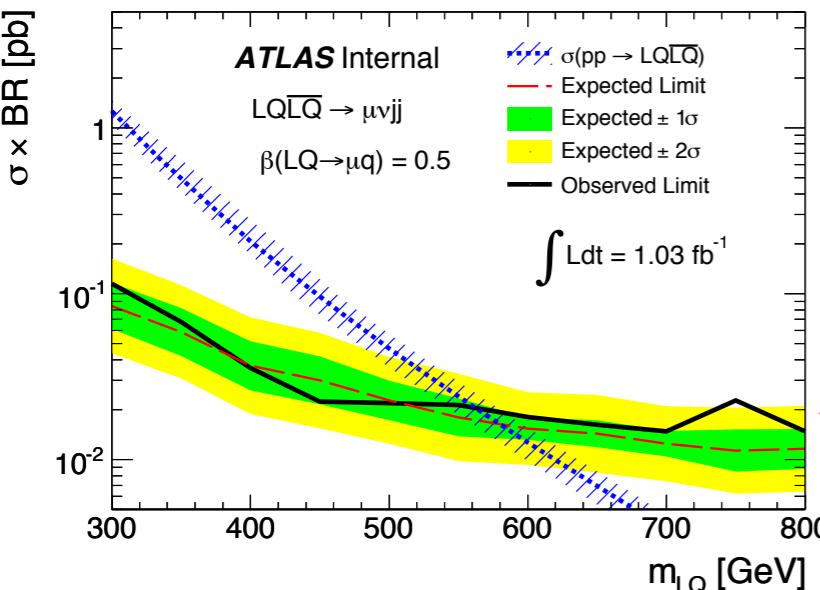
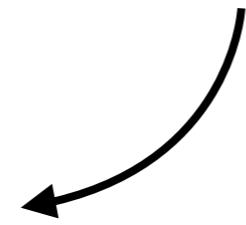
m_{LQ} Limits	$\mu\nu jj$ ($\beta=0.5$)	$\mu\mu jj$ ($\beta=1.0$)	LQ_2 ($\beta=0.5$)	LQ_2 ($\beta=1.0$)
Expected [GeV]	555	665	605	671
Observed [GeV]	545	675	594	685

Future Outlook

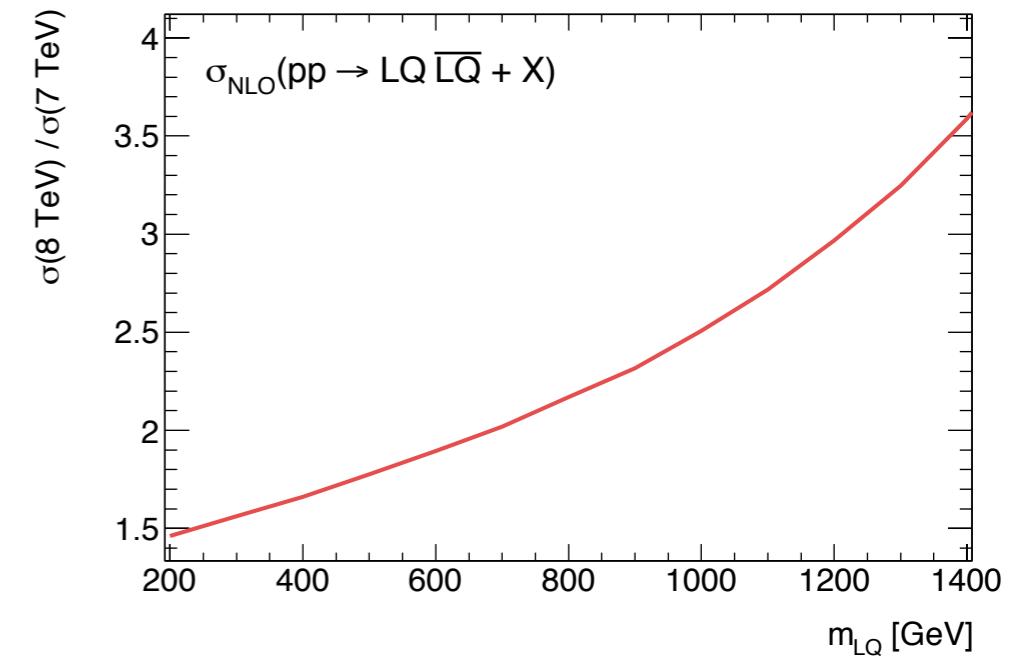
- 2012 LHC run: $L \approx 15 \text{ fb}^{-1}$, $\sqrt{s} = 8 \text{ TeV}$
 - more events, larger σ_{LQ} => extend sensitivity!
- Better control of systematic uncertainties



w/ systematics



w/o systematics



- Stronger signal-background discriminant
 - additional/other LLR variables?
 - fancier MVA technique, e.g. neural networks
- Add complementary $\nu\nu jj$ final state for sensitivity at low- β

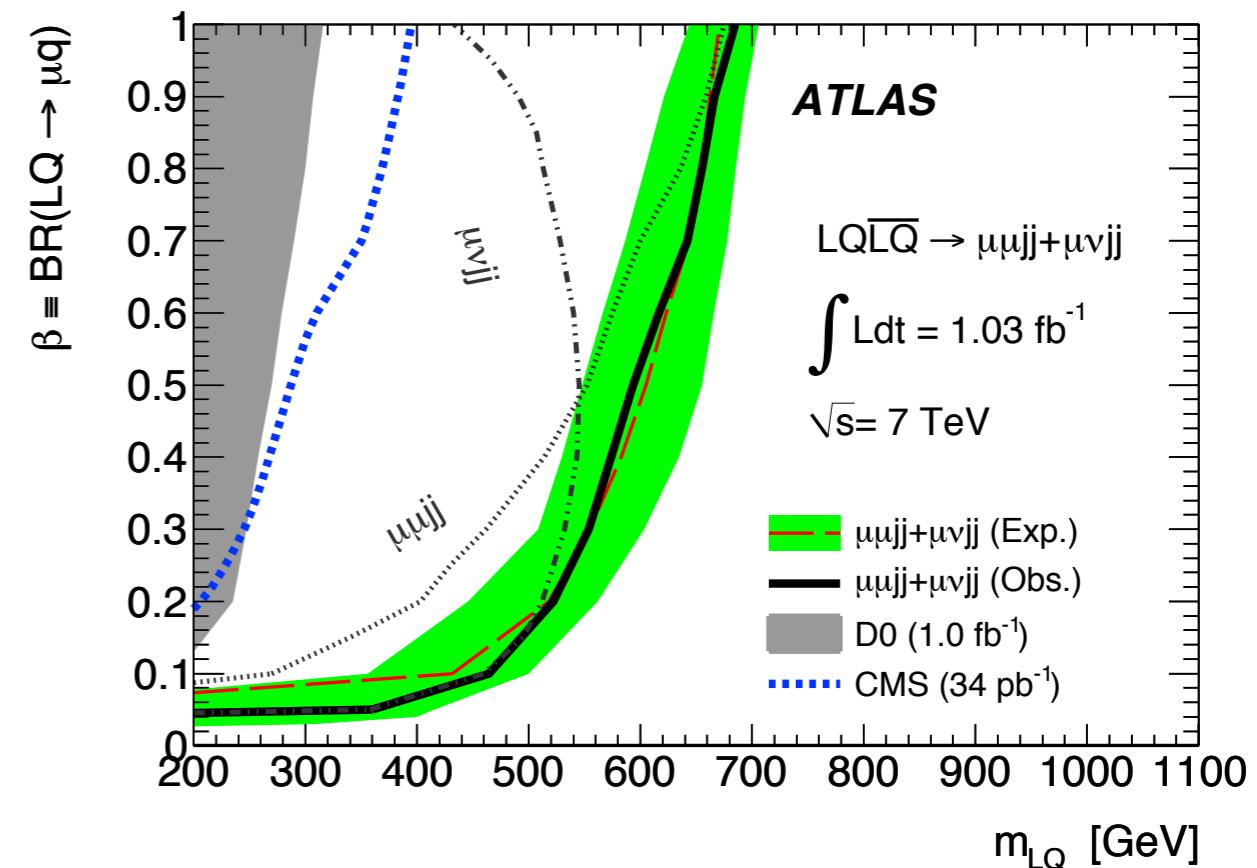
Outline

- **Introduction**
 - Standard Model
 - Leptoquarks
- **Experiment**
 - Large Hadron Collider
 - ATLAS detector
- **Event Simulation and Reconstruction**
- **A Leptoquark Search**
 - physics object and event selection
 - backgrounds and control regions
 - multivariate discriminant
 - limit-setting and results
 - future outlook
- **Conclusion**

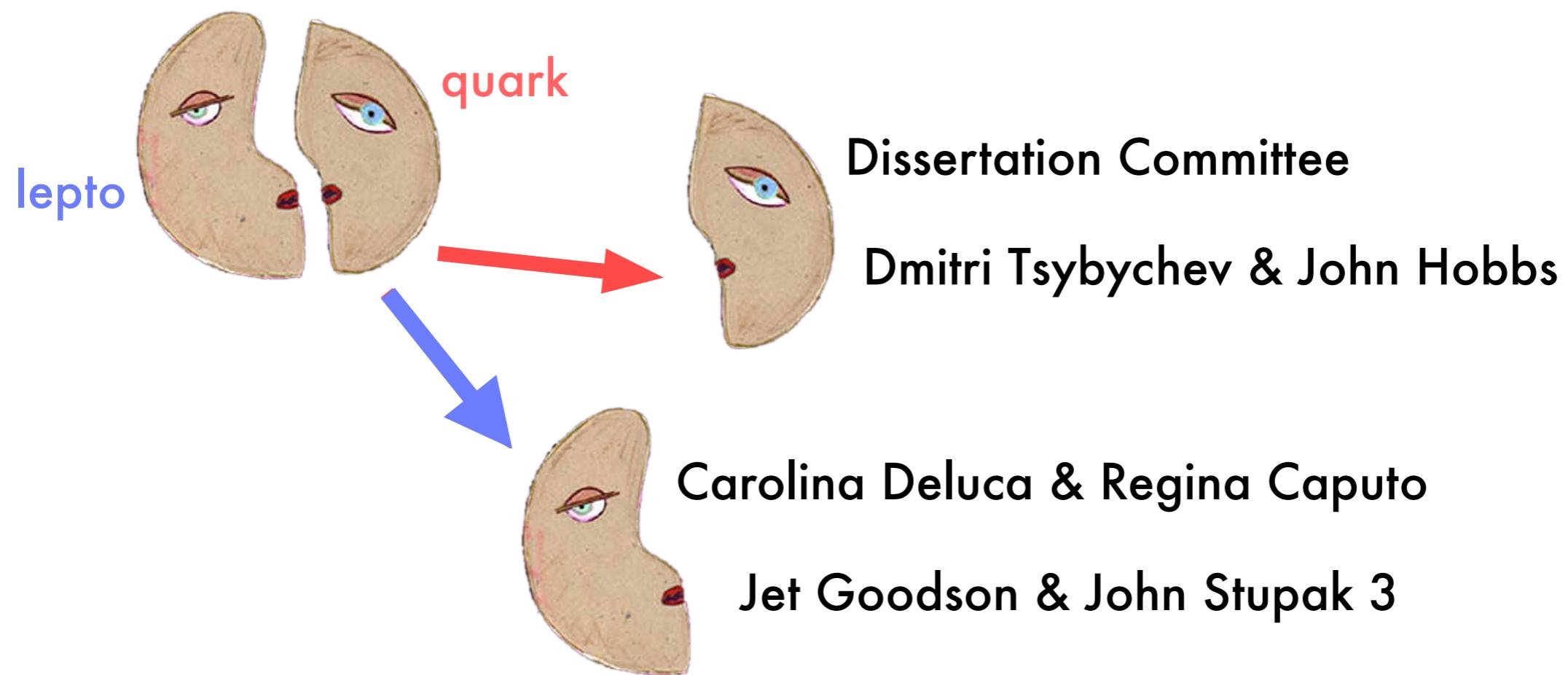


Conclusion

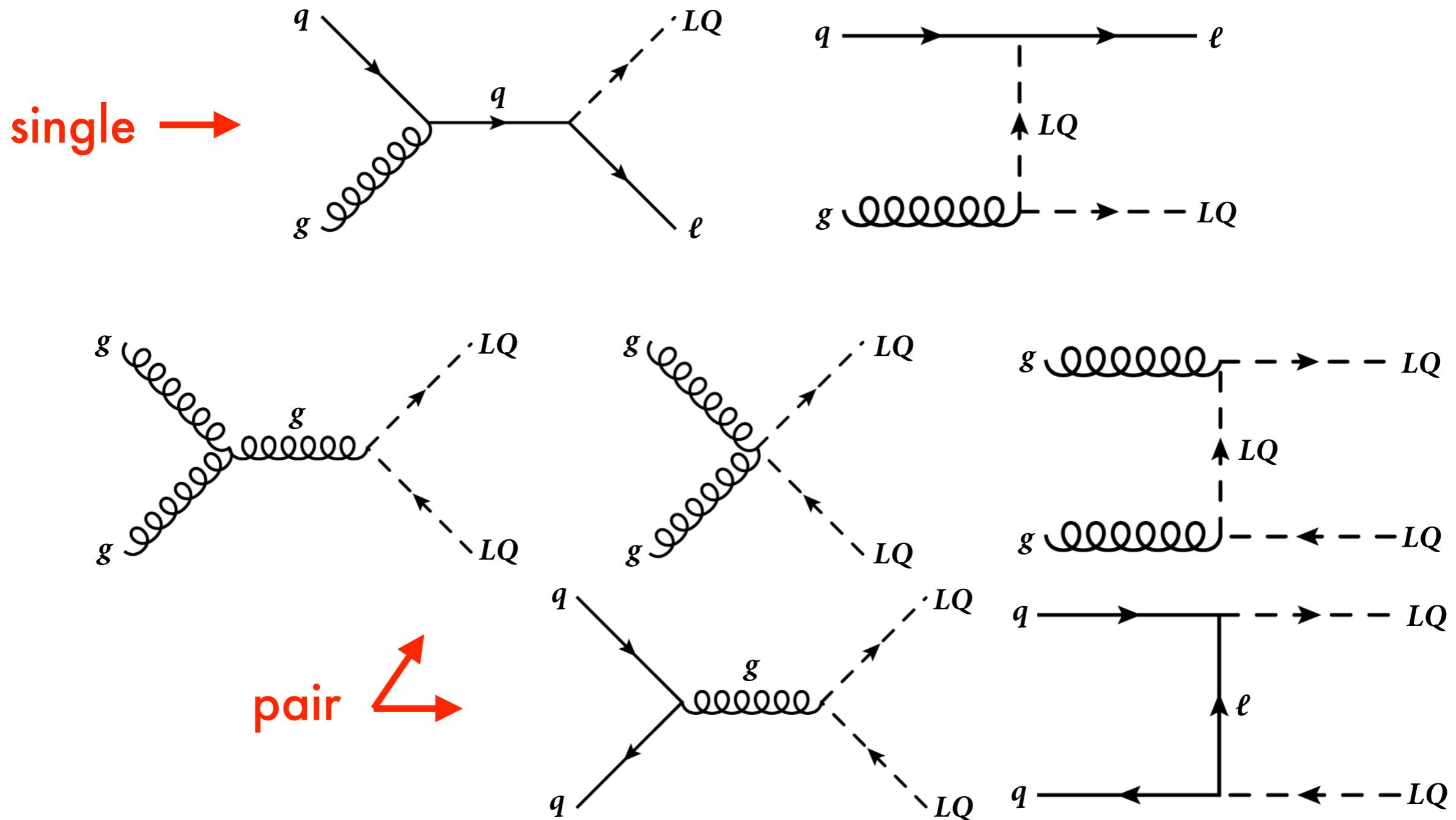
- Searched for 2nd-generation scalar LQs in the $\mu\nu jj$ channel
- Agreement within uncertainties between data and SM predictions in selected event samples... no evidence of LQs
- 2nd-generation scalar LQ pair-production excluded at 95% CL for $m_{LQ} < 594$ (685) GeV at $\beta = 0.5$ (1.0)
 - most stringent limits to date!
- Publication submitted to European Physical Journal C, currently online: [hep-ex > arXiv:1203.3172](#)



Thank you!



