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# Grammar-based Compression of RDF Graphs

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# Introduction

## 1.1 Motivation

The majority of data on the Internet is unstructured, because it is mainly text. That makes it difficult for machines to extract knowledge from the data and answer specific queries. In the context of the Semantic Web, an attempt is made to build a knowledge base using structured data. A possible framework for structured data is the Resource Description Framework (RDF)<sup>1</sup>, in which triples of the form (*subject*, *predicate*, *object*) are used in order to express certain facts. A set of triples naturally forms a graph, whereas the different *subjects* and *objects* are nodes and the *predicates* are edges of that graph. As those graphs express facts, they are called knowledge graphs.

In reality, such knowledge graphs can become very large with millions or even billions of nodes and edges. The following three use cases can then become very hard or even infeasible: storage, transmission and processing. One way to circumvent this problem is using compression. There are many existing compressors which work for all kinds of data, but the problem is that the compressed data is not query-able. Also, their compression might not be so strong, since they do not take advantage of the special features of RDF. For these reasons RDF-specific compression techniques are of interest. An example of such an RDF compressor is Header Dictionary Triples (HDT) from [FMPG<sup>+</sup>13]. Here, the data is made smaller by a compact representation of the triples.

There is a completely different compression technique which is called grammar-based compression. This method has so far been tested very little for RDF graphs. As the name suggests, it is based on the principle of a formal grammar, with productions that can be nested among each other. There are not yet many grammar-based compression algorithms for graphs. One example is GraphRePair (GRP) [MP18]. This is a compressor that works for any type of graph and is therefore also applicable for RDF.

In this thesis, it will be investigated to what extent grammar-based compression is suitable for RDF and whether it delivers even better results than HDT.

## 1.2 General Idea

As already mentioned, there are essentially three use cases for RDF data:

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<sup>1</sup><https://www.w3.org/RDF/>

1. Storage
2. Transmission
3. Processing/Consumption

The idea is to make all these use cases easier / possible by compression, especially if very large amounts of data have to be handled. In the first two use cases, compression can be helpful by reducing the size of the data. Thus the data can be stored more compactly and above all can be transferred faster, which occurs frequently in reality and can become a problem due to possibly slow transfer speeds.

The third use case (Processing/Consumption) is about reading or writing access to data. The more common case of read access is typically the execution of queries on RDF data. These are most often neighborhood queries. A compression algorithm can help in this respect by making it possible to answer such queries directly on the compressed graphs. This may even be faster than on the original data due to the reduced size.

As stated in [MP18], a graph compressed by GRP is not well suited for those just mentioned neighborhood queries. Such queries will take much longer than on the original graph. Therefore the thesis will focus on GRP's potential of compressing RDF data strongly and the query times will not be evaluated.

## 1.3 Thesis Structure

In Ch. 2 the necessary fundamentals are presented. It will mainly be about the two compressors HDT and GRP.

Ch. 3 deals with the approaches for the different aspects of the thesis. There, they will only be presented in a theoretical manner whereas in Ch. 4 the implementation details will be presented. In Ch. 5, the approaches to the different tasks will be evaluated using real RDF data in order to confirm the theoretical hypotheses stated before.

Finally, the results of the thesis are summarized in Ch. 6 and the future work on this topic is presented.



## Related Work

This chapter gives an introduction to RDF and presents the different compression algorithms discussed in the thesis.

### 2.1 RDF

RDF is a framework for structured data on the web. According to [HKRS08] it can be formally described as follows. Let the following sets be infinite and mutually disjoint:

- $U$  (URI references, typically represent unique entities or properties)
- $B$  (Blank nodes, represent an arbitrary value, necessary for displaying more complex logical statements)
- $L$  (Literals, represent fixed values, e.g. numbers or strings)

An RDF triple  $(s, p, o) \in (U \cup B) \times U \times (U \cup B \cup L)$  displays the statement that the subject  $s$  is related to the object  $o$  via the predicate  $p$ . So a subject can be anything but a literal. A predicate can only be a URI and an object can be anything.

Similar to entities or properties each blank node has unique ID in order reference it in the graph. But in contrast to URIs, these IDs do not have a semantic meaning. That fact will be used in Ch. 3.4.2.

#### 2.1.1 Ontology

In an RDF graph, relationships between entities or properties are displayed. In addition, entities or properties can also be assigned to types. In an ontology relationships between these types can be defined. More importantly for this thesis, features of types or properties are also described there. An ontology is itself also an RDF graph, which is described in one of the languages RDFS<sup>1</sup> or OWL<sup>2</sup> of which OWL is the more powerful one. [HKRS08]

In the course of this thesis, ontologies will be used to achieve a better compression. More precisely, specific features of properties will be used to do that.

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<sup>1</sup><https://www.w3.org/TR/rdf-schema/>

<sup>2</sup><https://www.w3.org/TR/owl-ref/>

## 2.2 HDT

HDT ([FMPG<sup>+</sup>13]) is an approach for compressing RDF data which is directly tailored to RDF and the data compressed by it is still query-able. The idea behind it is to make RDF's extensive representation more compact, thus reducing memory size. To achieve that, HDT creates three different components during the compression: A header, a dictionary and the triples.

The header contains statistical information about the RDF graph (e.g. number of subjects) and is not needed to decompress the file.

In the dictionary, all URIs and literals (which are usually quite long) are mapped to unique IDs (integers) and that mapping is stored persistently. HDT also compresses the dictionary to store it more efficiently. Since URIs typically have long common prefixes, a prefix-based text compression ([CW84]) is used here. It identifies longest common prefixes and takes advantage of the redundancy by storing the prefixes only once.

The triples component only uses the IDs produced by the dictionary in order to denote the triples. Usually, in many plain text formats for RDF (e.g. N-Triples <sup>3</sup>) each triple is written down after another. That simple notation is called 'Plain Triples' in HDT and can be seen in Fig. 2.1. This does not only require much space, but is also not good for query performance, since each single triple has to be traversed within a query execution.

It is easy to see that a more compact representation can be achieved by cleverly grouping the triples. That is exactly what HDT does. Imagine for example some triples that all have the same subject  $s$ . These would then be written in N-Triples as follows:

$$(s, p_1, o_{11}), \dots, (s, p_1, o_{1n_1}), (s, p_2, o_{21}), \dots, \\ (s, p_2, o_{2n_2}), \dots, (s, p_k, o_{kn_k})$$

In HDT the triples are then grouped by  $s$ :

$$s \rightarrow [(p_1, (o_{11}, \dots, o_{1n_1})), (p_2, (o_{21}, \dots, o_{2n_2})), \dots, \\ (p_k, (o_{kn_k}))]$$

Since all triples have the same subject  $s$ , it does not have to be written down at the beginning of each triple anymore. On the second level the triples are then grouped according to the predicates. So all triples with the predicate  $p_1$  come first, then all with the predicate  $p_2$  and so on. Finally only the different objects have to be enumerated since the subject and predicate are already implicitly given. It will now be explained how HDT implements this mechanism.

The above mentioned grouped representation is called 'Compact Triples' and can be seen in Fig. 2.1 in the middle. In the array 'Predicates' are the IDs of the predicates. A '0' means that from now on a new subject comes. For example, the first two entries in the 'Predicates' are linked to the first subject. At position 3 in 'Predicates', there is a '0'. Therefore, the following predicates are linked to the next subject (subject 2 in this case).

This works analogously for the objects, in the array 'Objects' the IDs of the objects are listed, and a '0' here means that from then on a new predicate comes. For instance, the first entry in 'Objects' is a '6', so the first derived triple would be  $(1, 2, 6)$ . The second entry of 'Objects' is a '0' since there is a change from predicate '2' to '3' in 'Predicates'.

The last representation of triples is called 'Bitmap Triples'. This is a slight adaption of 'Compact Triples'. The array  $S_p$  has the same content as 'Predicates', but without the zeros. That job is

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<sup>3</sup><https://www.w3.org/TR/n-triples/>

done by the bit-array  $B_p$  in which a '1' at position  $i$  means that at position  $i$  in  $S_p$  there comes a change of the subject (this change was previously denoted by a '0' in 'Predicates').

That works analogously for the objects where  $S_o$  has the same content as 'Objects', but without zeros.

The advantage of 'Bitmap Triples' is that queries can be executed faster on this representation. Also, the compressed size is slightly smaller than with 'Compact Triples'. Therefore, 'Bitmap Triples' are always used in the current version of HDT.

HDT has also procedures for answering queries, but those will not be mentioned here, because the thesis will focus on HDT's compression ability.

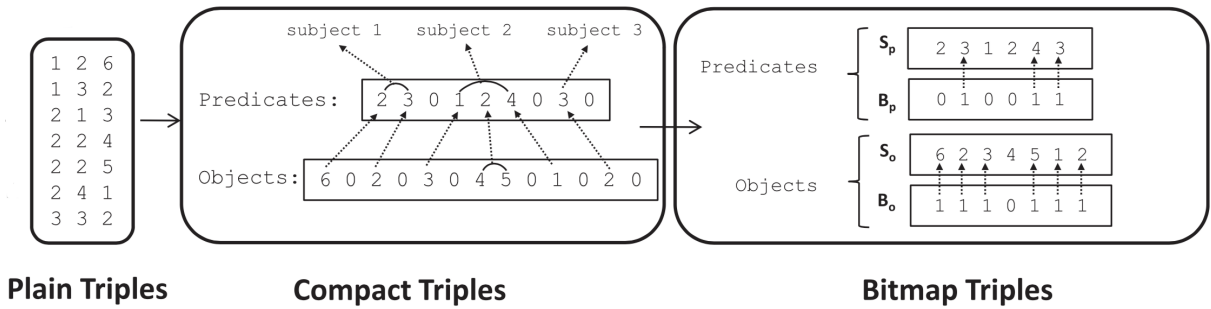


Figure 2.1: Three different representations of triples in HDT, figure from [FMPG<sup>+</sup>13].

## 2.3 Grammar-based Graph Compression

In this chapter, we will discuss two different approaches to grammar-based graph compression. First, [Dü16] is introduced and briefly explained why the approach is less suitable for RDF. Then [MP18], which the thesis will focus on, is introduced.

In general, grammar-based compressors try to find patterns that occur multiple times in the graph. Such patterns are subgraphs that can be of different kinds. Usually small patterns are searched for, since it is possible to find more occurrences of these. In addition, it is possible to combine several small patterns into one large one, so that even large parts can be compressed. These small patterns are often called digrams because they consist of two elements. The exact shape of the digrams depends on the respective algorithm.

### 2.3.1 Dürksen's Algorithm

An approach to grammar-based compression of graphs was developed in [Dü16]. Here the authors assume a hyper graph with node and edge labels. Such a graph can be seen in Fig. 2.2 on the left. To simplify the compression, a transformation is now executed, in which a new node is inserted for each edge  $e$ , which then has the same label as  $e$ . The original structure of the graph is obtained by connecting two nodes, which were previously connected by an edge, indirectly by the new node. The result of the transformation is a graph, which only has node labels, but no edge labels. Moreover, hyper edges (edges with more than two incident nodes) are no longer present due to the transformation.

Thus digrams like in Fig. 2.3 can be replaced. Here it is twice the case that a node with the label  $X$  is connected with a node with the label  $Y$ . This digram is then stored in a central location and can be referenced via the label  $X'$ . Thus only two nodes remain in the compressed graph (with  $X'$  as label) and the graph was reduced to a smaller size. There are some details which

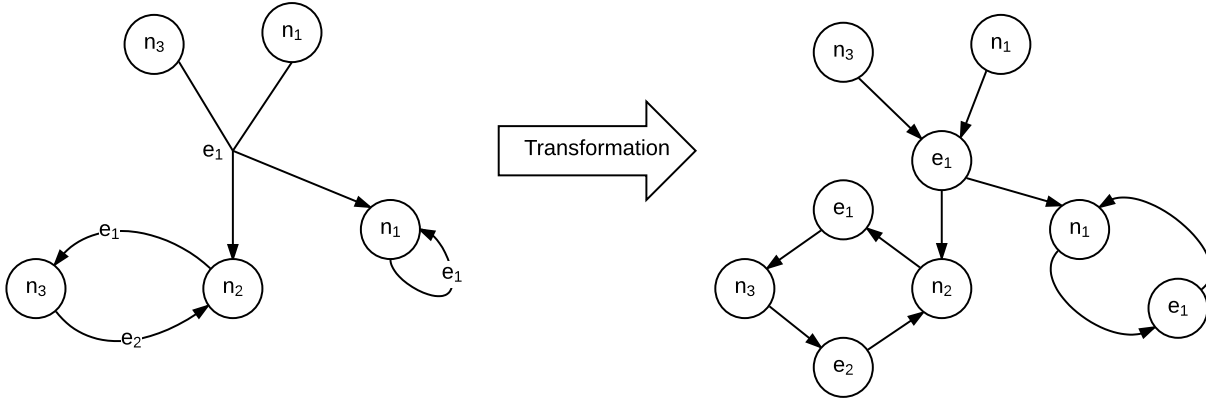


Figure 2.2: Transformation of a labeled graph (each edge is replaced by a new node having the label of the replaced edge).

make this digram replacement possible, but they are neglected at this point. The interested reader is referred to [Dü16].

Dürksen’s algorithm does not seem to be suitable for RDF, because it is based on the fact that there are several nodes with the same label. However, since in RDF a node represents an entity that does not occur twice, Dürksen’s basic assumption is not fulfilled in RDF.

In addition, Dürksen’s algorithm is not yet in a mature state, i.e., there is only a rudimentary implementation that does not work reliably for large graphs. Also, work is currently underway to find a compact representation of such a compressed graph in order to save the data with little memory. [Dü16]

For these reasons the thesis will focus on the compressor GraphRePair, which is presented in chapter 2.3.2.

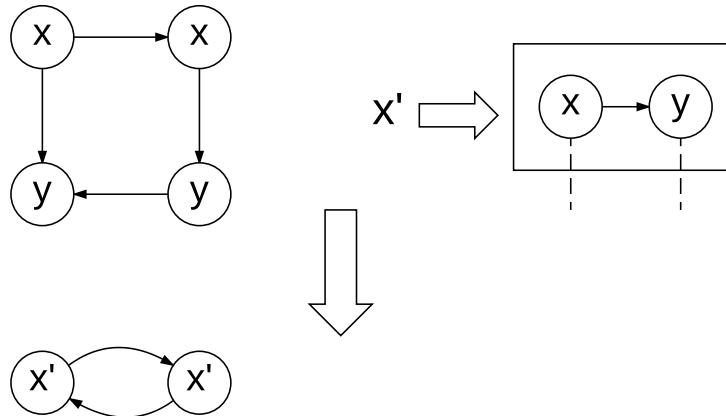


Figure 2.3: Replacement of two occurrences of the digram  $X \rightarrow Y$  by nodes with the label  $X'$ .

### 2.3.2 GraphRePair

This chapter deals with GRP, the compressor from [MP18]. It firstly presents some foundations and afterwards explains what digrams and digram occurrences are in GRP. Finally, the main routine of the compressor and the encoding of the compressed data are discussed.

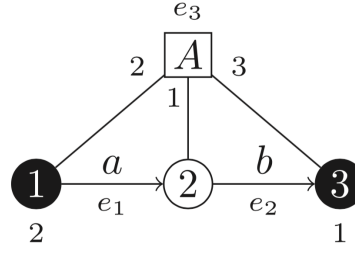


Figure 2.4: A hyper graph as defined in [MP18]. The black nodes 1 and 3 (consider the numbers within the nodes) are external nodes whereas the white node 2 is internal.  $e_3$  (with the label A) is a hyper edge while  $e_1$  and  $e_2$  (labeled with  $a$  and  $b$ , respectively) are normal edges.

The numbers 2, 1 and 3 around  $e_3$  denote the order of the nodes attached to  $e_3$ .

### Foundations

For a set  $M$ ,  $M^+ = \{x_1 \cdot x_2 \cdot \dots \cdot x_n | x_1, x_2, \dots, x_n \in M\}$  is defined as the set of all non-empty strings of  $M$  where  $\cdot$  stands for the concatenation of two symbols.  $M^* = M^+ \cup \{\epsilon\}$  is similar to  $M^+$ , but it also includes the empty string  $\epsilon$ .

