

$$p(s|\theta) = \frac{1}{Z(\lambda, \mu_1, \mu_2)} \exp(\mu_1 s_1 + \mu_2 s_2 + \lambda s_1 s_2)$$

$$Z = 1 + e^{\mu_1} + e^{\mu_2} + e^{\mu_1 + \mu_2 + \lambda}$$

$$\theta = (\mu_1, \mu_2, \lambda)$$

$$m_1 = E(s_1|\theta) = \frac{e^{\mu_1} + e^{\mu_1 + \mu_2 + \lambda}}{Z}$$

$$m_2 = E(s_2|\theta) = \frac{e^{\mu_2} + e^{\mu_1 + \mu_2 + \lambda}}{Z}$$

$$c = E(s_1 s_2|\theta) = \frac{e^{\mu_1 + \mu_2 + \lambda}}{Z}$$

$$\begin{aligned} 0 &\leq m_1, m_2, c \leq 1 \\ c &\leq m_1, m_2 \\ c &> 1 - m_1 - m_2 \end{aligned}$$

$$\mu_1 = \ln \frac{m_1 - c}{1 + c - m_1 - m_2}$$

$$\mu_2 = \ln \frac{m_2 - c}{1 + c - m_1 - m_2}$$

$$\lambda = \ln \frac{c (1 + c - m_1 - m_2)}{(m_1 - c) (m_2 - c)}$$

$$p(s_1, s_2 | t) =$$

$$t = (m_1, m_2, c)$$

$$(1 + c - m_1 - m_2) \left(\frac{m_1 - c}{1 + c - m_1 - m_2} \right)^{s_1} \left(\frac{m_2 - c}{1 + c - m_1 - m_2} \right)^{s_2} \left[\frac{c (1 + c - m_1 - m_2)}{(m_1 - c) (m_2 - c)} \right]^{s_1 s_2}$$

$$\det \left| \frac{\partial (m_1, m_2, \lambda)}{\partial (u_1, u_2, c)} \right| = \frac{1-c}{(u_1-c)(u_2-c)(1+c-u_1-u_2)}$$

$$\det \left| \frac{\partial (u_1, u_2, c)}{\partial (m_1, m_2, \lambda)} \right| = \frac{e^{2(m_1+m_2)+\lambda}}{\underbrace{(1+e^{m_1}+e^{m_2}+e^{m_1+m_2+\lambda})^4}_{z^4}} = p(\theta_0)p(\theta_1)p(\theta_2)p(\theta_3)$$

$$\frac{1}{z} \frac{e^{m_1}}{z} \frac{e^{m_2}}{z} \frac{e^{m_1+m_2+\lambda}}{z} \leftarrow \text{only way in which it can be decomposed}$$

$$\text{Therefore, } p(t|I)dt = p(t|I) \left| \frac{\partial t}{\partial \theta} \right| d\theta \equiv p(\theta|I)d\theta$$

$$p(t|I) p(\theta_0|\theta) p(\theta_1|\theta) p(\theta_2|\theta) p(\theta_3|\theta) d\theta$$

$$\Rightarrow p(t|I) = \text{const} \hat{=} p(\theta|I) = \text{const.} \times p(\theta_0|\theta) p(\theta_1|\theta) p(\theta_2|\theta) p(\theta_3|\theta)$$