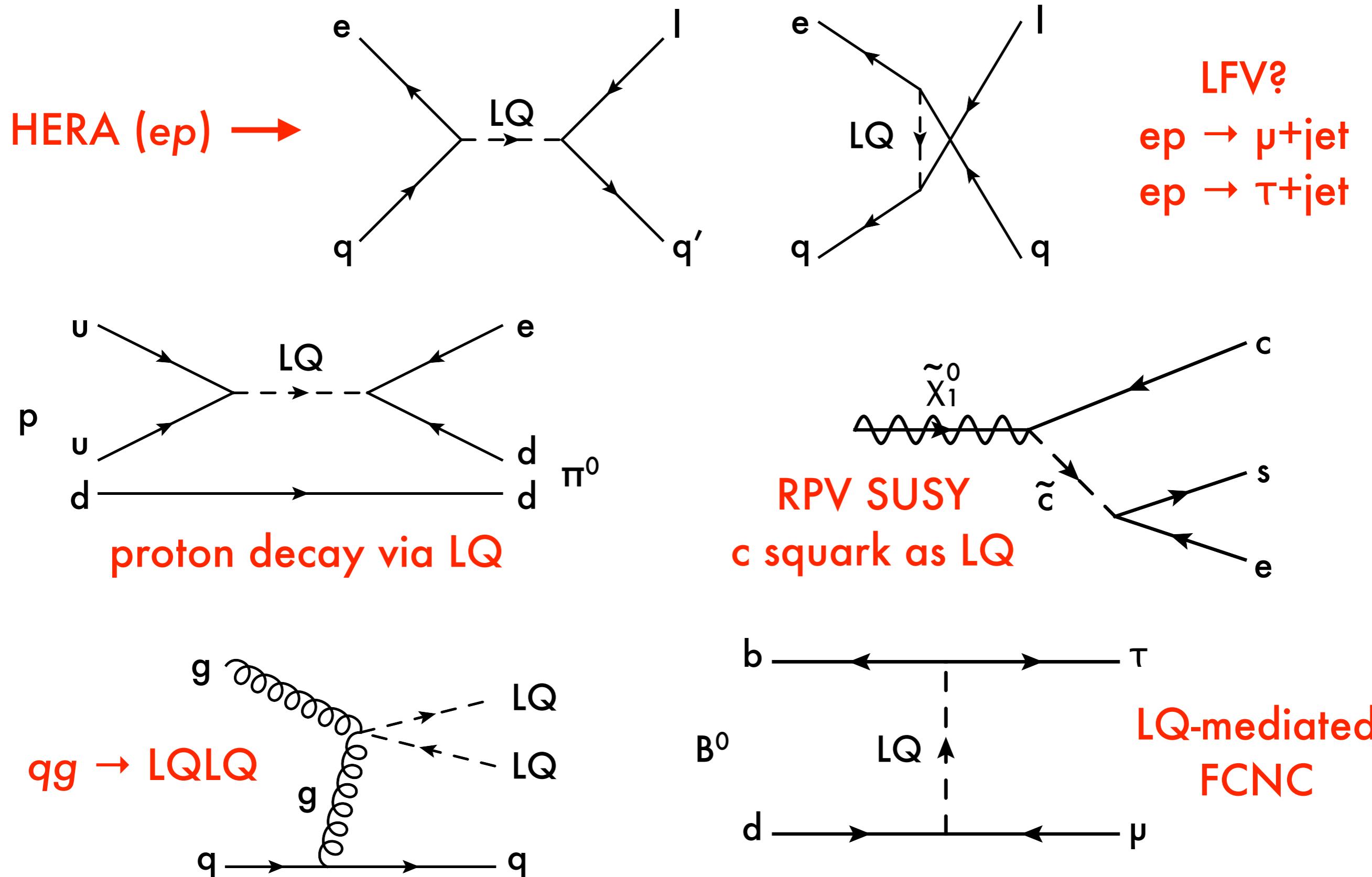
LQ Production in pp Collisions



$$\hat{\sigma}_{\text{LO}} [q\bar{q} \rightarrow LQ\overline{LQ}] = \frac{2\alpha_s^2 \pi}{27\hat{s}} v^3, \quad v \equiv (1 - 4m_{\text{LQ}}^2/\hat{s})^{1/2}$$

$$\hat{\sigma}_{\text{LO}} [gg \rightarrow LQ\overline{LQ}] = \frac{\alpha_s^2 \pi}{96\hat{s}} \left[v (41 - 31v^2) + (18v^2 - v^4 - 17) \log \frac{1+v}{1-v} \right]$$

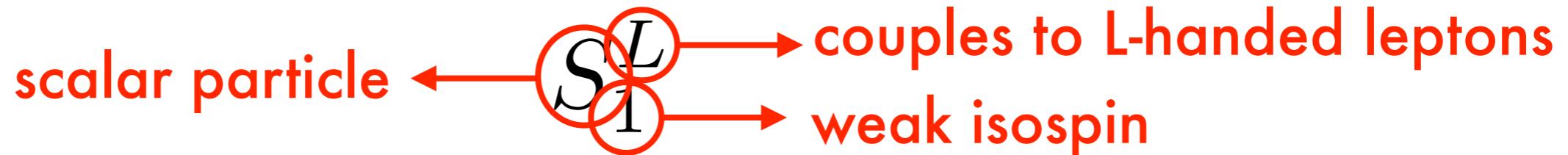
Other LQ Processes



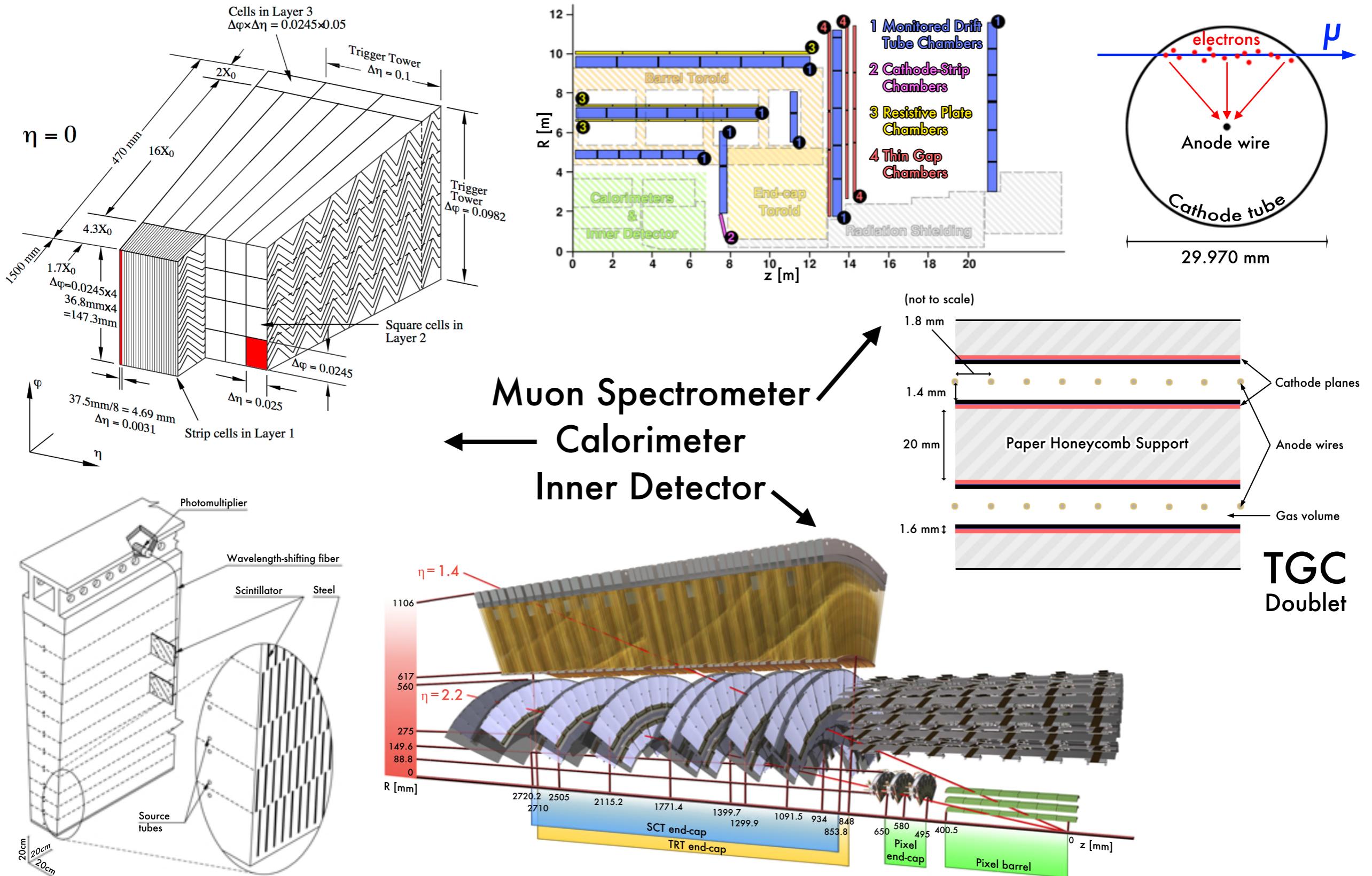
LQ States in BRW Model

LQ Type	$Q [e]$	T^3	$ F $	LQ Decay	BR(LQ $\rightarrow eq$)
S_0^L	-1/3	0	2	$e_L u_L$	0.5
				$v_e d_L$	0.5
S_0^R	-1/3	0	2	$e_R u_R$	1
\tilde{S}_0^R	-4/3	0	2	$e_R d_R$	1
				$-4/3$	-1
S_1^L	-1/3	0	2	$e_L u_L$	0.5
				$v_e d_L$	0.5
$V_{1/2}^L$	+2/3	+1	2	$v_e u_L$	0
				$-4/3$	-1/2
$V_{1/2}^R$	-1/3	+1/2	2	$v_e d_R$	0
				$-4/3$	-1/2
$\tilde{V}_{1/2}^L$	-1/3	+1/2	2	$e_L u_L$	1
				$-1/3$	-1/2
$\tilde{V}_{1/2}^R$	+2/3	+1/2	2	$v_e u_R$	0

V_0^L	-2/3	0	0	$e_L \bar{d}_R$	0.5
V_0^R	-2/3	0	0	$e_R \bar{u}_L$	1
\tilde{V}_0^R	-5/3	0	0	$e_R \bar{u}_L$	1
				$-5/3$	-1
V_1^L	-2/3	0	0	$e_L \bar{d}_R$	0.5
				$v_e \bar{u}_R$	0.5
V_1^R	+1/3	+1	0	$v_e \bar{d}_R$	0
				$-5/3$	-1/2
$S_{1/2}^L$	-2/3	+1/2	0	$v_e \bar{u}_L$	0
				$-5/3$	+1/2
$S_{1/2}^R$	-2/3	+1/2	0	$e_R \bar{u}_R$	1
				$-5/3$	-1/2
$\tilde{S}_{1/2}^L$	-2/3	+1/2	0	$e_R \bar{d}_R$	1
				$-2/3$	-1/2
$\tilde{S}_{1/2}^R$	+1/3	+1/2	0	$v_e \bar{d}_L$	0
				$-2/3$	-1/2

