1 Game and System Setup

This game considers a wireless communications network which includes a both macro cell and femto cell users.

1.1 Players

Individual femto cells are the players in this game. Here each player $f \in \{1...F\}$ is considered to have a number of antennas T_f with which to transmit to K_f femto cell users.

In this setting femto cells are assumed to be spaced far apart in distance permitting the simplification that femto cell f cause no interference to the users of femto cell $j \in \{1...F\} \backslash f$

Femto base stations with multiple antennas can beamform their transmission with transformation $\mathbf{U_f} \in \mathbb{C}_{T_f \times L_f}$.

Femto base station f has power constraint $\sum_{i=1}^{L_f} p_{f,i} \leq P_f^{Total}$.

Femto base stations are assumed to have a utility function $U_f()$ based upon the quality of service provided to its users.

Macro Cell user $m \in \{1...M\}$ experiences receiver interference to due transmission by femto cell base stations. These macro cell users have limits to the amount of interference they will tolerate $\sum_{f=1}^{F} \mathbf{p}_f^t \mathbf{\tilde{h}_m^T U_f} \leq I_m^{Threshold}$.

Femto base station f is assumed to have full channel information ($\mathbf{H_f}$) for all user with which it transmits. The received signal for user j of femto base station f experiences the inner product of $\mathbf{h_{fj}^H u_{fj}}$

Femto cell f is assumed to have full channel information ($\tilde{H}_f$) for all user with which it interferes .

Users of femto cell f have SINR $\gamma_{f,i} = \frac{p_{f,i}|\mathbf{h_{fi}^H u_{fi}}|^2}{\sigma_n^2 + \sum_{\tilde{f} \neq f} \sum_{u=1}^{K_{\tilde{f}}} + \sum_{\tilde{k} \neq i}} + \; i \in \{1...K_f\}$ with AWGN $\sim \mathcal{N}(0, \sigma_n^2)$

Assuming sufficient base station spacing this becomes $\gamma_{f,i} = \frac{p_{f,i}|\mathbf{h_{fi}^H u_{fi}}|^2}{\sigma_n^2 + \sum_{\tilde{k} \neq i}} +$ $i \in \{1...K_f\}$

This further simplifies assuming that users use a zero-forcing beam-former $\gamma_{f,i} = \frac{p_{f,i}|\mathbf{h_{fi}^H u_{fi}}|^2}{\sigma_n^2}$

1.2 Scenarios

1.2.1 Case: $T_f \geq M + K_f$

1.2.2 Case: $K_f \leq T_f < M + K_f$

1.3 Optimization Problem

Each player f attempts to maximize utility function $U_f()$ while playing a strategy that falls in the region constrained by the interference limits imposed by the macro cell users.

The player optimization problem can be written as:

$$U_f()$$

$$s.t. \sum_{f=1}^{F} \mathbf{p}_f^t \mathbf{\tilde{h}_m^T U_f} \leq I_m^{Threshold}$$

2 Solving