

## 1.1

Determine how many times the output statement is displayed in each of the following fragments. Indicate whether the algorithm is  $O(n)$  or  $O(n^2)$ .

- ```
for (int i = 0; i < n; i++)
    for (int j = 0; j < n; j++)
        System.out.println(i + " " + j);
```
- ```
for (int i = 0; i < n; i++)
    for (int j = 0; j < 2; j++)
        System.out.println(i + " " + j);
```
- ```
for (int i = 0; i < n; i++)
    for (int j = n - 1; j >= i; j--)
        System.out.println(i + " " + j);
```
- ```
for (int i = 1; i < n; i++)
    for (int j = 0; j < i; j++)
        if (j % i == 0)
            System.out.println(i + " " + j);
```

- $n^2$                        $O(n^2)$
- $2n$                            $O(n)$
- $n(n-1)/2$                    $O(n^2)$
- $n-1$                          $O(n)$

## 1.3

How does the performance grow as  $n$  goes from 2000 to 4000 for the following? Answer the same question as  $n$  goes from 4000 to 8000. Provide tables similar to Table 2.4.

- $O(\log n)$
- $O(n)$
- $O(n \log n)$
- $O(n^2)$
- $O(n^3)$

$O(f(n))$	$f(2000)$	$f(4000)$	$f(8000)/f(4000)$
$O(\log n)$	10.97	11.97	1.09
$O(n)$	2000	4000	2
$O(n \log n)$	21932	47863	2.18
$O(n^2)$	4000000	16000000	4
$O(n^3)$	$8 \times 10^9$	$6.4 \times 10^{10}$	8

$O(f(n))$	$f(4000)$	$f(8000)$	$f(16000)/f(8000)$
$O(\log n)$	11.97	12.97	1.08
$O(n)$	4000	8000	2
$O(n \log n)$	47863	103726	2.17
$O(n^2)$	16000000	64000000	4
$O(n^3)$	$6.4 \times 10^{10}$	$5.12 \times 10^{11}$	8

## 2.1