### Classification Tree - Brisbane

#### Kathryn Weissman

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#### Classification Tree: Brisbane

The goal is to predict if there will be rain the following day.

```
# The random seed must be set before each call to a function that uses random.
set.seed(1234) # for reproducibility of results
```

#### Load Train & Test Data

I am loading the same data that was used for the LDA modelling.

```
# Load the data
Btrain <- read.csv("Train_Test_CSVs/df_Brisbane_train.csv", stringsAsFactors = T)
Btest <- read.csv("Train_Test_CSVs/df_Brisbane_test.csv", stringsAsFactors = T)
Btrain$Date <- as.Date(Btrain$Date)
Btest$Date <- as.Date(Btest$Date)</pre>
```

#### Summarize Train Data

```
str(Btrain)
```

```
## 'data.frame':
                  1431 obs. of 30 variables:
                 : Date, format: "2008-07-01" "2008-07-02" ...
   $ Date
## $ ID
                 : int 84008 84009 84010 84011 84012 84013 84014 84015 84016 84017 ...
## $ Year
                        ## $ Month
                 : Factor w/ 12 levels "abril", "agosto",..: 6 6 6 6 6 6 6 6 6 ...
                 : int 1 2 3 4 5 6 7 8 9 10 ...
##
   $ Day
                 : Factor w/ 1 level "Brisbane": 1 1 1 1 1 1 1 1 1 1 ...
##
  $ Location
## $ Evaporation : num 1.4 2 5.8 1.8 2 5.2 2.4 2 1 4 ...
## $ Sunshine
                 : num 9.5 9.8 9.4 1.1 0.3 6.4 1.6 0.6 11.7 10 ...
## $ WindGustDir : Factor w/ 17 levels "E","ENE","ESE",..: 16 15 1 13 9 2 5 17 15 15 ...
## $ WindGustSpeed: int 26 30 22 24 37 31 17 31 43 39 ...
                : Factor w/ 18 levels "calm", "E", "ENE", ...: 13 16 14 14 10 13 14 14 18 18 ...
## $ WindDir9am
##
   $ WindDir3pm
                 : Factor w/ 18 levels "calm", "E", "ENE", ...: 16 17 2 12 13 2 6 9 16 18 ...
## $ WindSpeed9am : int 6 15 7 9 11 7 9 7 13 17 ...
## $ WindSpeed3pm : int
                       15 19 15 7 7 17 9 2 19 17 ...
## $ Humidity9am : int
                        81 41 55 76 81 78 83 94 48 47 ...
## $ Humidity3pm : int
                        37 30 52 53 89 52 63 73 34 34 ...
## $ Pressure9am : num 1020 1019 1021 1024 1027 ...
## $ Pressure3pm : num 1015 1015 1019 1022 1026 ...
## $ Cloud9am
                 : int 0017757810...
## $ Cloud3pm
                 : int 1047827611...
## $ Temp9am
                 : num 14.9 16.2 15.4 14.1 16.1 15.9 14.7 14.7 12.4 13.2 ...
```

```
: Factor w/ 2 levels "No", "Yes": 1 1 1 1 1 2 1 2 2 1 ...
##
    $ RainToday
    $ RainTomorrow : Factor w/ 2 levels "No", "Yes": 1 1 1 1 2 1 2 2 1 1 ...
    $ TempRange
                           14.9 14.8 12.7 8.2 4.4 8.9 9 2.9 10.7 9.4 ...
                    : num
##
    $ MaxTemp
                    : num
                           25.2 22.9 22.4 20 16.7 21.5 21.9 17.4 16.7 19.7 ...
##
                    : num 10.3 8.1 9.7 11.8 12.3 12.6 12.9 14.5 6 10.3 ...
    $ MinTemp
                    : num 0 0 0 0.8 0 16.2 0 24.2 3.8 0.2 ...
    $ Rainfall
                    : Factor w/ 47 levels "2008-agosto",..: 3 3 3 3 3 3 3 3 3 ...
##
    $ monthID
    $ Season
                    : Factor w/ 4 levels "autumn", "spring", ...: 4 4 4 4 4 4 4 4 4 4 ...
summary(Btrain)
##
         Date
                                ID
                                                Year
                                                                  Month
##
           :2008-07-01
                                  :84008
                                                   :2008
    Min.
                                                           agosto
                                                                     :124
                          Min.
                                           Min.
    1st Qu.:2009-06-23
                          1st Qu.:84358
                                           1st Qu.:2009
                                                           diciembre:124
##
    Median :2010-06-16
                          Median :84708
                                           Median:2010
                                                           enero
                                                                     :124
           :2010-06-16
                          Mean
                                  :84708
                                           Mean
                                                   :2010
                                                           julio
                                                                     :124
##
    3rd Qu.:2011-06-08
                          3rd Qu.:85058
                                           3rd Qu.:2011
                                                           marzo
                                                                     :124
                                  :85408
##
           :2012-05-31
                          Max.
                                           Max.
                                                   :2012
                                                           mayo
                                                                     :124
##
                          NA's
                                  :30
                                                           (Other)
                                                                     :687
                                       Evaporation
##
         Day
                         Location
                                                           Sunshine
##
    Min.
          : 1.00
                     Brisbane:1431
                                      Min.
                                            : 0.000
                                                        Min.
                                                               : 0.000
##
    1st Qu.: 8.00
                                      1st Qu.: 3.200
                                                        1st Qu.: 5.300
##
    Median :16.00
                                      Median : 4.800
                                                        Median: 9.200
    Mean
          :15.73
                                      Mean
                                            : 5.032
                                                        Mean
                                                               : 7.757
##
    3rd Qu.:23.00
                                      3rd Qu.: 6.800
                                                        3rd Qu.:10.500
##
    Max.
           :31.00
                                      Max.
                                             :13.800
                                                        Max.
                                                               :13.500
##
##
                                      WindDir9am
     WindGustDir
                  WindGustSpeed
                                                     WindDir3pm
                                                                  WindSpeed9am
##
    Ε
           :246
                   Min.
                          :13.00
                                    SW
                                           :315
                                                  ENE
                                                          :238
                                                                 Min.
                                                                         : 0.000
                                                   NE
##
    ENE
           :185
                   1st Qu.:22.00
                                    SSW
                                           :152
                                                          :202
                                                                  1st Qu.: 4.000
##
           :168
                   Median :28.00
                                    WSW
                                           :146
                                                   Ε
                                                          :183
                                                                  Median: 7.000
##
    SE
           :133
                   Mean
                          :29.14
                                    SE
                                           :106
                                                   ESE
                                                          :170
                                                                  Mean
                                                                         : 7.593
##
    ESE
           :129
                   3rd Qu.:33.00
                                    SSE
                                           : 95
                                                  NNE
                                                          :114
                                                                  3rd Qu.: 9.000
           :125
                                           : 92
##
    NE
                   Max.
                          :93.00
                                                          :111
                                                                  Max.
                                                                         :26.000
    (Other):445
                                    (Other):525
                                                   (Other):413
##
     WindSpeed3pm
                      Humidity9am
                                       Humidity3pm
                                                        Pressure9am
          : 0.00
                                                              : 997.8
##
    Min.
                     Min.
                            :20.00
                                      Min.
                                             : 8.00
                                                       Min.
##
    1st Qu.: 9.00
                     1st Qu.:57.00
                                      1st Qu.:46.00
                                                       1st Qu.:1014.1
    Median :11.00
                     Median :64.00
                                      Median :54.00
                                                       Median: 1017.8
##
    Mean
          :11.56
                     Mean
                            :64.94
                                      Mean
                                             :54.83
                                                       Mean
                                                              :1017.8
##
    3rd Qu.:15.00
                     3rd Qu.:73.00
                                      3rd Qu.:63.00
                                                       3rd Qu.:1021.6
##
           :28.00
                            :98.00
    Max.
                     Max.
                                      Max.
                                             :98.00
                                                       Max.
                                                              :1031.6
##
##
     Pressure3pm
                         Cloud9am
                                          Cloud3pm
                                                           Temp9am
                                              :0.000
##
           : 993.2
                             :0.000
    Min.
                      Min.
                                       Min.
                                                        Min.
                                                               :10.70
    1st Qu.:1011.1
                      1st Qu.:1.000
                                       1st Qu.:1.000
                                                        1st Qu.:17.90
    Median :1014.9
                      Median :4.000
                                       Median :4.000
##
                                                        Median :22.50
##
    Mean
           :1014.7
                      Mean
                             :4.126
                                       Mean
                                              :4.134
                                                        Mean
                                                               :21.70
##
    3rd Qu.:1018.5
                      3rd Qu.:7.000
                                       3rd Qu.:7.000
                                                        3rd Qu.:25.65
##
           :1028.8
                             :8.000
                                       Max.
                                              :8.000
                                                        Max.
                                                                :31.60
    Max.
                      Max.
##
##
       Temp3pm
                     RainToday
                                RainTomorrow
                                                TempRange
                                                                   MaxTemp
##
    Min.
           :12.00
                     No :1064
                                 No :1064
                                              Min.
                                                      : 0.400
                                                                Min.
                                                                        :12.60
    1st Qu.:21.60
                     Yes: 367
                                Yes: 367
                                              1st Qu.: 7.800
                                                                1st Qu.:23.10
```

: num 24.6 22.4 21.3 19.6 15 20 20.1 17 16.2 18.8 ...

