

Questionnaire on Well-Being (QWB)
CFA

Magnus Johansson

2024-09-13

Reproducing CFA

```
library(readxl)
library(tidyverse)
```

```
-- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
v dplyr      1.1.4      v readr      2.1.5
v forcats    1.0.0      v stringr    1.5.1
v ggplot2    3.5.1      v tibble     3.2.1
v lubridate  1.9.3      v tidyr      1.3.1
v purrr      1.0.2

-- Conflicts ----- tidyverse_conflicts() --
x dplyr::filter() masks stats::filter()
x dplyr::lag()     masks stats::lag()
i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to be
```

```
library(lavaan)
```

This is lavaan 0.6-18
lavaan is FREE software! Please report any bugs.

```
library(patchwork)
```

Questionnaire on Well-Being (QWB), 18 items, each item is scored on a scale of 0 to 4 (Hlynsson et al. 2024). Data from the same paper. We'll use the data from the second study that was used in the CFA in the paper.

Code and data were retrieved from the paper's [OSF page](#). Really great to see these materials made available, it is such an important step towards improving the standards of science!

```
# Read in study two data -----
dd <- read_excel("data/study_two.xlsx")

onefactor <- 'f1 =~ swb1 + swb2 + swb3 + swb4 + swb5 + swb6 + swb7 + swb8 +
               swb9 + swb10 + swb11 + swb12 + swb13 + swb14 + swb15 +
               swb16 + swb17 + swb18'

# Fit the model to the data
cfamodel <- sem(model = onefactor, data = dd, estimator = "WLSMV")
```

```
Warning: lavaan->lav_options_est_dwls():
  estimator "DWLS" is not recommended for continuous data. Did you forget to
  set the ordered= argument?
```

This warning message is important! For WLSMV to work properly, one also needs to specify `ordered = TRUE`.

Let's see if we can reproduce the fit metrics reported in the paper (p.15), using the output from the misspecified function call above.

```
cfamodel %>% summary(standardized=T, ci=F, fit.measures= TRUE, )
```

lavaan 0.6-18 ended normally after 33 iterations

| | | |
|---|-----------|----------|
| Estimator | DWLS | |
| Optimization method | NLMINB | |
| Number of model parameters | 36 | |
| | Used | Total |
| Number of observations | 1561 | 1795 |
| Model Test User Model: | | |
| | Standard | Scaled |
| Test Statistic | 603.028 | 1576.509 |
| Degrees of freedom | 135 | 135 |
| P-value (Chi-square) | 0.000 | 0.000 |
| Scaling correction factor | | 0.391 |
| Shift parameter | | 33.384 |
| simple second-order correction | | |
| Model Test Baseline Model: | | |
| Test statistic | 40316.305 | 8701.238 |
| Degrees of freedom | 153 | 153 |
| P-value | 0.000 | 0.000 |
| Scaling correction factor | | 4.698 |
| User Model versus Baseline Model: | | |
| Comparative Fit Index (CFI) | 0.988 | 0.831 |
| Tucker-Lewis Index (TLI) | 0.987 | 0.809 |
| Robust Comparative Fit Index (CFI) | | 0.986 |
| Robust Tucker-Lewis Index (TLI) | | 0.984 |
| Root Mean Square Error of Approximation: | | |
| RMSEA | 0.047 | 0.083 |
| 90 Percent confidence interval - lower | 0.043 | 0.079 |
| 90 Percent confidence interval - upper | 0.051 | 0.086 |
| P-value H ₀ : RMSEA ≤ 0.050 | 0.887 | 0.000 |
| P-value H ₀ : RMSEA ≥ 0.080 | 0.000 | 0.892 |
| Robust RMSEA | | 0.052 |
| 90 Percent confidence interval - lower | | 0.049 |
| 90 Percent confidence interval - upper | | 0.054 |
| P-value H ₀ : Robust RMSEA ≤ 0.050 | | 0.106 |
| P-value H ₀ : Robust RMSEA ≥ 0.080 | | 0.000 |
| Standardized Root Mean Square Residual: | | |
| SRMR | 0.053 | 0.053 |

Parameter Estimates:

| | |
|----------------------------------|--------------|
| Standard errors | Robust.sem |
| Information | Expected |
| Information saturated (h1) model | Unstructured |

