# Mathematics in the Modern World

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## Course syllabus:

### Prelim

- Mathematics in our World (Patterns and Sequence)
- Mathematical Language and Symbols (Language of Math, Language of Functions, Language of Sets, Unary and Binary Operations, Logic)
- Problem Solving and Reasoning

## $\mathbf{Midterm}$

- Mathematics as a Tool Data Gathering
- Measures of Central Tendency
- Measures of Variability
- Measures of Position
- Correlation
- Hypothesis Testing

### **Finals**

- Right Triangle Trigonometry
- Codes (Cryptography)
- Tautologies and Fallacies
- Nature of Financial Management

## Prelim

## L-2 - Patterns

• Visible regularity in world or man-made design.

## G. H. Hardy

- British mathematician.
- Characterized mathematics as the study of patterns.

## Logic Patterns

- Deals with characteristics of similar attribute with the following various:
  - objects (eg: shapes)
  - order (eg: placement)
  - sequence (eg: array)

#### Geometric Patterns

- Deals with a motif or design typically repeating like a wallpaper that depicts the following:
  - shapes,
  - lines,
  - polygons,
    - \* circles.

### Word Patterns

- Deals with metrical patterns of poems and syntatic patterns of how we make:
  - noun plurality,
  - past tense of verbs,
  - also supports mathematics,
  - also supports natural language understanding.
- Examples:
  - Letter jumbling (cryptography)
    - \* Encryption: making the message not readable but keeps the meaning.
    - \* Decryption: process of finding the meaning of the encrypted message.
  - Word associations

#### **Number Patterns**

- Deals with predition of the next term in a sequence.
- Leads directly to the concept of functions in mathematics.
  - Functions are formal descriptions of the relationships among different quantities

## L-2-A Fibonacci Sequence

## Leonardo of Pisa

- Also known as:
  - Leonardo Bigollo Pisano (Leonardo, traveller of Pisa),
  - Leonardo Bonacci,
  - Leonardo Fibonacci.
- European Mathematician.
  - Italian, from the Republic of Pisa.
- **Date** lived: 1175-1250
- Discovered the Fibonacci Sequence from:
  - how fast **rabbits breed** under ideal circumstances.

## Fibonacci Sequence

• Series of numbers where the next term is found by adding the two previous terms

1 <sup>st</sup> -	2 <sup>nd</sup> - term	3 <sup>rd</sup> - term	4 <sup>th</sup> - term	5 <sup>th</sup> - term	6 <sup>th</sup> - term	7 <sup>th</sup> - term	8 <sup>th</sup> - term	9 <sup>th</sup> - term	10 <sup>th</sup> - term
1	1	2	3	5	8	13	21	34	55
11 <sup>st</sup> -	12 <sup>nd</sup> -	13 <sup>rd</sup> -	14 <sup>th</sup> -	15 <sup>th</sup> -	16 <sup>th</sup> -	17 <sup>th</sup> -	18 <sup>th</sup> -	19 <sup>th</sup> -	20 <sup>th</sup> -
$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$
89	144	233	377	610	987	1,597	2,584	4,181	6,765
21 <sup>st</sup> -	22 <sup>nd</sup> -	23 <sup>rd</sup> -	24 <sup>th</sup> -	25 <sup>th</sup> -	26 <sup>th</sup> -	27 <sup>th</sup> -	28 <sup>th</sup> -	29 <sup>th</sup> -	30 <sup>th</sup> -
$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$
10,946	17,711	28,657	46,368	75,025	121,393	196,418	317,811	514,229	832,040

31 <sup>st</sup> term	$32^{\rm nd}$ term	$33^{\rm rd}$ term	$34^{\rm th}$ term	$35^{\rm th}~{\rm term}$
1,346,269	1,346,269	3,524,578	5,702,887	9,227,465

36 <sup>th</sup> term	$37^{\rm th}~{\rm term}$	$38^{\rm th}~{\rm term}$	$39^{\rm th}~{\rm term}$	40 <sup>th</sup> term
14,930,352	24,157,817	39,088,169	63,245,986	102,334,155