\$ Temp3pm

```
Median :24.60
                                           Median : 9.700
                                                            Median :26.40
                                           Mean : 9.777
##
   Mean :24.53
                                                            Mean
                                                                  :26.16
   3rd Qu.:27.40
                                           3rd Qu.:11.700
                                                            3rd Qu.:29.05
   Max.
          :36.30
                                                  :22.000
                                                                   :37.10
##
                                           Max.
                                                            Max.
##
##
                      Rainfall
                                                              Season
      MinTemp
                                               monthID
##
   Min. : 3.70
                   Min. : 0.000
                                      2008-agosto
                                                           autumn:368
                                                  : 31
   1st Qu.:12.60
                   1st Qu.: 0.000
                                     2008-diciembre:
                                                           spring:364
##
                                                      31
##
   Median :17.10
                   Median :
                             0.000
                                      2008-julio
                                                   :
                                                      31
                                                           summer:361
##
   Mean :16.39
                                      2008-octubre
                                                           winter:338
                   Mean
                         : 3.758
                                                      31
   3rd Qu.:20.40
                   3rd Qu.: 1.200
                                      2009-agosto
   Max. :25.20
                                      2009-diciembre: 31
##
                   Max. :168.400
##
                                      (Other)
                                                   :1245
```

#### Summarize Test Data

#### summary(Btest)

```
##
        Date
                               ID
                                              Year
                                                              Month
##
          :2012-06-01
                                :85409
                                                :2012
   Min.
                                         Min.
                                                        agosto
                                                                 : 31
                        Min.
   1st Qu.:2012-08-31
                         1st Qu.:85486
                                         1st Qu.:2012
                                                        diciembre: 31
##
   Median :2012-11-30
                        Median :85562
                                         Median:2012
                                                        enero
                                                                 : 31
   Mean :2012-11-30
                        Mean :85562
                                         Mean :2012
                                                        iulio
                                                                 : 31
##
   3rd Qu.:2013-03-01
                         3rd Qu.:85638
                                         3rd Qu.:2013
                                                        junio
                                                                 : 31
   Max. :2013-06-01
                        Max.
                                :85715
                                        Max.
                                                :2013
                                                        marzo
                                                                 : 31
##
                         NA's
                                :59
                                                        (Other) :180
##
        Day
                        Location
                                    Evaporation
                                                       Sunshine
                                                                      WindGustDir
##
                    Brisbane:366
                                   Min.
                                                          : 0.000
                                                                     unkn
                                                                            : 63
   Min. : 1.00
                                         : 0.000
                                                    Min.
   1st Qu.: 8.00
##
                                   1st Qu.: 3.400
                                                    1st Qu.: 6.100
                                                                     Ε
                                                                            : 51
##
   Median :16.00
                                   Median : 5.000
                                                    Median : 9.000
                                                                     NE
                                                                            : 39
##
   Mean :15.68
                                   Mean : 5.203
                                                    Mean
                                                         : 7.898
                                                                     ENE
                                                                            : 38
   3rd Qu.:23.00
                                   3rd Qu.: 7.000
                                                                            : 34
##
                                                    3rd Qu.:10.400
##
   Max. :31.00
                                   Max.
                                         :11.800
                                                          :13.200
                                                                     SE
                                                                            : 30
                                                    Max.
##
                                                                     (Other):111
##
   WindGustSpeed
                     WindDir9am
                                    WindDir3pm
                                                 WindSpeed9am
                                                                  WindSpeed3pm
                                                                      : 0.00
   Min.
          :13.00
                          : 79
                                  unkn
                                         : 59
                                                Min. : 0.000
                                                                 Min.
   1st Qu.:22.00
                                         : 46
                                                1st Qu.: 4.000
                                                                 1st Qu.: 7.00
##
                           : 59
                                  NE
                    unkn
##
   Median :26.00
                    WSW
                           : 40
                                  ENE
                                         : 45
                                                Median : 6.000
                                                                 Median: 9.00
                                         : 41
##
   Mean :28.08
                    SSW
                           : 28
                                  Ε
                                                Mean
                                                     : 6.434
                                                                 Mean :10.19
    3rd Qu.:31.00
                           : 19
                                  ESE
                                         : 36
                                                3rd Qu.: 7.000
                                                                 3rd Qu.:13.00
   Max. :70.00
                          : 17
                                  NNE
                                        : 27
                                                Max.
                                                      :37.000
                                                                 Max.
##
                    ENE
                                                                        :24.00
##
                    (Other):124
                                  (Other):112
##
    Humidity9am
                   Humidity3pm
                                    Pressure9am
                                                     Pressure3pm
##
   Min.
           :25.0
                  Min.
                          :16.00
                                  Min.
                                         : 998.4
                                                    Min.
                                                          : 998.1
                                                    1st Qu.:1010.9
##
   1st Qu.:57.0
                   1st Qu.:47.00
                                   1st Qu.:1014.4
                                   Median :1018.1
##
   Median:65.0
                   Median :55.00
                                                    Median :1015.0
##
   Mean
         :65.8
                   Mean :55.66
                                   Mean :1018.0
                                                    Mean
                                                         :1014.8
##
   3rd Qu.:74.0
                   3rd Qu.:63.00
                                   3rd Qu.:1022.0
                                                    3rd Qu.:1018.5
   Max. :98.0
                   Max. :98.00
                                   Max. :1030.4
##
                                                    Max.
                                                          :1027.9
##
##
       Cloud9am
                       Cloud3pm
                                       Temp9am
                                                       Temp3pm
                                                                    RainToday
                    Min.
                                                    Min. :14.10
##
         :0.000
                          :0.000
                                    Min. :10.60
                                                                    No :280
   Min.
   1st Qu.:1.000
                    1st Qu.:1.000
                                    1st Qu.:17.43
                                                    1st Qu.:21.73
                                                                    Yes: 86
   Median :4.000
                    Median :4.000
                                    Median :22.00
                                                    Median :24.50
```

```
:3.956
                             :4.044
                                              :21.55
                                                               :24.42
##
    Mean
                     Mean
                                      Mean
                                                       Mean
    3rd Qu.:7.000
                     3rd Qu.:7.000
                                      3rd Qu.:25.48
                                                       3rd Qu.:26.90
##
                                              :31.90
##
    Max.
            :8.000
                     Max.
                             :8.000
                                      Max.
                                                       Max.
                                                               :33.70
##
##
    RainTomorrow
                    TempRange
                                      MaxTemp
                                                       MinTemp
                                                                        Rainfall
    No :282
                         : 2.00
                                                                            : 0.000
##
                  Min.
                                           :15.10
                                                            : 4.10
                                   Min.
                                                    Min.
                                                                     Min.
    Yes: 84
                  1st Qu.: 7.80
                                   1st Qu.:23.20
                                                    1st Qu.:12.72
                                                                      1st Qu.:
                                                                                0.000
##
##
                  Median: 9.90
                                   Median :26.60
                                                    Median :16.40
                                                                     Median :
                                                                                0.000
##
                  Mean
                         :10.09
                                   Mean
                                           :26.22
                                                    Mean
                                                            :16.13
                                                                     Mean
                                                                                3.377
##
                  3rd Qu.:12.30
                                   3rd Qu.:29.20
                                                    3rd Qu.:20.00
                                                                      3rd Qu.:
                                                                                0.600
##
                  Max.
                         :18.20
                                   Max.
                                           :37.90
                                                    Max.
                                                            :26.10
                                                                     Max.
                                                                             :145.000
##
##
              monthID
                              Season
##
    2012-agosto
                   : 31
                          autumn:92
##
    2012-diciembre: 31
                          spring:91
##
    2012-julio
                   : 31
                          summer:90
                   : 31
##
    2012-octubre
                          winter:93
    2013-enero
                   : 31
                   : 31
##
    2013-marzo
    (Other)
                   :180
```

#### Compare Target Variables for Train and Test Data

It is important that our training data and testing data have similar characteristics in order to optimize the performance of our model. The test set has a slightly lower percentage of rainy days than the training set.

```
print ("Percentage of Days with Rain Tomorrow in Train Data")
## [1] "Percentage of Days with Rain Tomorrow in Train Data"
round(prop.table(table(Btrain$RainTomorrow))*100,1)
##
## No Yes
## 74.4 25.6
print ("Percentage of Days with Rain Tomorrow in Test Data")
## [1] "Percentage of Days with Rain Tomorrow in Test Data"
round(prop.table(table(Btest$RainTomorrow))*100,1)
##
## No Yes
## 77 23
```

The seasons are mostly balanced between the training and testing data. The testing data has a slightly larger proportion of winter days. This is due to the span of dates in the training data not including one of the full years. The training data spans from July 1, 2008 to May 31, 2012. We don't have data for the month of June 2008 to include in the training set.

```
print ("Percentage of Days in each Season in Train Data")
## [1] "Percentage of Days in each Season in Train Data"
round(prop.table(table(Btrain$Season))*100,1)
##
## autumn spring summer winter
```

```
## 25.7 25.4 25.2 23.6
print ("Percentage of Days in each Season in Test Data")

## [1] "Percentage of Days in each Season in Test Data"
round(prop.table(table(Btest$Season))*100,1)

##
## autumn spring summer winter
## 25.1 24.9 24.6 25.4
```

#### Classification Tree

https://cran.r-project.org/web/packages/rpart/vignettes/longintro.pdf

"The rpart programs build classification or regression models of a very general structure using a two stage procedure; the resulting models can be represented as binary trees."

