## Assignment 3: Predicting insurance charges by age and BMI

## Your name and student ID

July 14, 2022

#### Run this chunk of code to load the autograder package!

#### Instructions

- Solutions will be released Friday, July 15th.
- This semester, homework assignments are for practice only and will not be turned in for marks.

#### Helpful hints:

- Every function you need to use was taught during lecture! So you may need to revisit the lecture code to help you along by opening the relevant files on Datahub. Alternatively, you may wish to view the code in the condensed PDFs posted on the course website. Good luck!
- Knit your file early and often to minimize knitting errors! If you copy and paste code for the slides, you are bound to get an error that is hard to diagnose. Typing out the code is the way to smooth knitting! We recommend knitting your file each time after you write a few sentences/add a new code chunk, so you can detect the source of knitting errors more easily. This will save you and the GSIs from frustration! You must knit correctly before submitting.
- It is good practice to not allow your code to run off the page. To avoid this, have a look at your knitted PDF and ensure all the code fits in the file. If it doesn't look right, go back to your .Rmd file and add spaces (new lines) using the return or enter key so that the code runs onto the next line.



## Predicting insurance charges by age and BMI

**Problem:** Medical insurance charges can vary according to the complexity of a procedure or condition that requires medical treatment. You are tasked with determining how these charges are associated with age, for patients who have a body mass index (bmi) in the "normal" range (bmi between 16 and 25) who are smokers.

**Plan**: You have chosen to use tools to examine relationships between two variables to address the problem. In particular, scatter plots and simple linear regression.

Data: You have access to the dataset insurance.csv, a claims dataset from an insurance provider.

**Analysis and Conclusion**: In this assignment you will perform the analysis and make a conclusion to help answer the problem statement.

1. [1 point] Type one line of code to import these data into R. Assign the data to insure\_data. Execute the code by hitting the green arrow and ensure the dataset has been saved by looking at the environment tab and viewing the data set by clicking the table icon to the right of its name.

```
. = " # BEGIN PROMPT
insure_data <- NULL</pre>
insure_data
" # END PROMPT
# BEGIN SOLUTION
insure_data <- read_csv("data/insurance.csv")</pre>
## Rows: 1338 Columns: 7
## -- Column specification -----
## Delimiter: ","
## chr (3): sex, smoker, region
## dbl (4): age, bmi, children, charges
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
# END SOLUTION
. = ottr::check("tests/p1.R")
```

Execute the functions below one line at a time to get to know your dataset.

```
dim(insure_data)
## [1] 1338
              7
names(insure_data)
## [1] "age"
                             "bmi"
                  "sex"
                                        "children" "smoker"
                                                              "region"
                                                                         "charges"
str(insure_data)
## spec_tbl_df [1,338 x 7] (S3: spec_tbl_df/tbl_df/tbl/data.frame)
             : num [1:1338] 19 18 28 33 32 31 46 37 37 60 ...
              : chr [1:1338] "female" "male" "male" "male" ...
## $ sex
              : num [1:1338] 27.9 33.8 33 22.7 28.9 ...
## $ children: num [1:1338] 0 1 3 0 0 0 1 3 2 0 ...
##
   $ smoker : chr [1:1338] "yes" "no" "no" "no" ...
  $ region : chr [1:1338] "southwest" "southeast" "southeast" "northwest" ...
##
   $ charges : num [1:1338] 16885 1726 4449 21984 3867 ...
##
   - attr(*, "spec")=
##
##
     .. cols(
##
         age = col_double(),
##
         sex = col_character(),
##
         bmi = col_double(),
     . .
##
         children = col_double(),
##
         smoker = col_character(),
     . .
         region = col_character(),
##
##
         charges = col_double()
     . .
##
     ..)
   - attr(*, "problems")=<externalptr>
head(insure_data)
## # A tibble: 6 x 7
                   bmi children smoker region
##
       age sex
                                                  charges
                                                    <dbl>
##
     <dbl> <chr> <dbl>
                           <dbl> <chr> <chr>
## 1
       19 female 27.9
                              0 yes
                                        southwest 16885.
## 2
       18 male
                  33.8
                              1 no
                                        southeast
                                                    1726.
## 3
       28 male
                                                    4449.
                  33
                               3 no
                                        southeast
## 4
       33 male
                  22.7
                               0 no
                                        northwest 21984.
## 5
       32 male
                  28.9
                               0 no
                                        northwest
                                                   3867.
## 6
       31 female 25.7
                               0 no
                                        southeast
                                                    3757.
```