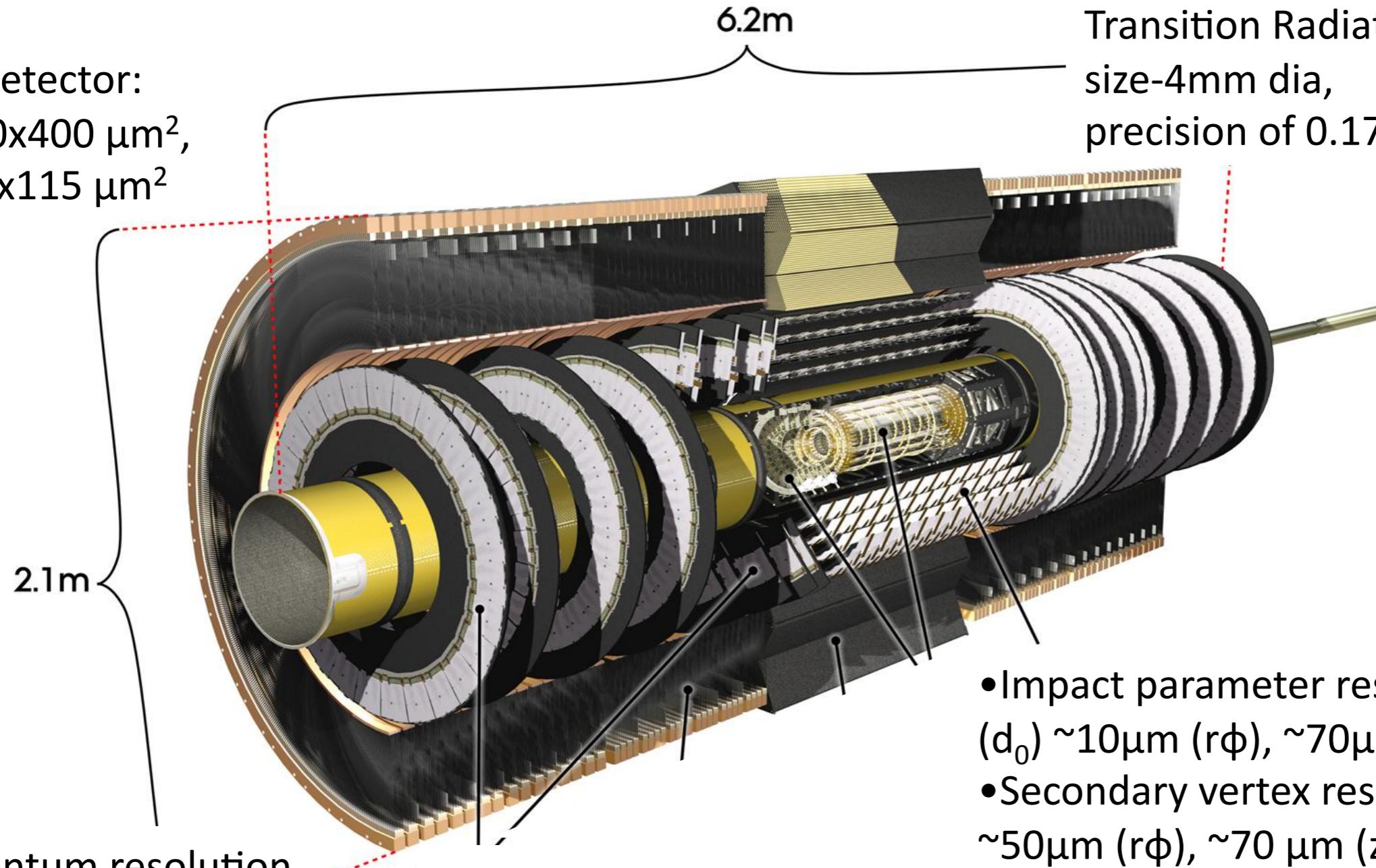


ATLAS Sub-detectors



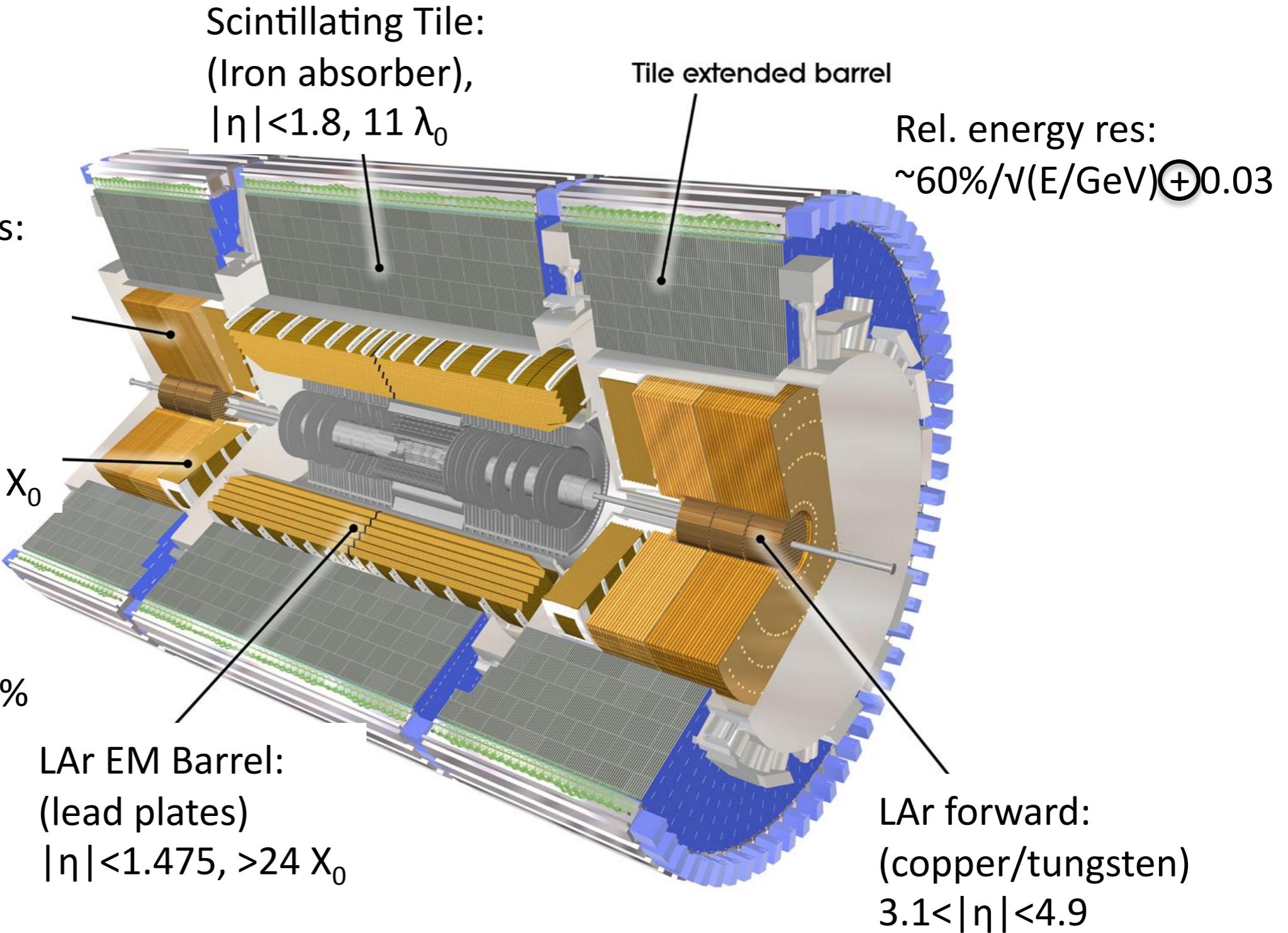
ATLAS Inner Detector

Pixel detector:
size- $50 \times 400 \mu\text{m}^2$,
res- $14 \times 115 \mu\text{m}^2$



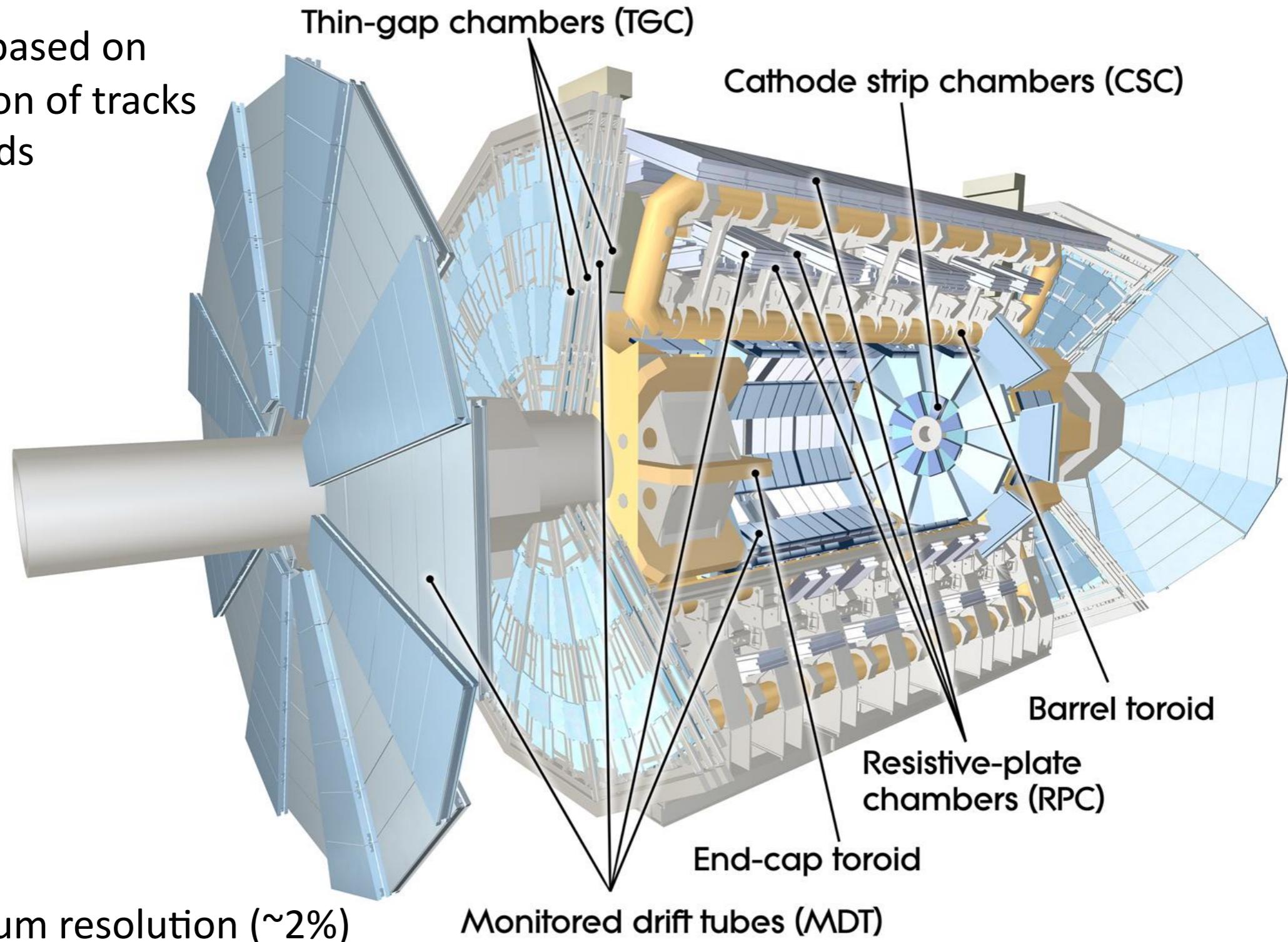
- Impact parameter resolution (d_0) $\sim 10 \mu\text{m}$ ($r\phi$), $\sim 70 \mu\text{m}$ (z)
- Secondary vertex resolution $\sim 50 \mu\text{m}$ ($r\phi$), $\sim 70 \mu\text{m}$ (z)
- Primary (main) vertex resolution $\sim 11 \mu\text{m}$ ($r\phi$), $\sim 45 \mu\text{m}$ (z)

ATLAS Calorimetry



ATLAS Inner Detector

Layout based on
deflection of tracks
by toroids



Full Selection

MUONS

ID+MS tracks combined

$$|\eta| < 2.4$$

$$p_T > 30 \text{ GeV}$$

`nBLHits > 0 OR expectBLayerHit FALSE`

$$\text{nPixHits} + \text{nPixDeadSensors} > 1$$

$$\text{nSCTHits} + \text{nSCTDeadSensors} > 5$$

$$\text{nPixHoles} + \text{nSCTHoles} < 3$$

if $|\eta| < 1.9$: `nTRTHits > 5 AND nTRTOutliers < 0.9*nTRTHits`

if $|\eta| \geq 1.9$: if `nTRTHits > 5, nTRTOutliers < 0.9*nTRTHits`

$$|d_0| < 0.1\text{mm}, |z_0| < 5.0\text{mm}$$

$$\text{isolated: } p_T^{\text{cone}20}/p_T < 0.2$$

trigger matched (MC only)

ELECTRONS (veto)

`Author = 1 OR 3`

$$|\eta| < 2.47 \text{ (w/o crack)}$$

$$p_T > 20 \text{ GeV}$$

"isEM Medium"

$$E_T^{\text{cone}20}/E_T < 0.1$$

JETS

$$|\eta| < 2.8$$

$$p_T > 30 \text{ GeV}$$

"loose cleaning" (data only)

$$\text{TileGap3} > 0.5 \text{ OR } \text{BCH_CORR_CELL} > 0.5$$

$$\Delta R(\text{jet}, \text{l}) > 0.4$$

EVENTS

Passes SUSY GRL (data only)

fires `EF_mu18_MG OR EF_mu40_MSonly_barrel trigger`

at least one primary vertex with at least 3 associated tracks

exactly one good muon and zero good electrons

missing transverse energy (MET) $> 30 \text{ GeV}$

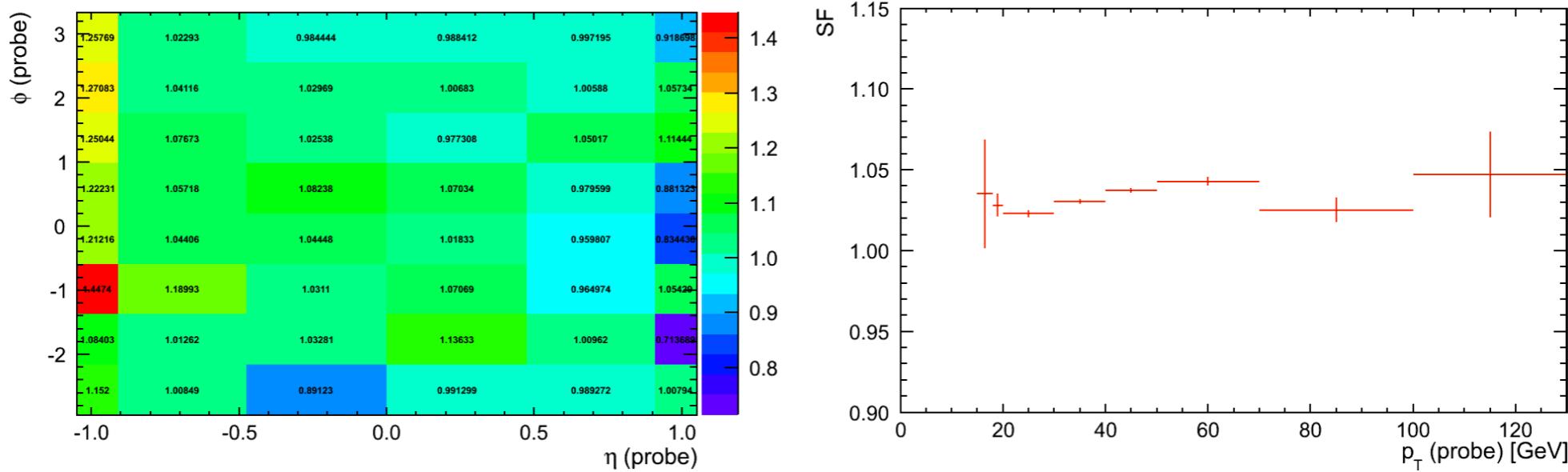
at least two good jets

transverse mass $M_T(\mu, \text{MET}) > 40 \text{ GeV}$

zero jets in LAr hole and no "LAr Error"

