

Rho-calculus Constructions

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1 Workpaper week 10

The notation of the ρ -Calculus.[?]

$P, Q ::= \mathbf{0}$ Nil

$|x(y).P$ Input

$|x\langle P \rangle$ Lift

$|^{\neg}x^{\neg}$ Drop

$|P|Q$ Parallel

$x, y ::= \ulcorner P \urcorner$ Quot

1.1 Numbers

This example could be a way of expressing numbers in ρ - Calculus. Where the number takes place as x or y in the notation. By quoting the last number you get a higher number, and by dropping a number you get a lower number, and at 0 you get the process P .

$0 : \ulcorner \mathbf{0} \urcorner$

$1 : \ulcorner \ulcorner \mathbf{0} \urcorner \langle \mathbf{0} \rangle \urcorner$

$2 : \ulcorner \ulcorner \mathbf{0} \urcorner \langle \ulcorner \mathbf{0} \urcorner \langle \mathbf{0} \rangle \rangle \urcorner$

$3 : \ulcorner \ulcorner \mathbf{0} \urcorner \langle \ulcorner \mathbf{0} \urcorner \langle \ulcorner \mathbf{0} \urcorner \langle \mathbf{0} \rangle \rangle \rangle \urcorner$

$4 : \ulcorner \ulcorner \mathbf{0} \urcorner \langle \ulcorner \mathbf{0} \urcorner \langle \ulcorner \mathbf{0} \urcorner \langle \ulcorner \mathbf{0} \urcorner \langle \mathbf{0} \rangle \rangle \rangle \rangle \urcorner$

1.2 Structure

We can express some of the programming terms in ρ -Calculus, but more has to be discovered.

if $a == b$ then P Can be express in ρ -Calculus as: $a\langle \mathbf{0} \rangle |b(x).P$

We send $\mathbf{0}$ on channel a and if channel a and channel b is equal then channel

b will get a $\mathbf{0}$ and execute P .

$P + Q$ Can be express in ρ -Calculus as: $a\langle 0 \rangle \mid a(x).P \mid a(x).Q$

We can make a deterministic choice between P and Q by sending $\mathbf{0}$ on channel a and in parallel two channel a tries both to receive, but only one would succeed and would run its process P or process Q .

1.3 Yet to be solved

We need to express more programming structures, before we can use the ρ -Calculus to model a blockchain structure or even r-chain. These are a few examples of what we need to express, and more should follow.

- if $a \neq b$ then P
- if $a < b$ then P
- if $a > b$ then P
- if $a == b$ then P else Q