

CS573 Assignment 1

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Problem 1

Sub-problem a

1. Solution:

$$\begin{aligned} &P(\text{second card is heart}|\text{first card is heart}) \\ &= P(\text{second card is heart}) \text{ (as probability of drawing second card is independent of first card being a heart)} = \frac{12}{51} \end{aligned}$$

2. Solution:

$$\begin{aligned} &P(\text{none of the cards are hearts}|\text{atmost one card is heart}) = \\ &\frac{P(\text{none of the cards are hearts, atmost one card is heart})}{P(\text{atmost one card is heart})} \\ &P(\text{none of the cards are hearts, atmost one card is heart}) = P(\text{none of the cards are hearts}) \\ &P(\text{none of the cards are hearts}) = \frac{39}{52} \\ &P(\text{atmost one card is heart}) = 1 - P(\text{atleast one card is heart}) \\ &P(\text{atleast one card is heart}) = \frac{1}{13} \\ &P(\text{atmost one card is heart}) = 1 - \frac{1}{13} = \frac{12}{13} \\ &P(\text{none of the cards are hearts}|\text{atmost one card is heart}) = \frac{\frac{39}{52}}{\frac{12}{13}} = \frac{3}{4} \end{aligned}$$

Sub-problem b

1. Solution:

$$\begin{aligned} &P(\text{card drawn from second deck is ace}) = \\ &P(\text{card drawn from first deck is ace}) + P(\text{card drawn from first deck is not ace}) \\ &= \frac{48}{52} \times \frac{4}{53} + \frac{4}{52} \times \frac{5}{53} = 0.0769 \end{aligned}$$

2. Solution:

$$\begin{aligned} &P(\text{card drawn from second deck is ace}) = \\ &P(\text{card drawn from first deck is ace}) + P(\text{card drawn from first deck is not ace}) \\ &= \frac{48}{52} \times \frac{4}{55} + \frac{4}{52} \times \frac{5}{55} = 0.0741 \end{aligned}$$

3. Solution:

$$\begin{aligned} &P(\text{ace was transferred from first deck}|\text{ace was drawn from second deck}) \\ &= \frac{P(\text{ace was transferred from first deck, ace was drawn from second deck})}{P(\text{ace was drawn from second deck})} \\ &P(\text{ace was transferred from first deck, ace was drawn from second deck}) = \frac{4}{52} \times \frac{5}{55} \\ &P(\text{ace was drawn from second deck}) = \frac{48}{52} \times \frac{4}{55} + \frac{4}{52} \times \frac{5}{55} \\ &\text{(We have calculated the probability of drawing an ace from the second deck in the previous problem b.2)} \end{aligned}$$

$$\begin{aligned} &P(\text{ace was transferred from first deck}|\text{ace was drawn from second deck}) \\ &= \frac{\frac{4}{52} \times \frac{5}{55}}{\frac{48}{52} \times \frac{4}{55} + \frac{4}{52} \times \frac{5}{55}} = 0.094 \end{aligned}$$