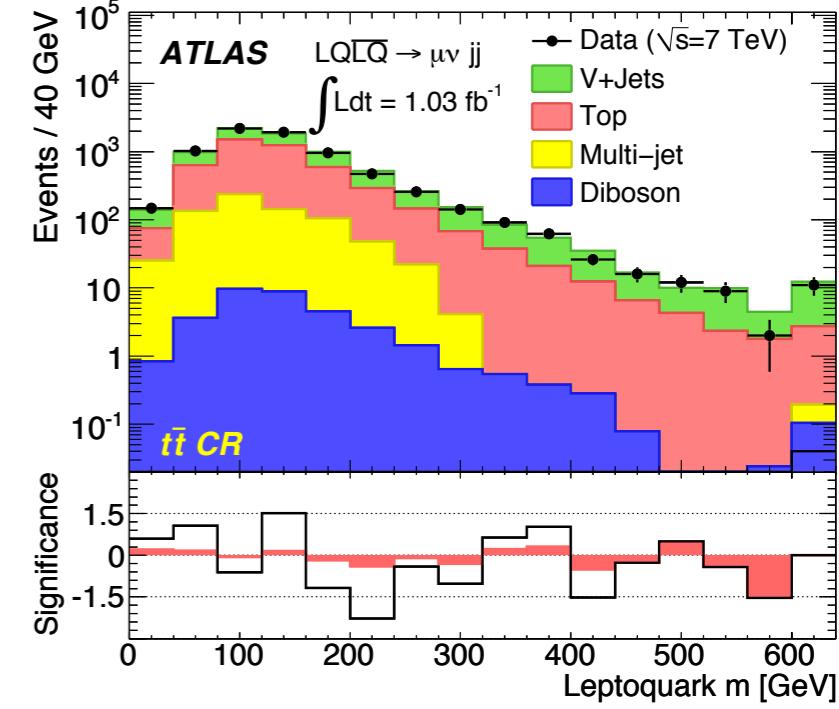
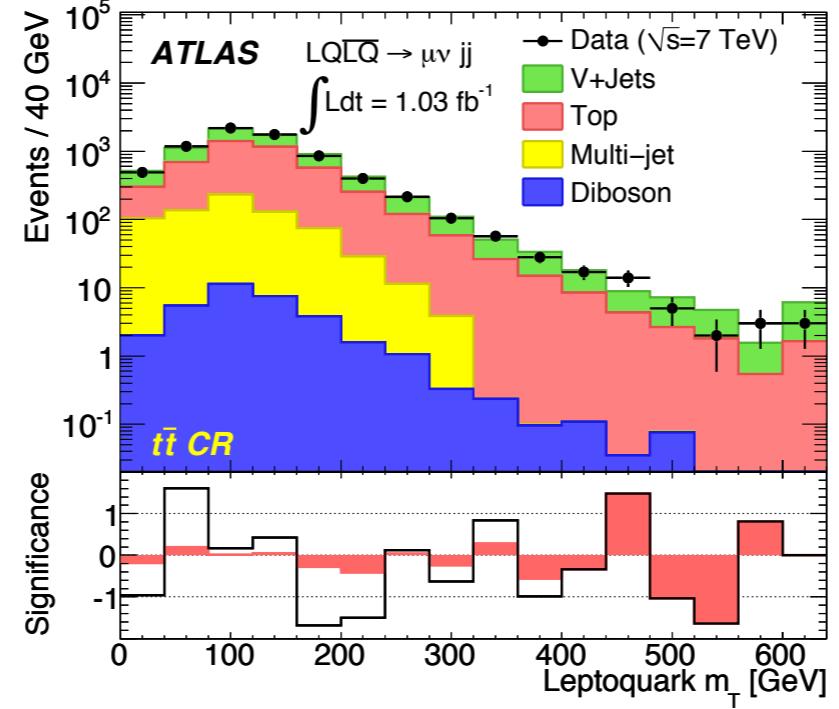
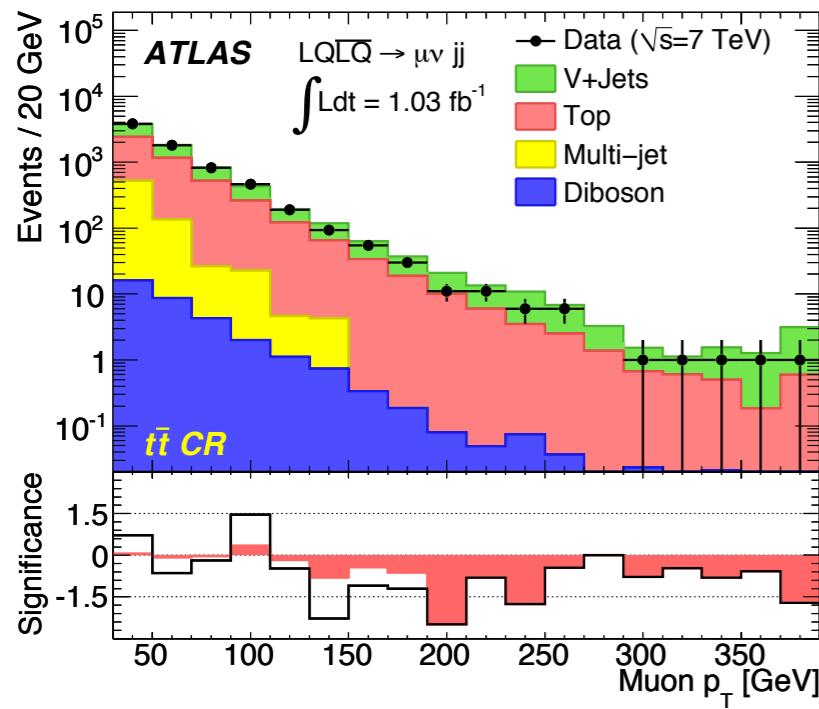
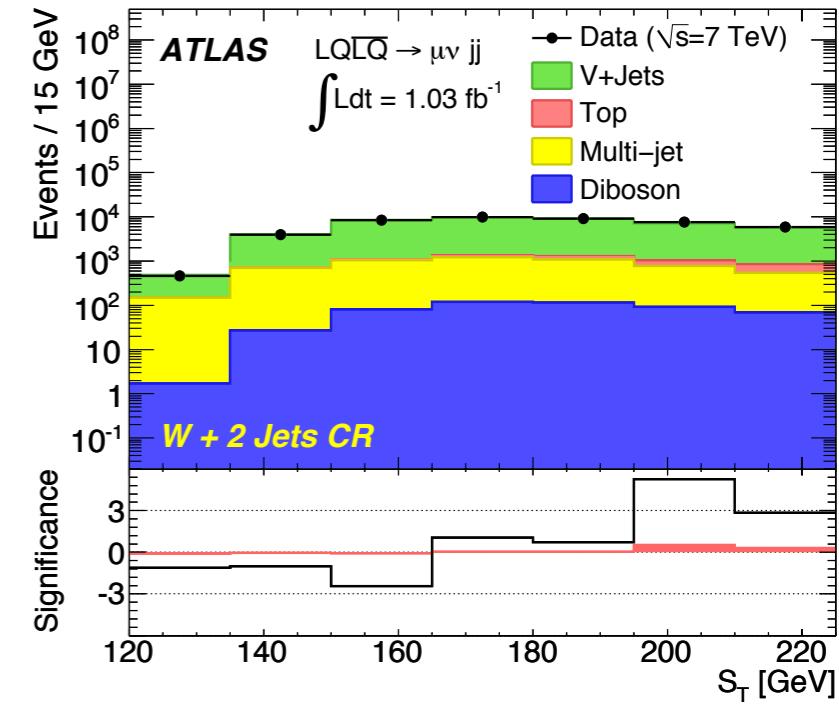
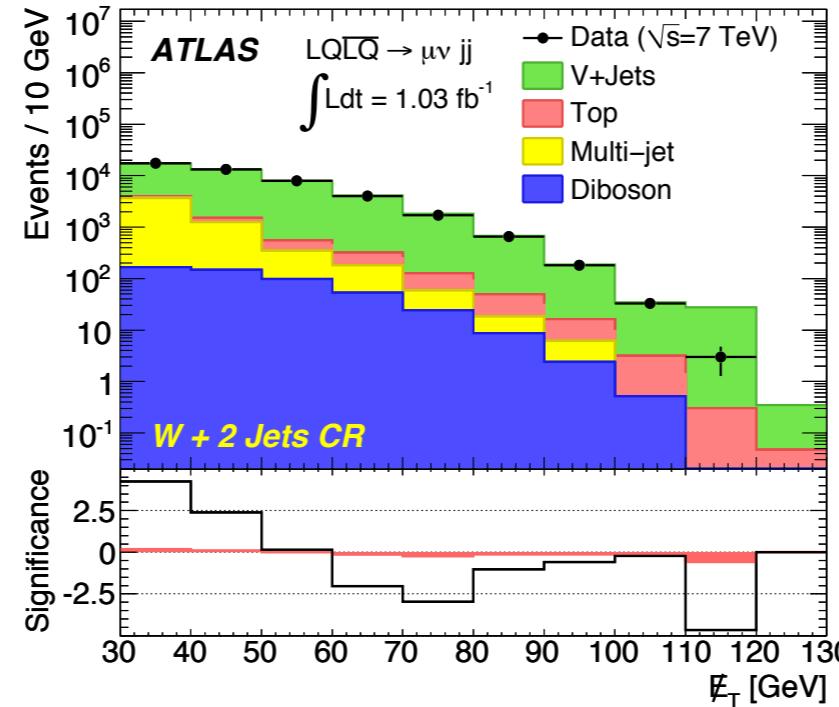
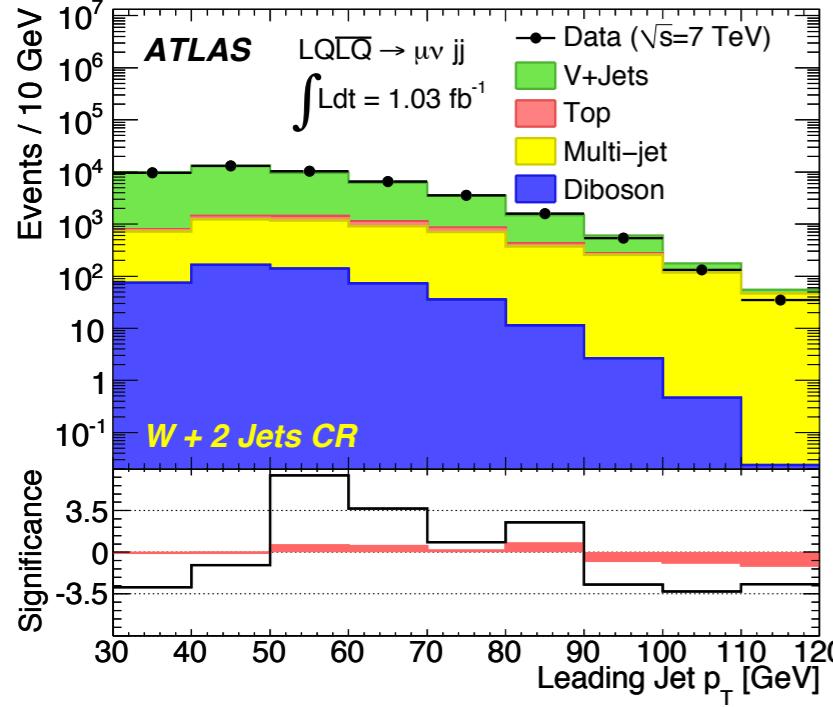
	Loose
HEC spikes	<code>HECf>0.5 && HECQ >0.5 or neg. E >60GeV</code>
EM coherent noise	<code>EMf>0.95 && LArQ >0.8 && eta <2.8</code>
Non-collision background & Cosmics	<code> t >25ns or EMf<0.05 && Chf<0.05 && eta <2 or EMf<0.05 && eta >=2 or FMax>0.99 && eta <2</code>

MC Corrections



- Muon trigger and identification efficiencies
 - tag-and-probe study of $Z \rightarrow \mu\mu$ events; η , ϕ (p_T) dependent in barrel (end-cap)
- Muon momentum resolution “smeared” to match data
- Pile-up re-weighting
 - average number of interactions per bunch crossing made to match that in data
- “LAr Hole” (dead region of LAr barrel calorimeter)
 - veto good electrons in the LAr hole, veto events with a good jet in the LAr hole

More CR Plots



W+jets, t-tbar Normalization

- Discrepancy between data and MC resulting in large deviation from unity of SFs is attributed to mis-modeling of pileup in MC samples
 - occurs in low- p_T regime
 - first appeared when switching from MC10a to MC10b
 - SFs closer to unity when p_T thresholds are raised
 - SFs closer to unity when $|JVF| > 0.75$ cut to remove pileup is applied, as shown in table below

	t-tbar SF	W+jets SF
nominal	1.092 ± 0.25	0.911 ± 0.005
$ JVF > 0.75$	1.066 ± 0.025	1.063 ± 0.026

Systematic Uncertainties

- Full shape information taken into account in limit-setting procedure
- Summary table of approximate values shown below: L' is nominal LLR distribution, $\delta L'$ is difference between LLR with $\pm 1\sigma$ systematic uncertainty applied and nominal distributions

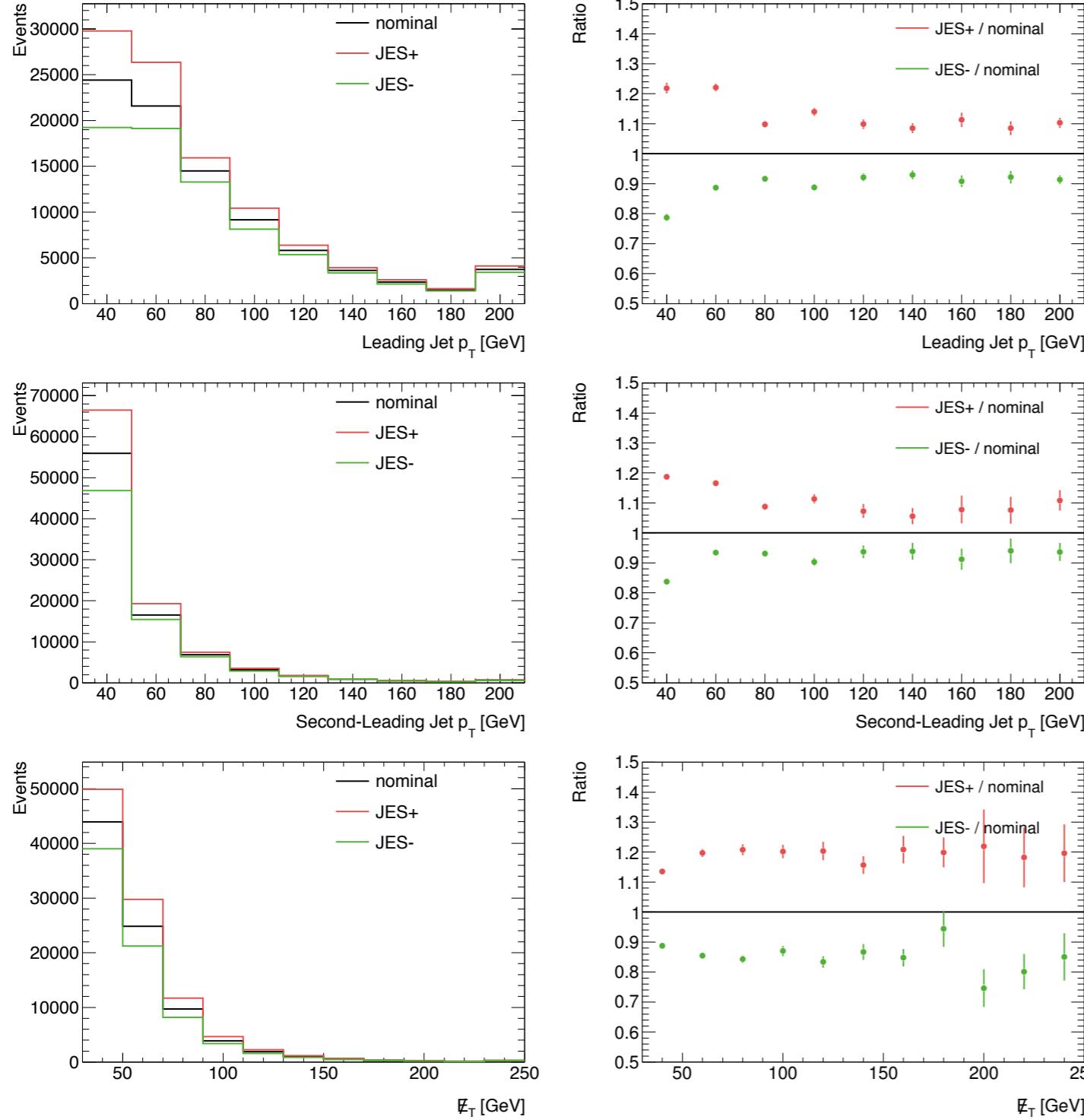
$$\text{systematic} = \left| \frac{\int L' + \frac{1}{2} (|\delta L'_{+1\sigma}| + |\delta L'_{-1\sigma}|) dL'}{\int L' dL'} - 1 \right|$$