Latent Variables:

| | Estimate | Std.Err | z-value | P(> z) | Std.lv | Std.all |
|-------|----------|---------|---------|---------|--------|---------|
| f1 =~ | | | | | | |
| swb1 | 1.000 | | | | 0.639 | 0.695 |
| swb2 | 0.861 | 0.035 | 24.575 | 0.000 | 0.550 | 0.544 |
| swb3 | 0.550 | 0.036 | 15.121 | 0.000 | 0.352 | 0.413 |
| swb4 | 0.876 | 0.034 | 25.809 | 0.000 | 0.560 | 0.647 |
| swb5 | 0.929 | 0.039 | 23.849 | 0.000 | 0.594 | 0.635 |
| swb6 | 0.967 | 0.040 | 24.054 | 0.000 | 0.618 | 0.656 |
| swb7 | 1.064 | 0.036 | 29.625 | 0.000 | 0.680 | 0.765 |
| swb8 | 1.142 | 0.034 | 33.522 | 0.000 | 0.730 | 0.808 |
| swb9 | 1.124 | 0.036 | 30.957 | 0.000 | 0.718 | 0.780 |
| swb10 | 1.182 | 0.040 | 29.564 | 0.000 | 0.755 | 0.751 |
| swb11 | 1.202 | 0.045 | 26.933 | 0.000 | 0.768 | 0.730 |
| swb12 | 0.872 | 0.037 | 23.385 | 0.000 | 0.557 | 0.654 |
| swb13 | 0.707 | 0.039 | 17.969 | 0.000 | 0.452 | 0.493 |
| swb14 | 0.980 | 0.035 | 27.907 | 0.000 | 0.626 | 0.666 |
| swb15 | 1.202 | 0.043 | 28.182 | 0.000 | 0.768 | 0.743 |
| swb16 | 1.104 | 0.036 | 30.255 | 0.000 | 0.706 | 0.715 |
| swb17 | 1.097 | 0.040 | 27.296 | 0.000 | 0.701 | 0.728 |
| swb18 | 0.981 | 0.045 | 21.770 | 0.000 | 0.627 | 0.587 |

Variances:

| | Estimate | Std.Err | z-value | P(> z) | Std.lv | Std.all |
|--------|----------|---------|---------|---------|--------|---------|
| .swb1 | 0.436 | 0.018 | 24.187 | 0.000 | 0.436 | 0.517 |
| .swb2 | 0.721 | 0.025 | 28.874 | 0.000 | 0.721 | 0.704 |
| .swb3 | 0.601 | 0.024 | 24.670 | 0.000 | 0.601 | 0.829 |
| .swb4 | 0.435 | 0.017 | 25.780 | 0.000 | 0.435 | 0.581 |
| .swb5 | 0.523 | 0.019 | 27.276 | 0.000 | 0.523 | 0.597 |
| .swb6 | 0.506 | 0.019 | 26.097 | 0.000 | 0.506 | 0.570 |
| .swb7 | 0.327 | 0.014 | 22.718 | 0.000 | 0.327 | 0.414 |
| .swb8 | 0.283 | 0.012 | 23.155 | 0.000 | 0.283 | 0.347 |
| .swb9 | 0.332 | 0.013 | 25.432 | 0.000 | 0.332 | 0.392 |
| .swb10 | 0.441 | 0.018 | 24.399 | 0.000 | 0.441 | 0.436 |
| .swb11 | 0.518 | 0.022 | 23.263 | 0.000 | 0.518 | 0.468 |
| .swb12 | 0.415 | 0.017 | 24.855 | 0.000 | 0.415 | 0.572 |
| .swb13 | 0.634 | 0.022 | 28.570 | 0.000 | 0.634 | 0.757 |
| .swb14 | 0.493 | 0.019 | 26.580 | 0.000 | 0.493 | 0.557 |
| .swb15 | 0.480 | 0.020 | 24.323 | 0.000 | 0.480 | 0.449 |
| .swb16 | 0.476 | 0.019 | 25.534 | 0.000 | 0.476 | 0.489 |
| .swb17 | 0.436 | 0.019 | 22.826 | 0.000 | 0.436 | 0.470 |
| .swb18 | 0.749 | 0.028 | 26.616 | 0.000 | 0.749 | 0.656 |
| f1 | 0.408 | 0.026 | 15.931 | 0.000 | 1.000 | 1.000 |

The “standard” column in the output looks like what has been reported in the paper (see quote below) regarding χ^2 , RMSEA, and CFI. Good to see that it is reproducible.

A single-factor solution for the Confirmatory factor analysis for the Questionnaire on Well-Being. QWB resulted in a good fit for the data: $\chi^2(135) = 603.03$, $p < 0.001$, CFI = 0.988, SRMR = 0.053, RMSEA = 0.047 [90% CI: 0.043, 0.051]. Thus, our single-factor model for the QWB exhibits all of our predetermined criteria for a good model fit.