2. [1 point] How many individuals are in the dataset? Assign this number to p2.

```
. = " # BEGIN PROMPT
p2 <- NULL
p2
" # END PROMPT

# BEGIN SOLUTION
p2 <- nrow(insure_data)
# END SOLUTION</pre>
```

```
. = ottr::check("tests/p2.R")
```

## All tests passed!

3. [1 point] What are the nominal variables in the dataset? Assign the names of these variables to a vector of strings, p3.

```
. = " # BEGIN PROMPT
p3 <- NULL
p3
" # END PROMPT

# BEGIN SOLUTION
p3 <- c("sex", "smoker", "region")
# END SOLUTION</pre>
```

```
. = ottr::check("tests/p3.R")
```

## All tests passed!

4. [1 point] How many ordinal variables are in the dataset? Assign the *number* of ordinal variables to p4.

```
. = " # BEGIN PROMPT
p4 <- NULL
p4
" # END PROMPT

# BEGIN SOLUTION
p4 <- 0
# END SOLUTION
```

```
. = ottr::check("tests/p4.R")
```

## All tests passed!

5. [1 point] Are there continuous variables in the dataset? Assign the names of these variables to a vector of strings, p5.

```
. = " # BEGIN PROMPT
p5 <- NULL
p5
" # END PROMPT

# BEGIN SOLUTION
p5 <- c("bmi", "charges", "age")
p5 <- c("bmi", "charges") # also accepted
# END SOLUTION</pre>
```

```
. = ottr::check("tests/p5.R")
```

## All tests passed!

6. [1 point] What are the discrete variables in the dataset? Assign the names of these variables to a vector of strings, p6.

```
. = " # BEGIN PROMPT
p6 <- NULL
p6
" # END PROMPT

# BEGIN SOLUTION
p6 <- c("children")
p6 <- c("children", "age") # also accepted
# END SOLUTION</pre>
```

```
. = ottr::check("tests/p6.R")
```

Run the following code. Remind yourself what the mutate() function does in general, and notice that a new function called case\_when() is also being used.

## 7. What did the code above accomplish?

The above code created a new variable called bmi\_cat that created four categories of BMI: underweight, normal, overweight, and obese, based on the continuous variable BMI.

8. [1 point] What type of variable is bmi\_cat? Uncomment one of the choices below.

```
. = " # BEGIN PROMPT
# p8 <- 'ordinal'
# p8 <- 'continuous'
# p8 <- 'discrete'
" # END PROMPT

# BEGIN SOLUTION
p8 <- 'ordinal'
# END SOLUTION
. = ottr::check("tests/p8.R")</pre>
```

9. [1 point] Read the problem statement proposed at the beginning of this exercise. Who belongs to the population of interest? Uncomment one of the choices below.

```
. = " # BEGIN PROMPT
# p9 <- 'Smokers of normal BMI'
# p9 <- 'Smokers of overweight BMI'
# p9 <- 'Smokers who have abnormal BMI'
# p9 <- 'All people at risk of high medical charges'
" # END PROMPT

# BEGIN SOLUTION
p9 <- 'Smokers of normal BMI'
# END SOLUTION
. = ottr::check("tests/p9.R")</pre>
```

## All tests passed!

10. [1 point] Using a dplyr function, make a new dataset called insure\_subset containing the population of interest.

```
. = " # BEGIN PROMPT
insure_subset <- NULL
insure_subset
" # END PROMPT

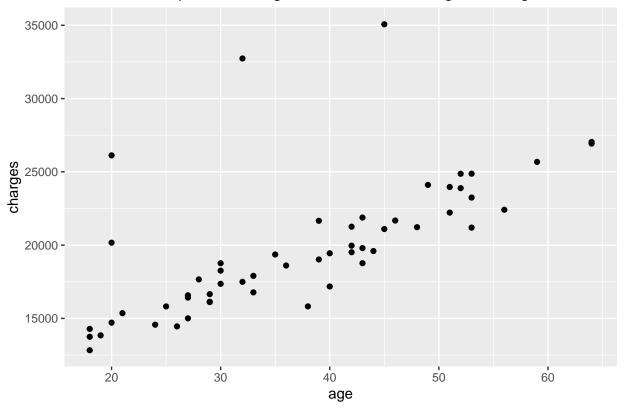
# BEGIN SOLUTION
insure_subset <- insure_data %>% filter(smoker == "yes" & bmi_cat == "Normal")
# END SOLUTION
. = ottr::check("tests/p10.R")
```