Systematic	V+jets	$t\bar{t}$	Single top	Dibosons	MJ	LQ Signal	Systematic	W+jets	Z+jets	$t\bar{t}$	Single top	Dibosons	MJ	LQ Signal
Muon Eff. SF	0.011	0.019	0.067	0.060	–	0.045	Muon Eff. SF	<0.01	0.022	<0.01	0.015	<0.01	–	0.041
Muon pT Res.	<0.01	0.018	0.076	0.063	–	0.046	Muon Energy Res.	<0.01	0.024	<0.01	0.015	<0.01	–	0.038
Jet Energy Scale	0.102	0.040	0.124	0.094	–	0.056	Jet Energy Scale	0.170	0.176	0.054	0.060	0.127	–	0.067
Jet Energy Res.	0.128	0.054	0.164	0.120	–	0.040	Jet Energy Res.	0.126	0.102	0.039	0.053	0.109	–	0.056
Top Mass	–	0.087	–	0.060	–	–	Top Mass	–	–	0.039	–	<0.01	–	–
ISR/FSR	–	0.098	–	0.060	–	–	ISR/FSR	–	–	0.051	–	<0.01	–	–
POWHEG/MC@NLO	–	0.062	–	0.060	–	–	POWHEG/MC@NLO	–	–	0.064	–	<0.01	–	–
PYTHIA/HERWIG	–	0.049	–	0.060	–	–	PYTHIA/HERWIG	–	–	0.031	–	<0.01	–	–
SHERPA/ALPGEN	0.030	–	–	–	–	–	SHERPA/ALPGEN	0.021	0.022	–	–	–	–	–
MJ Normalization	–	–	–	–	0.916	–	MJ Normalization	–	–	–	–	–	0.332	–
PDF, signal	–	–	–	–	–	0.086	PDF, signal	–	–	–	–	–	–	0.067
LLR Input pdf	0.044	0.064	0.092	0.061	–	0.034	LLR Input pdf	0.046	0.045	0.114	0.080	0.067	–	0.057
Luminosity	–	–	0.037	0.037	–	0.037	Luminosity	–	–	–	0.037	0.037	–	0.037
Data Normalization	0.100	0.036	–	–	–	–	Data Normalization	0.100	0.100	0.100	–	–	–	–
Total	0.20	0.18	0.25	0.22	0.92	0.14	Total	0.24	0.23	0.19	0.12	0.18	0.33	0.14

ppii

pvii

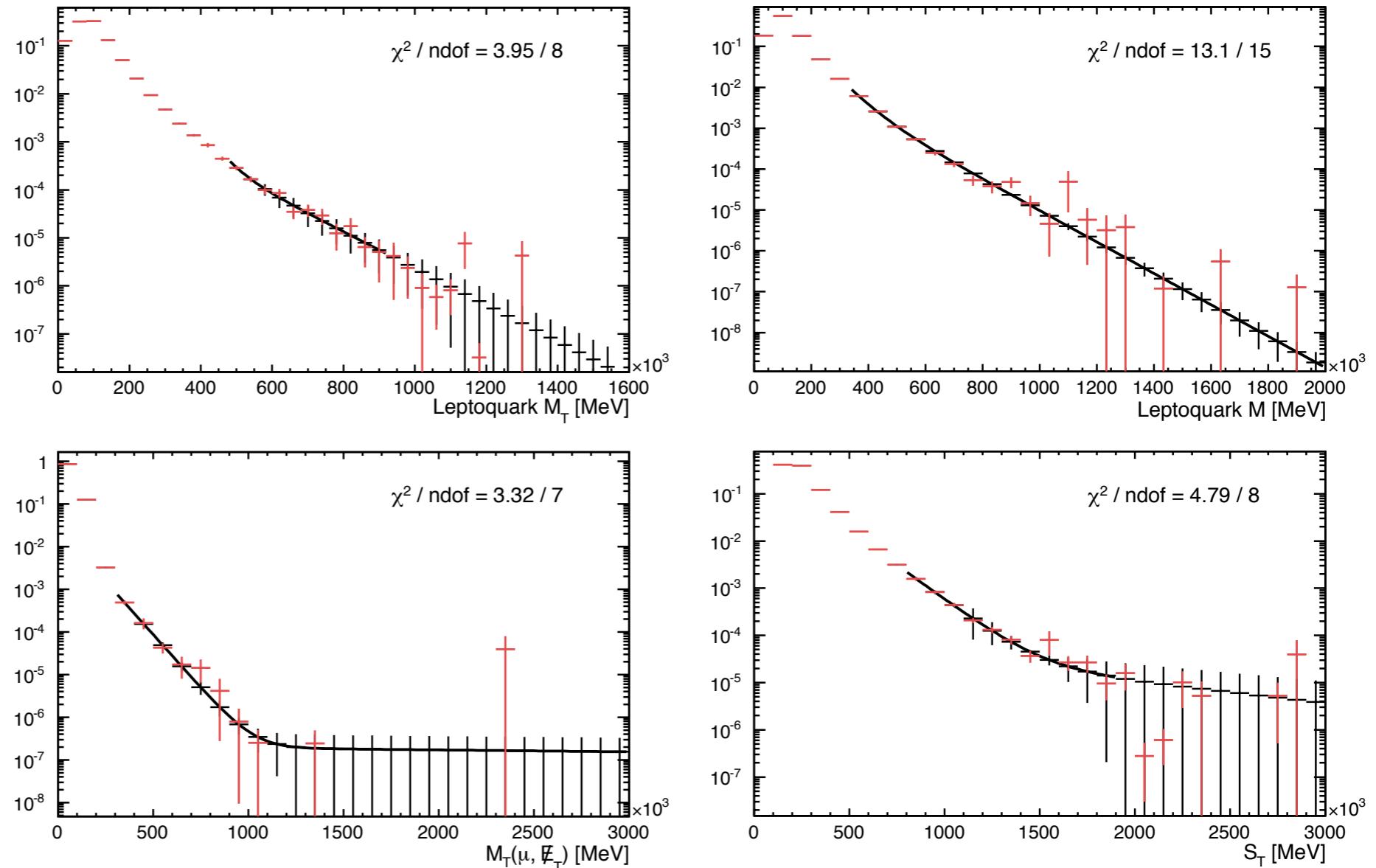
JES Systematic Variation



- jet energy scale: large systematic uncertainty
- significant impact on jet p_{T} and MET distributions
- relatively small impact on LLR distribution

PDF Fits as LLR Input

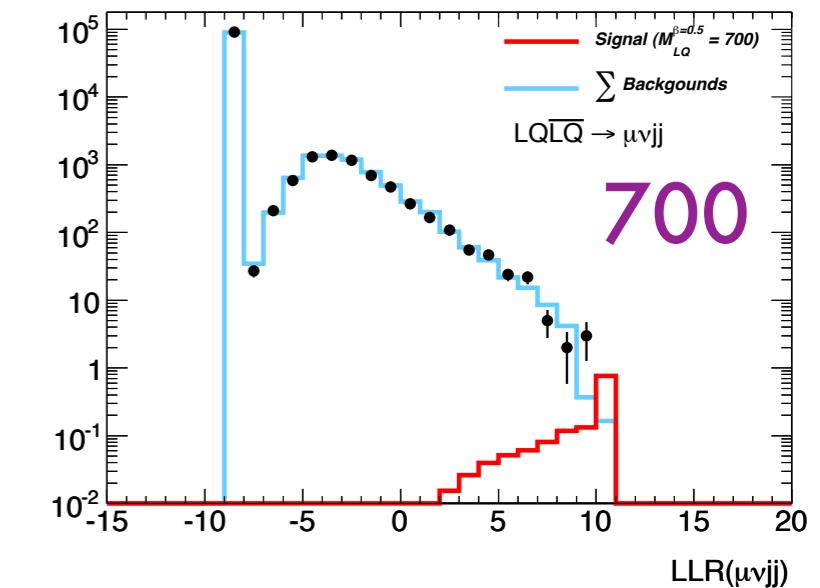
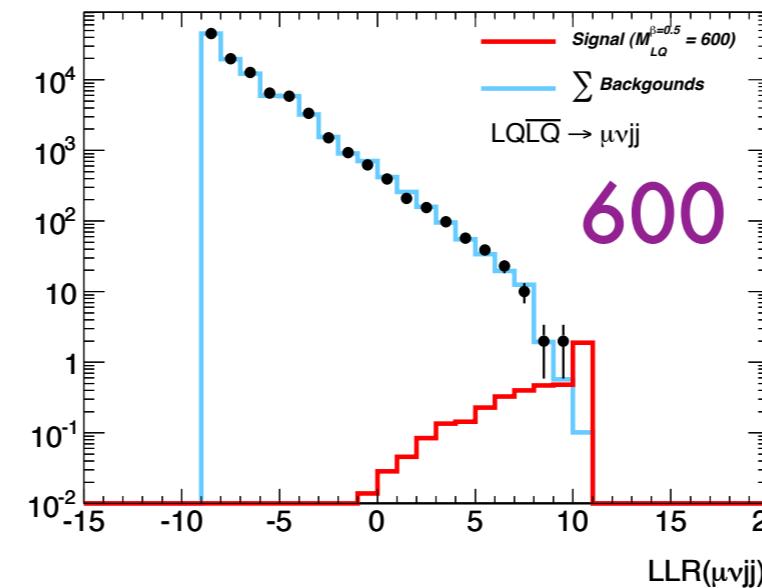
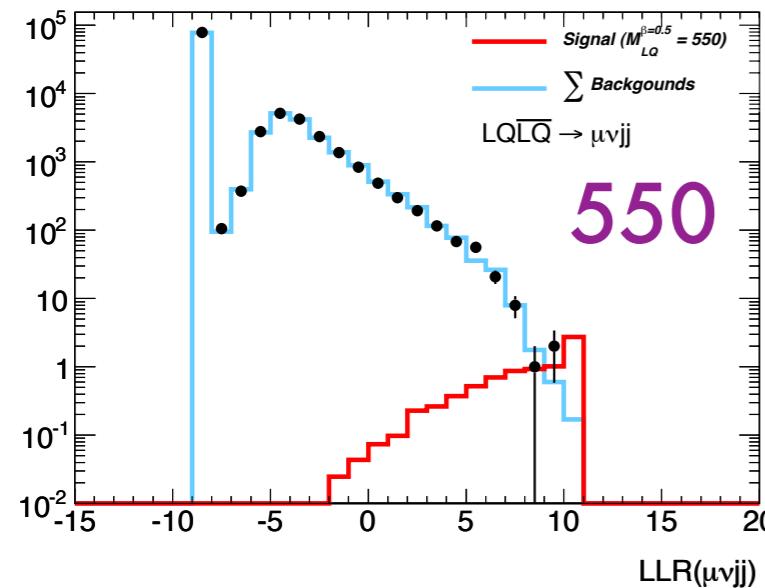
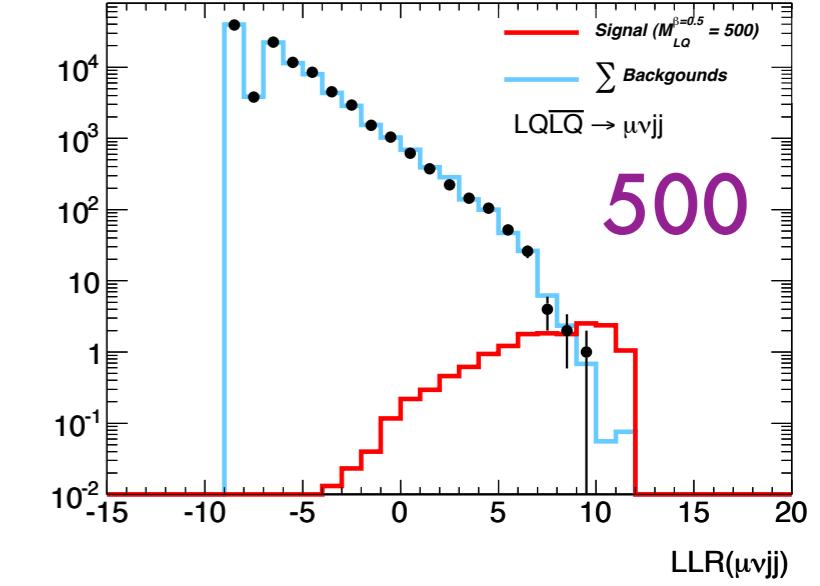
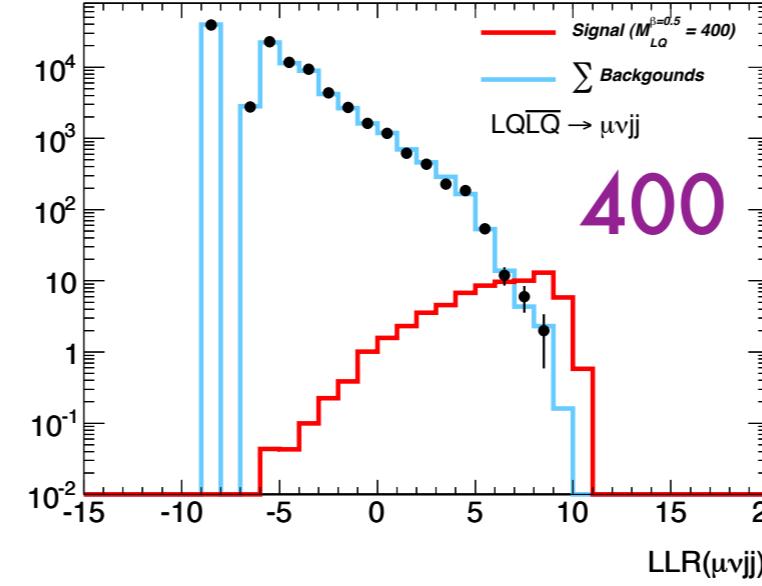
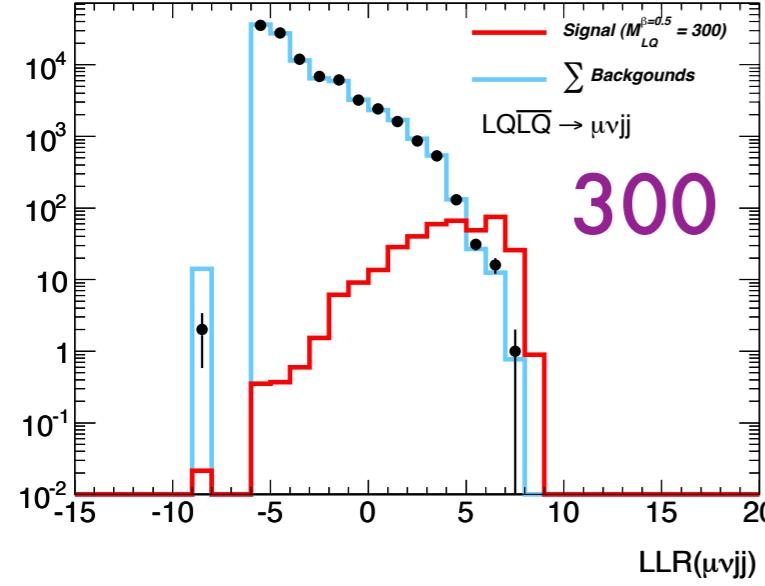
- Low stats in tails => event weights driven by fluctuations
- Fit double exponential to good stat range, extrapolate out
- Replace bin contents with fit value if $n_{\text{evts}}=0$ or stat uncertainty > $0.1 * n_{\text{evts}}$