Let  $\Sigma$  be an alphabet. A hypergraph over  $\Sigma$  is a tuple  $g = (V, E, att, lab, ext)$  where  $V = \{1, \dots, n\}$  is the set of nodes.  $E \subseteq \{(i, j) | i, j \in V\}$  is the set of edges.  $att : E \rightarrow V^+$  is the attachment mapping assigning start and end nodes to all edges.  $lab : E \rightarrow \Sigma$  is the edge label mapping, and  $ext \in V^*$  is a series of external nodes. A hypergraph does not contain multi-edges, which means for two edges  $e_1 \neq e_2$  it holds  $att(e_1) \neq att(e_2) \vee lab(e_1) \neq lab(e_2)$ . For a hypergraph  $g = (V, E, att, lab, ext)$   $V_g, E_g, att_g, lab_g, ext_g$  are used to refer to its components.

An example for a hypergraph is illustrated in Fig. 2.4. Formally, the graph can be described as  $V = \{1, 2, 3\}$ ,  $E = \{e_1, e_2, e_3\}$ ,  $att = \{e_1 \mapsto 1 \cdot 2, e_2 \mapsto 2 \cdot 3, e_3 \mapsto 2 \cdot 1 \cdot 3\}$ ,  $lab = \{e_1 \mapsto a, e_2 \mapsto b, e_3 \mapsto A\}$  and  $ext = 3 \cdot 1$ .

External nodes are black and the numbers below them indicate indexes for their position in  $ext$ . Analogously, hyper edges ( $e_3$  in this case) have indexes indicating the order of the attached nodes. The utility of external nodes is explained below. [MP18]

### Digrams in GRP

A digram  $d$  is a hyper graph with  $E_d = \{e_1, e_2\}$  so that the following conditions hold:

1.  $\forall v \in V_d : v \in att_d(e_1) \vee v \in att_d(e_2)$
2.  $\exists v \in V_d : v \in att_d(e_1) \wedge v \in att_d(e_2)$
3.  $ext_d \neq \epsilon$

Condition 1 ensures that all nodes in  $d$  are incident to one of the two edges of  $d$ . Conditions 2 is used to make sure that there is one 'middle node' incident to both edges of  $d$ . Finally, condition 3 ensures that there are external nodes. External nodes are not a real part of the digram, they represent other nodes of the overall graph which are connected to elements of the digram. [MP18]

### Digram Occurrences in GRP

Digram occurrences are concrete instances of a digram.

Let  $g$  be a hyper graph and  $d$  be a digram with the two edges  $e_1^d, e_2^d$ . Let  $o = \{e_1, e_2\} \subseteq E_g$  and let  $V_o$  be the set of nodes incident with edges in  $o$ . Then  $o$  is an occurrence of  $d$  in  $g$  if there exists a bijection  $b : V_o \rightarrow V_d$  so that for  $i \in \{1, 2\}$  and  $v \in V_o$  all following conditions hold:

1.  $b(v) \in att_d(e_i^d)$  iff  $v \in att_g(e_i)$
2.  $lab_d(e_i^d) = lab_g(e_i)$
3.  $b(v) \in ext_d$  iff  $v \in att_g(e)$  for some  $e \in E_g \setminus o$

Condition 1 and 2 ensure that the two edges of  $o$  form a graph isomorphic to  $d$ . Condition 3 makes sure that every external node of  $d$  is mapped to a node in  $g$  that is incident to at least one edge in  $g$  that is not contained in  $o$ . [MP18]

### Algorithm

Algorithm 1 is the main routine of GraphRePair. The algorithm take a graph as input and returns a grammar whereas  $N$  is the set of non terminals,  $P$  is the set of productions and  $S \in P$  is the start production. It maintains a list of digram occurrences in  $g$ . As long as this list contains multiple occurrences for one digram the loop will continue. In the loop, the most frequent digram is found and then replaced and the grammar is extended. After a digram replacement the occurrence list has to be updated, because the graph has changed and former digram occurrences may not exist anymore. Moreover, new digram occurrences can be present. This occurrence update is a complex process and will not be discussed here, since it is not relevant for the thesis. [MP18]

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#### Algorithm 1 GraphRePair (Graph $g = (V, E, att, lab, ext)$ )

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- 1:  $N, P \leftarrow \emptyset$
  - 2:  $S \leftarrow g$
  - 3:  $L(d) \leftarrow$  list of non-overlapping occurrences of every digram  $d$  appearing in  $g$
  - 4: **while**  $|L(d)| > 1$  for at least one digram  $d$  **do**
  - 5:    $mf d \leftarrow$  most frequent digram
  - 6:    $A \leftarrow$  new non terminal for  $mf d$
  - 7:   Replace every occurrence of  $mf d$  in  $g$
  - 8:    $N \leftarrow N \cup \{A\}$
  - 9:    $P \leftarrow P \cup \{A \rightarrow mf d\}$
  - 10:   Update the occurrence list  $L$
  - 11: **return** Grammar  $(N, P, S)$
- 

### Grammar Encoding

After GRP has constructed a grammar for some graph, this grammar has to be stored in an efficient way. The start production (the graph) is most often much bigger than the other productions and is therefore encoded differently.

The start production is encoded using  $k^2$  trees which is illustrated in Fig. 2.5. The adjacency matrix of the compressed graph (start rule of the grammar) is considered here. First, that matrix is extended with zeros to the next power of two. Then it is partitioned into  $k^2$  equally large partitions ( $k = 2$  here).

The tree's root represents the whole matrix and its child order correspond to the order of the just created partitions. If a partition only contains zeros, a zero leaf is added to the tree (e.g. in Fig. 2.5 (a), partition 4, right bottom). Otherwise a one-node is added and the corresponding condition will be partitioned itself. The recursive procedure continues until there is zero-leaf for each path of the tree. Afterwards, the tree is represented by bit-strings which is shown in Fig. 2.5 (c).  $T_1$  and  $T_2$  encode the first and second level and  $L$  encodes the level of the leaves.

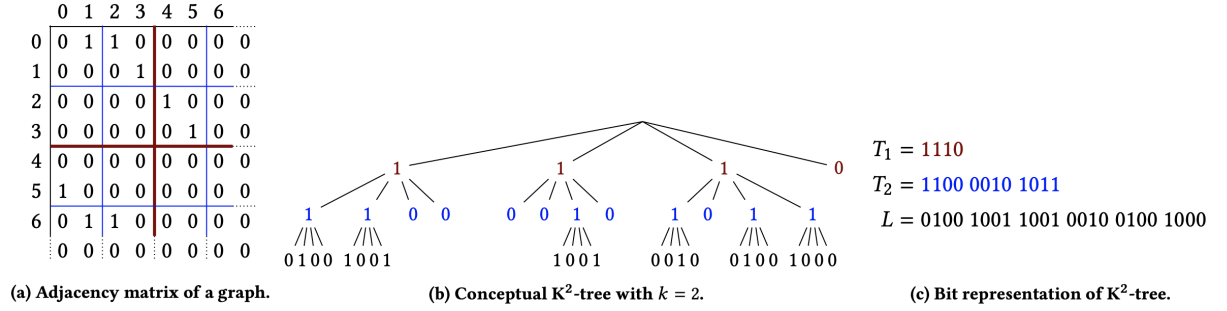


Figure 2.5: An adjacency matrix, its  $k^2$  tree representation and the tree's bit representation.

Since the graph has also edge labels, an adjacency matrix and its corresponding tree will be created for each of those labels. Furthermore, the compressed graph grammar contains hyper edges. An adjacency matrix only displays the nodes connected to the hyper edge, but not the order they are connected to it. Hence, for each hyper edge a permutation is stored in addition to the adjacency matrix.

That encoding method does not always work well together with the grammar, i.e., a smaller grammar sometimes results in a bigger encoded size of the start rule. If GRP can compress well that results in a high number of non terminals and hyper edges, in most cases. That will increase the storage amount for the start rule. Moreover, the compression potential of the  $k^2$ -tree highly depends on the content of the adjacency matrix. That is, a small change in the matrix can deliver a much higher storage amount of the tree.

The remaining productions of the grammar are encoded differently, because they are usually quite small compared to the start production. Here,  $\delta$ -codes with variable length are used. Essentially, this is a way of displaying objects as a bit-string. Every production starts with the number of edges. For each edge, one bit is used to mark terminal/non-terminal edges, followed by the number of attached nodes. Next, the  $\delta$ -codes of the list of IDs is mentioned. Finally, a  $\delta$ -code is used for the edge label. [MP18]

## Implementation

GRP has been implemented by the authors of [MP18] in the Scala language<sup>4</sup>. It has to be seen as a proof of concept implementation, i.e., it has quite a high run time for bigger graphs. The software can take an RDF file (in N-triples format) as the input and produces three different output files:

**Prod:** Contains all productions except the start rule.

**Perms:** Contains the hyper edge permutations.

**Start :** Contains the start rule.

All these files are necessary to decompress the graph.[MP18]

<sup>4</sup><https://www.scala-lang.org/>





This chapter contains the solution approaches to the parts of the thesis. Firstly, a formal model of a compressor is defined. Based on that, the key performance indicators which will be used to measure the performance of the single compressors are introduced. Secondly, the two existing compressors HDT and GRP are compared. Finally, improvements of the compression will be suggested.

### 3.1 Compressor Models

Here, two compressor models will be introduced, one for general compressors and another one for RDF compressors.

#### 3.1.1 General Compressor Model

A general purpose compressor  $C$  can be described as follows:  $C$  takes an input  $in$  and produces an output  $out$ . That step is called compression. Decompression can be described as tasking  $out$  as an input and producing  $in$ .

An example for a general compressor is GZip <sup>1</sup>.

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<sup>1</sup><https://www.gzip.org/>

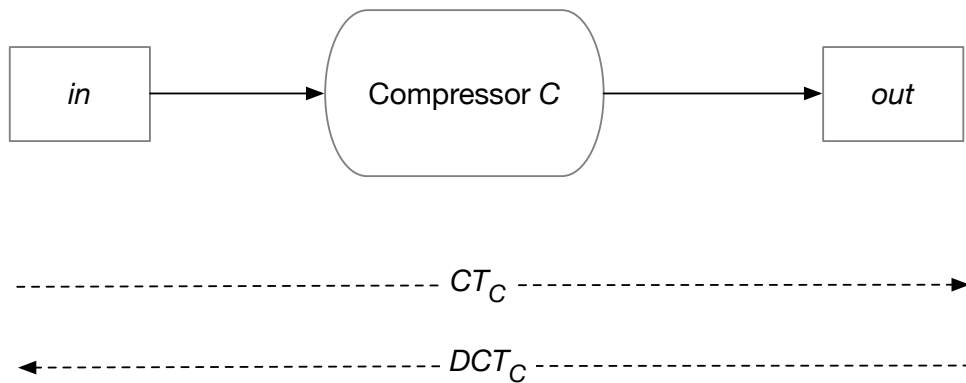


Figure 3.1: Visualization of the General Compressor Model.

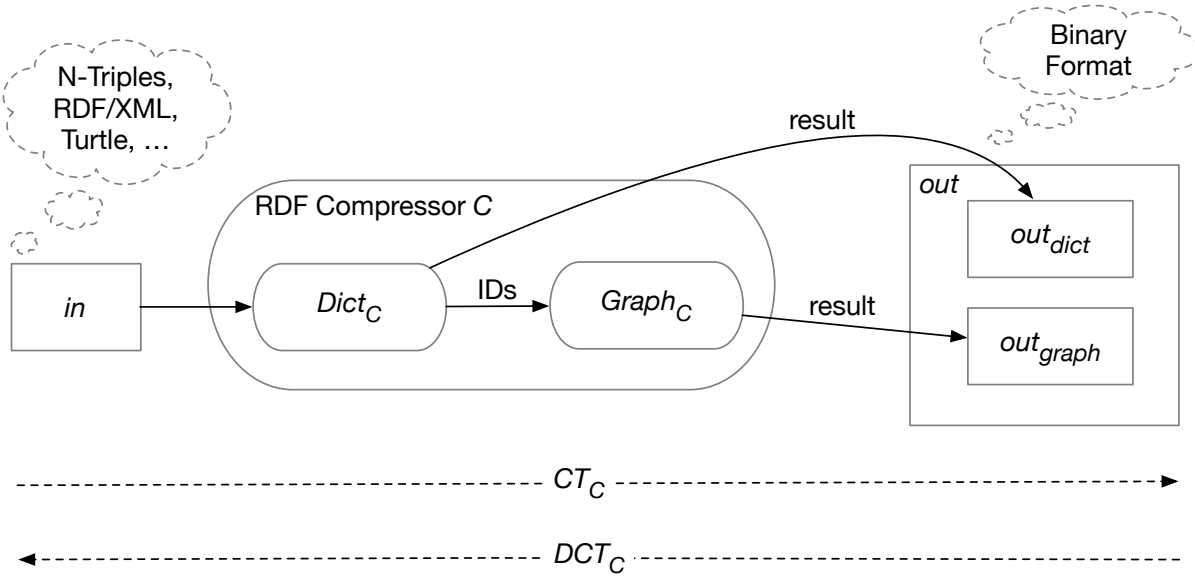


Figure 3.2: Visualization of the RDF Compressor Model.

### 3.1.2 RDF Compressor Model

This section introduces a formal model for an RDF compressor which can be seen as a sub class or extension of the general model in Ch. 3.1.1. It is illustrated in Fig. 3.2. Here, the compressor  $C$  is more complex as it consists of two components. The first one is called  $Dict_C$  and it handles the dictionary compression. That mechanism has already been introduced in the context of HDT (see Ch. 2.2). It assigns an ID to each URI, literal or blank node ID of the graph and can then also further compress the dictionary (like in HDT with prefix trees). The result of  $Dict_C$  is  $out_{dict}$  which is displayed in the right of Fig. 3.2.

The IDs created by  $Dict_C$  are then delivered to the second component  $Graph_C$  which is responsible for compressing the RDF graph. It only uses the IDs from  $Dict_C$  and does not know about the URIs, literals and blank node IDs. Its result is called  $out_{graph}$  which, together with  $out_{dict}$ , forms the complete output  $out$  ( $out = \{out_{dict}, out_{graph}\}$ ).  $out_{graph}$  and  $out_{dict}$  can each be a single file or a set of files.

### 3.1.3 Existing RDF Compressors

Table 3.1 shows an overview of the RDF compressors discussed in this thesis and in which way they fulfill the model. As already explained in Ch. 2.2,  $Dict_{HDT}$  assigns IDs and compresses the dictionary. In contrast,  $Dict_{GRP}$  only assigns IDs and omits the dictionary afterwards.  $Dict_{GRP}$  is therefore not a real dictionary compressor. We solve this problem by replacing  $Dict_{GRP}$  with  $Dict_{HDT}$ . This way, comparing HDT and GRP in a fair way is possible. It must also be mentioned that  $Graph_{HDT}$  includes the HDT header (see Ch. 2.2). Even if the header is not needed for decompression, its size will be part of  $out_{graph}$ . But this is not a problem, because the header's size is so small that it does not add a significant amount to  $out_{graph}$ .

	$Dict_C$	$Graph_C$
HDT	✓	✓
GRP	only ID assignment (no storage of $out_{dict}$ )	✓

Table 3.1: Overview of RDF compressors presented in this thesis.

## 3.2 Key Performance Indicators

In the following two sections, key performance indicators for general and RDF compressors are introduced. Those indicators will be measured in order to determine the overall performance for the different compressors.

### 3.2.1 Compression Ratio

One of the key performance indicators for a compressor  $C$  is its compression ratio. Let  $m$  be a single file or a set of files. Then  $|m|$  is defined as the size which is measured in bytes. The compression ratio is defined by the following equations:

$$CR_C = \frac{|out|}{|in|} \quad (3.1)$$

$$CR_{Dict_C} = \frac{|out_{dict}|}{|in|} \quad (3.2)$$

$$CR_{Graph_C} = \frac{|out_{graph}|}{|in|} \quad (3.3)$$

Eq. 3.1 defines the compression ratio for the whole output  $out$ . Therefore, it is applicable to general and RDF compressors.

In contrast, Eq. 3.2 and 3.3 define the compression ratio only with regard to  $out_{dict}$  and  $out_{graph}$ , respectively. They are only applicable for RDF compressors, since a general compressor has no distinction between  $out_{dict}$  and  $out_{graph}$ . In some cases it is of interest to only consider either the dictionary or graph compression.

Sometimes  $CR$  is used instead of  $CR_C$  if it is clear from the context, which compressor  $C$  is considered.

As shown in Fig. 3.2,  $in$  can have different formats. That has to be taken into account with regard to  $CR$  as those formats implicate different input sizes. When  $CR$  of two compressors is compared, their input has to have the same format.