Let’s run the CFA function call with `ordered = TRUE` added to make the WLSMV estimator, which was correctly described in the paper, work as intended.

```
cfamodel2 <- sem(model = onefactor, data = dd, estimator = "WLSMV", ordered = TRUE)
cfamodel2 %>% summary(standardized=T, ci=F, fit.measures= TRUE, )
```

lavaan 0.6-18 ended normally after 34 iterations

| | |
|----------------------------|--------|
| Estimator | DWLS |
| Optimization method | NLMINB |
| Number of model parameters | 90 |

| | | |
|------------------------|------|-------|
| | Used | Total |
| Number of observations | 1561 | 1795 |

Model Test User Model:

| | | |
|--------------------------------|----------|----------|
| | Standard | Scaled |
| Test Statistic | 1832.971 | 2940.978 |
| Degrees of freedom | 135 | 135 |
| P-value (Chi-square) | 0.000 | 0.000 |
| Scaling correction factor | | 0.630 |
| Shift parameter | | 32.413 |
| simple second-order correction | | |

Model Test Baseline Model:

| | | |
|---------------------------|------------|-----------|
| Test statistic | 131413.959 | 40457.340 |
| Degrees of freedom | 153 | 153 |
| P-value | 0.000 | 0.000 |
| Scaling correction factor | | 3.257 |

User Model versus Baseline Model:

| | | |
|------------------------------------|-------|-------|
| Comparative Fit Index (CFI) | 0.987 | 0.930 |
| Tucker-Lewis Index (TLI) | 0.985 | 0.921 |
| Robust Comparative Fit Index (CFI) | | 0.831 |
| Robust Tucker-Lewis Index (TLI) | | 0.808 |

Root Mean Square Error of Approximation:

| | | |
|--|-------|-------|
| RMSEA | 0.090 | 0.115 |
| 90 Percent confidence interval - lower | 0.086 | 0.112 |
| 90 Percent confidence interval - upper | 0.093 | 0.119 |
| P-value H_0: RMSEA <= 0.050 | 0.000 | 0.000 |
| P-value H_0: RMSEA >= 0.080 | 1.000 | 1.000 |
| Robust RMSEA | | 0.126 |
| 90 Percent confidence interval - lower | | 0.122 |
| 90 Percent confidence interval - upper | | 0.130 |
| P-value H_0: Robust RMSEA <= 0.050 | | 0.000 |
| P-value H_0: Robust RMSEA >= 0.080 | | 1.000 |

Standardized Root Mean Square Residual:

| | | |
|------|-------|-------|
| SRMR | 0.060 | 0.060 |
|------|-------|-------|

Parameter Estimates:

| | |
|----------------------------------|--------------|
| Parameterization | Delta |
| Standard errors | Robust.sem |
| Information | Expected |
| Information saturated (h1) model | Unstructured |

Latent Variables:

| | Estimate | Std.Err | z-value | P(> z) | Std.lv | Std.all |
|-------|----------|---------|---------|---------|--------|---------|
| f1 =~ | | | | | | |
| swb1 | 1.000 | | | | 0.740 | 0.740 |
| swb2 | 0.788 | 0.022 | 35.977 | 0.000 | 0.583 | 0.583 |
| swb3 | 0.614 | 0.029 | 21.080 | 0.000 | 0.454 | 0.454 |
| swb4 | 0.946 | 0.021 | 44.763 | 0.000 | 0.700 | 0.700 |
| swb5 | 0.944 | 0.022 | 43.672 | 0.000 | 0.699 | 0.699 |
| swb6 | 0.940 | 0.023 | 41.605 | 0.000 | 0.695 | 0.695 |
| swb7 | 1.123 | 0.020 | 56.041 | 0.000 | 0.831 | 0.831 |
| swb8 | 1.187 | 0.019 | 62.155 | 0.000 | 0.878 | 0.878 |
| swb9 | 1.112 | 0.019 | 59.591 | 0.000 | 0.823 | 0.823 |
| swb10 | 1.061 | 0.020 | 54.326 | 0.000 | 0.785 | 0.785 |
| swb11 | 1.076 | 0.021 | 50.727 | 0.000 | 0.796 | 0.796 |
| swb12 | 0.954 | 0.022 | 42.924 | 0.000 | 0.706 | 0.706 |
| swb13 | 0.713 | 0.026 | 27.920 | 0.000 | 0.527 | 0.527 |
| swb14 | 0.946 | 0.020 | 46.765 | 0.000 | 0.700 | 0.700 |
| swb15 | 1.064 | 0.020 | 52.990 | 0.000 | 0.787 | 0.787 |
| swb16 | 1.009 | 0.019 | 54.088 | 0.000 | 0.747 | 0.747 |
| swb17 | 1.066 | 0.020 | 52.085 | 0.000 | 0.789 | 0.789 |
| swb18 | 0.840 | 0.024 | 35.203 | 0.000 | 0.622 | 0.622 |

