

Check Your Gap or Get Scrapped

An Investigation of a Car Following Model

Kaeshav Danesh Kevin Phan

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Table of Contents

1 Introduction

2 Model

3 Implementation

4 Examining Scenarios

- Homogeneous Traffic
- Obstacle
- Multi-lane Bottleneck

Table of Contents

1 Introduction

2 Model

3 Implementation

4 Examining Scenarios

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- Obstacle
- Multi-lane Bottleneck

Introduction

- Traffic flow theory deals with modeling vehicular flow.
- Focus on microscopic model which model cars as a single unit.
- Goal: Model and examine
 - ① Homogeneous traffic
 - ② Obstacles on a road
 - ③ Multi-lane bottleneck

Table of Contents

1 Introduction

2 Model

3 Implementation

4 Examining Scenarios

- Homogeneous Traffic
- Obstacle
- Multi-lane Bottleneck

Introducing variables

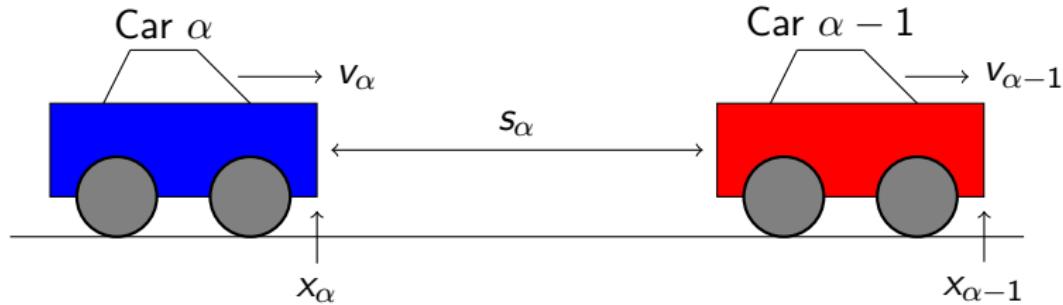


Figure 1: Defining index, position, velocity, and gap of a car.

- x_α , position of α th car.
- v_α , velocity of α th car.
- a_α , acceleration of α th car.
- s_α , gap of α th car.
- Will denote the car $\alpha - 1$ by car l .

Coupled Differential Equations

$$\begin{aligned}\frac{dx_\alpha(t)}{dt} &= v_\alpha(t), \\ \frac{dv_\alpha(t)}{dt} &= a_{\text{mic}}(s_\alpha, v_\alpha, v_I).\end{aligned}$$

Each car following model has a specific acceleration function:
 $a_{\text{mic}}(s_\alpha, v_\alpha, v_I)$.

Full Velocity Difference Model

$$a_{\text{mic}}(s_\alpha, v_\alpha, v_l) = \frac{v_{\text{opt}}(s) - v_\alpha}{\tau} - \gamma \Delta v,$$
$$v_{\text{opt}}(s) = \max \left(0, \min \left(v_0, \frac{s - s_0}{T} \right) \right).$$