We use two different sets of modeling variables to see if there is a difference in the performance of the model for classifying whether or not there will be rain tomorrow.

```
# We use two different sets of variables for the model to consider
# Set 1 includes "RainToday" and "TempRange"
modeling_vars1 <- c("Evaporation", "Sunshine", "WindGustSpeed", "WindSpeed9am",
                   "WindSpeed3pm", "Humidity9am", "Humidity3pm", "Pressure9am",
                   "Pressure3pm", "Cloud9am", "Cloud3pm", "TempRange",
                   "RainToday", "Season", "RainTomorrow")
# Set 2 includes all temperature variables and "Rainfall" instead of "RainToday"
modeling_vars2 <- c("Evaporation", "Sunshine", "WindGustSpeed", "WindSpeed9am",
                   "WindSpeed3pm", "Humidity9am", "Humidity3pm", "Pressure9am",
                   "Pressure3pm", "Cloud9am", "Cloud3pm", "Temp9am", "Temp3pm",
                   "TempRange", "MaxTemp", "MinTemp", "RainToday", "Rainfall", "Season",
                   "RainTomorrow")
train1 <- Btrain[,modeling_vars1]</pre>
test1 <- Btest[,modeling_vars1]</pre>
train2 <- Btrain[,modeling_vars2]</pre>
test2 <- Btest[,modeling_vars2]</pre>
```

#### SMOTE algorithm for unbalanced classification problems

From the library {performanceEstimation}

"This function handles unbalanced classification problems using the SMOTE method. Namely, it can generate a new "SMOTEd" data set that addresses the class unbalance problem."

Balanced Training Sets 1 and 2 have different observations due to the nearest neighbors defined by the subset of variables contained in each training data set.

```
set.seed(1234) # for reproducibility of results
# Create balanced training data sets
trainBal1 <- smote(RainTomorrow ~., train1, perc.over = 2, k = 5, perc.under = 2)
trainBal2 <- smote(RainTomorrow ~., train2, perc.over = 2, k = 5, perc.under = 2)</pre>
```

```
print("Training Data: Count of Rain Tomorrow")
## [1] "Training Data: Count of Rain Tomorrow"
(table(Btrain$RainTomorrow))
##
##
    No Yes
## 1064 367
print("Balanced Training 1 Data: Count of Rain Tomorrow")
## [1] "Balanced Training 1 Data: Count of Rain Tomorrow"
(table(trainBal1$RainTomorrow))
##
##
    No Yes
## 1468 1101
print("Balanced Training 1 Data: Percent of Days with Rain Tomorrow")
## [1] "Balanced Training 1 Data: Percent of Days with Rain Tomorrow"
round(prop.table((table(trainBal1$RainTomorrow)))*100,2)
##
##
     No
           Yes
## 57.14 42.86
print("Balanced Training 2 Data: Count of Rain Tomorrow")
## [1] "Balanced Training 2 Data: Count of Rain Tomorrow"
(table(trainBal2$RainTomorrow))
##
##
    No Yes
## 1468 1101
print("Balanced Training 2 Data: Percent of Days with Rain Tomorrow")
## [1] "Balanced Training 2 Data: Percent of Days with Rain Tomorrow"
round(prop.table(table(trainBal2$RainTomorrow))*100,2)
##
##
     No
           Yes
## 57.14 42.86
print("Balanced Training 1 Data: Percent of Days in each Season")
## [1] "Balanced Training 1 Data: Percent of Days in each Season"
round(prop.table(table(trainBal1$Season))*100,1)
##
## autumn spring summer winter
     26.5
            23.3
                   29.2
                          21.0
print("Balanced Training 2 Data: Percent of Days in each Season")
## [1] "Balanced Training 2 Data: Percent of Days in each Season"
```

```
round(prop.table(table(trainBal2$Season))*100,1)

##
## autumn spring summer winter
## 26.7 24.6 28.2 20.6

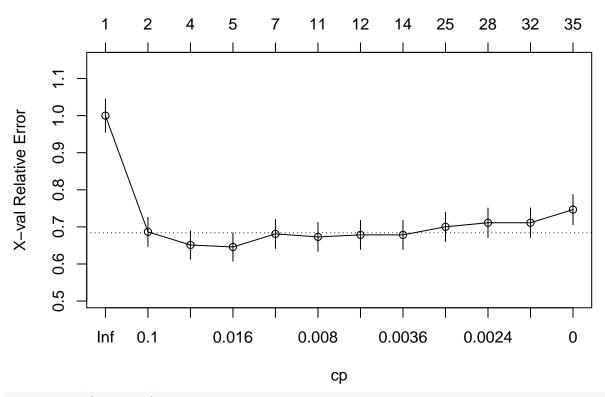
Using Fitting & Pruning Strategy shown in Lab

# Best strategy for tree fitting, start with cp = 0, then prune.
set.seed(1234) # for reproducibility of results
treeFit1 <- rpart(RainTomorrow ~., data = train1, method = "class", cp = 0)
printcp(treeFit1)</pre>
```

#### First Set of Variables on Unbalanced Data

```
##
## Classification tree:
## rpart(formula = RainTomorrow ~ ., data = train1, method = "class",
##
      cp = 0)
##
## Variables actually used in tree construction:
  [1] Cloud3pm
                     Cloud9am
                                                              Humidity9am
                                   Evaporation
                                                 Humidity3pm
                                   RainToday
## [6] Pressure3pm
                     Pressure9am
                                                 Season
                                                              Sunshine
## [11] TempRange
                     WindGustSpeed WindSpeed9am
##
## Root node error: 367/1431 = 0.25646
##
## n= 1431
##
##
            CP nsplit rel error xerror
## 1 0.3324251
                    0
                       1.00000 1.00000 0.045011
## 2 0.0313351
                        0.66757 0.68665 0.039262
## 3 0.0190736
                    3 0.60490 0.65123 0.038446
## 4 0.0136240
                    4
                       0.58583 0.64578 0.038317
## 5 0.0118074
                    6 0.55858 0.68120 0.039139
## 6 0.0054496
                   10 0.50681 0.67302 0.038953
## 7 0.0040872
                 11 0.50136 0.67847 0.039077
## 8 0.0032202
                   13 0.49319 0.67847 0.039077
## 9 0.0027248
                   24 0.45777 0.70027 0.039565
## 10 0.0020436
                   27
                       0.44959 0.71117 0.039804
## 11 0.0018165
                   31
                        0.44142 0.71117 0.039804
## 12 0.0000000
                   34
                        0.43597 0.74659 0.040556
plotcp(treeFit1)
```





```
#rpart.plot(treeFit1)
```

CP

##

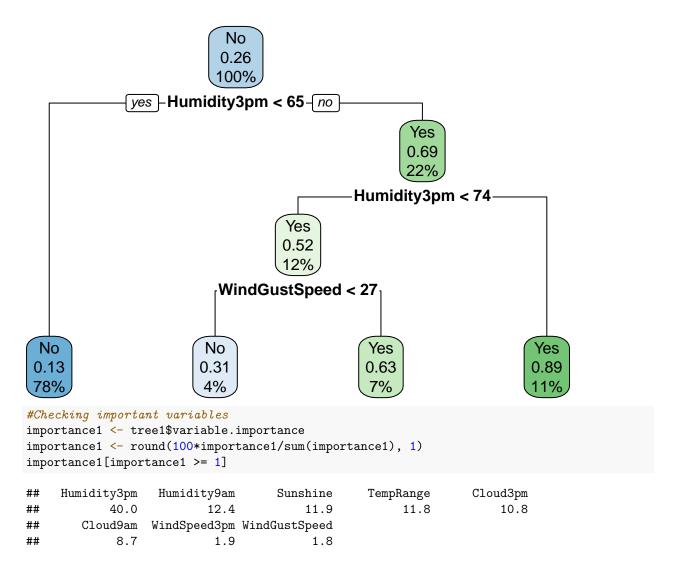
```
# Find the cp with lowest error, then prune.
xerror <- treeFit1$cptable[,"xerror"]</pre>
imin.xerror <- which.min(xerror)</pre>
treeFit1$cptable[imin.xerror, ]
```

```
nsplit rel error
                                           xerror
## 0.01362398 4.00000000 0.58583106 0.64577657 0.03831691
upper.xerror <- xerror[imin.xerror] + treeFit1$cptable[imin.xerror, "xstd"]</pre>
icp <- min(which(xerror <= upper.xerror))</pre>
cp <- treeFit1$cptable[icp, "CP"]</pre>
```

xstd

The pruned tree produced using imbalanced training data on the first set of variables is extremely simple, and only uses two variables, Humidity3pm and WindGustSpeed.

```
# prune using cp
tree1 <- prune(treeFit1, cp = cp)</pre>
rpart.plot(tree1)
```