Thresholds:

| | Estimate | Std.Err | z-value | P(> z) | Std.lv | Std.all |
|---------|----------|---------|---------|---------|--------|---------|
| swb1 t1 | -2.252 | 0.088 | -25.646 | 0.000 | -2.252 | -2.252 |

| | | | | | | |
|----------|--------|-------|---------|-------|--------|--------|
| swb1 t2 | -1.076 | 0.039 | -27.312 | 0.000 | -1.076 | -1.076 |
| swb1 t3 | -0.102 | 0.032 | -3.213 | 0.001 | -0.102 | -0.102 |
| swb1 t4 | 1.117 | 0.040 | 27.866 | 0.000 | 1.117 | 1.117 |
| swb2 t1 | -1.949 | 0.067 | -29.073 | 0.000 | -1.949 | -1.949 |
| swb2 t2 | -0.847 | 0.036 | -23.368 | 0.000 | -0.847 | -0.847 |
| swb2 t3 | -0.020 | 0.032 | -0.633 | 0.527 | -0.020 | -0.020 |
| swb2 t4 | 1.082 | 0.039 | 27.392 | 0.000 | 1.082 | 1.082 |
| swb3 t1 | -2.613 | 0.129 | -20.271 | 0.000 | -2.613 | -2.613 |
| swb3 t2 | -1.627 | 0.053 | -30.772 | 0.000 | -1.627 | -1.627 |
| swb3 t3 | -0.886 | 0.037 | -24.149 | 0.000 | -0.886 | -0.886 |
| swb3 t4 | 0.316 | 0.032 | 9.776 | 0.000 | 0.316 | 0.316 |
| swb4 t1 | -2.341 | 0.096 | -24.399 | 0.000 | -2.341 | -2.341 |
| swb4 t2 | -1.189 | 0.041 | -28.723 | 0.000 | -1.189 | -1.189 |
| swb4 t3 | -0.075 | 0.032 | -2.353 | 0.019 | -0.075 | -0.075 |
| swb4 t4 | 1.212 | 0.042 | 28.968 | 0.000 | 1.212 | 1.212 |
| swb5 t1 | -2.044 | 0.073 | -28.162 | 0.000 | -2.044 | -2.044 |
| swb5 t2 | -0.908 | 0.037 | -24.557 | 0.000 | -0.908 | -0.908 |
| swb5 t3 | 0.191 | 0.032 | 5.993 | 0.000 | 0.191 | 0.191 |
| swb5 t4 | 1.257 | 0.043 | 29.397 | 0.000 | 1.257 | 1.257 |
| swb6 t1 | -2.232 | 0.086 | -25.911 | 0.000 | -2.232 | -2.232 |
| swb6 t2 | -1.151 | 0.041 | -28.285 | 0.000 | -1.151 | -1.151 |
| swb6 t3 | -0.133 | 0.032 | -4.174 | 0.000 | -0.133 | -0.133 |
| swb6 t4 | 0.948 | 0.037 | 25.272 | 0.000 | 0.948 | 0.948 |
| swb7 t1 | -2.317 | 0.094 | -24.744 | 0.000 | -2.317 | -2.317 |
| swb7 t2 | -1.312 | 0.044 | -29.847 | 0.000 | -1.312 | -1.312 |
| swb7 t3 | -0.208 | 0.032 | -6.498 | 0.000 | -0.208 | -0.208 |
| swb7 t4 | 0.978 | 0.038 | 25.798 | 0.000 | 0.978 | 0.978 |
| swb8 t1 | -2.294 | 0.092 | -25.065 | 0.000 | -2.294 | -2.294 |
| swb8 t2 | -1.105 | 0.040 | -27.710 | 0.000 | -1.105 | -1.105 |
| swb8 t3 | -0.038 | 0.032 | -1.189 | 0.234 | -0.038 | -0.038 |
| swb8 t4 | 1.145 | 0.041 | 28.210 | 0.000 | 1.145 | 1.145 |
| swb9 t1 | -1.852 | 0.062 | -29.836 | 0.000 | -1.852 | -1.852 |
| swb9 t2 | -0.602 | 0.034 | -17.755 | 0.000 | -0.602 | -0.602 |
| swb9 t3 | 0.534 | 0.033 | 15.978 | 0.000 | 0.534 | 0.534 |
| swb9 t4 | 1.542 | 0.050 | 30.794 | 0.000 | 1.542 | 1.542 |
| swb10 t1 | -1.664 | 0.054 | -30.703 | 0.000 | -1.664 | -1.664 |
| swb10 t2 | -0.645 | 0.034 | -18.832 | 0.000 | -0.645 | -0.645 |
| swb10 t3 | 0.311 | 0.032 | 9.625 | 0.000 | 0.311 | 0.311 |
| swb10 t4 | 1.375 | 0.045 | 30.257 | 0.000 | 1.375 | 1.375 |
| swb11 t1 | -2.018 | 0.071 | -28.422 | 0.000 | -2.018 | -2.018 |
| swb11 t2 | -1.099 | 0.040 | -27.631 | 0.000 | -1.099 | -1.099 |
| swb11 t3 | -0.279 | 0.032 | -8.668 | 0.000 | -0.279 | -0.279 |
| swb11 t4 | 0.598 | 0.034 | 17.657 | 0.000 | 0.598 | 0.598 |
| swb12 t1 | -2.423 | 0.104 | -23.194 | 0.000 | -2.423 | -2.423 |
| swb12 t2 | -1.367 | 0.045 | -30.210 | 0.000 | -1.367 | -1.367 |
| swb12 t3 | -0.092 | 0.032 | -2.909 | 0.004 | -0.092 | -0.092 |
| swb12 t4 | 1.082 | 0.039 | 27.392 | 0.000 | 1.082 | 1.082 |
| swb13 t1 | -2.070 | 0.074 | -27.876 | 0.000 | -2.070 | -2.070 |
| swb13 t2 | -1.236 | 0.042 | -29.203 | 0.000 | -1.236 | -1.236 |
| swb13 t3 | -0.183 | 0.032 | -5.741 | 0.000 | -0.183 | -0.183 |