$41^{\rm st}$ term	$42^{\rm nd}$ term	$43^{\rm rd}$ term	$44^{\rm th}~{\rm term}$	$45^{\rm th}$ term
165,580,141	267,914,296	433,494,437	701,408,733	1,134,903,170

46 <sup>th</sup> term	47 <sup>th</sup> term	48 <sup>th</sup> term	49 <sup>th</sup> term	50 <sup>th</sup> term
1,836,311,903	2,971,215,073	4,807,526,976	7,778,742,049	12,586,269,025

## Fibonacci Rule

 $x_{n} = x_{n\text{-}1} + x_{n\text{-}2}$ 

Where:

 $\boldsymbol{x}_n$  is the term number "n"

 $\mathbf{x}_{\mathbf{n}\text{-}\mathbf{1}}$  is the previous term "n-1"

 $\mathbf{x}_{\text{n-2}}$  is the previous 2 terms "n-2"

L-2-B Lucas Number

1 <sup>st</sup> - term	2 <sup>nd</sup> - term	3 <sup>rd</sup> - term	4 <sup>th</sup> - term	5 <sup>th</sup> - term	6 <sup>th</sup> - term	7 <sup>th</sup> - term	8 <sup>th</sup> - term	9 <sup>th</sup> - term	10 <sup>th</sup> - term
2	1	3	4	7	11	18	29	76	123
11 <sup>st</sup> -	12 <sup>nd</sup> -	13 <sup>rd</sup> -	14 <sup>th</sup> -	15 <sup>th</sup> -	16 <sup>th</sup> -	17 <sup>th</sup> -	18 <sup>th</sup> -	19 <sup>th</sup> -	20 <sup>th</sup> -
term	$\operatorname{term}$	$\operatorname{term}$	$\operatorname{term}$	term	term	$\operatorname{term}$	$\operatorname{term}$	term	term
199	322	521	843	1,364	2,207	3,571	5,778	9,349	15,127
21 <sup>st</sup> -	22 <sup>nd</sup> -	$23^{\mathrm{rd}}$ -	$24^{ m th}$ -	$25^{ m th}$ -	26 <sup>th</sup> -	27 <sup>th</sup> -	28 <sup>th</sup> -	$29^{\mathrm{th}}$ -	30 <sup>th</sup> -
$\operatorname{term}$									
24,476	39,603	64,079	103,682	167,761	271,443	439,204	710,647	1,149,851	1,860,498

$\overline{31^{\rm st}}$ term	32 <sup>nd</sup> term	$33^{\rm rd}$ term	$34^{\rm th}$ term	35 <sup>th</sup> term
3,010,349	4,870,847	7,881,196	12,752,043	20,633,239

36 <sup>th</sup> term	$37^{\rm th}~{\rm term}$	$38^{\rm th}$ term	$39^{\mathrm{th}}$ term	40 <sup>th</sup> term
33,385,282	54,018,521	87,403,803	141,422,324	228,826,127

41 <sup>st</sup> term	42 <sup>nd</sup> term	$43^{\rm rd}$ term	44 <sup>th</sup> term	45 <sup>th</sup> term
370,248,451	599,074,578	969,323,029	1,568,397,607	2,537,720,636

$46^{\rm th}$ term $47^{\rm th}$ term		$48^{\rm th}$ term	$49^{\rm th}~{\rm term}$	$50^{\rm th}~{\rm term}$
4,106,118,243	6,643,838,879	10,749,957,122	17,393,796,001	28,143,753,123

## 8-22 ...

### a. ...

There are three parts to this solution.

- 1. write the equations to solve the problem in R-readable strings.
- 2. loop over the list and eval(parse()) the equation strings
- 3. wrap strings in \$\$ \$\$ with cat(paste0())

Chunks should be set to echo=FALSE and results="asis. You may need to suppress some function output with invisible().