 ${\bf Confusion\ Matrix} \quad {\bf Help\ for\ Confusion\ Matrix:\ https://towards datascience.com/understanding-confusion-matrix-a9ad 42 dcfd 62 }$ 

Recall, Precision and Accuracy should be high as possible

Balanced Accuracy represents area under ROC.

Although the accuracy is fairly high, 84%, the sensitivity is low, below 60%, which is how well the model predicts it will rain on a rainy day. Since the data is imbalanced, we should try using SMOTE sampling for the training data to see if it improves the performance of the model.

```
#Evaluation
#Confusion matrix-train
pred_train1 <- predict(tree1, train1, type = 'class') # using train data
#Make sure to state positive class in the confusion matrix.
confusionMatrix(pred_train1, train1$RainTomorrow, positive="Yes")

## Confusion Matrix and Statistics
##
## Reference
## Prediction No Yes
##
No 1009 167</pre>
```

```
##
                  Accuracy : 0.8449
##
                    95% CI: (0.8251, 0.8632)
##
##
       No Information Rate: 0.7435
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                     Kappa: 0.548
##
    Mcnemar's Test P-Value: 9.346e-14
##
##
##
               Sensitivity: 0.5450
##
               Specificity: 0.9483
##
            Pos Pred Value: 0.7843
##
            Neg Pred Value: 0.8580
##
                Prevalence: 0.2565
##
            Detection Rate: 0.1398
##
      Detection Prevalence: 0.1782
##
         Balanced Accuracy: 0.7466
##
##
          'Positive' Class : Yes
##
# Best strategy for tree fitting, start with cp = 0, then prune.
set.seed(1234) # for reproducibility of results
treeFitBal1 <- rpart(RainTomorrow ~., data = trainBal1, method = "class", cp = 0)</pre>
printcp(treeFitBal1)
```

#### First Set of Variables on Balnced Training Data using SMOTE

##

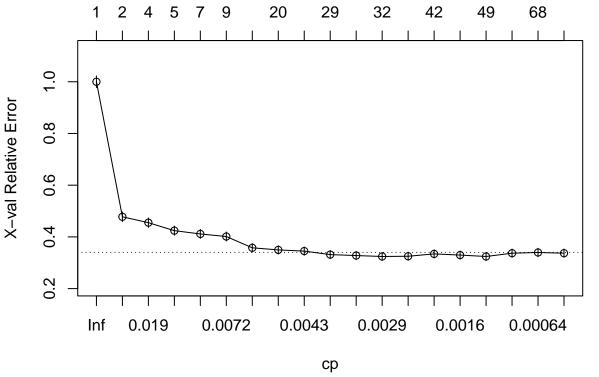
Yes

55 200

```
## Classification tree:
## rpart(formula = RainTomorrow ~ ., data = trainBal1, method = "class",
##
## Variables actually used in tree construction:
  [1] Cloud3pm
                      Cloud9am
                                                                Humidity9am
                                   Evaporation
                                                  Humidity3pm
   [6] Pressure3pm
                     Pressure9am
                                                  Sunshine
                                                                TempRange
                                    Season
## [11] WindGustSpeed WindSpeed3pm
                                   WindSpeed9am
## Root node error: 1101/2569 = 0.42857
##
## n= 2569
##
##
              CP nsplit rel error xerror
## 1 0.52316076
                     0
                          1.00000 1.00000 0.022782
## 2
     0.02134423
                      1
                         0.47684 0.47775 0.018576
## 3 0.01725704
                     3
                         0.43415 0.45504 0.018240
## 4 0.00862852
                     4
                         0.41689 0.42416 0.017754
## 5
     0.00817439
                     6
                         0.39964 0.41144 0.017544
## 6
     0.00635786
                     8
                         0.38329 0.40145 0.017375
## 7 0.00544959
                     16
                         0.31789 0.35786 0.016589
## 8 0.00454133
                     19
                         0.30154 0.34968 0.016432
## 9 0.00408719
                     21
                         0.29246 0.34514 0.016344
```

```
## 10 0.00363306
                           0.25613 0.33152 0.016072
                     28
## 11 0.00317893
                     29
                           0.25250 0.32788 0.015999
                           0.24614 0.32425 0.015924
## 12 0.00272480
## 13 0.00242204
                           0.22707 0.32516 0.015943
                     38
## 14 0.00181653
                     41
                           0.21980 0.33424 0.016127
## 15 0.00145322
                     43
                           0.21617 0.32970 0.016036
## 16 0.00102180
                     48
                           0.20890 0.32425 0.015924
## 17 0.00090827
                           0.20073 0.33697 0.016182
                     56
## 18 0.00045413
                     67
                           0.19074 0.33969 0.016236
## 19 0.00000000
                     71
                           0.18892 0.33697 0.016182
plotcp(treeFitBal1)
```

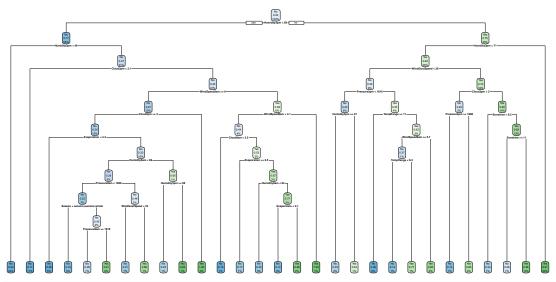
#### size of tree



```
#rpart.plot(treeFitBal1)
# Find the cp with lowest error, then prune.
xerror <- treeFitBal1$cptable[,"xerror"]</pre>
imin.xerror <- which.min(xerror)</pre>
treeFitBal1$cptable[imin.xerror, ]
##
             CP
                       nsplit
                                  rel error
                                                   xerror
                                                                   xstd
##
   0.002724796 31.000000000 0.246139873 0.324250681
                                                           0.015924188
upper.xerror <- xerror[imin.xerror] + treeFitBal1$cptable[imin.xerror, "xstd"]
icp <- min(which(xerror <= upper.xerror))</pre>
cp <- treeFitBal1$cptable[icp, "CP"]</pre>
```

The pruned tree using the balanced data is much more complex than the tree produced using imbalanced data.

```
# prune using cp
treeBal1 <- prune(treeFitBal1, cp = cp)
rpart.plot(treeBal1)</pre>
```