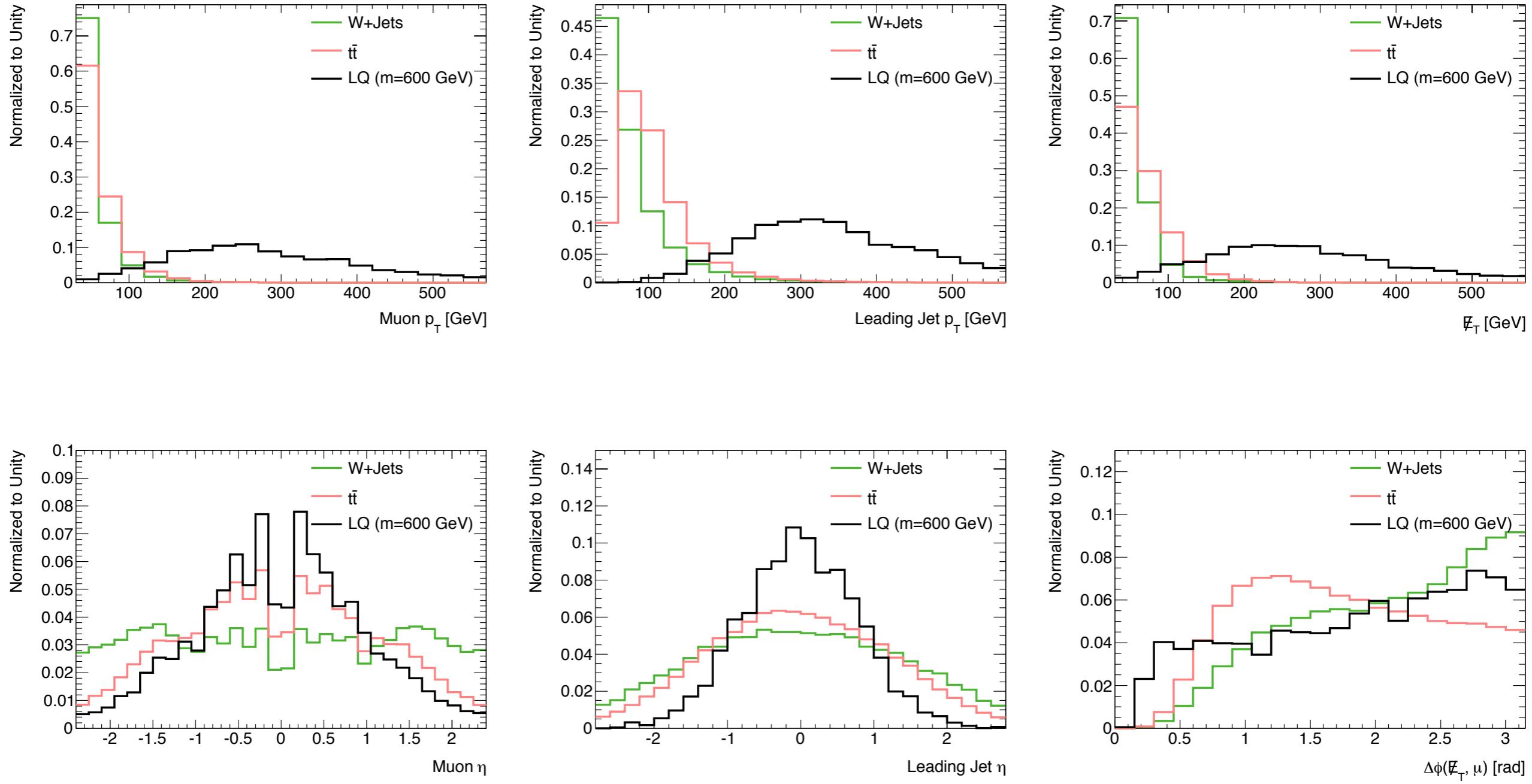
$$f(x) = N \cdot \frac{a \cdot e^{-x/b} + (1-a) \cdot e^{-x/c}}{ab \cdot e^{-d/b} + (1-a)c \cdot e^{-d/c}}$$

N is overall normalization, a ($1-a$) is fraction of first (second) exponential,
 b (c) is normalization of first (second) exponential's slope,
 d is maximum x-value included in fit

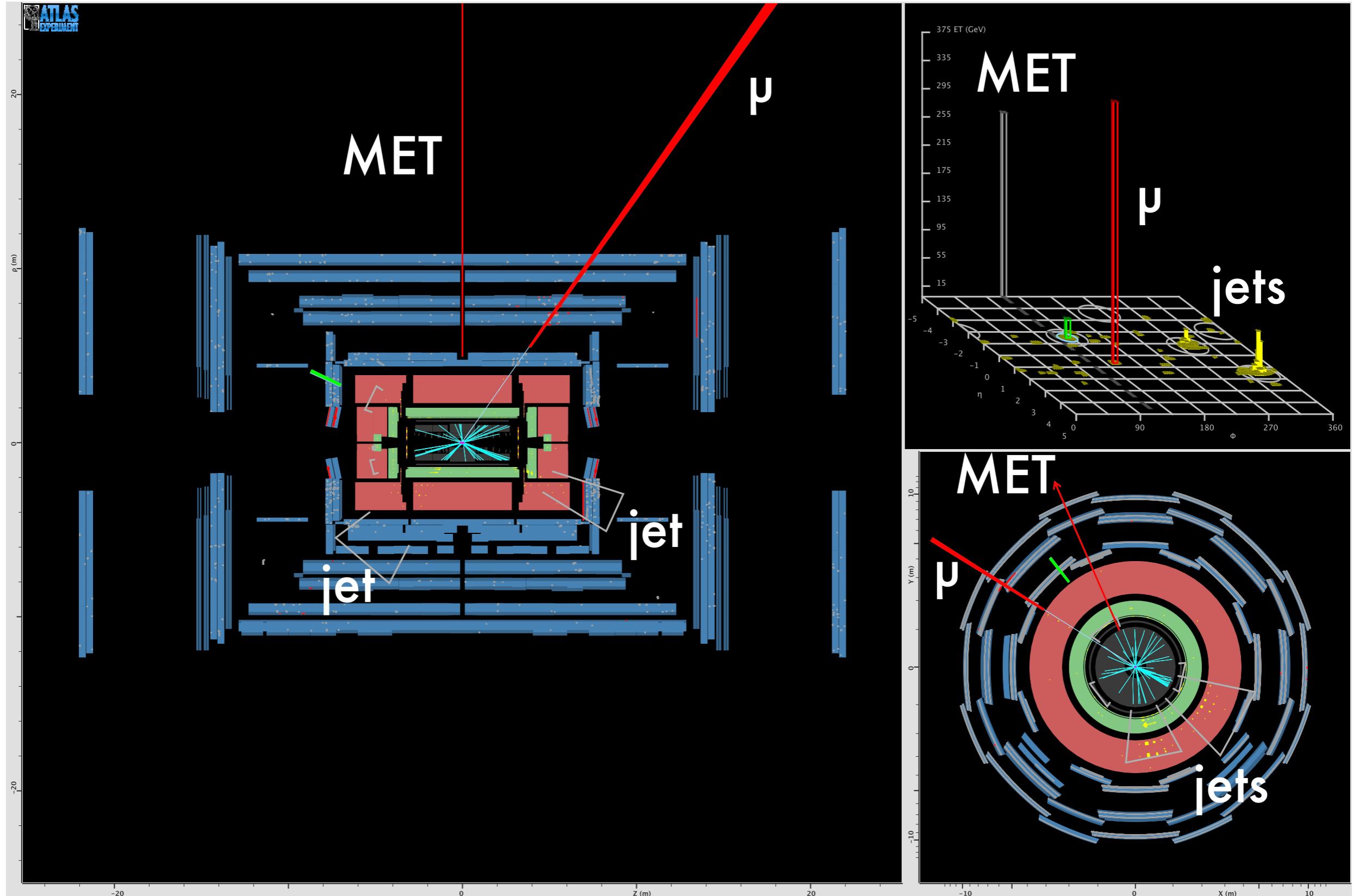
Re-binned LLR(m_{LQ})



More Shape Comparisons



Event Display



Simple Case, Generalized

- x is data, s and b are expected signal and background yields; likelihoods \mathcal{L} are Poisson probability distribution functions

$$Q(x) = \frac{\mathcal{L}(x | H_1)}{\mathcal{L}(x | H_0)} = \frac{(s+b)^x e^{-(s+b)} / x!}{(b)^x e^{-(b)} / x!}$$

- bin discriminating variable? \mathcal{L} is product of bin-by-bin likelihoods; combine orthogonal channels? also product of individual \mathcal{L} 's!

$$Q(x) = \prod_i^{\text{channels}} \prod_j^{\text{bins}} \frac{(s_{ij} + b_{ij})^{x_{ij}} e^{-(s_{ij} + b_{ij})} / x_{ij}!}{(b_{ij})^{x_{ij}} e^{-(b_{ij})} / x_{ij}!} = \prod_i^{\text{channels}} \prod_j^{\text{bins}} e^{-(s_{ij})} \left(\frac{s_{ij} + b_{ij}}{b_{ij}} \right)^{x_{ij}}$$

- take log-likelihood ratio for convenience/stability

$$\text{LLR}(x) = -2 \ln(Q(x)) = \sum_i^{\text{channels}} \sum_j^{\text{bins}} \left[s_{ij} - x_{ij} \ln \left(1 + \frac{s_{ij}}{b_{ij}} \right) \right]$$

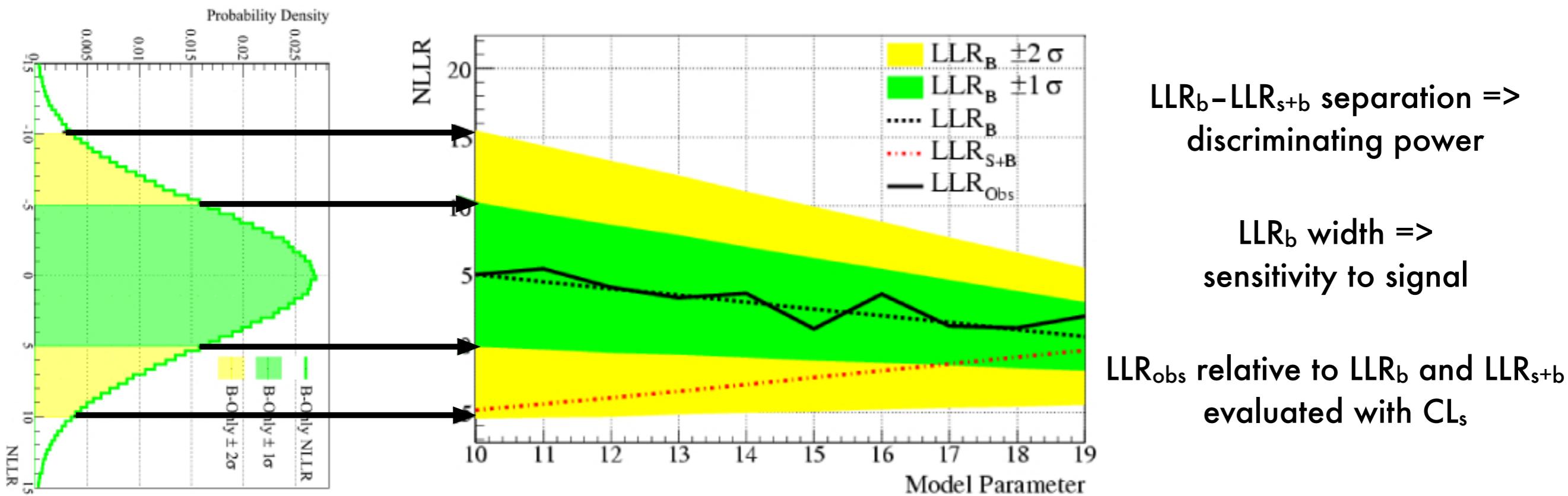
- compute p-values, confidence levels, etc. as before

$$CL_b = \int_{\text{LLR}(b|x)}^{\infty} P(b|x') d(\text{LLR}(b|x')) , CL_{s+b} = \int_{\text{LLR}(s+b|x)}^{\infty} P(s+b|x') d(\text{LLR}(s+b|x'))$$

$$CL_s = CL_{s+b} / CL_b$$

The CL_s Method

- “Modified-Frequentist” approach: $CL_s \equiv CL_{s+b}/CL_b = p_{s+b}/(1 - p_b)$
- normalize CL_{s+b} by CL_b , “penalizing” when sensitivity is poor
- CL_s can be interpreted as the approximate confidence obtained if background events were removed from selected event sample
- Gives conservative limits! Exclusion when $CL_s \leq \alpha$ ($0.05 \Rightarrow 95\% CL$)
- CL_s is always larger than CL_{s+b} , so upper limit is higher (weaker)



Wade Fisher, Collie: A Confidence Level Limit Evaluator

Bayesian-Frequentist Hybrid

- In Bayesian statistics, our *degree of belief* is a probability associated with a hypothesis, given by a *prior PDF* $\pi(\theta)$

- e.g. a Gaussian distribution: $\left(1/\sqrt{2\pi}\sigma\right) e^{-\frac{(x-\mu)^2}{2\sigma^2}}$

- Bayes' theorem tells how our beliefs should be updated, given data:

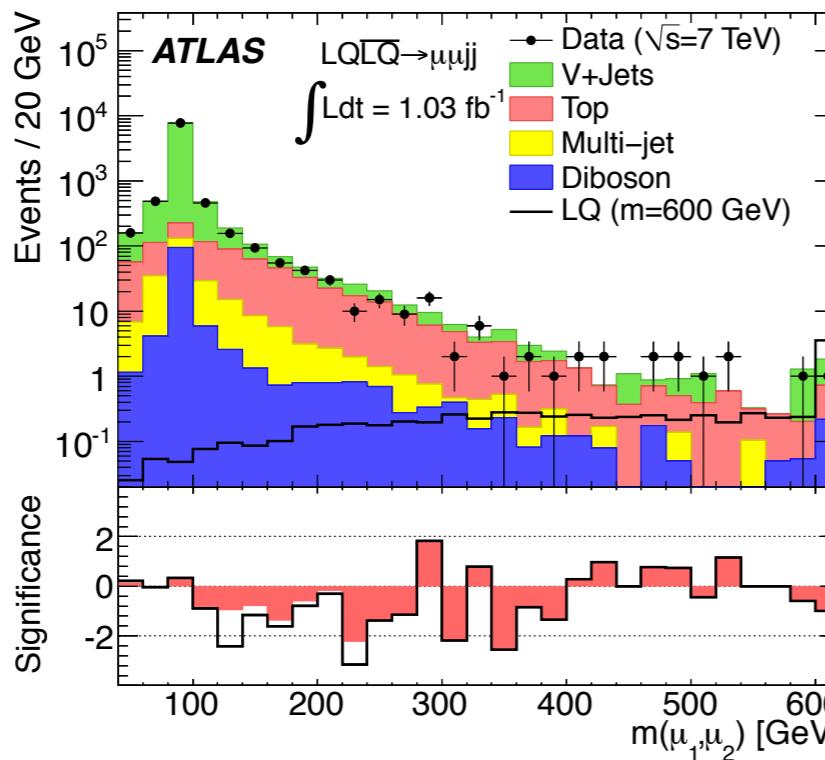
$$\text{"posterior PDF"} \rightarrow P(\theta | x) = \frac{P(x | \theta) \pi(\theta)}{P(x)} \quad \leftarrow \text{normalization}$$

- Integrate over ("marginalize") nuisance parameters:

