L07: Relationships between two categorical variables

variables in R

Simpson's Paradox

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variables in R

Learning objectives for today

L07: Relationships between two categorical variables

> sualizing categoric riables in R

Today we will focus on how to visualize and quantify relationships between two categorical variables

- ► Two way tables
 - marginal vs conditional distributions
- Bar graphs
 - side by side
 - stacked
- Simpson's paradox

Reminder

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Categorical variables are just that, categories.

These can be nominal (no underlying order)

or

ordinal (ordered)

- ► Two-way, or 2X2 (for a table with two columns and two rows)
 - ▶ Used to examine the relationship between 2 categorical variables, originally for those with two levels each
- ► Foundational to epidemiology, because of the types of variables we are often interested in

Classic 2X2 looks like this:

Exposure group	Disease	No disease	Row total
Exposed	A	В	A+B
Not Exposed	C	D	C+D
Column total	A+C	B+D	Total # observations

Example: Lung cancer and smoking

Group	Lung Cancer	No Lung Cancer	Row total
Smoker	12	238	250
Non-smoker	7	743	750
Column total	19	981	1000

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Marginal distributions

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- ► The marginal distribution of a variable is the one that is in the margin of the table (i.e., the Row total or the Column total are the two margins of a two-way table).
- The marginal distribution is the distribution for a single categorical variable
- ▶ When we plotted categorical variables with geom_bar() in the earlier lectures, we were plotting marginal distributions

Marginal distributions

Group	Lung Cancer	No Lung Cancer	Row total
Smoker	12	238	250
Non-smoker	7	743	750
Column total	19	981	1000

- ▶ Overall, what % of the population has lung cancer?
- ▶ Overall, what % of the population are smokers?

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Marginal distributions

Group	Lung Cancer	No Lung Cancer	Row total	
Smoker	12	238	250	
Non-smoker	7	743	750	
Column total	19	981	1000	

▶ Overall, what % of the population has lung cancer?

• Answer: 19/1000 = 1.9%

▶ Overall, what % of the population are smokers?

► Answer: 250/1000 25% smoking

► The marginal distribution of lung cancer is 1.9% lung cancer, 98.1% no lung cancer.

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Conditional distributions

		N. I. C	Row total	
Group	Lung Cancer	No Lung Cancer		
Smoker	12	238	250	
Non-smoker	7	743	750	
Column total	19	981	1000	

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- ► The conditional distribution is the distribution of one variable within or conditional on the level of a second variable
- ► What is the distribution of lung cancer conditional on the individuals being smokers?
- ► What is the conditional distribution of lung cancer given individuals are non-smoking?

Conditional distributions

Group	Lung Cancer	No Lung Cancer	Row total
Smoker	12	238	250
Non-smoker	7	743	750
Column total	19	981	1000

- The conditional distribution of lung cancer given smoking is: 12/250 = 4.8% have lung cancer and 238/250 = 95.2% do not
- The conditional distribution of lung cancer given non-smoking is: 7/750 = 0.9% have lung cancer and 743/750 = 99.1% do not

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Marginal and Conditional distributions in R

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- ▶ We learned in Ch.1 how to plot marginal distributions of categorical variables using geom_bar()
- ► Can we generalize our use of geom_bar() to allow us to plot multiple conditional distributions? I.e., can we show the conditional distribution of lung cancer for smokers and non-smokers on the same plot?

Visualization in R

First, we encode the data to read into R:

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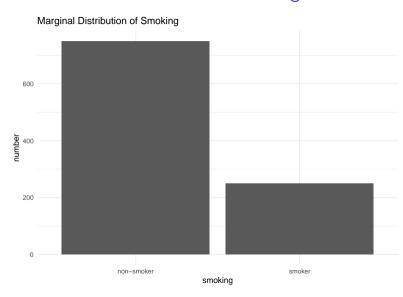
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"non-smoker", "lung cancer", 0.9, 7,

"non-smoker", "no lung cancer", 99.1, 743)

Bar chart for the visualization of marginal distributions



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Conditional distributions

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A Conditional distribution shows the distribution of a variable "conditioned on" or by levels of another variable.

► This allows you to visualize the differences in the response variable for varying levels of the exposure variable.

With the lung cancer example we are asking the question, is the distribution of lung cancer different for smokers than it is for non-smokers. . .

Dodged bar chart for the visualization of conditional distributions

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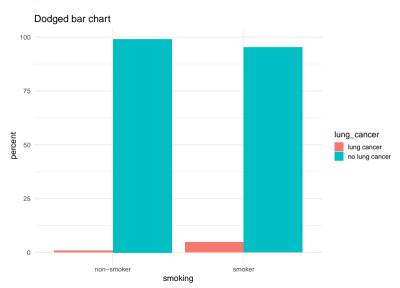
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```
Syntax:
```