# #Classification Rules rpart.rules(treeBal1, style = "tall")

```
## RainTomorrow is 0.00 when
##
       Humidity3pm is 59 to 71
##
       WindGustSpeed < 26
##
       Pressure3pm >= 1016
##
       TempRange >= 10.9
##
## RainTomorrow is 0.04 when
##
       Humidity3pm < 49
##
  RainTomorrow is 0.08 when
##
       Humidity3pm is 49 to 59
##
##
       Cloud3pm >= 3.0
##
       WindSpeed9am >= 6.0
##
       Evaporation < 4.3
##
## RainTomorrow is 0.10 when
##
       Humidity3pm is 49 to 59
       Cloud3pm >= 2.1
##
##
       WindSpeed9am < 4.1
##
       Cloud9am < 3.5
##
## RainTomorrow is 0.11 when
       Humidity3pm is 49 to 59
##
##
       Cloud3pm < 2.1
##
## RainTomorrow is 0.14 when
       Humidity3pm is 59 to 71
##
       WindSpeed9am >= 5.7
##
##
       WindGustSpeed < 26
       Pressure3pm >= 1016
##
```

```
TempRange < 8.3
##
##
## RainTomorrow is 0.14 when
##
       Humidity3pm is 49 to 59
##
       Cloud3pm >= 2.1
##
       WindSpeed9am < 4.1
##
       Evaporation < 2.1
       Humidity9am >= 62
##
##
       Cloud9am >= 3.5
##
## RainTomorrow is 0.14 when
##
       Humidity3pm is 59 to 71
       Cloud3pm < 2.0
##
       WindGustSpeed >= 26
##
##
       Pressure3pm >= 1008
##
## RainTomorrow is 0.16 when
       Humidity3pm is 49 to 59
##
       Cloud3pm >= 3.0
##
       WindSpeed9am >= 6.0
##
##
       Evaporation >= 4.3
##
       Humidity9am < 68
##
       Pressure9am < 1020
##
       Season is autumn or summer or winter
##
## RainTomorrow is 0.17 when
##
       Humidity3pm is 49 to 59
##
       Cloud3pm >= 2.1
       WindSpeed9am < 4.1
##
##
       Evaporation >= 6.5
       Cloud9am >= 3.5
##
##
## RainTomorrow is 0.20 when
       Humidity3pm is 49 to 59
##
       Cloud3pm >= 2.1
##
       WindSpeed9am < 4.1
##
##
       Evaporation < 6.5
##
       Humidity9am < 62
       Cloud9am >= 3.5
##
##
## RainTomorrow is 0.21 when
       Humidity3pm is 49 to 59
##
##
       Cloud3pm >= 3.0
##
       WindSpeed9am >= 6.0
##
       WindGustSpeed < 33
##
       Evaporation >= 4.3
##
       Humidity9am < 68
##
       Pressure9am >= 1020
##
## RainTomorrow is 0.23 when
##
       Humidity3pm is 61 to 71
##
       WindGustSpeed < 26
##
       Pressure3pm < 1016
##
```

```
## RainTomorrow is 0.23 when
##
       Humidity3pm is 58 to 59
       Cloud3pm >= 3.0
##
##
       WindSpeed9am >= 6.0
       Evaporation >= 4.3
##
##
       Humidity9am >= 68
##
## RainTomorrow is 0.24 when
##
       Humidity3pm is 59 to 71
##
       Cloud3pm >= 2.0
##
       WindGustSpeed >= 26
##
       Sunshine < 0.2
##
## RainTomorrow is 0.28 when
##
       Humidity3pm is 49 to 59
##
       Cloud3pm >= 3.0
##
       WindSpeed9am >= 6.0
       Evaporation >= 4.3
##
##
       Humidity9am < 68
       Pressure9am is 1015 to 1020
##
##
       Season is spring
##
## RainTomorrow is 0.36 when
##
       Humidity3pm is 59 to 71
       Cloud3pm >= 2.0
##
##
       WindGustSpeed >= 26
##
       Sunshine >= 10.9
## RainTomorrow is 0.63 when
       Humidity3pm is 59 to 61
##
       WindGustSpeed < 26
##
##
       Pressure3pm < 1016
##
## RainTomorrow is 0.77 when
       Humidity3pm is 59 to 71
##
       WindSpeed9am >= 5.7
##
##
       WindGustSpeed < 26
##
       Pressure3pm >= 1016
       TempRange is 8.3 to 10.9
##
##
## RainTomorrow is 0.80 when
       Humidity3pm is 59 to 71
##
##
       Cloud3pm < 2.0
##
       WindGustSpeed >= 26
##
       Pressure3pm < 1008
##
## RainTomorrow is 0.80 when
##
       Humidity3pm is 59 to 71
       WindSpeed9am < 5.7
##
##
       WindGustSpeed < 26
##
       Pressure3pm >= 1016
##
       TempRange < 10.9
##
## RainTomorrow is 0.86 when
```

```
##
       Humidity3pm is 49 to 59
##
       Cloud3pm >= 3.0
       WindSpeed9am >= 6.0
##
       WindGustSpeed >= 33
##
##
       Evaporation >= 4.3
       Humidity9am < 68
##
##
       Pressure9am >= 1020
##
##
   RainTomorrow is 0.86 when
##
       Humidity3pm is 59 to 71
##
       Cloud3pm >= 2.0
##
       WindGustSpeed >= 26
       Sunshine is 0.2 to 10.9
##
##
##
   RainTomorrow is 0.88 when
##
       Humidity3pm is 49 to 59
       Cloud3pm >= 2.1
##
##
       WindSpeed9am < 4.1
##
       Evaporation is 2.1 to 6.5
##
       Humidity9am >= 62
##
       Cloud9am >= 3.5
##
## RainTomorrow is 0.91 when
       Humidity3pm is 49 to 59
##
       Cloud3pm >= 3.0
##
##
       WindSpeed9am >= 6.0
##
       Evaporation >= 4.3
       Humidity9am < 68
##
##
       Pressure9am < 1015
##
       Season is spring
##
##
   RainTomorrow is 0.91 when
##
       Humidity3pm >= 71
##
##
   RainTomorrow is 0.94 when
##
       Humidity3pm is 49 to 58
##
       Cloud3pm >= 3.0
##
       WindSpeed9am >= 6.0
##
       Evaporation >= 4.3
##
       Humidity9am >= 68
##
##
   RainTomorrow is 1.00 when
       Humidity3pm is 49 to 59
##
       Cloud3pm is 2.1 to 3.0
##
       WindSpeed9am >= 6.0
##
##
##
  RainTomorrow is 1.00 when
       Humidity3pm is 49 to 59
##
##
       Cloud3pm >= 2.1
##
       WindSpeed9am is 4.1 to 6.0
```

In the Imbalanced Training Data for the first set of variables, Humidity3pm, Humidity9am, Sunshine, TempRange, Cloud3pm, Cloud9am, WindSpeed3pm, and WindGustSpeed were the only variables with important greater than 1%. Using the balanced training data spreads out the importance to more variables

including WindSpeed9am, Pressure variables, Evaporation, and Season.

```
#Checking important variables
importanceBal1 <- treeBal1$variable.importance
importanceBal1 <- round(100*importanceBal1/sum(importanceBal1), 1)
importanceBal1[importanceBal1 >= 1]
```

```
##
     Humidity3pm
                        Cloud3pm
                                       Sunshine
                                                     TempRange
                                                                  Humidity9am
##
                            14.0
             25.2
                                            13.4
                                                           12.7
                                                                          11.3
##
        Cloud9am
                   WindSpeed9am WindGustSpeed
                                                   Pressure3pm
                                                                   Evaporation
##
             10.7
                             2.6
                                             2.4
                                                            1.8
                                                                           1.7
    WindSpeed3pm
##
                    Pressure9am
                                         Season
##
              1.5
                             1.3
                                             1.3
```

Using the model created by balancing the data produces better results when checking predictions on the training data. Accuracy improved from 84.5% to 86.2%. Sensitivity improved from 54.5% to 78.2%. Specificity decreased from 94.8% to 89%, but Balanced Accuracy (Area under ROC) improved from 74.6% to 83.6%

```
#Evaluation of model created with balanced data
#Confusion matrix-train
pred_trainBal1 <- predict(treeBal1, train1, type = 'class') # using original train data
#Make sure to state positive class in the confusion matrix.
confusionMatrix(pred_trainBal1, train1$RainTomorrow, positive="Yes")</pre>
```

```
## Confusion Matrix and Statistics
##
             Reference
##
  Prediction No Yes
##
          No 947
                   80
##
##
          Yes 117 287
##
##
                  Accuracy: 0.8623
##
                    95% CI: (0.8434, 0.8798)
       No Information Rate: 0.7435
##
##
       P-Value [Acc > NIR] : < 2e-16
##
##
                     Kappa: 0.6506
##
##
    Mcnemar's Test P-Value: 0.01032
##
##
               Sensitivity: 0.7820
               Specificity: 0.8900
##
            Pos Pred Value: 0.7104
##
##
            Neg Pred Value: 0.9221
##
                Prevalence: 0.2565
##
            Detection Rate: 0.2006
##
      Detection Prevalence: 0.2823
##
         Balanced Accuracy: 0.8360
##
##
          'Positive' Class : Yes
##
```

The default probability threshold is 50% for classification. We can use trial and error to determine if a different probability threshold improves results.

In this case, lowering the probability threshold to 30% did not improve our model evaluation metrics.

When the tree produces a probability of greater than 30% chance of rain tomorrow, predicting that it will

rain lowers the balanced accuracy of the model.

We can use the default threshold of 50%.

```
#Train Set Evaluation of Balanced Model with probabilities
#Confusion matrix-train
pred_trainBal1_prob <- predict(treeBal1, train1, type = 'prob') # using imbalanced training data</pre>
# predict rain if chance of rain is more than 30% (default is 50%)
pred_trainBal1_prob30 <- ifelse(pred_trainBal1_prob[,2]>0.3,"Yes","No")
confusionMatrix(data= as.factor(pred trainBal1 prob30), train1$RainTomorrow, positive="Yes")
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction No Yes
          No 937 77
##
##
          Yes 127 290
##
##
                  Accuracy : 0.8574
##
                    95% CI: (0.8382, 0.8752)
       No Information Rate: 0.7435
##
##
       P-Value [Acc > NIR] : < 2.2e-16
##
                     Kappa : 0.6422
##
##
   Mcnemar's Test P-Value: 0.0006021
##
##
##
               Sensitivity: 0.7902
##
               Specificity: 0.8806
##
            Pos Pred Value: 0.6954
##
            Neg Pred Value: 0.9241
##
                Prevalence: 0.2565
##
            Detection Rate: 0.2027
##
      Detection Prevalence: 0.2914
##
         Balanced Accuracy: 0.8354
##
##
          'Positive' Class : Yes
##
```

Some of our key metrics decrease slightly when expanded to the test set, which could be an indicator of overfitting to the training data, but it is not too different.