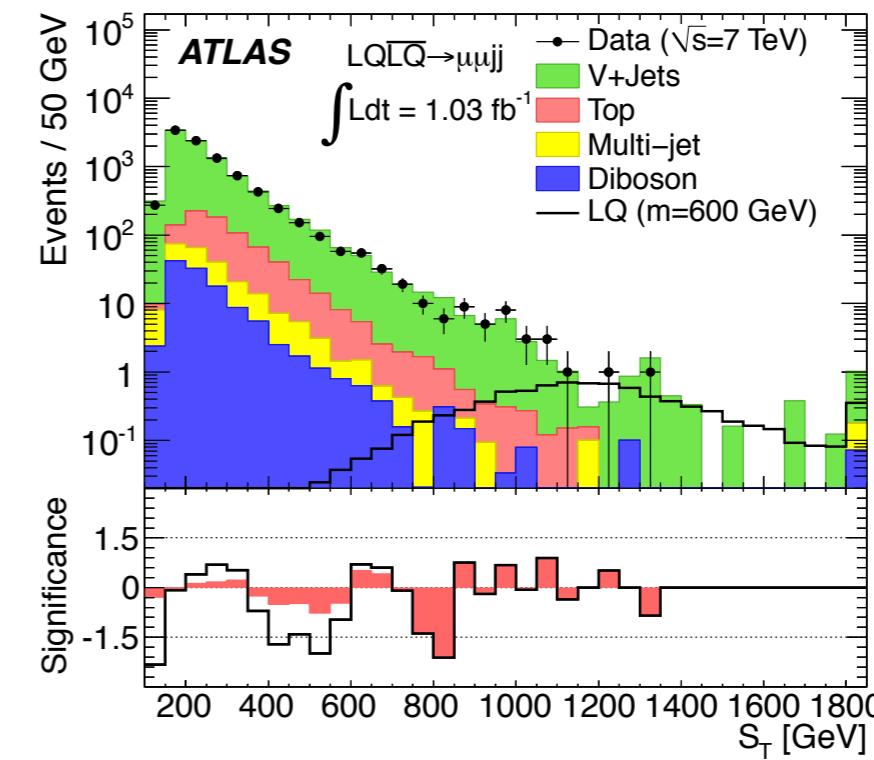
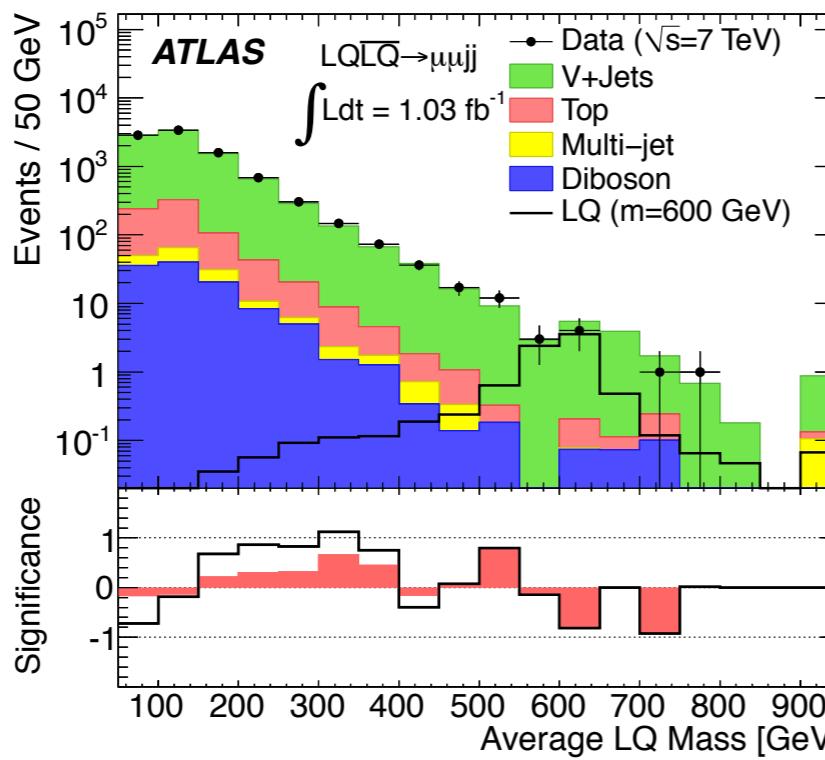
$$p(x | \theta) = \int P(x | \theta, \nu) \pi(\nu) d\nu$$

- numerically: in each pseudo-exp., sample Gaussian ($\mu=0$, $\sigma=\text{frac. uncert.}$) for each systematic, shift nominal mean of Poisson likelihood by that value
- Hybrid approach: Use Modified-Frequentist methods for central value, Bayesian methods for treatment of nuisance parameters

$\mu\mu jj$: Selected Events



EVENTS
 good detector status (data only)
 fires muon trigger
 ≤ 1 primary vertex with ≤ 3 associated tracks
 exactly two good muons, $\Delta\phi(\mu, \mu) > 3.125$
 at least two good jets, zero "bad" jets
 invariant mass $M(\mu, \mu) > 40 \text{ GeV}$

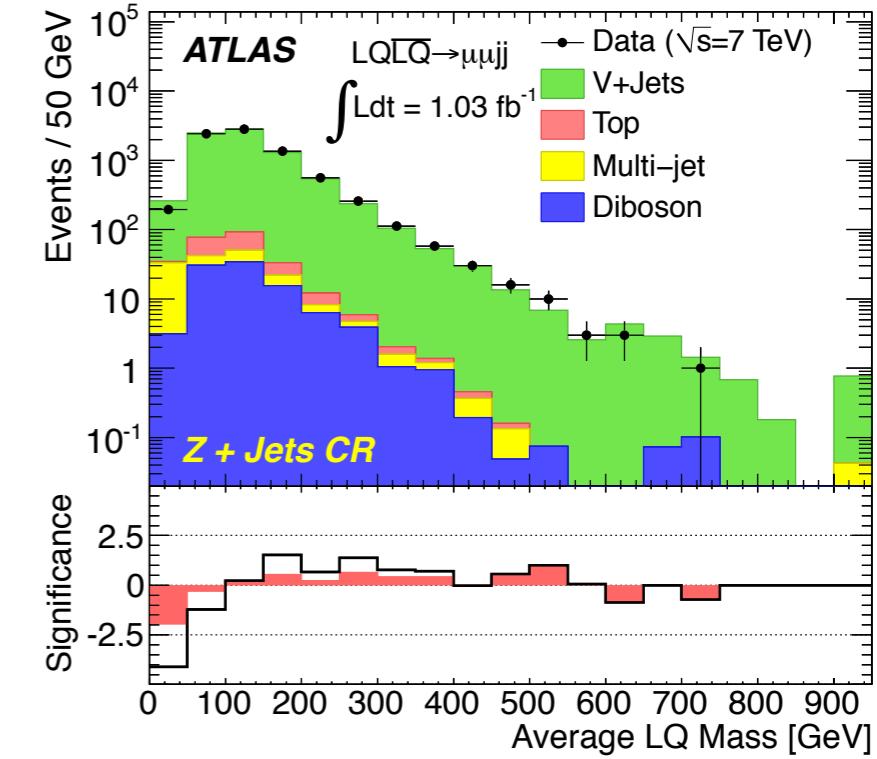
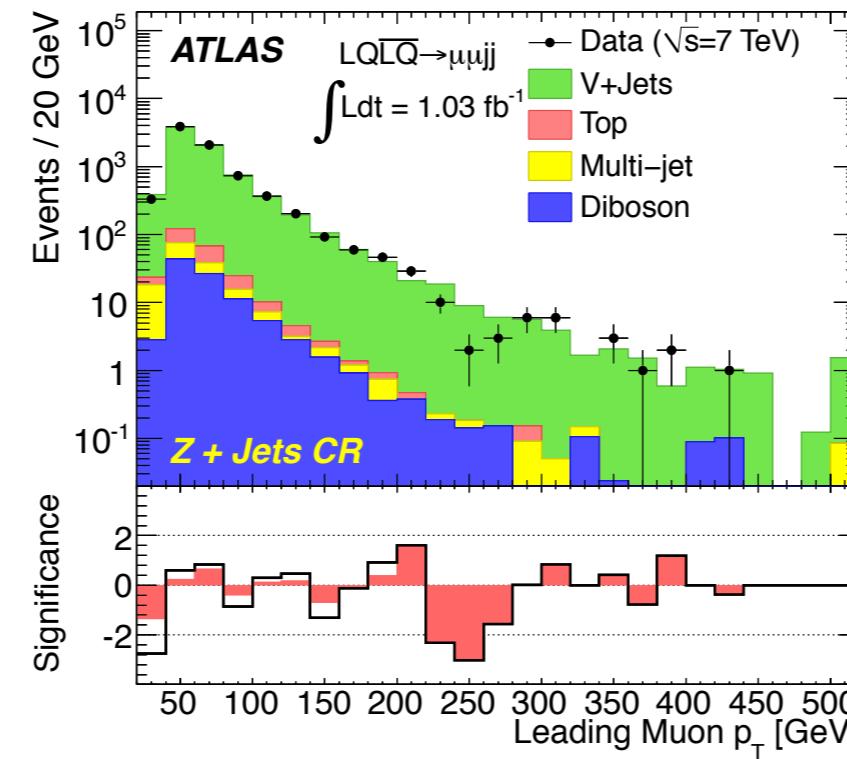


$\mu\mu jj$: Control Regions

Z+jets CR

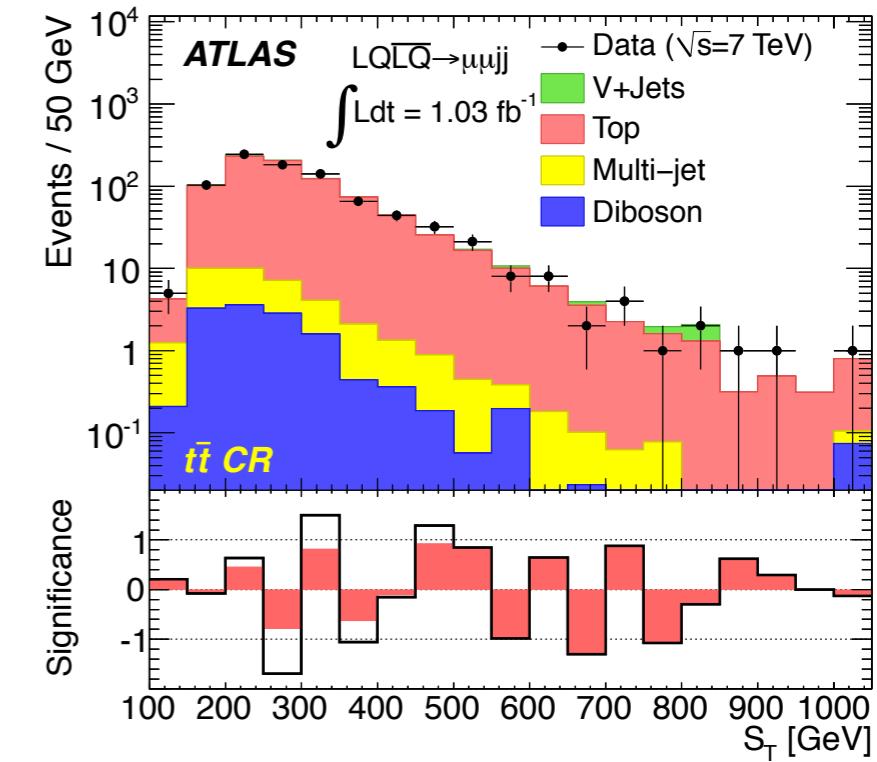
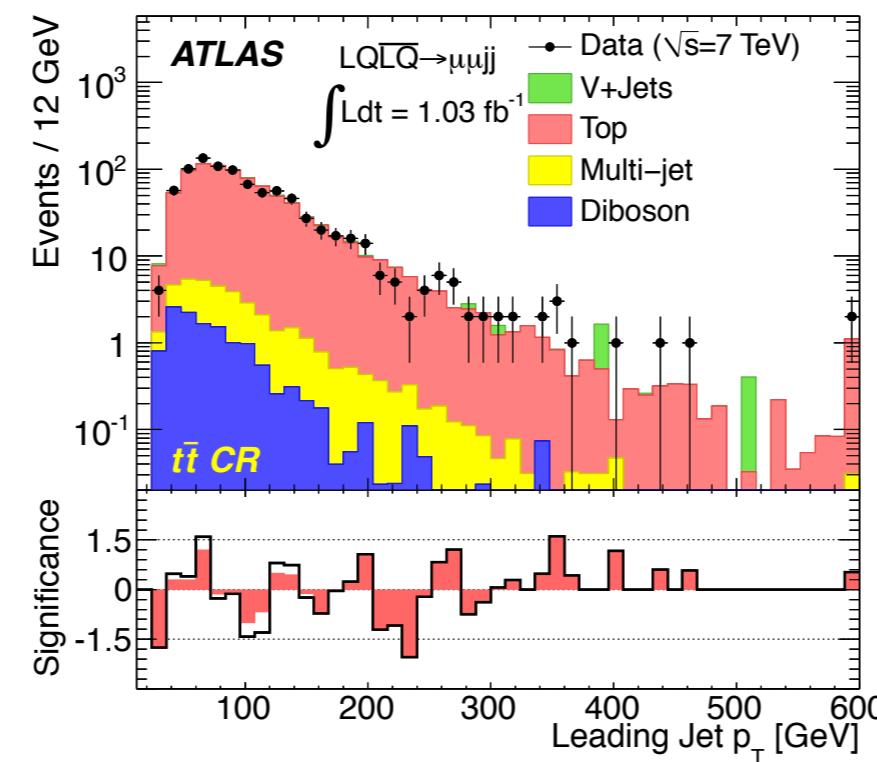
passes event selection

$81 < M(\mu, \mu) < 101$ GeV
(window around Z peak)



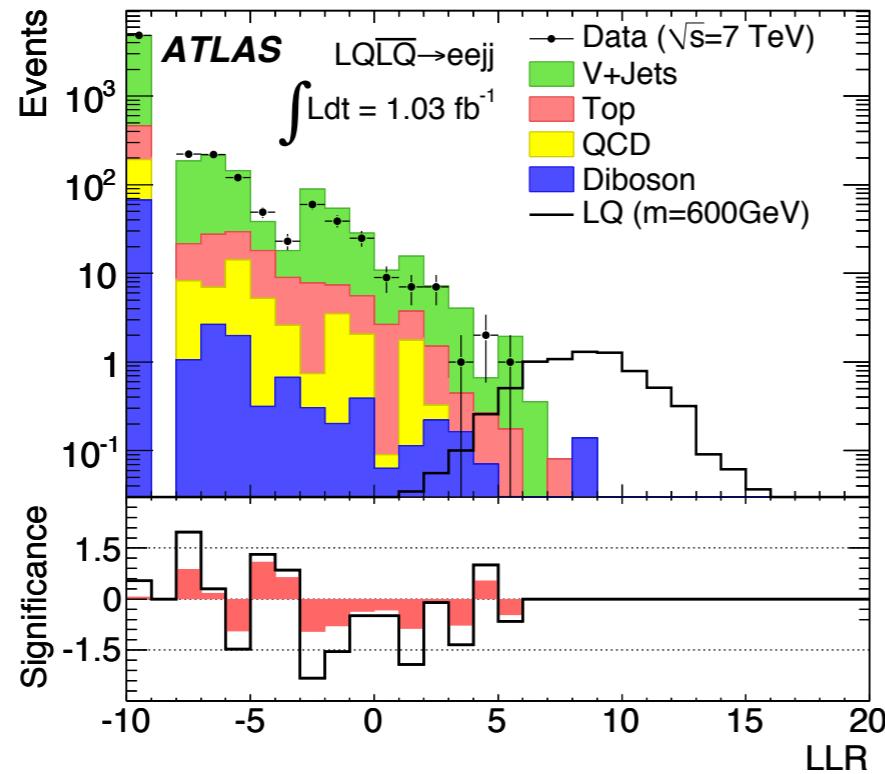
t-tbar CR

same as event selection,
but “two muons”
requirement replaced by
“one electron and one
muon”