11. [3 points] Make a scatter plot of the relationship between age and insurance charges for the population of interest. Give your plot an informative title.

```
. = " # BEGIN PROMPT
p11 <- NULL
p11
" # END PROMPT

# BEGIN SOLUTION
p11 <- ggplot(insure_subset, aes(x = age, y = charges)) +
    geom_point() +
    labs(title = "The relationship between age and insurance charges among smokers of normal BMI")
p11</pre>
```

## The relationship between age and insurance charges among smokers of



## # END SOLUTION

```
. = ottr::check("tests/p11.R")
```

12. [2 points] Run a linear regression model on the relationship between age and charges. Think about which variable is explanatory (X) and which is response (Y). Assign the regression model to the object insure\_mod and uncomment the line of code below the model to tidy the output.

```
. = " # BEGIN PROMPT
insure_model <- NULL</pre>
insure_model
# tidy(insure_model)
" # END PROMPT
# BEGIN SOLUTION
insure_model <- lm(formula = charges ~ age, data = insure_subset)</pre>
tidy(insure model)
## # A tibble: 2 x 5
##
                 estimate std.error statistic
                                                       p.value
     term
                                                         <dbl>
##
     <chr>
                     <dbl>
                               <dbl>
                                          <dbl>
## 1 (Intercept)
                    10656.
                              1471.
                                           7.24 0.00000000184
                      246.
                                           6.58 0.0000000217
## 2 age
                                37.4
# END SOLUTION
. = ottr::check("tests/p12.R")
```

## All tests passed!

13. [1 point] Interpret the slope parameter in the context of this problem.

For every year increase in age, medical charges increase by \$246.14.

14. [1 point] Interpret the intercept parameter.

The model predicts that the insurance charged would be \$10,656.14 for a person of aged 0.

15. [1 point] Does the intercept make sense in this context?

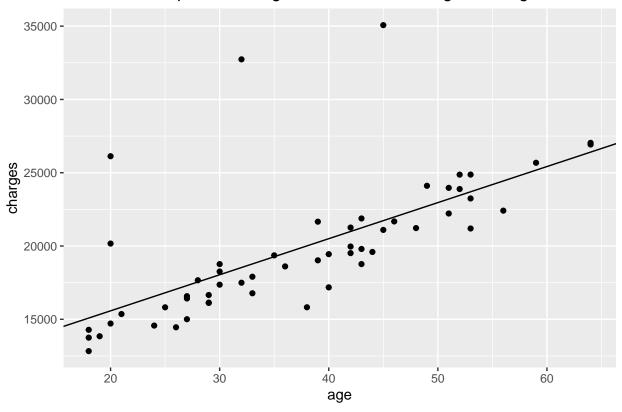
No because being 0 years old is non sensical. Further, the minimum age in the dataset is 18, so extrapolation to 0 is not supported by the data. (student can say either of these items or both.)

16. [1 point] Add the line of best fit to your scatterplot by copying and pasting the plot's code from question 11 in the chunk below and adding a geom that can be used to add a regression line.

```
. = " # BEGIN PROMPT
p16 <- NULL
p16
" # END PROMPT

# BEGIN SOLUTION
p16 <- ggplot(insure_subset, aes(x = age, y = charges)) +
    geom_point() +
    labs(title = "The relationship between age and insurance charges among smokers of normal BMI") +
    geom_abline(intercept = 10656.1, slope = 246.1)
p16</pre>
```

## The relationship between age and insurance charges among smokers of



```
# END SOLUTION
```

```
. = ottr::check("tests/p16.R")
```

# 17. [2 points] What do you notice about the fit of the line in terms of the proportion of points above vs. below the line? Why do you think that is?

The line seems high. There is a large proportion of points below the line. That's because there exists some notable outliers above the line which don't follow the linear trend of the data points.

Run the following filter() function in the chunk below.

```
insure_smaller_subset <- insure_subset %>%
filter(charges < 30000 & ! (charges > 25000 & age == 20))
```

## 18. [2 points] How many individuals were removed? Who were they?

Three individuals were removed. They were the "y outliers", the two people with the highest charges in the dataset and a third person who was 20 years old with a charge > \$25,000.