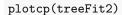
Accuracy is 80%, Sensitivity is 79.7%, Specificity is 80%, and Balanced Accuracy is 80%.

```
#Test Set Evaluation of Balanced Model 1
#Confusion matrix-test
pred_testBal1 <- predict(treeBal1, test1, type = 'class') # using testing data</pre>
confusionMatrix(pred_testBal1, test1$RainTomorrow, positive="Yes")
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction No Yes
          No 226 17
##
##
          Yes 56 67
##
##
                  Accuracy: 0.8005
```

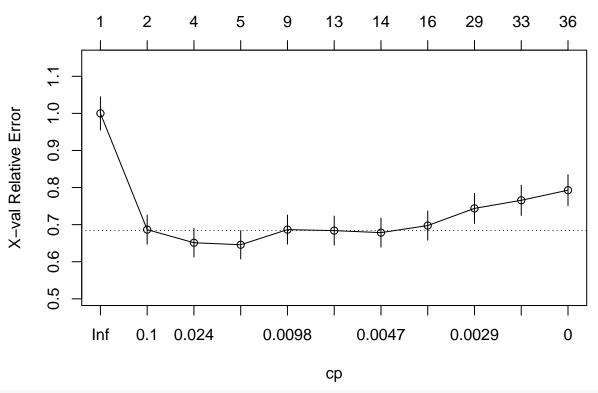
```
##
                    95% CI: (0.7559, 0.8403)
##
       No Information Rate: 0.7705
       P-Value [Acc > NIR] : 0.09445
##
##
##
                     Kappa: 0.5151
##
   Mcnemar's Test P-Value: 8.685e-06
##
##
##
               Sensitivity: 0.7976
##
               Specificity: 0.8014
##
            Pos Pred Value: 0.5447
            Neg Pred Value: 0.9300
##
##
                Prevalence: 0.2295
##
            Detection Rate: 0.1831
##
      Detection Prevalence: 0.3361
##
         Balanced Accuracy: 0.7995
##
##
          'Positive' Class : Yes
##
```

**Second Set of Variables** This set includes more variables than the first set. Set 1 included "RainToday", but set 2 also includes "Rainfall". Set 1 included "TempRange", but set 2 includes all temperature related variables including TempRange.

```
# Best strategy for tree fitting, cp = 0
set.seed(1234) # for reproducibility of results
treeFit2 <- rpart(RainTomorrow ~., data = train2, method = "class", cp = 0)
printcp(treeFit2)
## Classification tree:
## rpart(formula = RainTomorrow ~ ., data = train2, method = "class",
##
##
## Variables actually used in tree construction:
   [1] Cloud3pm
                      Evaporation
                                    Humidity3pm
                                                  Humidity9am
                                                                MinTemp
##
   [6] Pressure3pm
                      Pressure9am
                                    Rainfall
                                                  RainToday
                                                                Sunshine
## [11] Temp3pm
                      TempRange
                                    WindGustSpeed WindSpeed3pm
                                                                WindSpeed9am
##
## Root node error: 367/1431 = 0.25646
##
## n= 1431
##
##
             CP nsplit rel error xerror
## 1
     0.3324251
                     0
                         1.00000 1.00000 0.045011
## 2 0.0313351
                     1
                         0.66757 0.68665 0.039262
## 3 0.0190736
                     3
                         0.60490 0.65123 0.038446
## 4 0.0118074
                     4
                         0.58583 0.64578 0.038317
## 5 0.0081744
                     8
                        0.53406 0.68665 0.039262
## 6 0.0054496
                    12
                        0.49591 0.68392 0.039201
## 7 0.0040872
                         0.49046 0.67847 0.039077
                    13
## 8
     0.0031141
                    15
                         0.48229 0.69755 0.039505
                    28
## 9 0.0027248
                         0.43869 0.74387 0.040500
## 10 0.0018165
                    32 0.42779 0.76567 0.040946
## 11 0.0000000
                    35 0.42234 0.79292 0.041487
```



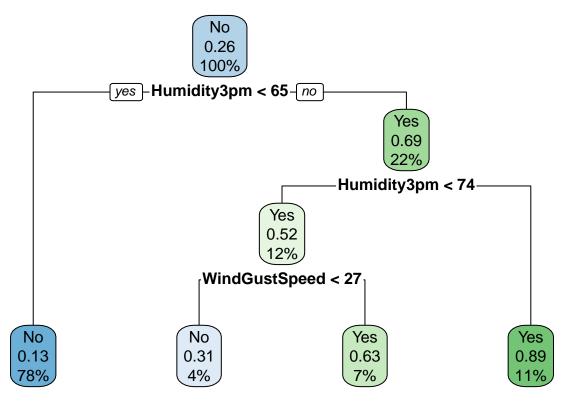
### size of tree



#### #rpart.plot(treeFit2)

After pruning, the trees for both sets of variables that use the imbalanced training data are the identical for Brisbane, and they only use the Humidity3pm and WindGustSpeed variable to make a prediction.

```
tree2 <- prune(treeFit2, cp = cp)
rpart.plot(tree2)</pre>
```



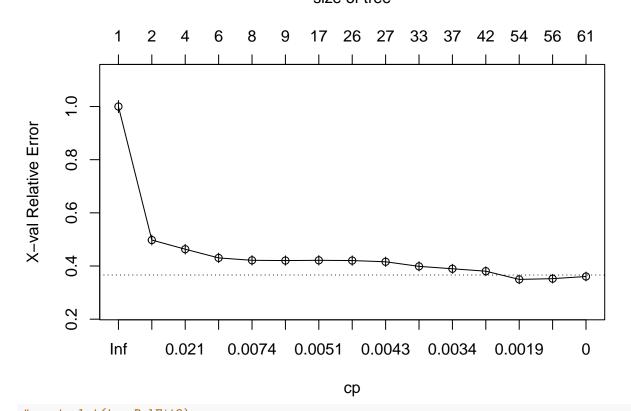
The important variables are the same for tree1 and tree2, even though some different variables were added to the second training set. Humidity3pm is the most important.

Second Set of Variables on Balanced Training Data using SMOTE The next step is to create the tree using a more balanced training set with the second set of variables to see if our model performance improves.

```
# Best strategy for tree fitting, cp = 0
set.seed(1234) # for reproducibility of results
treeBalFit2 <- rpart(RainTomorrow ~., data = trainBal2, method = "class", cp = 0)</pre>
printcp(treeBalFit2)
##
## Classification tree:
## rpart(formula = RainTomorrow ~ ., data = trainBal2, method = "class",
##
##
## Variables actually used in tree construction:
   [1] Cloud3pm
                      Cloud9am
                                    Evaporation
                                                   Humidity3pm
                                                                 Humidity9am
   [6] MinTemp
                      Pressure3pm
                                    Pressure9am
                                                   Rainfall
##
                                                                 Season
## [11] Sunshine
                      Temp3pm
                                    TempRange
                                                   WindGustSpeed WindSpeed3pm
  [16] WindSpeed9am
##
##
## Root node error: 1101/2569 = 0.42857
##
## n= 2569
##
##
              CP nsplit rel error xerror
## 1 0.50681199
                      0
                          1.00000 1.00000 0.022782
     0.02861035
                      1
                          0.49319 0.49773 0.018858
## 2
                      3
                          0.43597 0.46322 0.018363
## 3 0.01589464
```

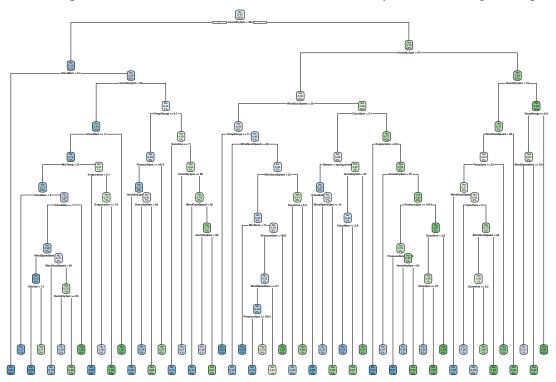
```
## 4 0.00862852
                          0.40418 0.43052 0.017857
## 5
     0.00635786
                      7
                          0.38692 0.42144 0.017710
                          0.38056 0.42053 0.017695
     0.00514684
     0.00499546
                          0.33697 0.42144 0.017710
## 7
                     16
## 8
     0.00454133
                     25
                          0.28792 0.42053 0.017695
## 9 0.00408719
                     26
                          0.28338 0.41599 0.017620
## 10 0.00363306
                          0.25704 0.39873 0.017328
## 11 0.00326975
                     36
                          0.24251 0.38965 0.017170
## 12 0.00272480
                     41
                          0.22616 0.38056 0.017008
## 13 0.00136240
                     53
                          0.19346 0.34968 0.016432
## 14 0.00090827
                     55
                          0.19074 0.35241 0.016484
## 15 0.00000000
                     60
                          0.18619 0.36058 0.016640
plotcp(treeBalFit2)
```

