

Estimation of Channel Distribution Functions using a Neural Network

Peter Hartig

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The channel state perspective

The optimization framework

Extension of ViterbiNet: Reduced

Simulation Results

Molecular Communication Application

Conclusion

Outline

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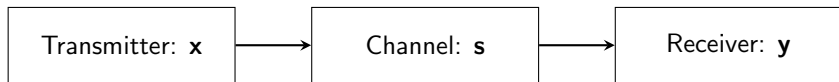
Conclusion

The Channel State

- ▶ Observations are made of some channel in a point-to-point communication system.
- ▶ For each observation, this channel takes on a state $s[k] \in \mathcal{S}$.
- ▶ The true state $s[k]$ is hidden by the addition of noise to an observation $y[k]$.

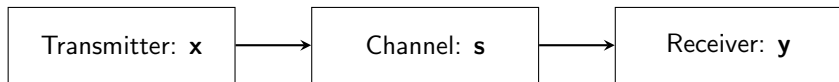
Sampling Channel State

Over many observations, the sequence \mathbf{y} corresponds to a sequence of channel states $\mathbf{s} \in S^N$



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For a channel represented by an LTI system, the state is determined entirely by the transmitted information \mathbf{x} .

Estimating the True Channel State

Goal:

We attempt to estimate the true, hidden, sequence of channel states, \mathbf{s} , based the sequence of samples \mathbf{y} .

Note

We assume that we know how many states the channel has such that S

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MAP Sequence Detection

$$\underset{\mathbf{s} \in S^N}{\text{maximize}} \ p(\mathbf{s}|\mathbf{y}).$$

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Using Bayes' theorem

$$p(\mathbf{s}|\mathbf{y}) = \frac{p(\mathbf{y}|\mathbf{s})p(\mathbf{s})}{p(\mathbf{y})}$$

Noting that $p(\mathbf{y})$ can be ignored

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$$\underset{\mathbf{s} \in S^N}{\text{maximize}} \ p(\mathbf{y}|\mathbf{s})p(\mathbf{s}) \tag{1}$$

Example with LTI channel

$$\underset{\mathbf{s} \in S^N}{\text{maximize}} \ p(\mathbf{y}|\mathbf{s})p(\mathbf{s})$$

Assuming

$$p(\mathbf{y}|\mathbf{s}) = \prod_{k=0}^{N-1} p(y[k]|\mathbf{s})$$

and

$$p(y[k]|\mathbf{s}) = p(y[k]|s[k])$$

this simplifies to

$$\underset{\mathbf{s} \in S^N}{\text{maximize}} \ \prod_{k=0}^{N-1} p(y[k]|s[k])p(\mathbf{s}).$$

Example with LTI channel - Continued

For the LTI channel

$$\begin{aligned} p(\mathbf{s}) \\ = \\ p(s[N]|s[N-1] \dots s[0])p(s[N-1]|s[N-2] \dots s[0]) \dots p(s[1]|s[0])p(s[0]) \end{aligned}$$

describes the consistency of transmitted symbols implied by the state sequence.

The channel states of the LTI channel satisfy the Markov property

$$p(s[N]|s[N-1] \dots s[0]) = p(s[N]|s[N-1]).$$

Example with LTI channel - Continued

The optimization problem is now

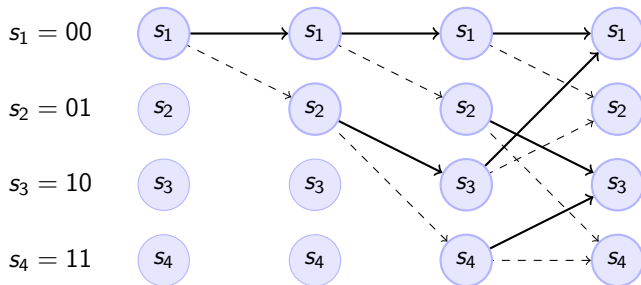
$$\underset{\mathbf{s} \in S^N}{\text{minimize}} \sum_{k=0}^{N-1} -\log(p(y[k]|s[k])p(s[k]|s[k-1])).$$

The individual terms in this sum can be rewritten

$$p(y[k]|s[k])p(s[k]|s[k-1]) = \frac{p(s[k]|y[k])p(y[k])}{p(s[k])}p(s[k]|s[k-1]).$$

For the LTI channel $p(s[k]|s[k-1])$ is 0 if states contradict and otherwise constant.

Viterbi Algorithm



Example with channel impulse response length 2 and constellation size 2.

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Decomposing Terms in the Viterbi Algorithm

Neural Network Component

Mixture Model Component

State Only Components

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State Redundancy

Exploiting State Redundancy

Don't go into details about how this is solved.

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Detection Performance

Without ISI

With ISI

Detection Performance

Reduced Training data (100 vs. 1000 symbols)

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Next Steps

Discuss how this can be applied to other factor graph related algorithms.

Testing on more complicated channels

- ▶ Improve decoding performance with neural net.
- ▶ Apply to a sampled molecular communications channel.
 - Estimate matched filter
- ▶ Generate training data for molecular communications channel and test "transfer learning" to real data.

Thank You.

Questions or Comments?