19. [2 points] Run a regression model on insure\_smaller\_subset between charges and age. Assign the model to insure\_better\_model and analyze the output using the tidy() function.

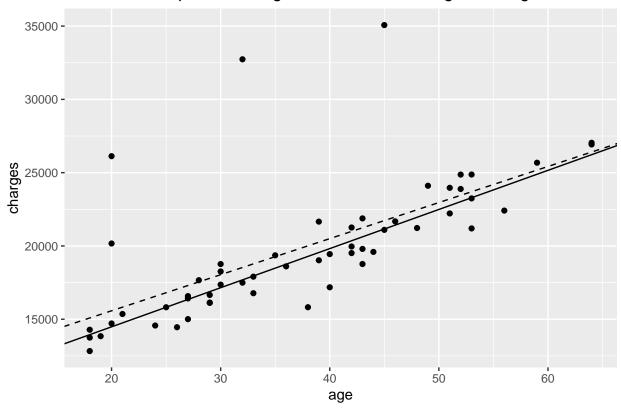
```
. = " # BEGIN PROMPT
insure_better_model <- NULL</pre>
# tidy(insure_better_model)
" # END PROMPT
# BEGIN SOLUTION
insure_better_model <- lm(formula = charges ~ age, data = insure_smaller_subset)</pre>
tidy(insure_better_model)
## # A tibble: 2 x 5
            estimate std.error statistic p.value
##
##
     <chr>
                    <dbl>
                              <dbl>
                                        <dbl>
                                                 <dbl>
                              633.
                                        14.4 1.81e-19
## 1 (Intercept)
                    9144.
                                         16.7 4.44e-22
## 2 age
                     267.
                               16.0
# END SOLUTION
. = ottr::check("tests/p19.R")
```

20. [2 points] Add the new regression line to your ggplot from question 16. Keep the original regression line on the plot for comparison. To distinguish the lines, change the color, line type, or line width of one of the lines.

```
. = " # BEGIN PROMPT
p20 <- NULL # YOUR CODE HERE
p20
" # END PROMPT

# BEGIN SOLUTION
p20 <- ggplot(insure_subset, aes(x = age, y = charges)) +
    geom_point() +
    labs(title = "The relationship between age and insurance charges among smokers of normal BMI") +
    geom_abline(intercept = 10656.1, slope = 246.1, lty = 2) +
    geom_abline(intercept = 9144.1, slope = 266.9)
p20</pre>
```

## The relationship between age and insurance charges among smokers of



```
# END SOLUTION
```

```
. = ottr::check("tests/p20.R")
```

21. [1 point] Calculate the r-squared value for insure\_model and assign this value to insure\_model\_r2.

```
. = " # BEGIN PROMPT
insure_model_r2 <- NULL
insure_model_r2
" # END PROMPT

# BEGIN SOLUTION
insure_model_r2 <- glance(insure_model) %>% pull(r.squared)
# END SOLUTION
```

```
. = ottr::check("tests/p21.R")
```

## All tests passed!

22. [1 point] Calculate the r-squared value for insure\_better\_model using a function learned in class. Assign this value to insure\_better\_model\_r2.

```
. = " # BEGIN PROMPT
insure_better_model_r2 <- NULL
insure_better_model_r2
" # END PROMPT

# BEGIN SOLUTION
insure_better_model_r2 <- glance(insure_better_model) %>% pull(r.squared)
# END SOLUTION
```

```
. = ottr::check("tests/p22.R")
```

23. [2 points] Calculate the correlation coefficient between age and charges using insure\_subset. Also calculate the squared correlation coefficient. You should use summarize() to create a dataframe of these two values and name the two variables corr and corr\_sq, respectively. What do you notice about the relationship between the correlation coefficient and r-squared values that you calculated earlier?

```
. = " # BEGIN PROMPT
p23 <- NULL
p23
" # END PROMPT
# BEGIN SOLUTION
p23 <- insure_subset %>% summarize(corr = cor(age, charges), corr_sq = corr^2)
p23
## # A tibble: 1 x 2
##
      corr corr_sq
##
     <dbl>
             <dbl>
## 1 0.670
             0.449
# END SOLUTION
. = ottr::check("tests/p23.R")
```