# size of tree



### #rpart.plot(treeBalFit2)

## Warning: labs do not fit even at cex 0.15, there may be some overplotting



## #Classification Rules rpart\_rules(trooRal2\_styl

rpart.rules(treeBal2, style = "tall")

```
## RainTomorrow is 0.00 when
##
       Humidity3pm < 55</pre>
##
       Cloud9am >= 3.0
       MinTemp >= 23
##
##
       Evaporation < 6.1
##
## RainTomorrow is 0.00 when
       Humidity3pm is 58 to 67
##
       WindGustSpeed >= 26
##
       Cloud3pm >= 5.1
##
##
       Evaporation < 0.9
##
## RainTomorrow is 0.03 when
##
       Humidity3pm is 58 to 67
       WindGustSpeed < 26
##
##
       TempRange >= 11.1
##
##
  RainTomorrow is 0.04 when
       Humidity3pm < 58</pre>
##
##
       Cloud9am < 2.1
##
## RainTomorrow is 0.06 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed < 22
       TempRange < 11.1
##
##
       MinTemp < 13
```

```
##
## RainTomorrow is 0.07 when
       Humidity3pm is 58 to 67
##
##
       WindGustSpeed >= 26
       Cloud3pm >= 5.1
##
##
       Humidity9am >= 57
##
       Evaporation >= 0.9
       Pressure9am < 1016
##
##
       Pressure3pm >= 1014
##
## RainTomorrow is 0.08 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed >= 26
##
       Cloud9am < 4.0
##
       Cloud3pm < 5.1
##
       Season is spring or winter
##
## RainTomorrow is 0.09 when
       Humidity3pm < 55</pre>
##
       Cloud9am >= 7.0
##
##
       MinTemp < 23
##
       WindSpeed9am >= 7.0
##
       Rainfall < 13
##
## RainTomorrow is 0.09 when
##
       Humidity3pm is 67 to 73
##
       WindGustSpeed < 20
##
       Temp3pm >= 22
##
## RainTomorrow is 0.09 when
       Humidity3pm is 57 to 58
##
##
       Cloud9am >= 2.1
##
       TempRange >= 9.7
       Pressure9am >= 1013
##
##
## RainTomorrow is 0.10 when
##
       Humidity3pm is 55 to 58
##
       Cloud9am >= 2.1
##
       TempRange < 9.7
##
       Sunshine >= 10.6
##
## RainTomorrow is 0.10 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed < 22
##
       TempRange < 11.1
       MinTemp >= 13
##
##
       Pressure9am < 1023
##
       WindSpeed9am >= 3.7
##
       Pressure3pm >= 1012
##
## RainTomorrow is 0.11 when
##
       Humidity3pm < 55</pre>
       Cloud9am is 3.0 to 6.0
##
##
       MinTemp < 23
```

```
##
## RainTomorrow is 0.14 when
       Humidity3pm is 55 to 58
##
##
       WindGustSpeed < 20
       Cloud9am >= 2.1
##
##
       TempRange < 9.7
##
       Sunshine < 10.6
##
## RainTomorrow is 0.15 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed >= 26
##
       Cloud9am >= 2.8
##
       Cloud3pm < 5.1
       Humidity9am < 67
##
##
       Season is autumn or summer
##
## RainTomorrow is 0.16 when
       Humidity3pm is 58 to 67
##
       WindGustSpeed is 26 to 26
##
       TempRange < 11.1
##
##
## RainTomorrow is 0.18 when
##
       Humidity3pm < 55</pre>
##
       WindGustSpeed < 26
       Cloud9am >= 7.0
##
##
       MinTemp < 23
##
       WindSpeed9am < 7.0
## RainTomorrow is 0.19 when
##
       Humidity3pm is 55 to 57
       Cloud9am >= 2.1
##
##
       TempRange >= 9.7
##
       Humidity9am < 62
       Pressure9am >= 1013
##
##
## RainTomorrow is 0.22 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed >= 26
       Cloud9am >= 4.0
##
##
       Cloud3pm < 5.1
##
       Season is spring or winter
       WindSpeed3pm >= 14
##
##
##
  RainTomorrow is 0.25 when
##
       Humidity3pm is 58 to 67
       WindGustSpeed is 22 to 26
##
##
       TempRange < 11.1
##
       Sunshine < 6.2
## RainTomorrow is 0.25 when
       Humidity3pm is 58 to 67
##
##
       WindGustSpeed >= 26
##
       Cloud3pm >= 5.1
       Humidity9am is 57 to 63
##
```

```
Evaporation >= 0.9
##
##
       Pressure9am >= 1016
       Pressure3pm >= 1014
##
##
## RainTomorrow is 0.25 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed >= 26
       Cloud3pm >= 5.1
##
##
       Sunshine < 3.8
##
       Humidity9am >= 57
##
       Evaporation >= 0.9
##
       Pressure3pm < 1014
##
       Temp3pm >= 27
##
##
  RainTomorrow is 0.25 when
##
       Humidity3pm is 67 to 73
##
       WindGustSpeed is 20 to 26
##
       Sunshine >= 6.2
##
       Temp3pm >= 22
##
## RainTomorrow is 0.26 when
##
       Humidity3pm is 67 to 73
##
       WindGustSpeed is 20 to 30
##
       Sunshine < 2.0
       Temp3pm >= 22
##
##
## RainTomorrow is 0.27 when
##
       Humidity3pm is 58 to 58
##
       Cloud9am >= 2.1
##
       TempRange < 9.7
       Sunshine < 10.6
##
##
  RainTomorrow is 0.27 when
##
##
       Humidity3pm is 58 to 67
       WindGustSpeed >= 26
##
       Cloud3pm >= 5.1
##
##
       Humidity9am < 57
##
       Evaporation >= 0.9
##
## RainTomorrow is 0.29 when
##
       Humidity3pm is 53 to 55
       WindGustSpeed >= 26
##
##
       Cloud9am >= 7.0
##
       MinTemp < 23
##
       WindSpeed9am < 7.0
##
  RainTomorrow is 0.31 when
##
##
       Humidity3pm >= 73
       TempRange >= 8.5
##
##
       WindSpeed9am >= 5.9
##
## RainTomorrow is 0.36 when
##
       Humidity3pm < 55
       Cloud9am >= 3.0
##
```

```
##
       MinTemp >= 23
##
       Evaporation >= 7.6
##
## RainTomorrow is 0.38 when
##
       Humidity3pm is 55 to 58
##
       WindGustSpeed >= 20
##
       Cloud9am >= 2.1
       TempRange < 9.7
##
##
       Sunshine < 10.6
##
       Humidity9am < 59
##
## RainTomorrow is 0.62 when
       Humidity3pm is 58 to 67
##
##
       WindGustSpeed < 22
##
       TempRange < 11.1
##
       MinTemp >= 13
##
       Pressure9am < 1023
##
       WindSpeed9am < 3.7
##
## RainTomorrow is 0.70 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed < 22
##
       TempRange < 11.1
##
       MinTemp >= 13
##
       Pressure9am < 1023
##
       WindSpeed9am >= 3.7
##
       Pressure3pm < 1012
##
## RainTomorrow is 0.71 when
##
       Humidity3pm < 55
       Cloud9am >= 7.0
##
##
       MinTemp < 23
       WindSpeed9am >= 7.0
##
##
       Rainfall >= 13
##
## RainTomorrow is 0.75 when
##
       Humidity3pm is 55 to 58
##
       Cloud9am >= 2.1
       TempRange >= 9.7
##
##
       Pressure9am < 1013
##
## RainTomorrow is 0.80 when
##
       Humidity3pm is 67 to 73
##
       WindGustSpeed is 20 to 26
##
       Sunshine is 2.0 to 6.2
##
       Temp3pm >= 22
##
## RainTomorrow is 0.87 when
       Humidity3pm is 58 to 67
##
##
       WindGustSpeed >= 26
##
       Cloud9am < 2.8
##
       Cloud3pm < 5.1
##
       Humidity9am < 67
##
       Season is autumn or summer
```

```
##
## RainTomorrow is 0.88 when
       Humidity3pm is 55 to 57
##
##
       Cloud9am >= 2.1
       TempRange >= 9.7
##
##
       Humidity9am >= 62
       Pressure9am >= 1013
##
##
## RainTomorrow is 0.89 when
##
       Humidity3pm < 53
##
       WindGustSpeed >= 26
##
       Cloud9am >= 7.0
##
       MinTemp < 23
##
       WindSpeed9am < 7.0
##
## RainTomorrow is 0.90 when
##
       Humidity3pm is 58 to 67
       WindGustSpeed is 22 to 26
##
       TempRange < 11.1
##
       Sunshine >= 6.2
##
##
## RainTomorrow is 0.90 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed >= 26
       Cloud9am >= 4.0
##
##
       Cloud3pm < 5.1
##
       Season is spring or winter
##
       WindSpeed3pm < 14
##
## RainTomorrow is 0.91 when
       Humidity3pm is 55 to 58
##
##
       WindGustSpeed >= 20
##
       Cloud9am >= 2.1
##
       TempRange < 9.7
       Sunshine < 10.6
##
       Humidity9am >= 59
##
##
## RainTomorrow is 0.91 when
       Humidity3pm is 58 to 67
##
       WindGustSpeed >= 26
##
##
       Cloud3pm < 5.1
       Humidity9am >= 67
##
##
       Season is autumn or summer
##
## RainTomorrow is 0.92 when
       Humidity3pm >= 73
##
##
       TempRange >= 8.5
##
       WindSpeed9am < 5.9
##
## RainTomorrow is 0.92 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed >= 26
##
       Cloud3pm >= 5.1
       Humidity9am >= 63
##
```

```
##
       Evaporation >= 0.9
##
       Pressure9am >= 1016
       Pressure3pm >= 1014
##
##
## RainTomorrow is 0.92 when
##
       Humidity3pm is 67 to 73
##
       WindGustSpeed >= 30
##
## RainTomorrow is 0.93 when
##
       Humidity3pm is 67 to 73
##
       WindGustSpeed < 30
       Temp3pm < 22
##
##
## RainTomorrow is 0.98 when
##
       Humidity3pm >= 73
##
       TempRange < 8.5
##
## RainTomorrow is 0.98 when
       Humidity3pm is 58 to 67
##
       WindGustSpeed >= 26
##
##
       Cloud3pm >= 5.1
##
       Sunshine >= 3.8
##
       Humidity9am >= 57
##
       Evaporation >= 0.9
##
       Pressure3pm < 1014
##
## RainTomorrow is 1.00 when
##
       Humidity3pm < 55
       Cloud9am is 6.0 to 7.0
##
##
       MinTemp < 23
##
## RainTomorrow is 1.00 when
       Humidity3pm < 55
##
##
       Cloud9am >= 3.0
       MinTemp >= 23
##
##
       Evaporation is 6.1 to 7.6
##
## RainTomorrow is 1.00 when
##
       Humidity3pm < 55
##
       Cloud9am is 2.1 to 3.0
##
## RainTomorrow is 1.00 when
##
       Humidity3pm is 58 to 67
##
       WindGustSpeed < 22
##
       TempRange < 11.1
##
       MinTemp >= 13
##
       Pressure9am >= 1023
##
## RainTomorrow is 1.00 when
       Humidity3pm is 58 to 67
##
##
       WindGustSpeed >= 26
##
       Cloud3pm >= 5.1
##
       Sunshine < 3.8
       Humidity9am >= 57
##
```

```
##
       Evaporation >= 0.9
##
       Pressure3pm < 1014
       Temp3pm < 27
##
##
## RainTomorrow is 1.00 when
       Humidity3pm is 67 to 73
##
##
       WindGustSpeed is 26 to 30
       Sunshine >= 2.0
##
##
       Temp3pm >= 22
```