v_0 desired speed

s_0 minimum distance gap

T time gap

τ speed adaptation time

γ speed difference sensitivity

Optimal Velocity Function

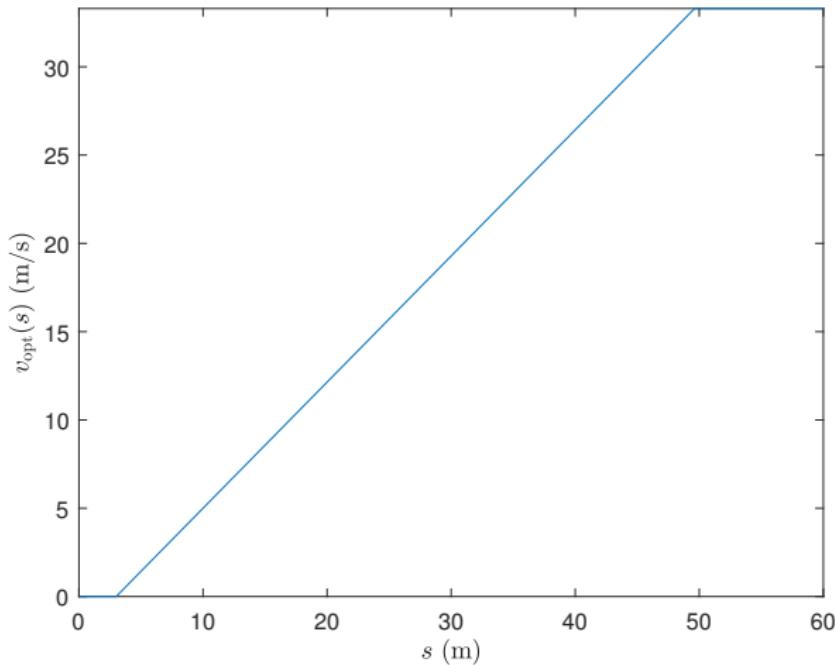


Figure 2: Graph of the optimal velocity function over a range of gaps.

Table of Contents

1 Introduction

2 Model

3 Implementation

4 Examining Scenarios

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Forwards Euler Method Scheme

During lane changes, the acceleration function is not continuous, so Euler's Method would be the most stable:

$$v_\alpha(t + \Delta t) = v_\alpha(t) + a_{\text{mic}}(s_\alpha(t), v_\alpha(t), v_l(t))\Delta t,$$
$$x_\alpha(t + \Delta t) = x_\alpha(t) + \frac{v_\alpha(t) + v_\alpha(t + \Delta t)}{2}\Delta t.$$

Lane Changes

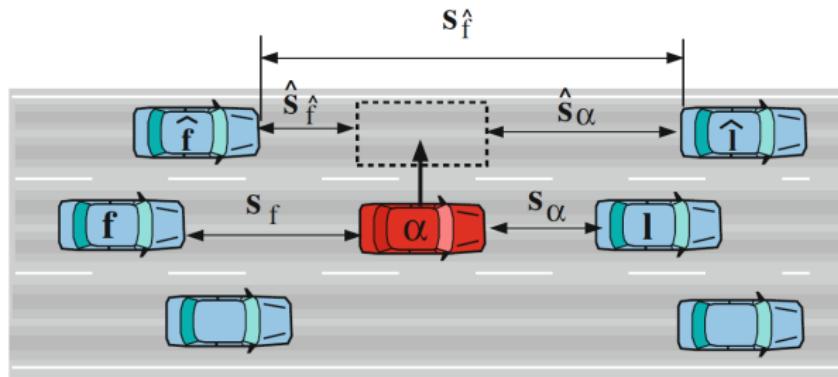


Figure 3: Multi-lane notation. From Treiber and Kesting *Traffic Flow Dynamics*

Define minimum $\hat{s}_{\hat{f}}$ and \hat{s}_α needed to change lanes:

$$s_{\text{safe}}(v_{\hat{f}}, v_\alpha) = v_{\text{opt}}^{-1} [v_{\hat{f}} - \tau b_{\text{safe}} + \tau \gamma (v_{\hat{f}} - v_\alpha)],$$

$$s_{\text{adv}} = s_\alpha + v_{\text{opt}}^{-1} [\tau (\Delta a + a_{\text{bias}} + \gamma (v_I - v_{\hat{f}}))].$$

Pseudocode for FVDM

Algorithm 1 Simplified algorithm for FDVM with lane changes

Require: Initial state variables for each car at $t = 0$.

Require: carArr, an array of cars.

```
for i = 1 :numsteps do
    for j = length(carArr):-1:1 do
        State variables of jth car  $\leftarrow$  Update jth car by a timestep.
        New lane of jth car  $\leftarrow$  carArr(j).changeLane()
    end for
    sort(carArr)
end for
```

Table of Contents

1 Introduction

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3 Implementation

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- Obstacle
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Homogeneous Traffic