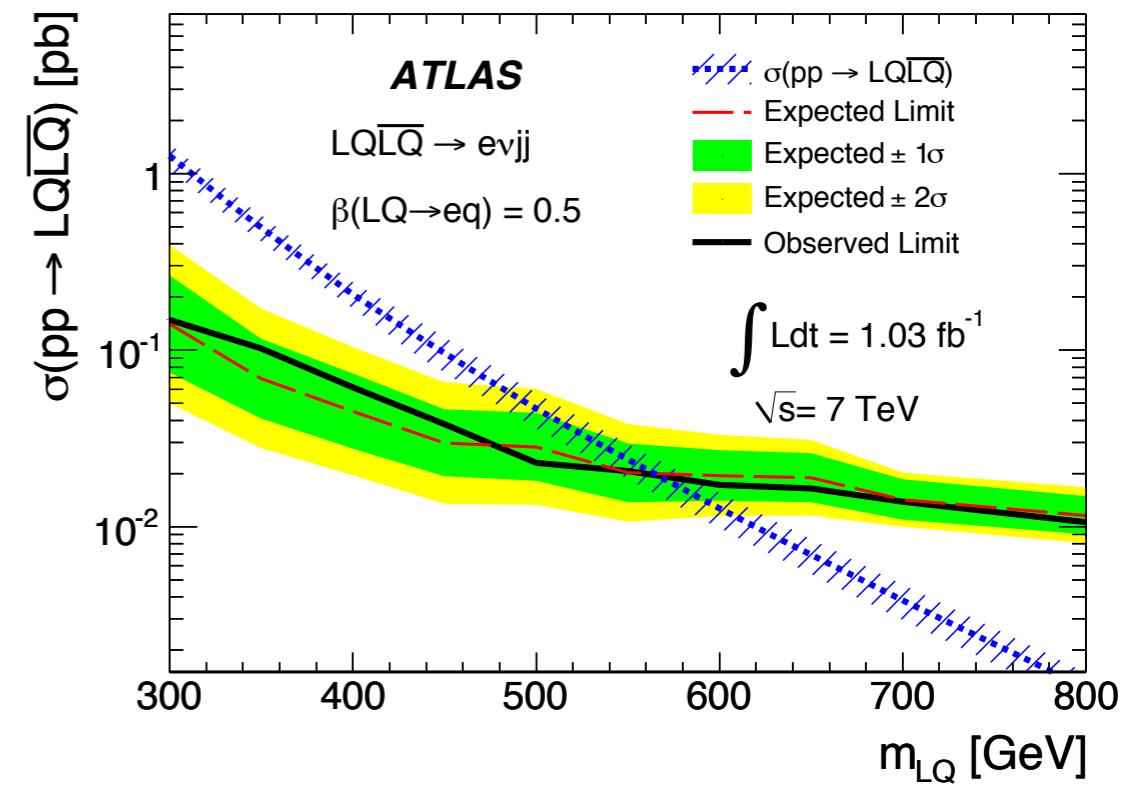
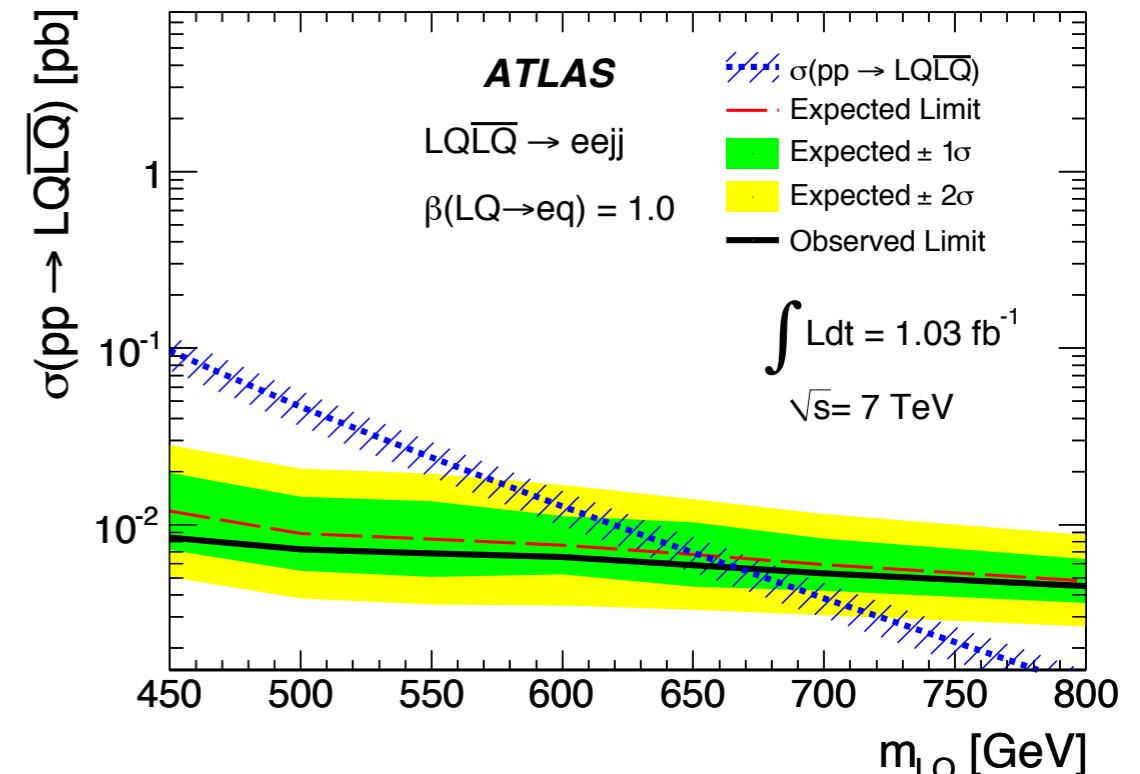
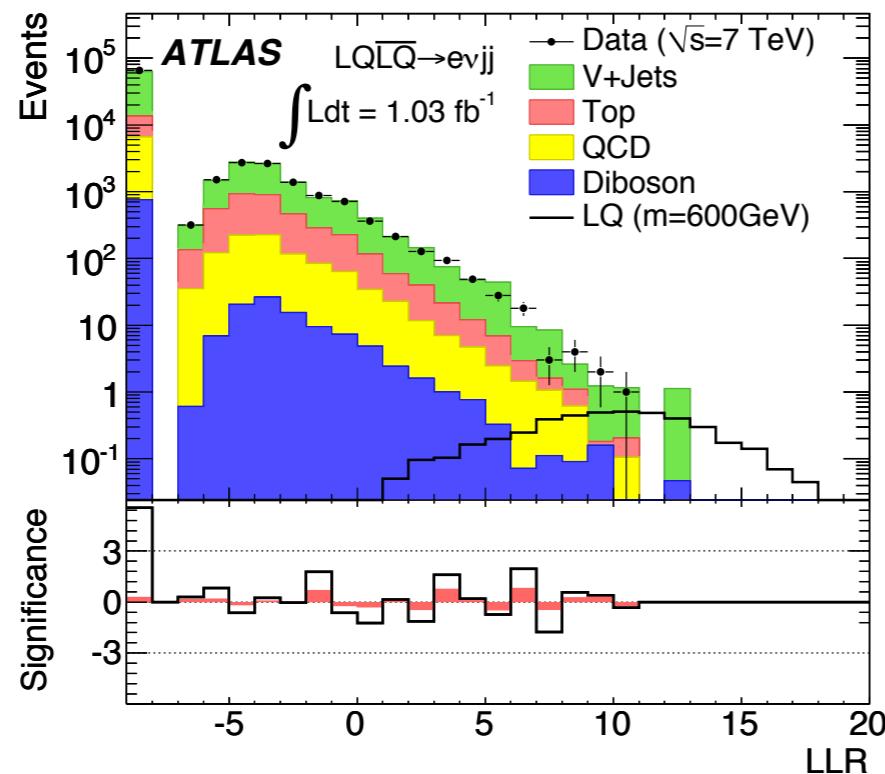


1st-generation LQ LLRs & Limits

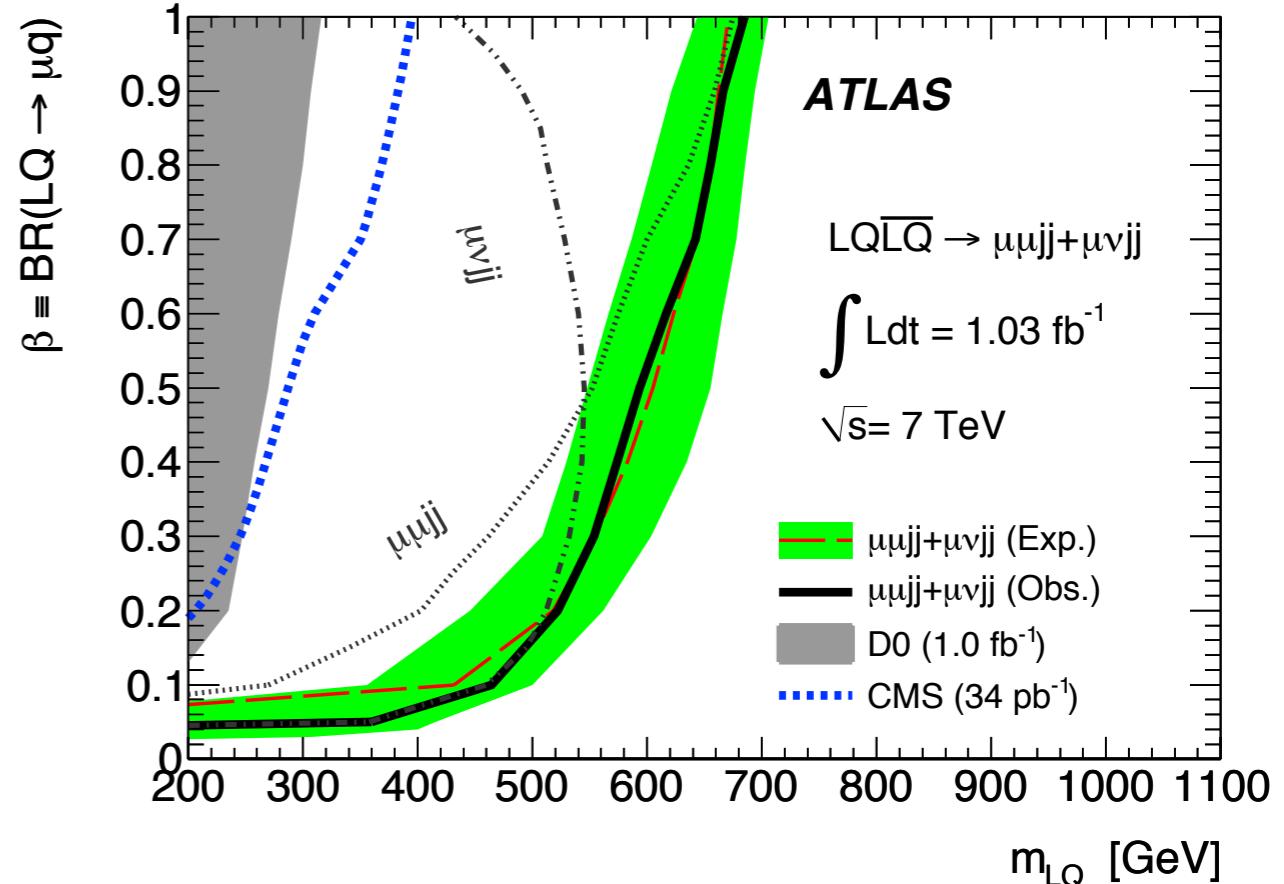
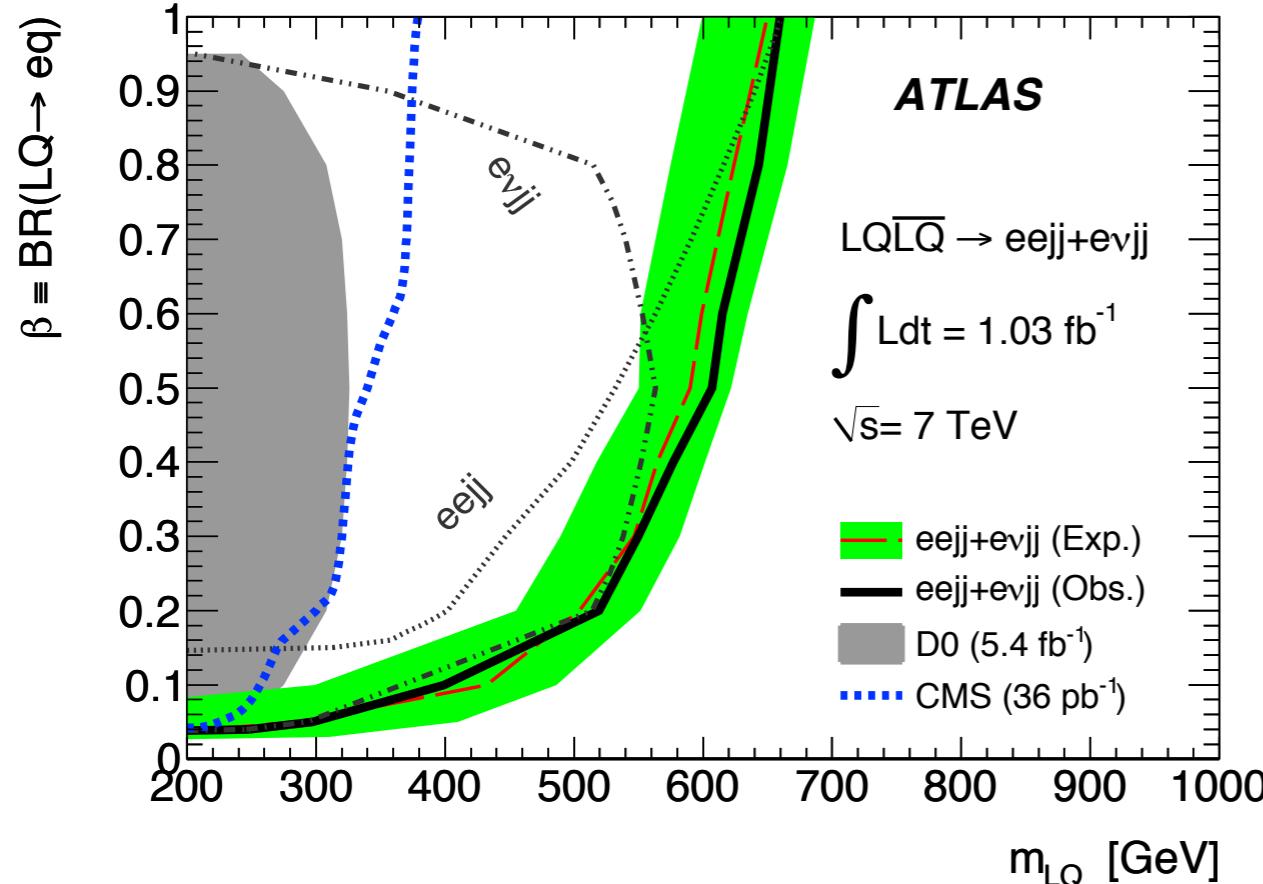
eejj



evjj



LQ Limits Comparison



m_{LQ} Limits	LQ ₁ ($\beta=0.5$)	LQ ₁ ($\beta=1.0$)	LQ ₂ ($\beta=0.5$)	LQ ₂ ($\beta=1.0$)
Expected [GeV]	587	650	605	671
Observed [GeV]	605	660	594	685