The tree using balanced training data with the second set of variables identified more variables with importance greater than 1% than the tree using the first set of variables, and they are also in a different order, however Humidity3pm is still the most important variable. All of the temperature variables have importance greater than 1% and Rainfall has importance of 1%.

```
#Checking important variables
importanceBal2 <- treeBal2$variable.importance
importanceBal2 <- round(100*importanceBal2/sum(importanceBal2), 1)
importanceBal2[importanceBal2 >= 1]
```

##	Humidity3pm	Sunshine	Cloud9am	TempRange	Cloud3pm
##	20.3	13.1	11.7	11.7	11.2
##	Humidity9am	${\tt WindGustSpeed}$	${\tt MinTemp}$	Temp9am	Pressure9am
##	11.0	3.1	2.3	1.9	1.8
##	WindSpeed3pm	${\tt MaxTemp}$	Evaporation	Temp3pm	Pressure3pm
##	1.7	1.6	1.6	1.6	1.4
##	WindSpeed9am	Season	Rainfall		
##	1.4	1.1	1.0		

The model using the second set of variables performs slightly better than the model created with the first set when evaluating the predictions on the same set of training data. This indicates that the rpart algorithm did a good job of choosing the important variables to use in the model.

Accuracy improves from 86.2% to 89.6%. Sensitivity improves from 78.2% to 79.8%. Specificity improves from 89% to 93%. Balanced accuracy improves from 83.6% to 86.4%

```
#Evaluation of second model using Training Set
#Confusion matrix-train
pred_trainBal2 <- predict(treeBal2, train2, type = 'class') # using unbalanced train data
#Make sure to state positive class in the confusion matrix.
confusionMatrix(pred_trainBal2, train2$RainTomorrow, positive="Yes")</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction No Yes
##
          No 989 74
##
          Yes 75 293
##
##
                  Accuracy : 0.8959
                    95% CI: (0.8789, 0.9112)
##
       No Information Rate: 0.7435
##
##
       P-Value [Acc > NIR] : <2e-16
##
##
                     Kappa: 0.7272
##
##
   Mcnemar's Test P-Value : 1
```

```
##
##
               Sensitivity: 0.7984
               Specificity: 0.9295
##
            Pos Pred Value: 0.7962
##
##
            Neg Pred Value: 0.9304
##
                Prevalence: 0.2565
##
            Detection Rate: 0.2048
##
      Detection Prevalence: 0.2572
##
         Balanced Accuracy: 0.8639
##
##
          'Positive' Class : Yes
##
```

Again we will leave the default of 50% probability to make the prediction, because when lowering the probability to 30%, the model performs slightly worse.

```
#Train Set Evaluation with probabilities
#Confusion matrix-train
pred_trainBal2_prob <- predict(treeBal2, train2, type = 'prob') # using train data</pre>
# predict rain if chance of rain is more than 30% (default is 50%)
pred_trainBal2_prob30 <- ifelse(pred_trainBal2_prob[,2]>0.3,"Yes","No")
confusionMatrix(data= as.factor(pred_trainBal2_prob30), train2$RainTomorrow, positive="Yes")
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction No Yes
##
          No 966
          Yes 98 300
##
##
##
                  Accuracy : 0.8847
##
                    95% CI: (0.867, 0.9008)
##
       No Information Rate: 0.7435
       P-Value [Acc > NIR] : < 2e-16
##
##
##
                     Kappa: 0.7058
##
##
   Mcnemar's Test P-Value: 0.01952
##
##
               Sensitivity: 0.8174
               Specificity: 0.9079
##
##
            Pos Pred Value: 0.7538
##
            Neg Pred Value: 0.9351
##
                Prevalence: 0.2565
##
            Detection Rate: 0.2096
      Detection Prevalence: 0.2781
##
##
         Balanced Accuracy: 0.8627
##
##
          'Positive' Class : Yes
##
```

Both balanced models with the two different sets of variables performed similarly when evaluated with the test data set. Accuracy decreased from 80% to 79% and Balanced Accuracy decreased from 80% to 75%. The sensitivity of the first model was better, with 80% compared to the second model's 69%, but the specificity was a little higher with the second model at 82% compare to 80%.

```
#Test Set Evaluation of Balanced Model 2
\#Confusion\ matrix-test
pred_testBal2 <- predict(treeBal2, test2, type = 'class') # using testing data</pre>
confusionMatrix(pred_testBal2, test2$RainTomorrow, positive="Yes")
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction No Yes
##
          No 231 26
##
          Yes 51 58
##
##
                  Accuracy : 0.7896
                    95% CI : (0.7442, 0.8303)
##
##
       No Information Rate: 0.7705
       P-Value [Acc > NIR] : 0.210684
##
##
##
                     Kappa: 0.4614
##
   Mcnemar's Test P-Value: 0.006237
##
##
               Sensitivity: 0.6905
##
##
               Specificity: 0.8191
##
            Pos Pred Value: 0.5321
##
            Neg Pred Value: 0.8988
##
                Prevalence: 0.2295
##
            Detection Rate: 0.1585
##
      Detection Prevalence: 0.2978
##
         Balanced Accuracy: 0.7548
##
##
          'Positive' Class : Yes
```

Balanced Model 1 performs better with the test data and should be the model that is implemented.

##