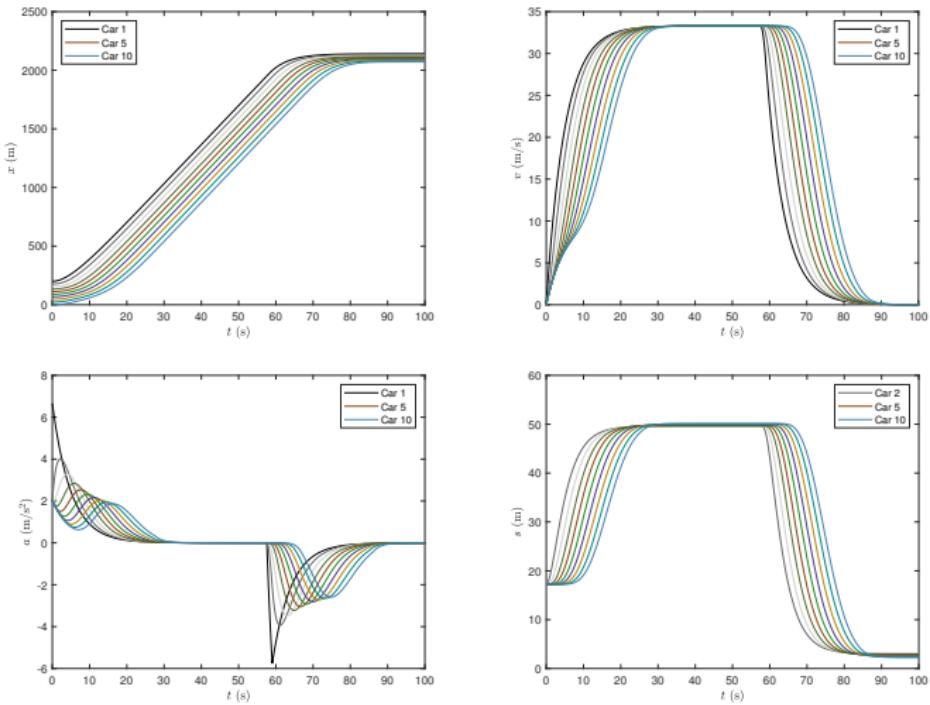


Figure 4: Position, velocity, acceleration, and gap versus time

Obstacle

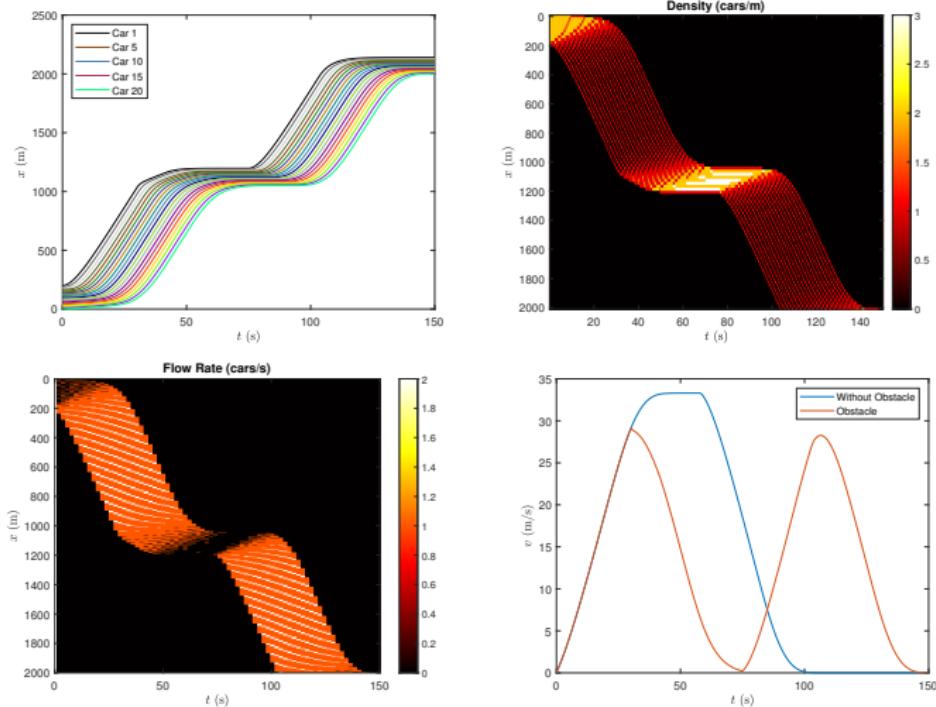


Figure 5: Position versus time graph.

Multi-lane Bottleneck

Conclusion