### 3.2.2 (De-)Compression Time

Another key performance indicator of a compressor  $C$  is its compression time ( $CT_C$ ) and decompression time ( $DCT_C$ ). These metrics also depends on the input data and indicate the run time needed for compression and decompression of the data, respectively. The run time is typically measured in milliseconds.  $CT_C$  and  $DCT_C$  are also shown in Fig. 3.1 and 3.2. They are defined the same for general compressors and RDF compressors. Furthermore,  $CT_C$  and  $DCT_C$  are only measured for the whole compressor  $C$ , not for  $Dict_C$  or  $Graph_C$ .

Analogously to  $CR$ , if is clear from the context which compressor is considered,  $CT$  and  $DCT$  are used instead of  $CT_C$  and  $DCT_C$ , respectively.

## 3.3 GRP vs HDT

In this chapter, the two existing compressors - HDT and GRP - will be compared. Therefore, the features of the compressors and their applicability to certain properties of RDF graphs are discussed.

The question is whether there are certain properties/features that an RDF graph can have, and which have a positive or negative impact on the compression ratio of one or both algorithms. As HDT and GRP use the same method for compressing the dictionary ( $Dict_{HDT}$ ), we only compare  $Graph_{HDT}$  and  $Graph_{GRP}$  in this chapter.

### 3.3.1 Relation Between Structure of Data and Compression Ratio

This chapter discusses how the structure of the input graph *in* influences the compression ratios ( $CR_{Graph_C}$ ) for GRP and HDT. In order to realize that it is necessary to first introduce the star pattern.

#### Star Pattern

In graph theory, a star is a graph in which one node is connected to all other nodes. The other nodes are not connected to each other. While a star is an extreme case, there exist graphs with a few nodes having very high degrees. We denote them to be similar to the star pattern.

In order to measure that we define the Star Pattern Similarity ( $SPS$ ). Let  $deg(n)$  be the degree of a node  $n$ . Let  $N$  be a list of all nodes sorted by their  $deg$ -values in descending order. Let  $N_{top}$  be the first  $x$  nodes of  $N$ . Hence,  $N_{top}$  contains  $x$  nodes with the highest degrees.  $x$  should be chosen related to the size of  $N$ , we choose  $x = 0.001 \times |N|$ . Then,  $SPS$  is defined as follows:

$$SPS = \frac{\sum_{n \in N_{top}} deg(n)}{\sum_{n \in N} deg(n)} \in [0, 1]$$

The higher the value of  $SPS$  is, the more similar the graph is to the star pattern, because then there are a few nodes having a high proportion of the sum of all degrees.

The star pattern can be further divided into hub pattern and authority pattern. As the name suggests, the hub pattern corresponds to a graph in which a few nodes have very high outgoing degrees, the authority pattern is the opposing case (high ingoing degrees). That distinction is needed in the following chapter.

#### HDT

Now, HDT's behavior with respect to the input is discussed. As HDT's way of compressing the graph structure is fairly simple compared to GRP, there do not seem to be many potential features of the input data that have a high impact on HDT's compression ratio. But one feature is clearly visible: When Fig. 2.1 is considered, it is noticeable that the number of 1's in  $B_p$  becomes less if there are only a few different subjects. This enables HDT to store  $B_p$  more efficiently and, thus,  $CR_{Graph_{HDT}}$  becomes smaller. Consequently, HDT should perform better if the graph is similar to the hub pattern.

#### GRP

For GRP, that input feature analysis is more complex. Since GRP constructs grammar rules by using the graph's structure, it can make use of sub graphs that are much more complex than the star pattern HDT is using. There can be many features that can lead to different constructible grammar rules. Those will not be discussed here, as these patterns can become arbitrarily complex, because they can be nested among each other. But one insight is that GRP's compression ratio tends to be bigger when there are more different predicates in the graph. This is true, because GRP's grammar rules are based on repeating patterns and, hence, repeating edge labels as part of these patterns.

Let

$$ELR = \frac{\text{number of different edge labels}}{\text{number of edges}}$$

(edge label ratio) be the ratio of the edge labels or properties to the total number of edges of the graph.

A lower value of *ELR* should increase the likelihood of a lower compression ratio. However, if the graph structure becomes unfavorable for GRP, the compression ratio may still be worse at a lower value for *ELR*.

In [MP18], the authors mentioned that a graph similar to the star pattern is beneficial for GRP, because GRP can create many digrams around those nodes with high degrees whereby, in contrast to HDT, GRP does not rely on the hub pattern.

### 3.4 Compression Improvements

First comparisons of *Graph<sub>HDT</sub>* and *Graph<sub>GRP</sub>* (see Ch. 5.1) showed that *Graph<sub>GRP</sub>* achieves a better compression ratio in many cases. Since this thesis' topic is grammar-based compression, Ch. 3.4.1 will focus on improving *Graph<sub>GRP</sub>*. But Ch. 3.4.2 is about the improvement of *Dict<sub>HDT</sub>* which is used for both HDT and GRP.

#### 3.4.1 Ontology Knowledge

As already discussed in Ch. 2.1.1, an ontology contains meta data about an RDF graph.

This chapter will investigate whether it is possible to change the structure of an RDF graph by applying knowledge from its ontology so that it is better compressible for GRP, but at the same time remains semantically equivalent to the original graph. In this way no data would be lost after the compression.

In Ch. 3.3.1 it has already been mentioned that GRP makes use of much more complex sub structures than HDT. It will therefore be interesting to see how applying ontology knowledge influences GRP's compression ratio.

This chapter is about elaborating the theoretical concepts of OWL and investigating how they can be used for grammar-based compression.

#### Symmetric Properties

anderes Bsp

There is a class in [owl] called `owl:SymmetricProperty`<sup>2</sup> which expresses that a certain other predicate *p* is symmetric. This means, if there is a triple  $(s, p, o)$  in the graph, then there can also be a triple  $(o, p, s)$  at the same time. In reality, however, it can happen that only one of the two triples is explicitly mentioned and the second triple is only implicitly present. The idea is to always add the other triple to the graph in such a case. This makes the graph larger at first, but more grammar rules can be found. This is because *ELR* can be reduced by adding it, which can lead to a better compression ratio. At the same time this will not result in an unfavorable structure. The procedure is illustrated in Fig. 3.3a. That graph shall be seen as a sub graph of a much larger graph. Here, *p* is the only symmetric property. Hence, the green edges were added to the graph. Due to the addition, the digram of Fig. 3.3b can now be found twice, whereas it was previously found only once. So, the addition delivers a better compression potential here. At the same time, the degrees of the nodes 2, 3, 5 and 6 are increased by one.

<sup>2</sup>The prefix `owl:` is used for every entity or property in the context of OWL.

But this should not really decrease the chance of finding other digrams in the graph, since those nodes were already connected before.

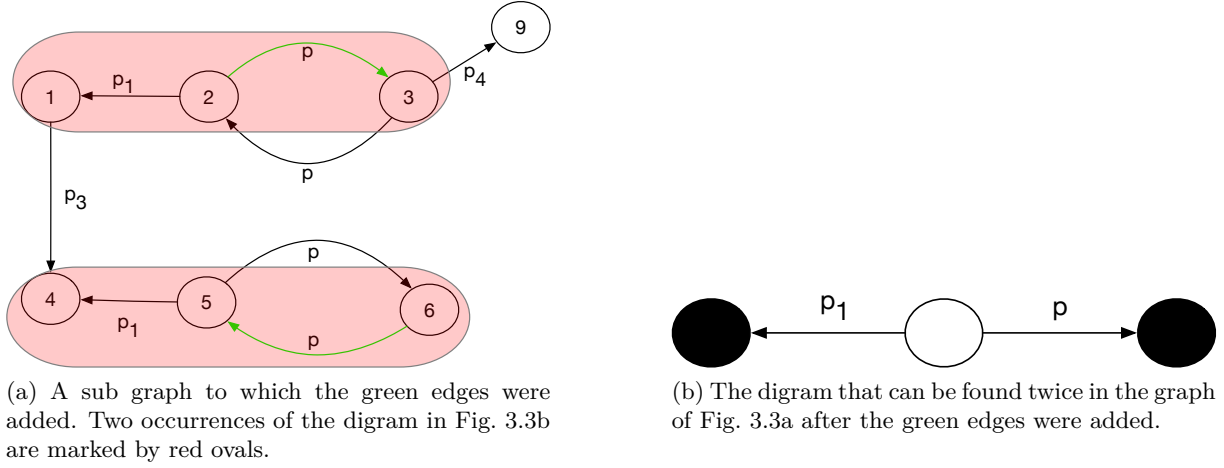


Figure 3.3: Visualization of the benefits of adding symmetric edges to the graph.  $p$  is symmetric, all other properties are not.

### Inverse Properties

One property of [owl] is `owl:inverseOf`, which is defined for two properties  $p_1, p_2$ . If  $(s, p_1, o)$  exists then  $(o, p_2, s)$  should also exist and vice versa. Analogously to `owl:SymmetricProperty` it can be the case that only one of the two triples is explicitly mentioned. The approach is similar to the symmetric properties. It is reasonable to argue in a similar way for adding those edges to graph here. It can decrease *ELR* if there are many occurrences of a few inverse properties. Also, adding those edges will not really make the graph's structure more complex since all the nodes were already connected before.

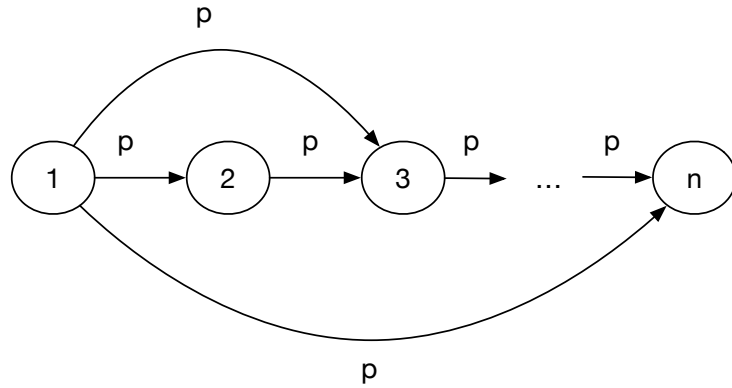
### Transitive Properties

In [owl], a predicate can be denoted as transitive (`owl:TransitiveProperty`). Let  $p$  be transitive. If the triples  $(1, p, 2)$ ,  $(2, p, 3)$  exist then  $(1, p, 3)$  should also exist. Consequently, this holds also for an arbitrarily long path from 1 to 3, as illustrated in Fig. 3.4. Such a path, with the length of at least two, is called *transitive path* from now on. If there exists a *transitive path* between two nodes  $i$  and  $j$ , then the edge  $(i, j)$  is called *direct transitive path*. So, in Fig. 3.4, the edges  $(1, 3)$  and  $(1, n)$  are *direct transitive paths*.

The shown graph shall again be seen as some sub graph. The approach is to remove all *direct transitive paths*. This is reasonable, as it gives the nodes  $i$  and  $j$  a lower degree, and therefore GRP can have a higher chance to find other digrams in which those nodes are involved (they are not shown in Fig. 3.4).

The opposing approach is to add all *direct transitive paths*. But a strong argument against this approach is that it would dramatically increase the number of edges, because for each pair  $(x, y)$  (with  $x, y \in \{1, \dots, n\}$  and distance between  $x$  and  $y$  greater than 1), an edge  $(x, y)$  would be added. After increasing the graph's size so much it is unlikely that  $out_{graph}$  becomes smaller even if more digrams could be found for some reason.

hier noch ein bs  
wo nach entfer  
mehr digramme  
gefunden werde

Figure 3.4: A sub graph with the transitive predicate  $p$ .

### Equal Properties

In OWL there are the properties `owl:equivalentProperty` and `owl:sameAs`. The first one denotes that two properties are equivalent, but it does not mean that they are equal. In contrast, the latter one is expressing equality. If there is a property  $p$  which is equal to other properties  $p_1, \dots, p_n$ , then one approach could be to replace each occurrence of  $p_1, \dots, p_n$  with  $p$ . This would reduce *ELR* and, at the same time, not change the structure of the graph. However, this approach was not implemented, since the thesis focuses on compressing single RDF graphs and `owl:sameAs` typically connects multiple graphs with each other. Compressing multiple graphs would lead to more complexity, because not only properties can be the same but single nodes can be marked as the same as well.

#### 3.4.2 Dictionary Improvements

According to [FMPG<sup>+</sup>13], the dictionary ( $out_{dict}$ ) makes up most of the memory of a compression output. First results in Ch. 5 also show that. It is therefore worth investigating whether the dictionary can be compressed better. It can be taken advantage of certain features of the dictionary to achieve that. In order to do that we use  $Dict_{HDT}$  as the basis and further improve it.

### Literals

Objects in RDF can be literals. Literals typically contain constant values and usually have no common prefixes. Therefore the compression of HDT is not suitable for these. It would be possible to use different compression techniques for different types of data values (integer, double, string, etc.). The thesis will focus on compressing strings.

Since those strings can contain whole flow texts, a text compression would probably be well applicable. An example of such a text compression is a Huffman Code [Sha10]. Here, every single character of a text is binary coded, whereby frequently occurring characters get short and rare characters get longer codes. These codes are expressed by a binary Huffman tree. An example can be seen in Fig. 3.5. Each leaf contains a symbol whereas the ones and zeros on the path to the symbol define its code. The tree is constructed in such a way that paths to frequent characters are shorter than those to rare characters. The whole procedure can be seen in [Sha10].

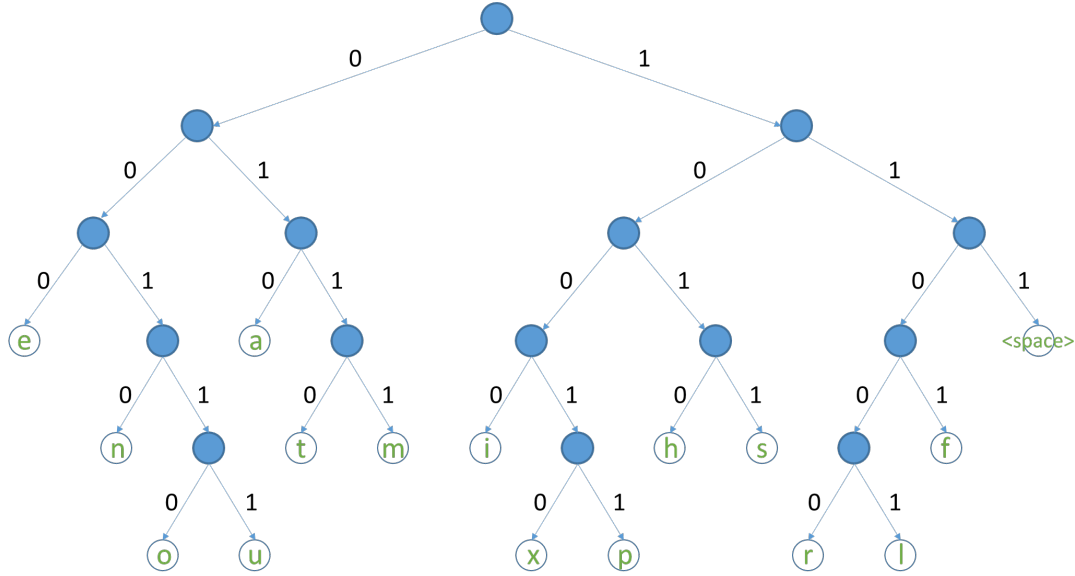


Figure 3.5: An example of a Huffman Tree.

### Blank Nodes

As already mentioned in Ch. 2.1 every blank node gets an ID. These IDs are usually chosen arbitrarily and have no meaning beyond that. When reading an RDF graph with the Jena-API <sup>3</sup> (which is used by HDT according to [FMPG<sup>+</sup>13]) random strings are assigned to the blank nodes, which are quite long. They also have no common prefixes, which makes the HDT dictionary compression ineffective here.

To improve the compression, the IDs of the blank nodes could be reassigned. For example, numbers from 1 to  $n$  ( $n$  = number of blank nodes) can be used to get short IDs.

Another possibility is not to save the IDs of the blank nodes at all. In HDT all strings in the dictionary (including the blank node IDs) are mapped to short IDs. Thus, the blank node IDs are in principle already stored. They can therefore be removed from the dictionary.

