

CS 550
Assignment 5
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Answers 1. 1 $AB \rightarrow C$ No

2 $A \rightarrow B$ Yes

3 $C \rightarrow A$ No

4 $BC \rightarrow A$ No

5 $ABC \rightarrow A$ No

6 $AB \rightarrow AC$ No

Answers 2. 1. Cover of F

$$F = \{B \rightarrow A, A \rightarrow C\}$$

Let G be cover of F

$\therefore G = \{\text{all of FD's logically implied}\}$

(i) $B \rightarrow C$ - Transitivity

(ii) $AB \rightarrow C$ - Transitivity covered by (i)

add (i) to G

$$\therefore G = \{B \rightarrow C\}$$

2.2. Non-empty instance of R

A	B	C
1	1	2
1	2	2

2.3 Above table does not satisfy $A \rightarrow B$
but satisfies every FD in F

2.4. No. $AB \rightarrow C$ is logically implied by
the FD's in F

$$\therefore A \rightarrow C \text{ and } B \rightarrow A$$

which gives $AB \rightarrow C$ after using
pseudo transitivity

Answer 3

$$F = \{B \rightarrow CE, E \rightarrow D, E \rightarrow CD, B \rightarrow CE, B \rightarrow A\}$$
$$G = \{E \rightarrow CD, B \rightarrow AE\}$$

Yes they are equivalent. Below is the explanation:

For FD's in F:

$$B \rightarrow CE \text{ \& } B \rightarrow A$$
$$\Rightarrow B \rightarrow ACE$$
$$\Rightarrow B \rightarrow AE$$

$$\cancel{B \rightarrow CE} \text{ \& } E \rightarrow D$$
$$\Rightarrow \cancel{B \rightarrow} E \rightarrow CD \text{ (directly given)}$$

For FD's in G:

$$E \rightarrow CD$$
$$\Rightarrow E \rightarrow C \quad \text{--- (i)}$$
$$\Rightarrow E \rightarrow D \quad \text{--- (ii)}$$

$$B \rightarrow AE$$
$$\Rightarrow B \rightarrow A \quad \text{--- (iii)}$$
$$\Rightarrow B \rightarrow E \quad \text{--- (iv)}$$

$$\Rightarrow B \rightarrow C \quad (\text{by (i) \& iv}) \quad \text{--- (V)}$$

$$\Rightarrow B \rightarrow CE \quad (\text{by (V) \& iv})$$

$$E \rightarrow D \quad (\text{directly given})$$

$$E \rightarrow CD \quad (\text{directly given})$$

$$B \rightarrow CE \quad (\text{proved})$$

$$B \rightarrow A \quad (\text{by (iii) decomposition})$$

Hence proved.

Answer 4 1. No, R is not in BCNF.

We know A is not super key since it does not appear LHS of any other FD other than $A \rightarrow DE$. $A \rightarrow DE$ must be trivial for R to be in ~~BA~~ BCNF, but it is not.

And $A \rightarrow DE$ where A is not a ~~sp~~ super key and it does not determine anything but D and E. Hence R is not in BCNF.

4.2. No, R is not in 3NF.

Proof:

If it were in 3NF, then all FD's in F are trivial, or LHS has to be superkey, or RHS must be part of a key.

As $A \rightarrow DE$ does not satisfy any of the options above & DE is not part of a key since only IJ is the key. Therefore R is not in 3NF.

Answer 5. 1. We see that E is a superkey and so C is also a superkey as $C \rightarrow E$ & D is also a superkey as $D \rightarrow BC$ we have

$D \rightarrow C$ and A is a superkey as $A \rightarrow D$.

Therefore B is a superkey as $B \rightarrow A$.

LHS of every FD is superkey. Therefore R is in 1NF BCNF.

5.2. S & T are lossless join decomposition of R
 if $CDE \cap BAD = D$ determines all
 attributes in S or T for every instance in R .
 By $D \rightarrow BC$ and $C \rightarrow E$
 we have $D \rightarrow CDE$

D is a superkey and shows that it is
 lossless decomposition.

5.3. $F_{CDE}^+ = \{$

- $C \rightarrow D, (C \rightarrow E \ \& \ E \rightarrow D)$
- $C \rightarrow E,$
- $D \rightarrow C, (D \rightarrow BC)$
- $D \rightarrow E, (D \rightarrow C \ \& \ E \rightarrow E)$
- $E \rightarrow C, (E \rightarrow D \ \& \ D \rightarrow C)$
- $E \rightarrow D,$
- $C \rightarrow CE,$
- $D \rightarrow CD,$
- $E \rightarrow ED,$
- $CE \rightarrow D,$
- $CD \rightarrow E,$
- $DE \rightarrow C \}$

5.4. $F_{ABD}^+ = \{$

- $A \rightarrow B,$
- $A \rightarrow D,$
- $B \rightarrow A,$
- $B \rightarrow D,$
- $D \rightarrow A,$
- $D \rightarrow B,$
- $A \rightarrow BD,$
- $B \rightarrow AD,$
- $D \rightarrow AB,$
- $AD \rightarrow B,$
- $AD \rightarrow D,$
- $BD \rightarrow A\}$

5.5. Yes. ~~We observe that~~ The decomposition of R into S and T is dependency-preserving if $(F_{CDE} \cup F_{ABD})^+ = F^+$.

We see that FD's in F imply that all attributes all attributes of i.e F^+ contains all possible FD's over ABCDE.

We already saw ~~D~~ all attributes determine D & vice versa.

Therefore all attributes determine all attributes

Answers- 1

A never appear on LHS, any key must have A. Similarly D never appear on LHS & determined by B. D will never be in candidate key.

If we add B ~~to A~~ we have
 $AB \rightarrow CEF$ & $B \rightarrow D$. Hence AB is candidate key.

If we add C, we have $AC \rightarrow F$
we add E, we get $ACE \rightarrow B$ and by
 $B \rightarrow D$. Therefore we have ACE as candidate key.

If we add F, $AEF \rightarrow BC$ & thus all attributes are determined. AEF is also candidate key.

So we have candidate keys as
 AB, ACE, AEF

6.2 No, The FD $B \rightarrow D$ holds for R , but is not trivial.

Also B is not superkey & D is not part of a key

6.3 No, same reason as for 6.2

6.4 $FE \rightarrow B$

$AC \rightarrow F$

$AC \rightarrow D$

$AB \rightarrow C$