```
\begin{split} & \mathsf{ggplot}(\mathsf{two\_way\_data}, \, \mathsf{aes}(\mathsf{x} = \mathsf{smoking}, \, \mathsf{y} = \mathsf{percent})) \, + \\ & \mathsf{geom\_bar}(\mathsf{aes}(\mathsf{fill} = \mathsf{lung\_cancer}), \, \mathsf{stat} = \mathsf{"identity"}, \, \mathsf{position} = \mathsf{"dodge"}) \, + \\ & \mathsf{labs}(\mathsf{title} = \mathsf{"Dodged \, bar \, chart"}) \, + \, \mathsf{theme\_minimal}(\mathsf{base\_size} = 15) \end{split}
```

Dodged bar chart for the visualization of conditional distributions



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A note about which syntax is necessary vs aesthetic

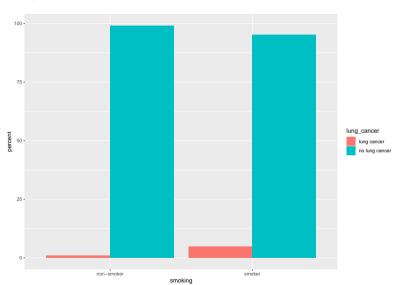
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```
Svntax:
```

```
\begin{split} & ggplot(two\_way\_data, \ aes(x = smoking, \ y = percent)) \ + \\ & geom\_bar(aes(fill = lung\_cancer), \ stat = "identity", \ position = "dodge") \end{split}
```

Dodged bar chart for the visualization of conditional distributions





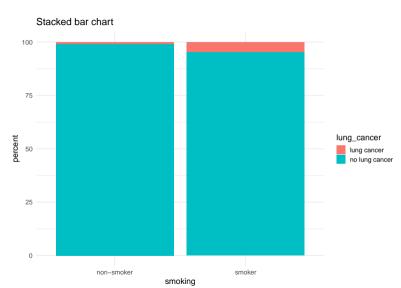
Stacked bar chart for the visualization of conditional distributions

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```

```
\begin{split} & \mathsf{ggplot}(\mathsf{two\_way\_data}, \ \mathsf{aes}(\mathsf{x} = \mathsf{smoking}, \ \mathsf{y} = \mathsf{percent})) \ + \\ & \mathsf{geom\_bar}(\mathsf{aes}(\mathsf{fill} = \mathsf{lung\_cancer}), \ \mathsf{stat} = \mathsf{"identity"}, \ \mathsf{position} = \mathsf{"stack"}) \ + \\ & \mathsf{labs}(\mathsf{title} = \mathsf{"Stacked \ bar \ chart"}) \ + \ \mathsf{theme\_minimal}(\mathsf{base\_size} = 15) \end{split}
```

Stacked bar chart for the visualization of conditional distributions



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▶ Plots like the one above make less sense when there are only two levels of both of the variables. This is because once you know the percent of lung cancer among smokers, you also know the percent of non-lung cancer

among smokers.

Visualizing categorical variables in R Simpson's Paradox

▶ Here is another example with 3 levels: Shoe support by gender (from ch. 5):

Group	Men	Women
Good support	94	137
Average support	1348	581
Poor support	30	1182
Column total	1472	1900

► The question: How does the distribution of support of shoes worn vary between shoes made for men and women?

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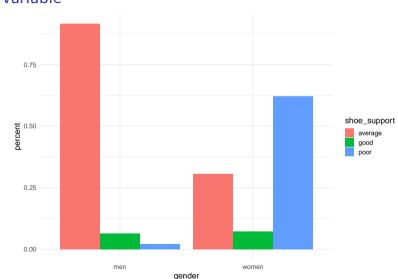
Example using shoe support data from Baldi & Moore page 124 of Ed.4

```
## # A tibble: 6 \times 3
##
     shoe support gender percent
##
     <chr>>
                   <chr>>
                              <dbl>
                            0.0639
   1 good
                   men
   2 average
                            0.916
                   men
   3 poor
                            0.0204
                   men
   4 good
                            0.0721
                   women
                            0.306
   5 average
                   women
   6 poor
                            0.622
                    women
```

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```
\begin{split} & \mathsf{ggplot}(\mathsf{shoe\_data},\ \mathsf{aes}(\mathsf{x} = \mathsf{gender},\ \mathsf{y} = \mathsf{percent})) \ + \\ & \mathsf{geom\_bar}(\mathsf{stat} = \mathsf{``identity''},\ \mathsf{aes}(\mathsf{fill} = \mathsf{shoe\_support}),\ \mathsf{position} = \mathsf{``dodge''}) \ + \\ & \mathsf{theme\_minimal}(\mathsf{base\_size} = 15) \end{split}
```

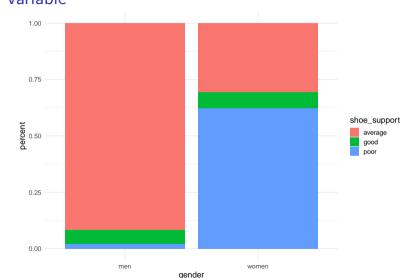


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```
\begin{split} & \mathsf{ggplot}(\mathsf{shoe\_data},\ \mathsf{aes}(\mathsf{x} = \mathsf{gender},\ \mathsf{y} = \mathsf{percent})) \ + \\ & \mathsf{geom\_bar}(\mathsf{stat} = \mathsf{``identity''},\ \mathsf{aes}(\mathsf{fill} = \mathsf{shoe\_support}),\ \mathsf{position} = \mathsf{``stack''}) \ + \\ & \mathsf{theme\_minimal}(\mathsf{base\_size} = 15) \end{split}
```