<sup>3</sup><https://jena.apache.org/index.html>



# Implementation

This chapter will explain how the different approaches of Ch. 3 have been implemented. First, the comparison of HDT and GRP is discussed. Second, improvements for both graph and dictionary compression are presented.

## 4.1 GRP vs HDT

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In this chapter, it will be explained how the comparison between HDT and GRP is implemented. As has just explained, HDT can compress a graph that is similar to a hub pattern (few subjects, many objects) very well. So it gets worse the further away the graph is from this pattern. The most unfavorable graph structure for HDT is therefore the authority pattern.

The task is to create a series of RDF graphs ( $G_1, \dots, G_m$ ) that first correspond to the hub pattern and then continue to change in the direction of the authority pattern. That can be done using Alg. 2. The first input parameter *steps* influences how many graphs will be created. It has to be chosen high enough to ensure a smooth transition from the hub to authority pattern. The second parameter *nodesFactor* influences the amount of nodes of the graphs. Concrete values for the parameter are not important to mention.

An example output of Alg. 2 is shown in Fig. 4.1. All graphs ( $G_1$  to  $G_m$ ) have the same number of nodes and edges. That is ensured by Line 6 in Alg. 2.  $G_1$  has only one subject connected to all objects.  $G_2$  then has two subjects more and correspondingly 2 objects less. This goes on and on until there is only one object that is connected to all subjects ( $G_m$ ). The edges are randomly distributed among the nodes, so that all nodes have a similar degree and each node has at least a degree of one.

It is also ensured that each of the generated files has exactly the same size. This is made possible by ensuring that each URI has the same length and ensuring that every RDF graph also has the same number of triples. This same size is important for the evaluation, since only the graph's structure is of interest here. An unequal size of the RDF files would lead to undesired effects in terms of  $CR_{Graph_G}$ .

A section of such a file (for  $G_1$ ) is shown in Fig. 4.2. In that example, there is only one distinct predicate for all triples. This is because, we first want to focus on the effect of the hub and authority patterns. The impact of an increasing number of predicates will be evaluated afterwards.

---

**Algorithm 2** BuildGraphs (*steps*, *nodesFactor*)

---

```

1:  $n \leftarrow \text{nodesFactor} * \text{steps} // n$  is number of nodes
2:  $\text{subj} \leftarrow 1$ 
3:  $i \leftarrow 1$ 
4: while  $\text{subj} \leq n$  do
5:    $\text{obj} \leftarrow n - \text{subj}$ 
6:    $G_i \leftarrow$  build graph with  $\text{subj}$  subjects and  $\text{obj}$  objects
7:    $\text{subj} \leftarrow \text{subj} + \text{steps}$ 
8:    $i \leftarrow i + 1$ 
9: return ( $G_1, \dots, G_m$ )

```

---

## 4.2 Compression Improvements

This chapter introduces the implementation details of Ch. 3.4. First, applying ontology knowledge in order to achieve a better compression ratio is discussed. Afterwards, implementation details of the dictionary compression improvements are presented.

### 4.2.1 Datasets

Here, an overview about the different datasets, that have been used for the evaluation, is given. Although the datasets are used in Ch. 5, they are presented here, since some implementation details are dependent on the data.

#### Semantic Web Dog Food

Semantic Web Dog Food <sup>1</sup> is a collection of RDF files from the RDF researchers community. It contains data about their conferences and workshops.

#### DBPedia

DBPedia <sup>2</sup> is an RDF version of the knowledge from Wikipedia. It contains many different data files of a quite big size, with some of them having hundreds of millions of triples. Also, DBPedia includes an ontology that is used for the evaluation.

#### Wordnet

Wordnet contains knowledge about the English language. Words that have the same meaning are grouped in to the same “synset”. Those sets are the nodes in an RDF graph and relations between them are edges/properties.

#### Nuts-RDF

The NUTS (Nomenclature of Territorial Units for Statistics) <sup>3</sup> contains the NUTS regions along with geographic information. It contains blank nodes and is therefore useful for the evaluation of the improvements regarding blank node IDs.

---

<sup>1</sup><http://www.scholarlydata.org/dumps/>

<sup>2</sup><https://wiki.dbpedia.org/Downloads2015-04>

<sup>3</sup><http://nuts.geovocab.org/>

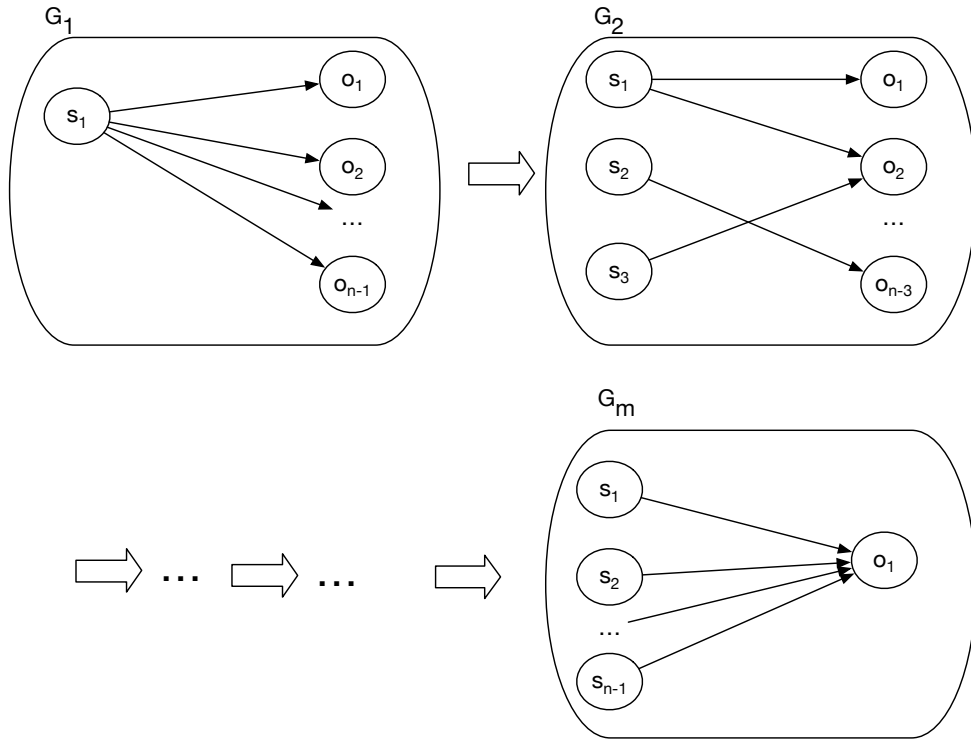


Figure 4.1: Example output of Alg. 2: Step-by-step transition from hub pattern to authority pattern. The number of nodes  $n$  is the same for each graph. The number of edges is also the same for each graph.

```
<http://subject/0000000000> <http://predicate/0000000000> <http://object/0000001036> .
<http://subject/0000000000> <http://predicate/0000000000> <http://object/0000000854> .
<http://subject/0000000000> <http://predicate/0000000000> <http://object/0000000991> .
<http://subject/0000000000> <http://predicate/0000000000> <http://object/0000000450> .
<http://subject/0000000000> <http://predicate/0000000000> <http://object/0000000456> .
<http://subject/0000000000> <http://predicate/0000000000> <http://object/0000000689> .
<http://subject/0000000000> <http://predicate/0000000000> <http://object/0000001166> .
<http://subject/0000000000> <http://predicate/0000000000> <http://object/0000000960> .
```

Figure 4.2: Excerpt from the generated RDF file for  $G_1$  (see Fig. 4.1). Each triple has the same length.

## Government Open Data

This is RDF data <sup>4</sup> published by the Ministry of Housing, Communities Local Government of the United Kingdom.

### 4.2.2 Ontology Knowledge

This chapter is about how to manipulate the RDF graphs to match the properties of Ch. 3.4.1. For this the query language SPARQL [spa] is used.

### Gathering Relevant Properties

First, all relevant properties must be determined. This information should normally be directly contained in the ontology of the data, by triples of the form:

<sup>4</sup><http://opendatacommunities.org/home>

(myProperty, rdf:type, owl:SymmetricProperty)

This triple states that `myProperty` is symmetric. The concept is analogous for inverse or transitive properties.

However, this is not the case with DBPedia. In their ontology such triples do not occur for the symmetric or inverse cases (only for transitive properties). Symmetric and inverse properties have to be determined in a different way. In DBPedia's ontology the equivalent properties of Wikidata <sup>5</sup> are given. Now it is possible to check in the Wikidata ontology whether the properties are symmetric or inverse, because there the information is given.

In Wordnet, transitive properties are explicitly given, but symmetric and inverse are not. It is necessary to determine them by understanding the meaning of Wordnet's relations. Properties connect different "synsets". One of those properties is **antonym**, which is like an opposite-relation between words. Therefore, the property can be seen as symmetric. The properties **hypernym** and **hyponym** are inverse. However, this only holds for nouns, not for verbs. Hence, a sub graph of Wordnet, which only contains nouns, has to be created in order to use those inverse properties. The following chapters show how the manipulations can be performed.

### Symmetric Properties

In order to remove or add symmetric properties SPARQL can be used. The code of listing 4.1 will be used to do add symmetric triples.

```
INSERT {?o ?p ?s}
WHERE{
    {?s ?p ?o}
    MINUS {?o ?p ?s}
}
```

Listing 4.1: SPARQL update for adding triples with the symmetric property `p`.

That update has to be executed for each symmetric property `p`. If it is desired to remove the second triple, a delete update would have to be executed. That delete is shown in Listing 4.2.

```
DELETE {?o ?p ?s}
WHERE{
    ?s ?p ?o .
    FILTER ( EXISTS { ?o ?p ?s } && ( str(?s) > str(?o) ) )
}
```

Listing 4.2: SPARQL update for removing triples with the symmetric property `p`.

Here it has to be taken care that not to delete both directions, this can be done by using a filter.

### Inverse Properties

Assume that `p1` and `p2` are inverse properties. Listing 4.3 is used to add the triple  $(o, p1, s)$  if  $(s, p2, o)$  already exists. That update has to be made in both directions

$(p1, p2)$  and  $(p2, p1)$

<sup>5</sup>[https://www.wikidata.org/wiki/Wikidata:Main\\_Page](https://www.wikidata.org/wiki/Wikidata:Main_Page)

in case the other direction exists. If the triples should be removed instead of adding them, a delete has to be performed which is shown in Listing 4.4

```
INSERT {?o ?p1 ?s}
WHERE{
    {?s ?p2 ?o}
    MINUS {?o ?p1 ?s}
}
```

Listing 4.3: SPARQL update for adding triples with the inverse properties p1 and p2.

```
DELETE {?o ?p1 ?s}
WHERE{
    ?s ?p2 ?o .
    FILTER (EXISTS { ?o ?p ?s })
}
```

Listing 4.4: SPARQL update for removing triples with the inverse properties p1 and p2.

### Transitive Properties

Here, the triple  $(s, p, o)$  will be removed if there exists a path from  $s$  to  $o$  via the transitive predicate  $p$  of a length of at least two edges. That can be achieved by Listing 4.5 in which a property path is used in the first line of the where clause.

Of course, it is also possible to add the triple  $(s, p, o)$  if it does not exist. That can be done similarly with an insert and is shown in Listing 4.6.

```
DELETE { ?s ?p ?o }
WHERE {
    ?s ?p/?p+ ?o.
    ?s ?p ?o
}
```

Listing 4.5: SPARQL update for removing triples with the transitive property p.

### Sub Graphs

Real datasets are quite big and it can happen that there are only a few relevant properties (symmetric/inverse/transitive). Even if there are many of those properties it can be that they do not occur often in the data. In that case, the effect of manipulating the data cannot have a big impact on the compression ratio. However, it is still desired to investigate if the effect is possibly there. Therefore, it is necessary to form a smaller graph in which those relevant properties occur often. So, a procedure to build a sub graph is needed.

First, all triples  $t_1, \dots, t_n$  are collected which contain one of the relevant properties. It would now be possible to randomly add a number of remaining triples in order to get a more diversified graph. But that would result in a graph far away from the original and would probably not contain structural patterns from the original one.

```

INSERT { ?s ?p ?o }
WHERE {
  ?s ?p/?p+ ?o.
  FILTER (NOT EXISTS { ?s ?p ?o })
}

```

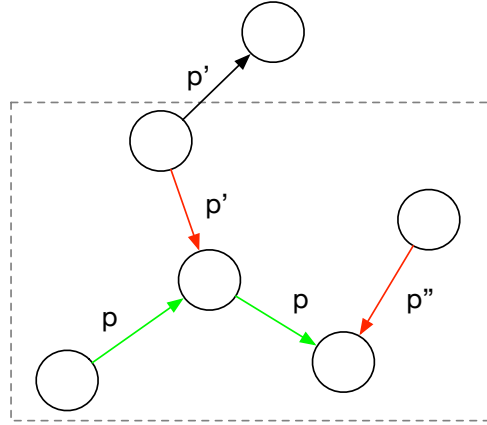
Listing 4.6: SPARQL update for adding triples with the transitive property  $p$ .

Figure 4.3: Extraction of a sub graph (marked by dashed line).

Therefore, we choose to add triples that are directly connect to the subjects or objects of  $t_1, \dots, t_n$ . By doing that, a real sub graph is extracted out of the original graph.

The procedure is illustrated in Fig. 4.3. There  $p$  is the only relevant property. Consequently, the green triples are collected in the first step. The red triples are collected in the second step, because they are connected to triples from the first step.

The results of Ch. 5.1 have also shown that GRP has a quite high run time even for smaller graphs. It was also mentioned in [MP18] that the rudimentary implementation (see Ch. 2.3.2) cannot handle very large graphs. However, we still want to evaluate GRP for real datasets which are often very large. To solve this problem, a realistic sub graph of the big graphs has to be extracted. As mentioned earlier, choosing random triples does not fulfill that. Hence, we choose an approach similar to the one shown in Fig. 4.3. But here we start with some entity  $e$  (not with a set of desired properties). Analogously to the other approach, we gather all triples  $e$  is part of and then add triples which the newly gathered entities  $e_1, \dots, e_n$  are part of. That step is repeated a few times until some defined number of triples has been reached. The result graph is called  $e$ -based subgraph.

### 4.2.3 Dictionary Improvements

For the dictionary improvements, HDT's dictionary compression is used as a basis. Therefore, the HDT-Java code <sup>6</sup> has been extended.

#### Literals

As already mentioned in Ch. 3.4.2, literals will be compressed using a Huffman code. To achieve that, HDT is changed such that it does not compress literals by prefix trees, but rather gives the literals to the newly created `HuffmanHandler`, which compresses all literals and finally stores

<sup>6</sup><https://github.com/rdfhdt/hdt-java>

them in a binary format. In order to make that possible, the `HuffmanHandler` has to traverse all literals in the beginning of the compression to establish a Huffman Tree.

In addition, the Huffman code/tree itself has to be stored in order to be able to decompress the data. There is no standard way for storing the binary tree. One approach can be seen in Algorithm 3 which has to be started at the root node. That method creates an unambiguous bit representation of the tree. It traverses the tree in a depth-first-search-manner and writes a one if the current node's character in case the current node is leaf. Otherwise it writes a zero and the procedure is then called recursively for the current node's children. This encoding is unambiguous, because each node is either a leaf or has exactly two children.

---

**Algorithm 3** EncodeNode (TreeNode node)

---

```

1: if node is leaf then
2:   writeBit(1)
3:   writeCharacter(node.character)
4: else
5:   writeBit(0)
6:   EncodeNode(node.leftChild)
7:   EncodeNode(node.rightChild)

```

---

Alternatively, there are pre-computed Huffman trees for natural languages such as English. There, it has already been investigated which letter occurs how often in English texts and in this way a generally valid Huffman code has been established. The advantage is that the Huffman tree does not have to be stored and it does not have to be calculated, which saves runtime. The disadvantage, however, is that the tree is not optimal for the text to be compressed, as it is more general. Another problem in our case is that the literals contain a lot of special characters that are not taken into account in prefabricated Huffman codes. Therefore, prefabricated codes will not be used.

### Blank Nodes

HDT normally uses the arbitrary and long strings generated by the Jena API and tries to compress them using prefix trees.

Now, two approaches, which have both been implemented, for improving the compression of blank nodes are presented.

The first approach is to use shorter IDs (e.g. numbers from 1 to  $n$ ). Then, during the run time a mapping from old ID to new ID is maintained by the new class `BlankNodeHandler` in order to make sure that the same blank node will get the same new ID if it occurs multiple times. That mapping does not have to be stored persistently and will therefore be omitted once the compression is finished.