| | | | | | | |
|----------|--------|-------|---------|-------|--------|--------|
| swb13 t4 | 1.029 | 0.039 | 26.611 | 0.000 | 1.029 | 1.029 |
| swb14 t1 | -1.994 | 0.070 | -28.659 | 0.000 | -1.994 | -1.994 |
| swb14 t2 | -0.915 | 0.037 | -24.692 | 0.000 | -0.915 | -0.915 |
| swb14 t3 | 0.105 | 0.032 | 3.314 | 0.001 | 0.105 | 0.105 |
| swb14 t4 | 1.275 | 0.043 | 29.553 | 0.000 | 1.275 | 1.275 |
| swb15 t1 | -1.718 | 0.056 | -30.542 | 0.000 | -1.718 | -1.718 |
| swb15 t2 | -0.842 | 0.036 | -23.275 | 0.000 | -0.842 | -0.842 |
| swb15 t3 | 0.112 | 0.032 | 3.516 | 0.000 | 0.112 | 0.112 |
| swb15 t4 | 1.099 | 0.040 | 27.631 | 0.000 | 1.099 | 1.099 |
| swb16 t1 | -1.834 | 0.061 | -29.952 | 0.000 | -1.834 | -1.834 |
| swb16 t2 | -0.901 | 0.037 | -24.422 | 0.000 | -0.901 | -0.901 |
| swb16 t3 | 0.075 | 0.032 | 2.353 | 0.019 | 0.075 | 0.075 |
| swb16 t4 | 1.179 | 0.041 | 28.616 | 0.000 | 1.179 | 1.179 |
| swb17 t1 | -2.098 | 0.076 | -27.561 | 0.000 | -2.098 | -2.098 |
| swb17 t2 | -1.260 | 0.043 | -29.429 | 0.000 | -1.260 | -1.260 |
| swb17 t3 | -0.323 | 0.032 | -9.977 | 0.000 | -0.323 | -0.323 |
| swb17 t4 | 0.756 | 0.035 | 21.440 | 0.000 | 0.756 | 0.756 |
| swb18 t1 | -1.658 | 0.054 | -30.718 | 0.000 | -1.658 | -1.658 |
| swb18 t2 | -0.828 | 0.036 | -22.996 | 0.000 | -0.828 | -0.828 |
| swb18 t3 | 0.010 | 0.032 | 0.329 | 0.742 | 0.010 | 0.010 |
| swb18 t4 | 1.034 | 0.039 | 26.695 | 0.000 | 1.034 | 1.034 |