## All tests passed!

24. [2 points] Calculate the correlation coefficient between age and charges using the smaller dataset insure\_smaller\_subset. Also calculate the squared correlation coefficient. You should use summarize() to create a dataframe of these two values and name the two variables corr and corr\_sq, respectively. What do you notice about the relationship between the correlation coefficient and r-squared values that you calculated earlier?

```
. = " # BEGIN PROMPT
p24 <- NULL
p24
" # END PROMPT

# BEGIN SOLUTION
p24 <- insure_smaller_subset %>% summarize(corr = cor(age, charges), corr_sq = corr^2)
# END SOLUTION
```

. = ottr::check("tests/p24.R")

Your supervisor asks you to extend your analysis to consider other smokers with BMIs classified as overweight or obese. In particular, she wanted to know if the relationship between age and medical charges is different for different BMI groups. You can use data visualization coupled with your skills in linear regression to help answer this question.

25. [1 point] Make a new dataframe called insure\_smokers that includes smokers of any BMI from the original insure\_data dataset.

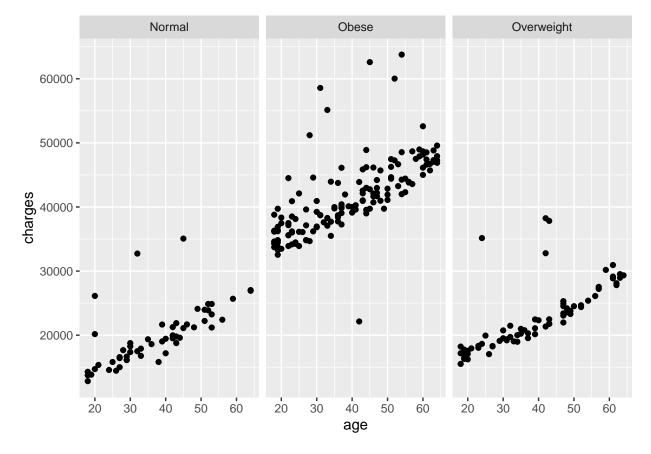
```
. = " # BEGIN PROMPT
insure_smokers <- NULL
insure_smokers
" # END PROMPT

# BEGIN SOLUTION
insure_smokers <- insure_data %>% filter(smoker == "yes")
# END SOLUTION
. = ottr::check("tests/p25.R")
```

26. [1 point] Make a scatterplot that examines the relationship between age and charges for normal, overweight, and obese individuals in three side by side plots. A facet\_ command may help you.

```
. = " # BEGIN PROMPT
p26 <- NULL
p26
" # END PROMPT

# BEGIN SOLUTION
p26 <- ggplot(insure_smokers, aes(x = age, y = charges)) +
    geom_point() +
    facet_wrap(~ bmi_cat)
p26</pre>
```



```
# END SOLUTION
. = ottr::check("tests/p26.R")
```

## All tests passed!

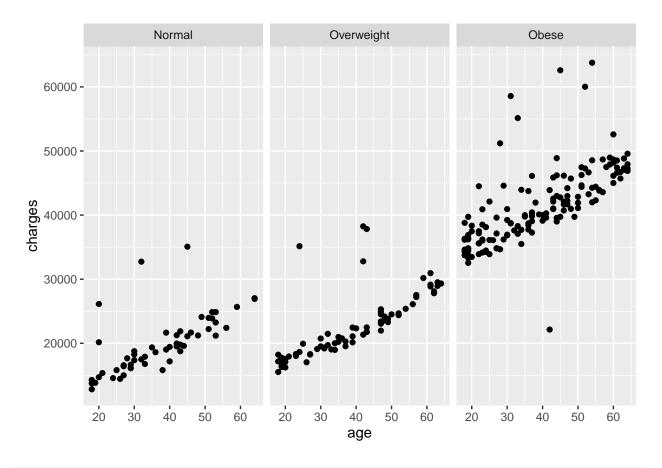
The plot above automatically displays the BMI categories alphabetically. Run the chunk below to assign a different order to the values of bmi\_cat.

```
insure_smokers <- insure_smokers %>%
  mutate(bmi_cat_ordered = forcats::fct_relevel(bmi_cat, "Normal", "Overweight", "Obese"))
```