The second approach is to omit blank node IDs completely. The HDT code is changed in such a way that skips blank nodes in the process of storing the dictionary. HDT must then be changed so that it can handle the case in which it does not find a corresponding string in the dictionary for a certain short ID. At this point it would know directly that the considered node is a blank node and the longer blank node ID is unimportant. Such a situation will occur when a decompression is performed. That mechanism has not been implemented, because this thesis is only interested in potential compression ratio improvements.





This chapter is about the evaluation of the several approaches presented in Ch. 3 and 4. First, the comparison of GRP and HDT is evaluated. Second, the evaluation results for the compression improvements are presented.

For the following experiments, HDT-Java 2.0 <sup>1</sup> (the currently newest version) has been used. For GRP the implementation presented in Ch. 2.3.2 has been used. The evaluated datasets are the ones introduced in Ch. 4.2.1.

## 5.1 GRP vs HDT

This chapter shows the evaluation results of the comparison between HDT and GRP. First, result for the synthetically generated graphs from Ch. 4.1 will be presented. Afterwards, the two compressors will also be evaluated for real world data.

### 5.1.1 Results for Synthetic Data

Fig. 5.1 shows the results for the synthetically generated data (see Ch. 4.1). Fig. 5.1a shows the compression ratios without the size of the dictionary. As expected,  $CR_{Graph_{HDT}}$  gets bigger as the graphs are further away from the hub pattern. Moreover,  $Graph_{GRP}$  compresses better if the graph is similar to the star pattern (greater value of  $SPS$ ), as stated earlier. It is noticeable that  $CR_{Graph_{GRP}}$  fluctuates much more than  $CR_{Graph_{HDT}}$  and the impact of the star pattern similarity is much higher for  $Graph_{GRP}$ .

Fig. 5.1b shows the values of  $CR_{HDT}$  and  $CR_{GRP}$ . It can be seen that the curves behave differently than in Fig. 5.1a, since the dictionary size  $|out_{dict}|$  is much bigger than  $|out_{graph}|$ . As both GRP and HDT use the same dictionary compressor ( $Dict_{HDT}$ ), they have been increased by the same amount and therefore  $CR_{GRP}$  is smaller than  $CR_{HDT}$ . Furthermore, it is noticeable that  $|out_{dict}|$  is bigger when the graph is further away from the star pattern.  $Dict_{HDT}$  seems to be more inefficient when there are about as many subject as objects.

Apart from the compression ratio, the run time is also important for the overall performance. Fig. 5.2 shows the average value of  $CT$  for both compressors, respectively. For this, the same scenario with the star pattern (and only one distinct predicate) was used. It has been executed 100 times to get a sophisticated run time measurement, because  $CT$  depends on the current CPU workload of the computer. Decompression is not supported by the currently implemented version of GRP and therefore decompression evaluations will be omitted.

<sup>1</sup><https://github.com/rdfhdt/hdt-java/releases/tag/v2.0>

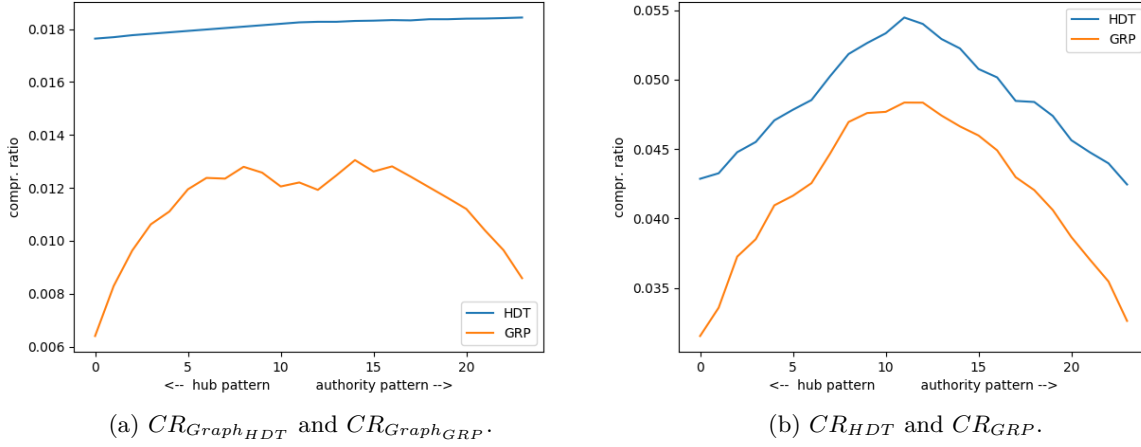


Figure 5.1: The compression ratios for GRP and HDT without and with dictionary sizes.

It can be seen that  $CT_{GRP}$  is significantly higher than  $CT_{HDT}$ . It is on average ca. 48 times as high. However, it should also be noted that the implementation of GRP is rather rudimentary (according to the authors of [MP18]), while that of HDT has been under development for some time. So they are not comparable in terms of quality. Unfortunately, it is not possible to say whether a more professional implementation of GRP will also be slower than HDT.

In Ch. 4.1, it was mentioned that only one distinct predicate will be used in the first comparison. However, it will now be shown how the compressors behave as that number of predicates increases. To realize that, the whole procedure from Ch. 4.1 is executed a few times with an increasing number of predicates each time. The plots for those executions is shown in Fig. 5.3. The  $Graph_{HDT}$  curves can be recognized by the low fluctuations and the monotonic growth, whereas the  $Graph_{GRP}$  curves fluctuate more and do not have monotonic behavior. For both algorithms, the  $CR_{Graph_C}$ -values get bigger as the number of predicates increases. For instance, the first  $Graph_{GRP}$  curve is the blue one, the second is the green curve. The curves with same colors have to be compared, since those pairs have the same number of predicates. The third execution is marked by the dashed red lines, because this is the first case in which  $CR_{Graph_{HDT}} < CR_{Graph_{GRP}}$  is true. So, there are cases in which  $Graph_{HDT}$  compresses better. That continues, as the number of predicates is further increased. Hence, higher amounts of predicates have a higher impact on  $Graph_{GRP}$  than on  $Graph_{HDT}$ . However, the next chapter will show that there is no fixed value for  $ELR$  at which  $Graph_{HDT}$  is always better.

### 5.1.2 Results for Real Data

The previous chapter used synthetic data to detect the behavior of the compressors to certain changes in the structure of the input data. Now, real data will be used to compare the compression ratios of  $Graph_{HDT}$  and  $Graph_{GRP}$ . For this, several datasets will be used (DBPedia, Semantic Web Dog Food, WikiData and Open Government Data).

33 different RDF graphs are used. On 31 of those  $Graph_{GRP}$  achieves a better compression ratio than  $Graph_{HDT}$ . On average,  $CR_{Graph_{HDT}}$  is 1.8 times higher than  $CR_{Graph_{GRP}}$ .

In order to investigate the correlation between the pairs  $(CR_{Graph_C}, ELR)$  and  $(CR_{Graph_C}, SPS)$  the Spearman correlation<sup>2</sup> is used. That function produces values from  $-1$  to  $1$ . Negative values imply a negative correlation, positive values imply a positive correlation. The value  $0$  means

<sup>2</sup>[https://en.wikipedia.org/wiki/Spearman%27s\\_rank\\_correlation\\_coefficient](https://en.wikipedia.org/wiki/Spearman%27s_rank_correlation_coefficient)

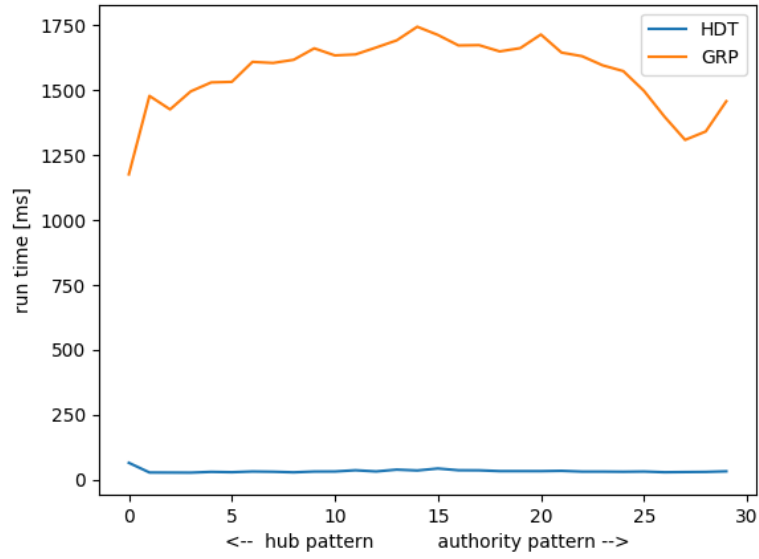


Figure 5.2:  $CT_{HDT}$  and  $CT_{GRP}$  (Average run time of 100 consecutive executions).

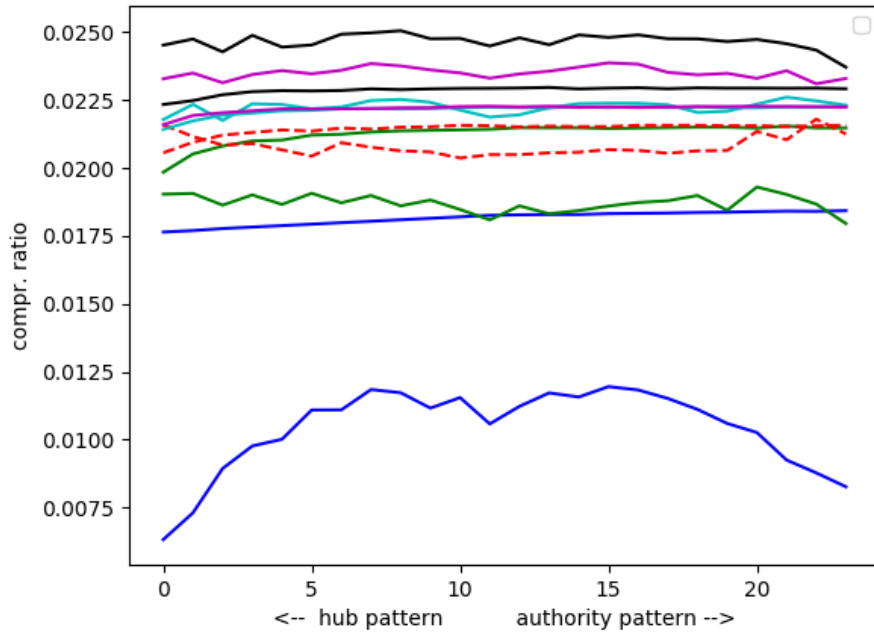


Figure 5.3:  $CR_{Graph_C}$ -values for HDT and GRP. GRP's curves can be recognized by the higher fluctuations. Same colors indicate that the number of distinct predicates is the same. The two dashed lines show the first case in which  $CR_{Graph_{HDT}} < CR_{Graph_{GRP}}$  holds.

that there is no correlation. The results are shown in Tab. 5.1. Due to the value 0.646 it becomes clear that higher numbers of different predicates bring a higher compression ratio for  $Graph_{GRP}$ . In contrast, a higher value of  $SPS$  implies a lower compression ratio for  $Graph_{GRP}$ , as expected. But the correlation is not as strong as with  $ELR$ .

$CR_{Graph_{HDT}}$  has a positive correlation with  $ELR$ , but that correlation is quite small. The correlation between  $CR_{Graph_{HDT}}$  and  $SPS$  is positive (but very close to 0) which is reasonable, since  $Graph_{HDT}$  only benefits from hub pattern, but  $SPS$  is defined for the general star pattern.

	$CR_{Graph_{GRP}}$	$CR_{Graph_{HDT}}$
$ELR$	0.646	0.181
$SPS$	-0.381	0.009

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genießen

Table 5.1: Spearman correlation values.

Fig. 5.4 and 5.5 show the compression ratios for the datasets, respectively. It has to be noticed that values of  $CR_{Graph_C}$  are not comparable between different RDF files. This is due to the fact that  $CR_{Graph_C}$  does not take the dictionary into account. Hence, if two files  $f_1, f_2$  have the same graph structure, but  $f_1$  is using longer URIs than  $f_2$ , then  $CR_{Graph_C}$  will be smaller for  $f_1$  (because  $|f_1| > |f_2|$ ). So, only the values for one graph/file should be compared.

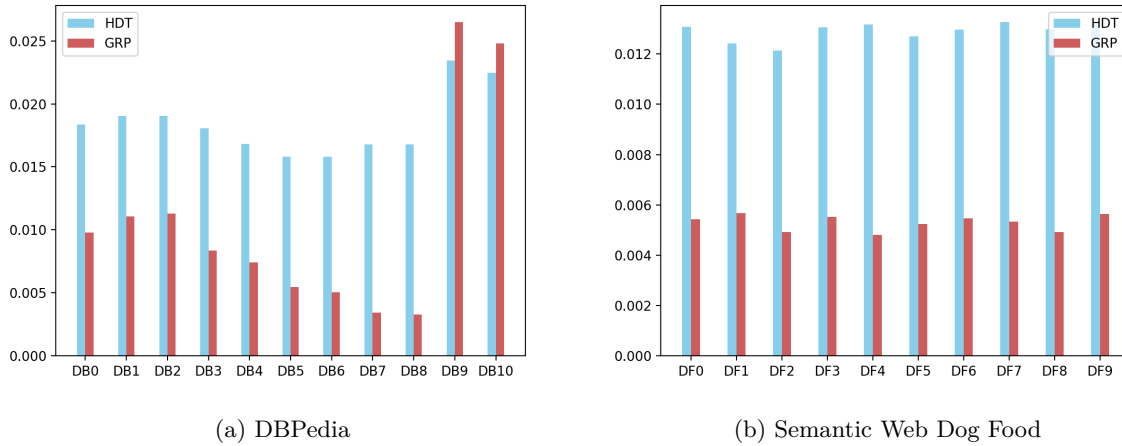


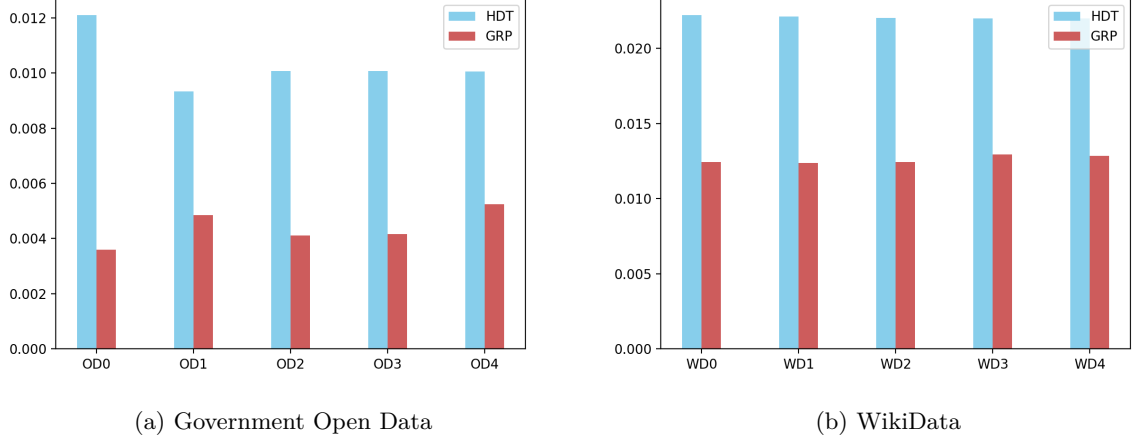
Figure 5.4:  $CR_{Graph_{HDT}}$  and  $CR_{Graph_{GRP}}$ .

## 5.2 Compression Improvements

This chapter evaluates the compression improvements. First, results for the graph compression improvements are discussed. Then, results for the dictionary compression improvements are presented. In the end, both approaches will be combined in a final evaluation.

### 5.2.1 Ontology Knowledge

In this chapter, it will be evaluated whether using meta data from the ontology can result in a better compression ratio for  $Graph_{GRP}$ . Here, not only the file size of the output ( $|out_{graph}|$ ) will be measured. Since these approaches have the intention to improve the ability for  $Graph_{GRP}$  to


 Figure 5.5:  $CR_{GraphHDT}$  and  $CR_{GraphGRP}$ .

produce a smaller grammar, the features of that grammar will be presented in more detail. That is because after the encoding of the grammar it might happen that, despite the fact that the grammar is smaller after the manipulations, that effect is not visible in the value of  $|out_{graph}|$ .