Variances:

| | Estimate | Std.Err | z-value | P(> z) | Std.lv | Std.all |
|--------|----------|---------|---------|---------|--------|---------|
| .swb1 | 0.453 | | | | 0.453 | 0.453 |
| .swb2 | 0.660 | | | | 0.660 | 0.660 |
| .swb3 | 0.794 | | | | 0.794 | 0.794 |
| .swb4 | 0.510 | | | | 0.510 | 0.510 |
| .swb5 | 0.512 | | | | 0.512 | 0.512 |
| .swb6 | 0.517 | | | | 0.517 | 0.517 |
| .swb7 | 0.310 | | | | 0.310 | 0.310 |
| .swb8 | 0.229 | | | | 0.229 | 0.229 |
| .swb9 | 0.323 | | | | 0.323 | 0.323 |
| .swb10 | 0.384 | | | | 0.384 | 0.384 |
| .swb11 | 0.366 | | | | 0.366 | 0.366 |
| .swb12 | 0.502 | | | | 0.502 | 0.502 |
| .swb13 | 0.722 | | | | 0.722 | 0.722 |
| .swb14 | 0.511 | | | | 0.511 | 0.511 |
| .swb15 | 0.380 | | | | 0.380 | 0.380 |
| .swb16 | 0.442 | | | | 0.442 | 0.442 |
| .swb17 | 0.378 | | | | 0.378 | 0.378 |
| .swb18 | 0.614 | | | | 0.614 | 0.614 |
| f1 | 0.547 | 0.018 | 29.873 | 0.000 | 1.000 | 1.000 |

Before looking closer at the results and making comparisons to the published/reported metrics, we need to address the issue of reporting the correct model fit metrics. For WLSMV, the [scaled metrics should be used](#).

Also, the Hu & Bentler (1999) cutoff values references in the paper are not appropriate for ordinal data analyzed with the WLSMV estimator (McNeish 2023; Savalei 2018). The R-package `dynamic` can produce [appropriate cutoff](#)

values for model fit indices. We'll get into that after reviewing the scaled fit metrics.

Scaled fit metrics

Another important issue is reporting the correct model fit metrics. For WLSMV, the `.scaled metrics` should be used.

```
fit_metrics_scaled <- c("chisq.scaled", "df", "pvalue.scaled",
                        "cfi.scaled", "tli.scaled", "rmsea.scaled",
                        "rmsea.ci.lower.scaled", "rmsea.ci.upper.scaled",
                        "srmr")

fitmeasures(cfamodel2, fit_metrics_scaled) %>%
  rbind() %>%
  as.data.frame() %>%
  mutate(across(where(is.numeric), ~ round(.x, 3))) %>%
  rename(Chi2.scaled = chisq.scaled,
         p.scaled = pvalue.scaled,
         CFI.scaled = cfi.scaled,
         TLI.scaled = tli.scaled,
         RMSEA.scaled = rmsea.scaled,
         CI_low.scaled = rmsea.ci.lower.scaled,
         CI_high.scaled = rmsea.ci.upper.scaled,
         SRMR = srmr) %>%
  knitr::kable()
```

| | Chi2.scaled | df | p.scaled | CFI.scaled | TLI.scaled | RMSEA.scaled | CI_low.scaled | CI_high.scaled | SRMR |
|---|-------------|-----|----------|------------|------------|--------------|---------------|----------------|------|
| . | 2940.978 | 135 | 0 | 0.93 | 0.921 | 0.115 | 0.112 | 0.119 | 0.06 |

Again, these were the metrics reported in the paper:

A single-factor solution for the Confirmatory factor analysis for the Questionnaire on Well-Being. QWB resulted in a good fit for the data: $2(135) = 603.03$, $p < 0.001$, $CFI = 0.988$, $SRMR = 0.053$, $RMSEA = 0.047$ [90% CI: 0.043, 0.051]. Thus, our single-factor model for the QWB exhibits all of our predetermined criteria for a good model fit.

The differences from the model fit metrics output in the table above and found in the paper are partially due to the missing `ordered = TRUE` option, but also from reporting the wrong metrics for the WLSMV estimator.

The correct model fit metrics indicate problems, no matter which cutoffs one would use, especially regarding RMSEA. Let us review the modification indices.