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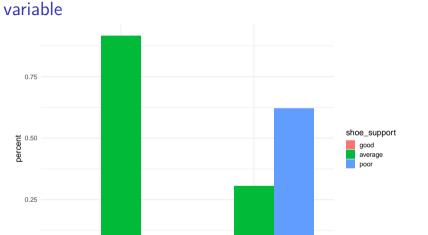
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Visualizing categorical variables in R

Recall from last class we learned how to reorder factor variables that affect the look of the plot:

```
shoe\_data <- shoe\_data %>\% \ mutate(shoe\_support = fct\_relevel(shoe\_support, "good", "average", "poor"))\\ ggplot(shoe\_data, aes(x = gender, y = percent)) + geom\_bar(stat = "identity", aes(fill = shoe\_support), position = "dodge") + theme\_minimal(base\_size = 15)
```

women



aender

0.00

men

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Why might we prefer dodged plots to stacked plots?

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Simpson's Paradox

- ▶ We will use an example of communit mortality that is presented in your book to illustrate Simpson's paradox.
- ▶ This dataset has 4 variables, age group, community, deaths and population

##	#	A tibble	e: 6 x 5			
##		age_grp	community	deaths	pop	$\mathtt{death_per_1000}$
##		<chr></chr>	<chr></chr>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
##	1	0-34	Α	20	1000	20
##	2	35-64	Α	120	3000	40
##	3	65+	Α	360	6000	60
##	4	all	Α	500	10000	50
##	5	0-34	В	180	6000	30
##	6	35-64	В	150	3000	50

Simpson's Paradox Example: Only Conditional data

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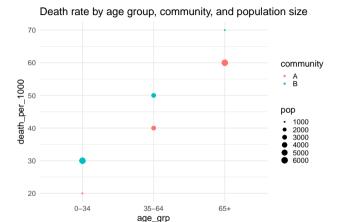
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Simpson's Paradox

Plot the mortality rates according to age group and community, linking size of dot to population size

```
\begin{split} & \mathsf{ggplot}(\mathsf{simp\_data\_no\_all},\ \mathsf{aes}(\mathsf{x} = \mathsf{age\_grp},\ \mathsf{y} = \mathsf{death\_per\_1000})) + \\ & \mathsf{geom\_point}(\mathsf{aes}(\mathsf{col} = \mathsf{community},\ \mathsf{size} = \mathsf{pop})) + \\ & \mathsf{labs}(\mathsf{title} = "\mathsf{Death}\ \mathsf{rate}\ \mathsf{by}\ \mathsf{age}\ \mathsf{group},\ \mathsf{community},\ \mathsf{and}\ \mathsf{population}\ \mathsf{size}") + \\ & \mathsf{theme\_minimal}(\mathsf{base\_size} = 15) \end{split}
```

Simpson's Paradox Example: Only Conditional data



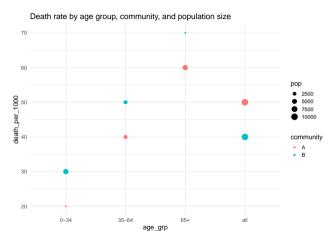
► What do you notice here? If someone ask you which community has higher mortality, what would you say?

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Simpson's Paradox Example: with marginal data



Notice that the mortality rates for the communities overall show community A having a higher rate than community B. Why is that?

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Simpson's Paradox

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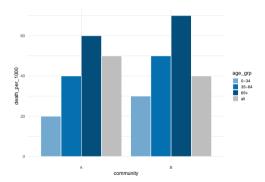
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Simpson's Paradox

"An association or comparison that holds for all of several groups can reverse direction when the data are combined to form a single group. This reversal is called Simpson's Paradox"

Simpson's Paradox

▶ Here are the same data shown using a bar chart



Which visualization gives you more information?

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Simpson's Paradox

Simpson's Paradox Berkeley example

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Simpson's Paradox

A famous example of Simpson's paradox related to admissions to Berkeley by gender:

 $Watch: \ https://www.youtube.com/watch?v=E_ME4P9fQbo$

Recap: Code and concepts

```
1. geom_bar(aes(col = var), stat = "identity", position =
   "dodge")
```

- 2. geom_bar(aes(col = var), stat = "identity", position =
 "stack")
- 3. Marginal vs conditional distributions
- 4. Simpson's Paradox

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Simpson's Paradox

Comic Relief

First, 3 looked in the book, but it wasn't an add-numbered problem.

Then 9 asked my fittle brother, but he wasn't an add-numbered problem.

Then 9 asked my fittle brother, but he wasn't with Google.

Finally, 9 found it on the Internet with Google.

Finally, 9 found it on the Internet with Google.

WANTS US TO SHOW HOW WE GET OUR ANSWERS.

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