### Occurrence of Properties

First, it is interesting to consider how often the relevant properties occur in real datasets. For that, DBpedia and Wordnet will be analyzed. Fig. 5.6 shows how often the relevant properties occur. (Relative amount =  $\frac{\text{number of occurrences}}{\text{number of triples}}$ ). It can be noticed that the amounts are quite low. This supports the hypothesis from Ch. 4.2.2 that building sub graphs with higher amounts of relevant properties is necessary to observe a real effect of the data manipulations. Consequently, those sub graphs (see Ch. 4.2.2) are used in the following evaluations.

Another interesting feature of the datasets is how many different relevant properties they contain. Fig. 5.7 illustrates the results. It can be concluded that these numbers of are quite low, especially for symmetric properties, considering the fact that these datasets are very large (millions of triples). That is also a reason for the low relative amounts in Fig. 5.6.

### Evaluation Process

Now, the overall process of applying ontology knowledge and evaluating whether it results in a better compression is explained. Fig. 5.8 shows the implemented of the process. First, the original graph or sub graph is given to GRP. That part is called  $in_1$  in Fig. 5.8 and it will deliver the first result  $out_1$ .

In the next step, relevant properties have to be determined and the original graph will be manipulated. Then the manipulated graph is given to GRP. In addition, the relevant ontology triples have to be compressed and stored as well. Otherwise, the original graph could not be restored. Both graphs together are merged together into one graph called  $in_2$  which is then compressed by GRP and the result is called  $out_2$ .

Finally,  $|out_1|$  and  $|out_2|$  have to be compared. The next chapter will explain how that is done. The evaluation process must be executed for the different manipulation aspects (symmetric, inverse etc.) independently. So, there is one manipulated graph where all symmetric edges are added or removed, and analogously for the other manipulations. Finally, it is also possible to

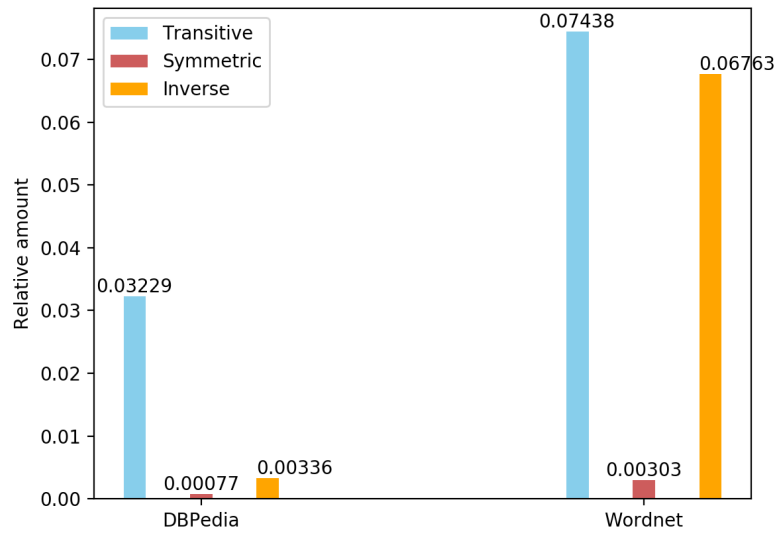


Figure 5.6: Relative amount of transitive/symmetric/inverse properties in real datasets.

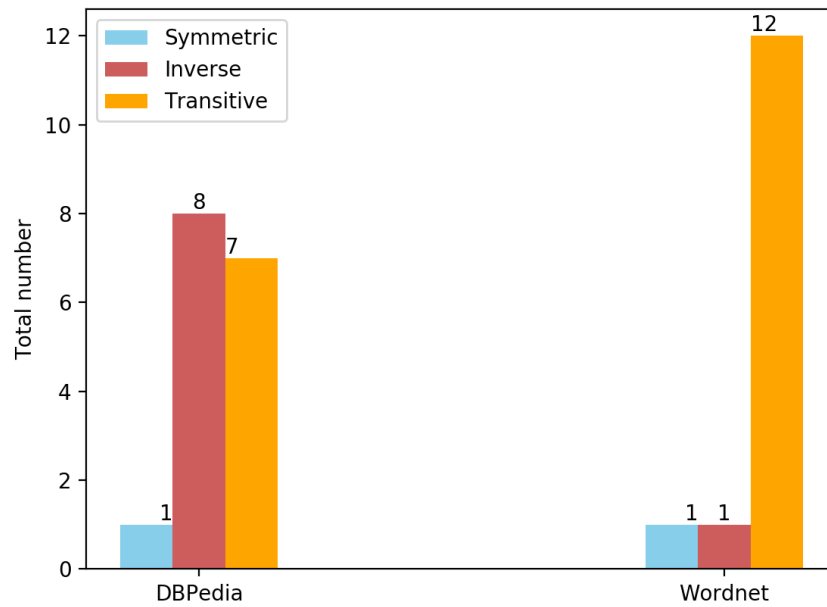


Figure 5.7: Number of different relevant properties for DBPedia and Wordnet.

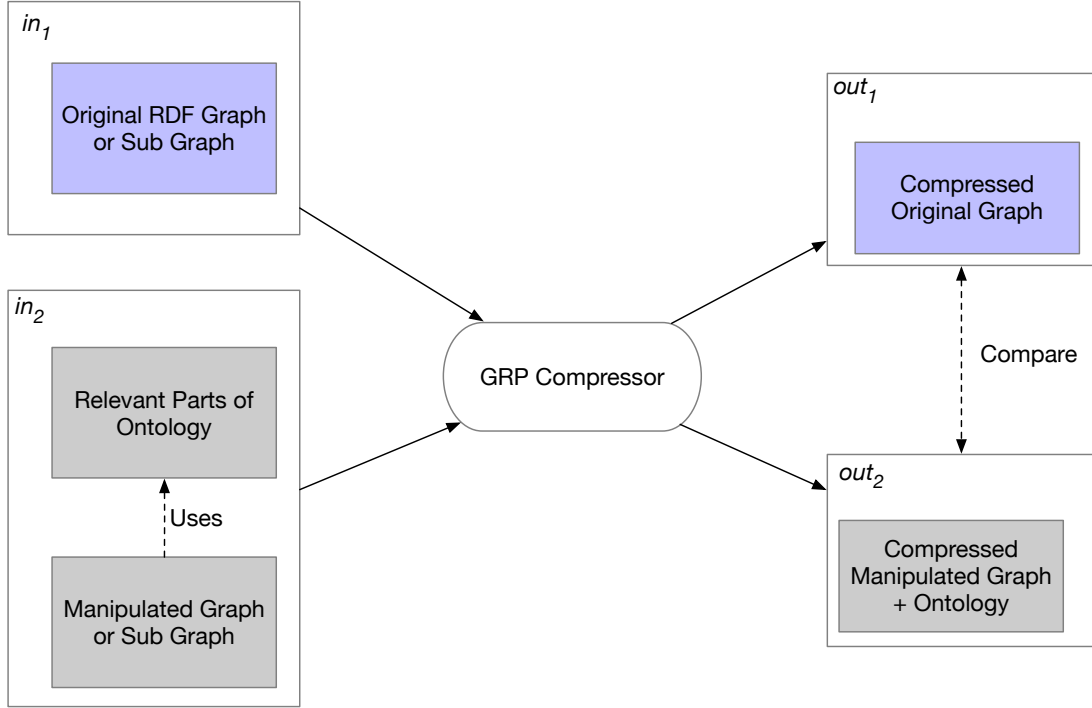


Figure 5.8: Overall process of applying ontology knowledge and comparing the compression results.

execute the process for one graph in which all different manipulations have been applied. This way, it is noticeable what the manipulations bring individually. A combined evaluation will be done in Ch. 5.2.3.

## Metrics

This chapter explains how the two outputs  $out_1$  and  $out_2$  are compared. Since the ontology-based manipulations are intended to achieve a better compression by enabling  $Graph_{GRP}$  to produce a smaller grammar, it is interesting to not only compare  $out_1$  and  $out_2$  at the file size level, but also in terms of their grammar/graph sizes. A reasonable metric for the size of a grammar/graph is its number of edges. In order to compare  $out_1$  and  $out_2$  with respect to their grammar/graph edge amounts, the metrics Input Edge Ratio ( $IER$ ) and Output Edge Ratio ( $OER$ ) are defined:

$$IER = \frac{\text{number of edges in } in_2}{\text{number of edges in } in_1}$$

$$OER = \frac{\text{number of edges in } out_2}{\text{number of edges in } out_1}$$

$IER$  shows how many edges have been added or removed by the manipulation which indicates how big the impact of the manipulation is.  $OER$  shows whether the manipulation results in a better ( $OER < 1$ ) or worse ( $OER > 1$ ) compression ratio.

In order to measure the manipulation it is necessary to define a new metric instead of re-using  $CR_{Graph_{GRP}}$  as defined in Ch. 3.1.2. For  $out_1$ ,  $CR_{Graph_{GRP}}$  would be in relation to  $in_1$

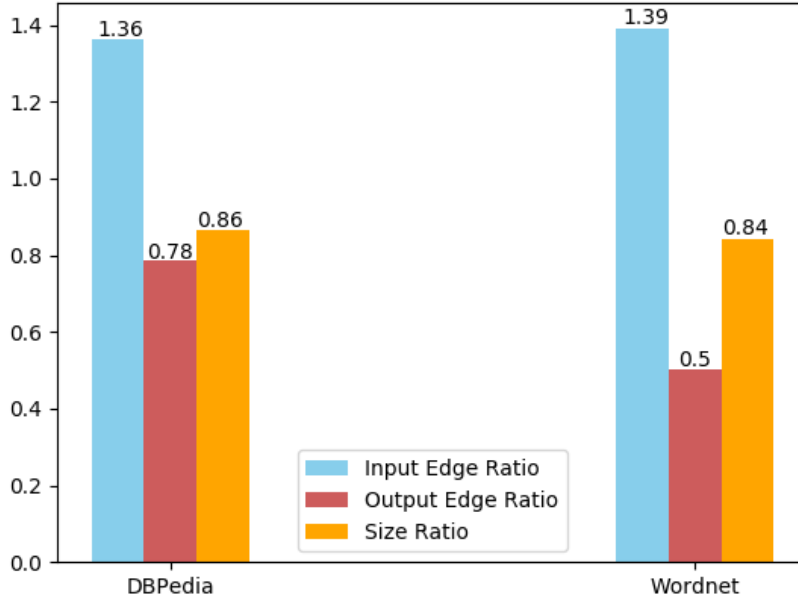


Figure 5.9: Results for adding symmetric properties, on the grammar level ( $IER$ ,  $OER$ ) and on the file size level ( $SR$ ).

(analogously for  $out_2$  and  $in_2$ ). But here it is necessary to compare  $out_1$  and  $out_2$ . Therefore, the new metric Size Ratio ( $SR$ ) is defined as follows:

$$SR = \frac{|out_{graph_2}|}{|out_{graph_1}|}$$

Here,  $out_{graph}$  is used instead of  $out$ . Normally, the dictionary size ( $out_{dict}$ ) should also be taken into account, because the added ontology triples have increased  $|out_{dict_2}|$ . However, due to the very small amount of relevant properties that increase is not even noticeable and can be omitted. If  $SR < 1$  holds then the manipulation has resulted in an improvement at the file size level, otherwise not. Of course, the file size level is in the end more relevant than the grammar level, because it is the real amount necessary to store the compressed data.

### Symmetric Properties

First, the approach suggested in Ch. 3.4.1 to add all possible triples with symmetric edges will be evaluated. Fig. 5.9 illustrates the results. As expected,  $IER$  is bigger than 1, as edges have been added to the graph. For both DBPedia and Wordnet  $IER$  is about 1.4. Also, it can be noticed that  $OER < 1$  holds, which means that adding symmetric triples is indeed beneficial for  $Graph_{GRP}$  and even brings a significant improvement on the grammar level as  $OER$  is about 0.8 for DBPedia, and about 0.5 for Wordnet.

Furthermore,  $SR < 1$  is true. Hence, also on the file size level the manipulation has delivered a better result. However, the improvement is not as good as on the grammar level. So, the statement from Ch. 2.3.2, that the encoding does not always work well, is supported by these results.



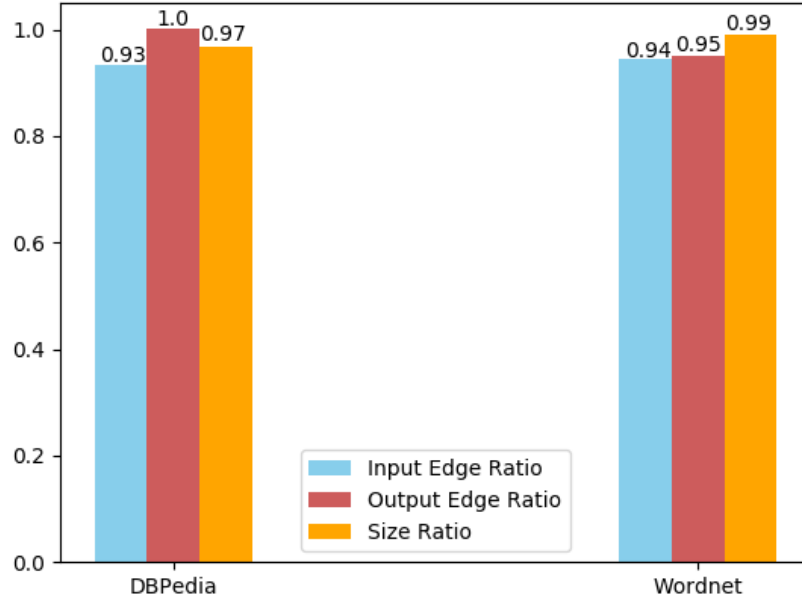


Figure 5.10: Results for deleting symmetric properties, on the grammar level ( $IER$ ,  $OER$ ) and on the file size level ( $SR$ ).

In order to show that adding symmetric properties is more beneficial than removing them, the results of the removal case are also shown (see Fig. 5.10). There, it is possible to see that  $IER < 1$  holds, since edges have been removed. But  $IER$  is still quite close to 1, because there are not many cases in which an edge could be removed. Hence, in most cases only one of the two directions for symmetric properties is present in the graph. Both  $OER$  and  $SR$  are close or equal to 1, which indicates that adding symmetric edges is more beneficial for  $Graph_{GRP}$ . Nevertheless, it can still be argued that there are only a few cases in which edges were removed and that the potentially positive effect is therefore not recognizable. To further investigate the removal case, the decompressed version of the graph  $out_2$  from Fig. 5.10 is taken as the input  $in_1$  for a new evaluation. So,  $in_1$  will be an artificial graph in which for each symmetric property only one direction of the triples exist. This extreme case can show whether adding or removing symmetric edges will be better, since  $in_1$  is a graph where all symmetric edges have been removed before hand.

The evaluation results are illustrated in Fig. 5.11. Of course,  $IER > 1$  is true and  $IER$  is bigger than in Fig. 5.9, since a higher amount of edges has been added. The fact that both  $OER$  and  $SR$  are lower than 1, support our hypothesis that adding symmetric edges is more beneficial than removing them. So, we conclude that adding symmetric edges enables  $Graph_{GRP}$  to find more digrams, and thus producing a smaller grammar.