Modification indices

We'll filter the list and only present those with $mi/2 > 30$.

```
modificationIndices(cfamodel2,
                    standardized = T) %>%
  as.data.frame(row.names = NULL) %>%
  filter(mi > 30) %>%
  arrange(desc(mi)) %>%
  mutate(across(where(is.numeric), ~ round(.x, 3))) %>%
  knitr::kable()
```

| lhs | op | rhs | mi | epc | sepc.lv | sepc.all | sepc.nox |
|-------|----|-------|---------|--------|---------|----------|----------|
| swb4 | ~~ | swb5 | 213.550 | -0.242 | -0.242 | -0.474 | -0.474 |
| swb5 | ~~ | swb12 | 155.477 | -0.211 | -0.211 | -0.416 | -0.416 |
| swb7 | ~~ | swb8 | 132.329 | -0.143 | -0.143 | -0.536 | -0.536 |
| swb11 | ~~ | swb17 | 102.493 | -0.144 | -0.144 | -0.388 | -0.388 |
| swb1 | ~~ | swb2 | 78.974 | -0.172 | -0.172 | -0.315 | -0.315 |
| swb1 | ~~ | swb16 | 68.421 | -0.138 | -0.138 | -0.309 | -0.309 |
| swb2 | ~~ | swb16 | 68.162 | -0.161 | -0.161 | -0.298 | -0.298 |
| swb5 | ~~ | swb6 | 63.609 | -0.146 | -0.146 | -0.284 | -0.284 |
| swb15 | ~~ | swb17 | 62.165 | -0.117 | -0.117 | -0.308 | -0.308 |
| swb12 | ~~ | swb13 | 58.963 | -0.162 | -0.162 | -0.269 | -0.269 |
| swb13 | ~~ | swb14 | 48.027 | -0.148 | -0.148 | -0.244 | -0.244 |
| swb9 | ~~ | swb18 | 42.649 | -0.120 | -0.120 | -0.269 | -0.269 |
| swb4 | ~~ | swb12 | 39.141 | -0.118 | -0.118 | -0.233 | -0.233 |
| swb2 | ~~ | swb17 | 34.139 | 0.137 | 0.137 | 0.275 | 0.275 |
| swb8 | ~~ | swb12 | 33.173 | 0.123 | 0.123 | 0.363 | 0.363 |
| swb2 | ~~ | swb3 | 31.034 | -0.132 | -0.132 | -0.182 | -0.182 |

Many very large mi/ 2 values due to residual correlations.

Dynamic cutoff values

As mentioned earlier, the often used Hu & Bentler (1999) cutoff values are based on simulations of continuous data and ML estimation. In order to establish useful cutoff values for the WLSMV estimator with ordinal data, we need to run simulations relevant to the current set of items and response data (McNeish 2023). This has been implemented in the [development version](#) of `dynamic`.

```
library(dynamic) # devtools::install_github("melissagwolf/dynamic") for development version
```

Beta version. Please report bugs: <https://github.com/melissagwolf/dynamic/issues>.

```
dyncut <- catOne(cfamodel2, reps = 500)
```

```
dyncut
```

Your DFI cutoffs:

| | SRMR | RMSEA | CFI |
|-----------------|-------|-------|-------|
| Level-0 | 0.015 | 0.011 | 0.999 |
| Specificity 95% | 95% | 95% | 95% |
| Level-1 | 0.026 | 0.04 | 0.991 |

Sensitivity 95% 95% 95%

Level-2 0.031 0.056 0.983

Sensitivity 95% 95% 95%

Level-3 0.034 0.066 0.977

Sensitivity 95% 95% 95%

Empirical fit indices:

| Chi-Square | df | p-value | SRMR | RMSEA | CFI |
|------------|-----|---------|------|-------|------|
| 2940.978 | 135 | 0 | 0.06 | 0.115 | 0.93 |

Notes:

- 'Sensitivity' is % of hypothetically misspecified models correctly identified by cutoff
- Cutoffs with 95% sensitivity are reported when possible
- If sensitivity is <50%, cutoffs will be suppressed

Explanations on Levels 0-3 from the dynamic [package vignette](#):

When there are 6 or more items, cfaOne will consider three levels of misspecification. As in catHB, the Level-0 row corresponds to the anticipated fit index values if the fitted model were the exact underlying population model. The Level-1 row corresponds to the anticipated fit index values if the fitted model omitted 0.30 residual correlations between approximately 1/3 of item pairs. The Level-2 row corresponds to the anticipated fit index values if the fitted model omitted 0.30 residual correlations between approximately 1/3 of item pairs. The Level-3 row corresponds to the anticipated fit index values if the fitted model omitted 0.30 residual correlations between all item pairs.

As we can see, the observed/empirical fit metrics from the data does not come close to even the Level-3 simulation based cutoff values.

Summary comments

The 18 items do not fit a unidimensional model, due to issues with residual correlations and potential multidimensionality.