## 27. [1 point] Re-run your code from question 26, but facet using bmi\_cat\_ordered.

```
. = " # BEGIN PROMPT
p27 <- NULL
p27
" # END PROMPT

# BEGIN SOLUTION
p27 <- ggplot(insure_smokers, aes(x = age, y = charges)) +
    geom_point() +
    facet_wrap(~bmi_cat_ordered)
p27</pre>
```



## # END SOLUTION

```
. = ottr::check("tests/p27.R")
```

28. [3 points] Run a separate linear model for each BMI group. To do this, you will need to subset your data into the three groups of interest. Call your models normal\_mod, overweight\_mod, obese\_mod. Use the tidy() function to display the output from each model.

```
. = " # BEGIN PROMPT
## subset your data here
# '<<<YOUR CODE HERE>>>>'
# '<<<YOUR CODE HERE>>>>'
# '<<<YOUR CODE HERE>>>>'
## generate your models
normal mod <- '<<<YOUR CODE HERE>>>>'
overweight_mod <- '<<<YOUR CODE HERE>>>>'
obese mod <- '<<<YOUR CODE HERE>>>>'
## tidy your models
# '<<<YOUR CODE HERE>>>>'
# '<<<YOUR CODE HERE>>>>'
# '<<<YOUR CODE HERE>>>>'
" # END PROMPT
# BEGIN SOLUTION
insure_smokers_normal <- insure_smokers %>% filter(bmi_cat == "Normal")
insure_smokers_overweight <- insure_smokers %>% filter(bmi_cat == "Overweight")
insure_smokers_obese <- insure_smokers %>% filter(bmi_cat == "Obese")
normal_mod <- lm(charges ~ age, data = insure_smokers_normal)</pre>
overweight_mod <- lm(charges ~ age, data = insure_smokers_overweight)</pre>
obese_mod <- lm(charges ~ age, data = insure_smokers_obese)</pre>
tidy(normal_mod)
## # A tibble: 2 x 5
##
                estimate std.error statistic
    term
                                                    p.value
     <chr>
                 <dbl> <dbl> <dbl> <dbl>
                                                       <dbl>
                                        7.24 0.00000000184
## 1 (Intercept)
                   10656.
                             1471.
## 2 age
                     246.
                               37.4
                                        6.58 0.0000000217
tidy(overweight_mod)
## # A tibble: 2 x 5
##
     term
                 estimate std.error statistic p.value
##
     <chr>>
                   <dbl>
                             <dbl>
                                        <dbl>
                                                 <dbl>
## 1 (Intercept)
                   12400.
                             1176.
                                        10.5 3.01e-16
                                        9.16 1.07e-13
                     264.
                               28.9
## 2 age
tidy(obese_mod)
```

For the next three problems, use the models to predict medical charges for a 20-year old by weight category. You don't need an R function to make these predictions, just the output from the models. Show your work for each calculation.

29. [1 point] Predict the medical charges for a 20 year old with a normal BMI.

```
. = " # BEGIN PROMPT

p29 <- NULL

p29
" # END PROMPT

# BEGIN SOLUTION

p29 <- 10656.1 + 246.1 * 20
# = $15578.1
# END SOLUTION
```

```
. = ottr::check("tests/p29.R")
```

## All tests passed!

30. [1 point] Predict the medical charges for a 20 year old with an overweight BMI.

```
. = " # BEGIN PROMPT
p30 <- NULL
p30
" # END PROMPT

# BEGIN SOLUTION
p30 <- 12399.7 + 264.2 * 20
# = $17683.7
# END SOLUTION
```

```
. = ottr::check("tests/p30.R")
```

## All tests passed!

31. [1 point] Predict the medical charges for a 20 year old with an obese BMI.

```
. = " # BEGIN PROMPT
p31 <- NULL
p31
" # END PROMPT

# BEGIN SOLUTION
p31 <- 30558.1 + 281.2 * 20
# = $36182.1
# END SOLUTION
```

```
. = ottr::check("tests/p31.R")
```

32. [3 points] In three sentences maximum, comment on (1) the direction of the association, (2) how much the slopes vary across the BMI groups, and (3) how much the predicted medical charges for a 20-year old varies by BMI category.

There was a positive association between age and medical charges for normal, overweight, and obese individuals. The relationship was of similar magnitude for each BMI group, though the slope increased in magnitude for overweight and obese individuals, implying that a steeper relationship for overweight individuals, and even steeper for obese individuals vs. normal BMI individuals. For a given age, obese individuals had much higher charges than overweight and normal weight individuals.

## END