### Inverse Properties

Next, the manipulation based on inverse properties is being evaluated. First, the approach presented in Ch. 3.4.1 (adding triples with inverse properties) is considered. The results are shown in Fig. 5.12. For DBpedia, the size of the input graph has already been doubled ( $IER = 2.1$ ). But  $OER = 0.99$  is almost 1, thus the manipulation has not resulted in a better end result

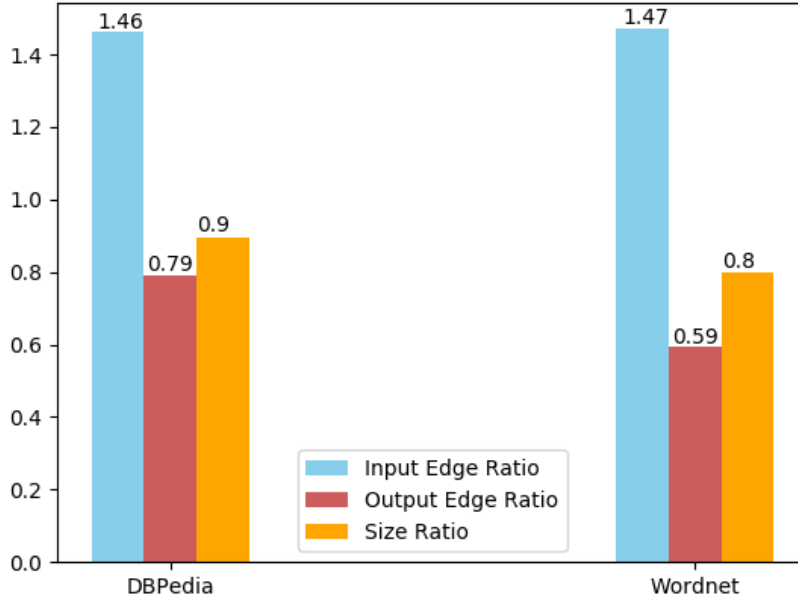


Figure 5.11: Results for adding symmetric properties, on the grammar level ( $IER$ ,  $OER$ ) and on the file size level ( $SR$ ). In contrast to Fig. 5.9, the input graph  $in_1$  contains only one direction for each triple with a symmetric property.

for DBPedia.  $SR$  is even bigger than 1, so the end result is worse on the file size level.

For Wordnet,  $IER$  is smaller than for DBPedia and more importantly,  $OER$  is significantly smaller than 1. Hence, in this case, the manipulation has delivered a positive result. On the file size level, the result is also better ( $OER = 0.9$ ).

In the case of DBPedia, a reason for the negative result can be that DBPedia has a relatively high number of different inverse properties. Therefore, adding all the edges with many different URIs to the relatively small graph in Fig. 5.12 (2000 triples) does not have an effect that is positive enough to compensate the high amount of edges added to it. In order to further investigate that, a graph that is ten times bigger, is created. The results for it are shown in Fig. 5.13. It can be seen that the results are now much better. While  $IER$  is about 2 again,  $OER = 0.85$  is now much smaller and also  $SR = 0.91$  is smaller. So, it can be stated that adding inverse properties has a positive effect on the graph compression potential, as mentioned in Ch. 3.4.1. The opposing approach (removing triples with inverse properties) is not explicitly evaluated here, because in Fig. 5.12 and 5.13 it is already recognizable that a graph with less inverse pairs of triples produces a worse compression ratio.

### Transitive Properties

The final evaluated ontology-based manipulation is adding or removing triples with transitive properties. The problem with the transitive case is that it is more restrictive than the others (symmetric or inverse). It is therefore more difficult to find data where this manipulation can be executed. In DBPedia, we could not find a graph in which *transitive paths* exist (defined in Ch. 3.4.1). Thus, only Wordnet will be used here, since it contains *transitive paths*.

First, the approach suggested in Ch. 3.4.1, to remove *direct transitive paths*, is evaluated. Unfor-

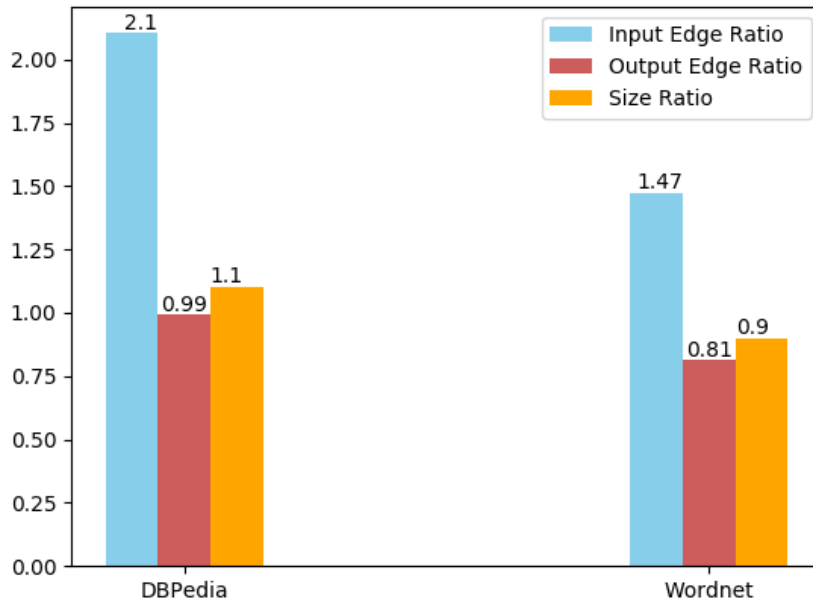


Figure 5.12: Results for adding inverse properties, on the grammar level ( $IER$ ,  $OER$ ) and on the file size level ( $SR$ ).

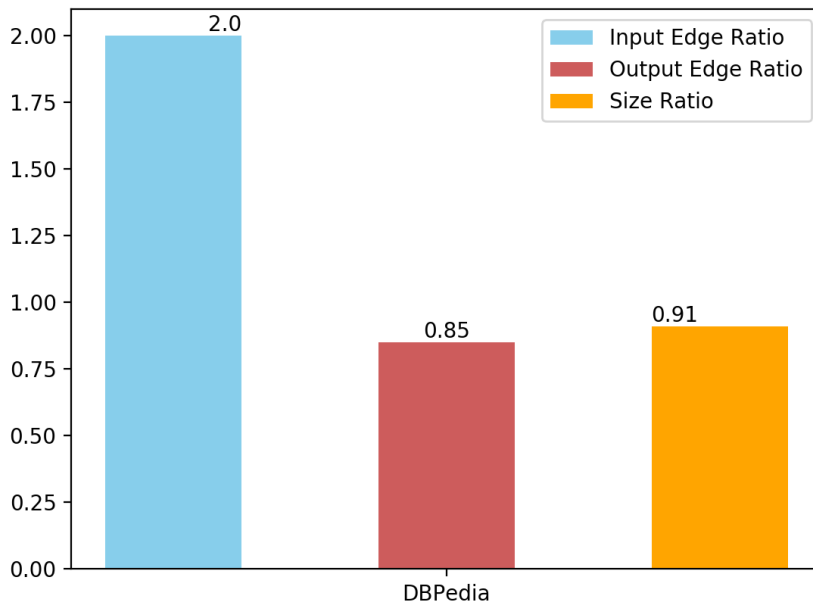


Figure 5.13: Results for adding inverse properties, on the grammar level ( $IER$ ,  $OER$ ) and on the file size level ( $SR$ ). DBpedia graph is now 10 times bigger than in Fig. 5.12.

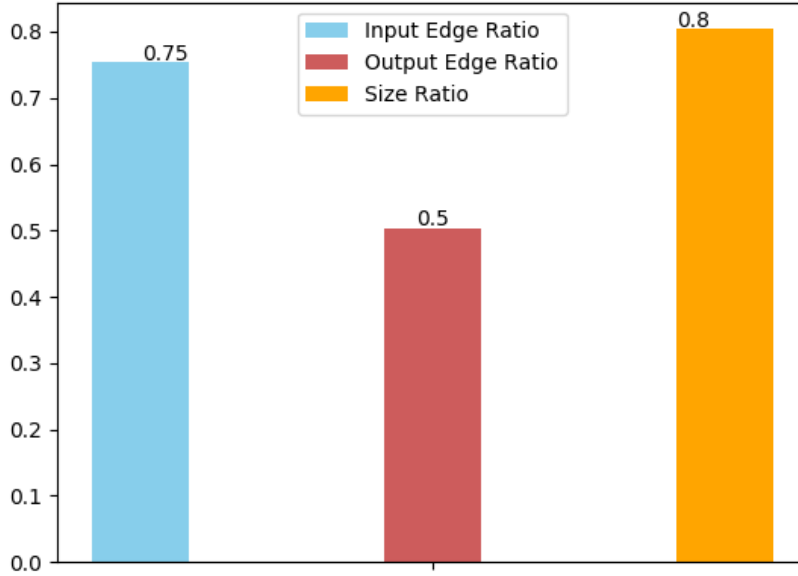


Figure 5.14:  $IER$ ,  $OER$  and  $SR$  for removing transitive edges in Wordnet.

Unfortunately, those edges do not exist in Wordnet. To circumvent that problem, an artificial graph has been created in the following way: The original graph has been divided into two halves (via its list of triples). In the first half, all possible *direct transitive paths* are added. Afterwards, the manipulated first half is merged with the untouched second half again. This gives us a graph in which both adding and removing *direct transitive paths* is possible. So, both approaches can be evaluated.

The results for removing *direct transitive paths* can be seen in Fig. 5.14.  $IER$  is about 0.75, as several edges have been removed.  $OER$  is about 0.5, which means that the removals have delivered a significant improvement on the grammar level. It could be argued that the improvement is only due to the reduced size of the graph. But this is not the case, since  $OER < IER$  holds. Hence, due to the removed *direct transitive paths*,  $Graph_{GRP}$  could indeed find more digrams, as stated in Ch. 3.4.1. On the file size level, the improved compression is also visible, because  $SR \approx 0.88$  is less than 1. Again, the improvement is not as good as on the grammar level.

Next, the opposing approach (adding *direct transitive paths*) is evaluated. The results are illustrated in Fig. 5.15. Obviously,  $IER > 1$  holds, since many edges have been added.  $OER \approx 3.5$  is significantly high, which means that adding *direct transitive paths* has resulted in a much larger end result, on the grammar level. In contrast to Fig. 5.14,  $IER < OER$  holds here, but that supports the hypothesis that adding *direct transitive paths* makes  $Graph_{GRP}$  find less digrams (see Ch. 3.4.1). On the file size level,  $SR \approx 1.8$  is higher than 1, but the result is not as bad as on the grammar level.

Thus, it can be concluded that removing *direct transitive paths* results in a better compression, and adding them delivers a worse compression. Although *direct transitive paths* do not exist in the considered datasets, they still can exist in other datasets. The evaluation results have shown that removing *direct transitive paths* leads to a insignificant improvement.

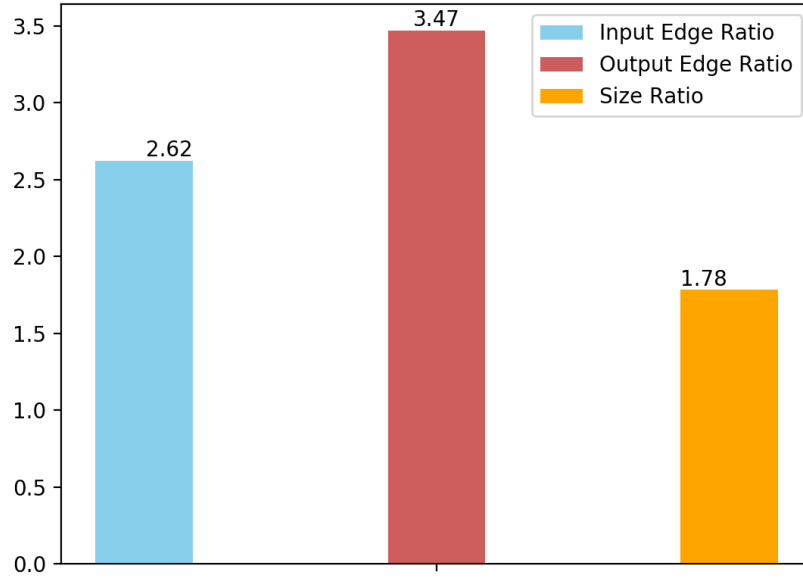


Figure 5.15:  $IER$ ,  $OER$  and  $SR$  for adding transitive edges in Wordnet.

### 5.2.2 Dictionary Improvements

This chapter evaluates the approaches from Ch. 4.2.3 which are intended to improve the dictionary compressor  $Dict_{HDT}$  which is used by HDT and GRP. First, the Huffman compression of literals is evaluated and afterwards, the improvements regarding blank node IDs.

#### Literals

As already mentioned, a self-generated Huffman code was used to compress the literals of an RDF graph, as it is likely to get a better compression than the with the prefix-based compression of HDT.

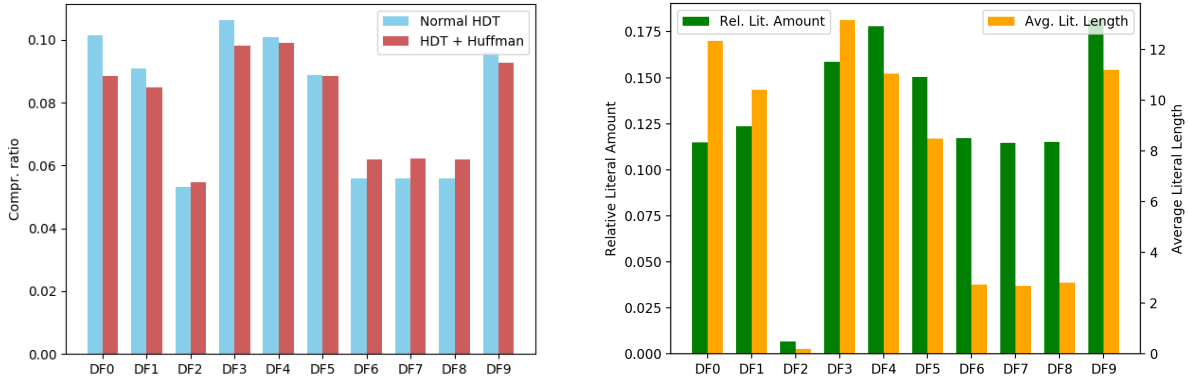
Now the results of the evaluation are presented. First, the Semantic Web Dog Food data set is used. This is well suited for an evaluation, since both literals and URIS are included here. Fig. 5.16a shows  $CR_{Dict_{HDT}}$  for a subset of the data (DF0 - DF9).

It can be seen that the use of the Huffman code only brings a small improvement in some cases. In some cases Normal  $Dict_{HDT}$  even compresses better than  $Dict_{HDT}$  with Huffman.

This is because the data does not have a very high proportion of literals. Also, literals are rather short here. This can be seen in Fig. 5.16b showing the relative proportion of literals and the average length of a literal. The proportion of literals in the triples is never higher than 17.5% and the highest average literal length is about 12. Hence, these are single words rather than whole texts. Only in cases where both the proportion and the literal length are relatively high, an improvement can be seen (e.g. DF9).

Next, the DBPedia data set is considered, because it has a different structure of data. Here, graphs are considered which contain the abstracts of Wikipedia, because these are longer texts. In addition, there are abstracts in different languages, so it can be seen whether some languages are better suited for Huffman than others.

Fig. 5.17a shows  $CR_{Dict_{HDT}}$  for the abstract files. The abbreviations stand for the languages the

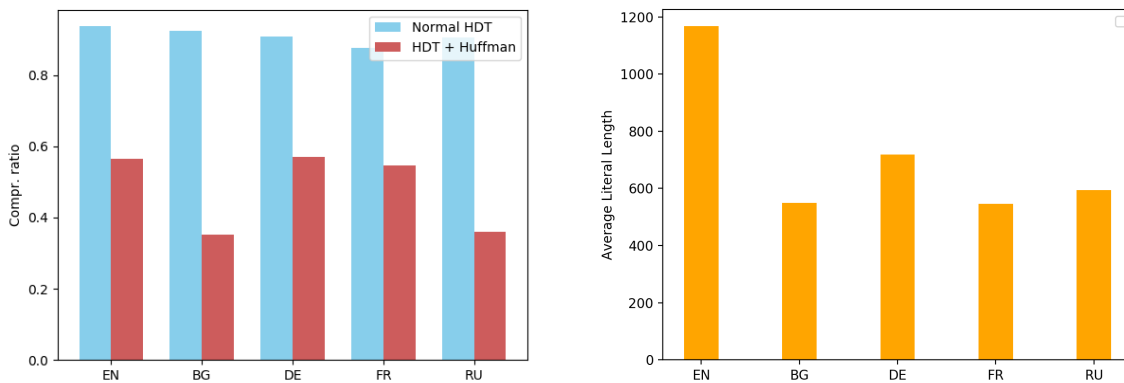


(a)  $CR(out_{dict})$  for Normal HDT and HDT + Huffman (b) Relative amounts of literals and average literal length.

Figure 5.16: Relation between literal percentage and literal length (right) and  $CR(out_{dict})$  (left) for Semantic Web Dog Food Data.

abstracts are written in. It can be seen that Huffman significantly improves  $CR_{Dict_{HDT}}$  here. The reason for this can be seen in Fig. 5.17b, where the average literal length is illustrated. The relative proportion of literals is not shown this time, since it is 100% for all files. The average literal length varies between languages, but is generally much higher than in Semantic Web Dog Food. Therefore, the improvement is much greater here.