Software used

```
sessionInfo()
```

```
R version 4.4.1 (2024-06-14)
Platform: aarch64-apple-darwin20
Running under: macOS Sonoma 14.6.1
```

```
Matrix products: default
```

```
BLAS: /Library/Frameworks/R.framework/Versions/4.4-arm64/Resources/lib/libRblas.0.dylib
LAPACK: /Library/Frameworks/R.framework/Versions/4.4-arm64/Resources/lib/libRlapack.dylib;
```

```

locale:
[1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8

time zone: Europe/Stockholm
tzcode source: internal

attached base packages:
[1] stats      graphics  grDevices  utils      datasets  methods   base

other attached packages:
[1] dynamic_1.1.0   patchwork_1.2.0 lavaan_0.6-18   lubridate_1.9.3
[5] forcats_1.0.0   stringr_1.5.1   dplyr_1.1.4     purrr_1.0.2
[9] readr_2.1.5     tidyr_1.3.1     tibble_3.2.1    ggplot2_3.5.1
[13] tidyverse_2.0.0 readxl_1.4.3

loaded via a namespace (and not attached):
[1] tidyselect_1.2.1   R.utils_2.12.3    fastmap_1.2.0
[4] digest_0.6.37      timechange_0.3.0  lifecycle_1.0.4
[7] Deriv_4.1.3        dcurver_0.9.2     cluster_2.1.6
[10] mirt_1.42          magrittr_2.0.3    compiler_4.4.1
[13] rlang_1.1.4        tools_4.4.1       utf8_1.2.4
[16] yaml_2.3.10        knitr_1.48        mnormt_2.1.1
[19] curl_5.2.2         Bayesrel_0.7.7    withr_3.0.1
[22] R.oo_1.26.0        grid_4.4.1        stats4_4.4.1
[25] fansi_1.0.6        colorspace_2.1-1  future_1.34.0
[28] progressr_0.14.0   GPArotation_2024.3-1 globals_0.16.3
[31] scales_1.3.0       MASS_7.3-61       GenOrd_1.4.0
[34] cli_3.6.3          mvtnorm_1.3-1     rmarkdown_2.27
[37] vegan_2.6-8        generics_0.1.3    rstudioapi_0.16.0
[40] future.apply_1.11.2 SimDesign_2.17.1  tzdb_0.4.0
[43] sessioninfo_1.2.2  pbapply_1.7-2     audio_0.1-11
[46] splines_4.4.1      parallel_4.4.1    cellranger_1.1.0
[49] beepr_2.0          vctrs_0.6.5       Matrix_1.7-0
[52] jsonlite_1.8.8     hms_1.1.3         listenv_0.9.1
[55] testthat_3.2.1.1   snow_0.4-4        parallelly_1.38.0
[58] glue_1.7.0         semTools_0.5-6    codetools_0.2-20
[61] stringi_1.8.4      gtable_0.3.5      quadprog_1.5-8
[64] munsell_0.5.1      pillar_1.9.0      brio_1.1.5
[67] htmltools_0.5.8.1  R6_2.5.1          Rdpack_2.6.1
[70] simstandard_0.6.3  evaluate_0.24.0   pbivnorm_0.6.0
[73] lattice_0.22-6     rbibutils_2.2.16  R.methodsS3_1.8.2
[76] RPushbullet_0.3.4  Rcpp_1.0.13       gridExtra_2.3
[79] nlme_3.1-165       permute_0.9-7     mgcv_1.9-1
[82] xfun_0.46          pkgconfig_2.0.3

```

References

- Hlynsson, Jón Ingi, Anders Sjöberg, Lars Ström, and Per Carlbring. 2024. “Evaluating the Reliability and Validity of the Questionnaire on Well-Being: A Validation Study for a Clinically Informed Measurement of Subjective Well-Being.” *Cognitive Behaviour Therapy* 0 (0): 1–23. <https://doi.org/10.1080/16506073.2024.2402992>.
- Hu, Li-tze, and Peter M. Bentler. 1999. “Cutoff Criteria for Fit Indexes in Covariance Structure Analysis: Conventional Criteria Versus New Alternatives.” *Structural Equation Modeling: A Multidisciplinary Journal* 6 (1): 1–55. <https://doi.org/10.1080/10705519909540118>.
- McNeish, Daniel. 2023. “Dynamic Fit Index Cutoffs for Categorical Factor Analysis with Likert-Type, Ordinal, or Binary Responses.” *American Psychologist* 78 (9): 1061–75. <https://doi.org/10.1037/amp0001213>.
- Savalei, Victoria. 2018. “On the Computation of the RMSEA and CFI from the Mean-And-Variance Corrected Test Statistic with Nonnormal Data in SEM.” *Multivariate Behavioral Research* 53 (3): 419–29. <https://doi.org/10.1080/00273171.2018.1455142>.