Another phenomenon can also be seen here: Although the English file contains the longest literals by far, the improvement by Huffman here is not as big as, for example, in the Bulgarian file. In the English case, the Huffman code is less effective, because there are fewer different characters than in the other languages. Huffman is generally more efficient on large alphabets, according to [Sha10].



(a)  $CR(out_{dict})$  for Normal HDT and HDT + Huffman.

(b) Average literal length.

Figure 5.17: Relation between literal length (b) and compression ratios (a) for DBpedia Abstracts (Abbreviations denote the languages the abstracts are written in).

As mentioned above, saving the Huffman code means almost no additional storage effort. The average fraction of the Huffman code is about 0.1% and was therefore not displayed in the

visualizations.

Since the calculation of the Huffman code increases the runtime of the whole compression, it is now considered how big this effect is. Fig. 5.18a shows  $CT$  for the compression of the DBPedia abstract data. Here,  $CT$  has been increased very much. This is because  $Dict_{HDT}$  can normally compress very little with this data, due to the numerous long literals and is therefore finished quite quickly. With Huffman the data can be compressed much better and it takes quite a long time. Here, especially the creation of the Huffman tree is expensive.

Fig. 5.18b shows  $CT$  for the Semantic Web Dog Food data, where the run times are only slightly longer, because Huffman hardly improves the compression.

Generally, it can be said that the use of a standard Huffman code could be worthwhile because of the otherwise high runtime. At this point, however, the evaluation with such a standard code was omitted, since such existing codes do not contain all the special characters that occur in RDF data.

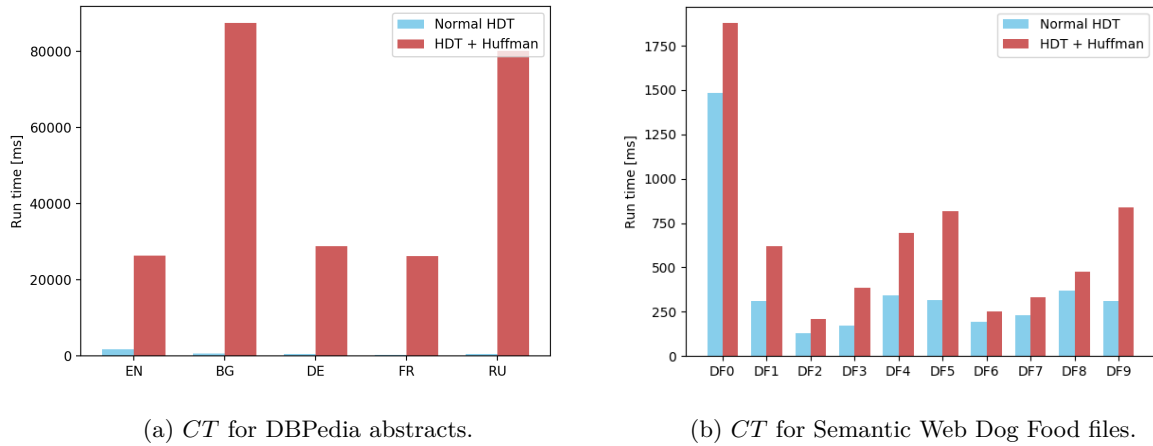


Figure 5.18: Run times ( $CT$ ) for Normal HDT and HDT + Huffman.

## Blank Nodes

This chapter evaluates the two approaches mentioned in Ch. 3.4.2 to store blank node IDs more efficiently. For that, the Nuts-RDF dataset is used as it contains solely blank nodes as subjects and objects. It is therefore prone to show the inefficiency of the prefix-based compression of  $Dict_{HDT}$  with respect to blank nodes. Fig. 5.19 shows the results for three different files from Nuts-RDF. It can be seen that Normal  $Dict_{HDT}$  even produces the result  $CR_{Dict_{HDT}} > 1$ . This is due to the fact that GC1-GC3 are in the turtle format which already reduces redundancy, since it does not store all triples extensively, like N-Triples does. Also, it does not use blank node IDs that are as long as those used by  $Dict_{HDT}$ . Using short IDs already brings a significant improvement as it delivers a compression ratio between 0.76 and 0.89. So, the compression is now really reducing the size of the files. Omitting the blank node IDs results in further slight improvement which is small, because storing the short IDs as numbers from 1 to  $n$  costs almost no memory size. Hence, it could be sufficient to use shorter IDs, because omitting IDs would imply more programming effort, as explained in Ch. 4.2.3.

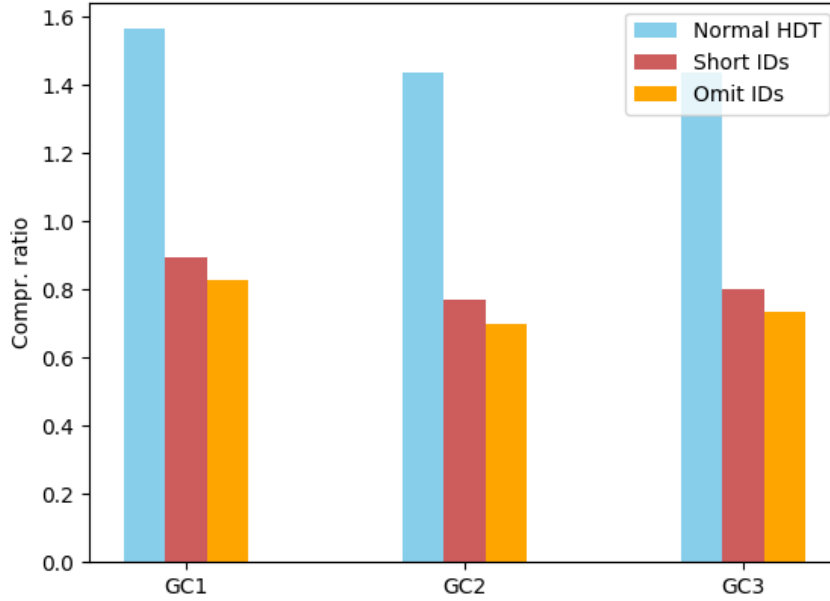


Figure 5.19: Results for Blank Node ID improvements for Geo Coordinates (GC) files. **Normal HDT** uses long IDs. **Short IDs** uses integer IDs. **Omit IDs** does not store the IDs at all.

### 5.2.3 Final Results

In the previous chapters, the compression improvements (graph and dictionary) were evaluated individually. This final evaluation chapter compares all improvements together. This makes it possible to see which improvement accounts for which portion of the overall improvement.

In order to realize this, an RDF graph is generated from several graphs. The graph used in Ch. 5.2.1 serves as a basis. However, there are not many long literals in it. Therefore, the DBpedia abstract text is added for each person in the graph (from the abstract data set from Ch. 5.2.2). Next, blank nodes are added to the graph. Thus, the coordinates (polygons) for each country of the graph are added. The data set from Ch. 5.2.2 is used for that. Finally, this results in a graph on which all improvements can be evaluated.

Fig. 5.20 shows the graph compression improvements. For the ontology-based improvement of  $Graph_{GRP}$  we write  $Graph_{GRP+Ont}$ . It can be seen that  $Graph_{GRP}$  already compresses better than  $Graph_{HDT}$ .  $Graph_{GRP+Ont}$  brings only a small improvement. This due to the encoding problem discussed in Ch. 5.2.1.

Fig. 5.21 shows the results regarding the dictionary compression. By  $Dict_{HDT++}$ , the improved HDT dictionary compression (literals and blank node IDs) is denoted. Here, the improvement is significant although the used RDF graph does not contain as much literals as the abstract graphs used in Ch. 5.2.2.

Finally, Fig. 5.22 shows both the graph and dictionary compressions in combination.  $HDT++$  denotes the improved HDT ( $HDT++ = \{Dict_{HDT++}, Graph_{HDT}\}$ ).  $GRP++$  denotes the ontology-based graph compression improvement combined with the improved dictionary compression ( $GRP++ = \{Dict_{HDT++}, Graph_{GRP+Ont}\}$ ). The horizontal lines drawn through the bars denote the respective values of  $CR_{Dict_C}$ . That shows how big the portion of the dictionary is in the compressed data.



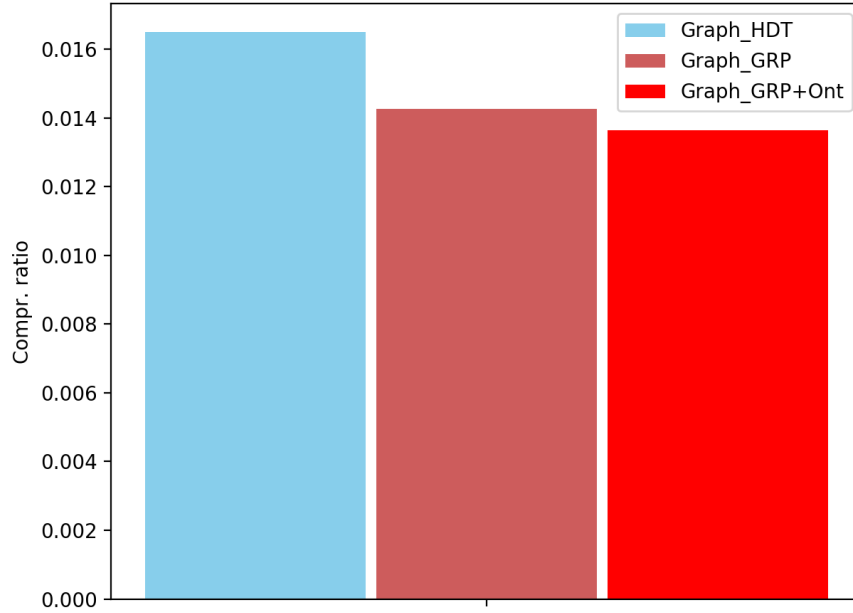


Figure 5.20: Graph compression ratios ( $CR_{Graph_C}$ ) for  $Graph_{HDT}$ ,  $Graph_{GRP}$  and  $Graph_{GRP+Ont}$ .

Apart from that, the difference between HDT++ and GRP++ is very small. This due to the fact that the graph ( $out_{graph}$ ) is so much smaller than  $out_{dict}$ .

GZip is used as a baseline. Since it is a general compressor, it does not have a horizontal line. It is noticeable that GZip achieved a slightly better compression ratio than HDT++ and GRP++. However, as already mentioned in Ch. 1, the data compressed by GZip is not query-able which makes it less usable.

In general, it can be concluded that the improvement makes a significant difference. The resulted compression ratio is almost as low as GZip's ratio. Considering the fact that data compressed by GRP++ or HDT++ is still query-able, it is reasonable to use one of them instead of a general compressor. With further improvements (will be discussed in Ch. 6.2) it could be that HDT++ or GRP++ outperform general compressors in many more cases.

Moreover, it becomes clear that compressing the dictionary has a much bigger impact on  $CR_C$  than compressing the graph. So, for future work it would be reasonable to focus on dictionary compression. However, one work around could be to compress multiple RDF files, which all have a similar dictionary, together. This way, the influences of the graphs can become bigger.

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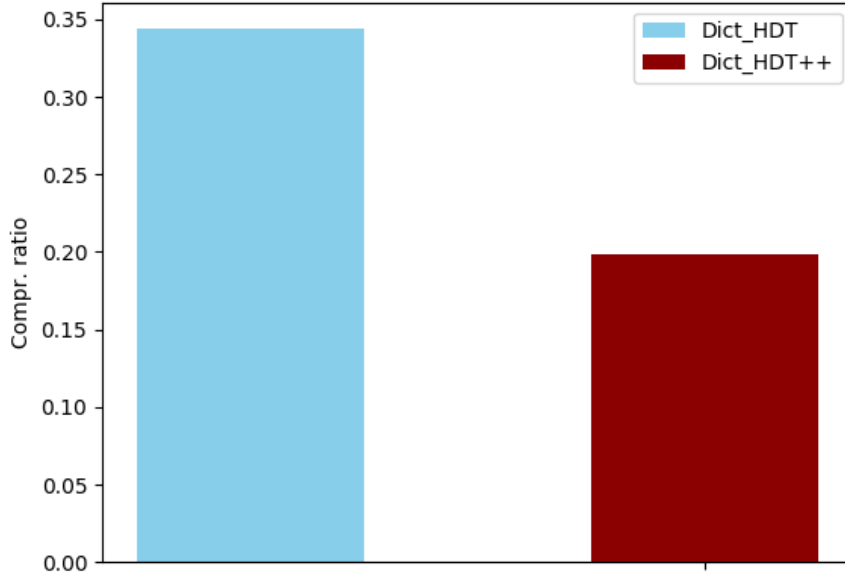


Figure 5.21: Dictionary compression ratios ( $CR_{Dict_C}$ ) for  $Dict_{HDT}$  and  $Dict_{HDT++}$ .

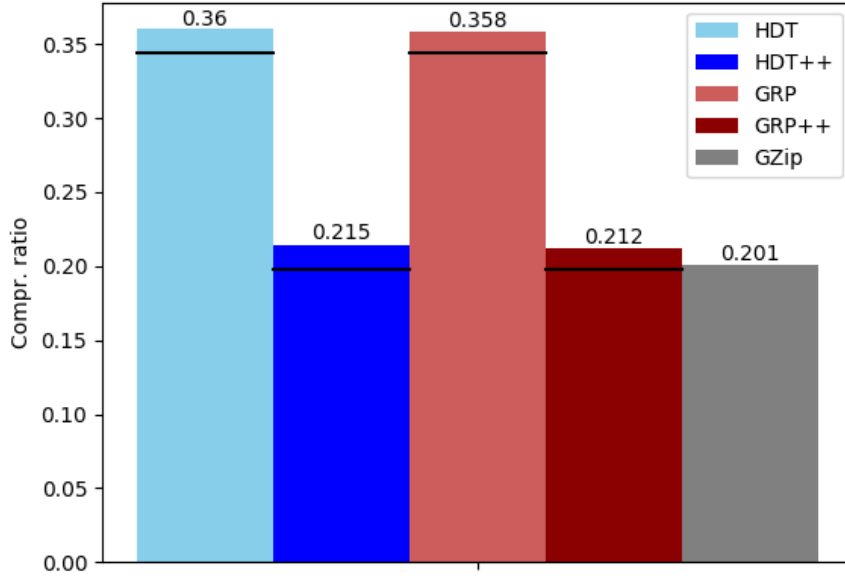


Figure 5.22: Complete compression ratios ( $CR_C$ ) for all compressors. Horizontal lines mark the values of  $CR_{Dict_C}$ . GZip is used as a baseline.

## Summary and Future Work

This last chapter concludes the thesis by firstly summarizing its most important results in a compact form and secondly, discussing what future work might be interesting to do in the area of RDF compression.

### 6.1 Summary

Due to the constantly growing size of the Semantic Web, scalability problems can occur in terms of storage, transmission and consumption of knowledge graphs. At this point, compression can help by reducing the size of the graphs. The focus of this thesis was on storage and transfer, since grammar-based compression, which was considered here, is best suited for these use cases.

The first part of the thesis was to compare GRP with HDT. There, it was shown that GRP achieves a better compression ratio in the vast majority of the used datasets. Moreover, it was shown that the structure of the input data has a much higher effect for GRP than for HDT, because GRP can build much more complex sub structures. In terms of the run time, HDT clearly outperforms GRP.

Based on those results, the next task was to improve the compression ratio. Here, the first sub task was to improve the graph component ( $Graph_{GRP}$ ) of GRP by applying knowledge from the ontology of an RDF graph. The results showed that GRP can find much more patterns (digrams) after symmetric and inverse triples were added and transitive triples were removed. The problem was that the grammar encoding method of GRP cannot take full advantage of that improvement.

The second sub task was to improve the dictionary component of HDT ( $Dict_{HDT}$ ) which is also used by GRP. As the results have shown, compressing long literals by using a Huffman Code brings a significant improvement. Also, the blank node improvement results in a much lower compression ratio.

The final evaluation results showed that the dictionary has a much higher effect on the compression ratio than the graph which is an important insight for future research on this topic.

Generally, the thesis has shown that grammar-based graph compression is suitable for RDF and also delivers better results than HDT in most cases. Moreover, it was shown that there is much potential in terms of improving the dictionary compression.

## 6.2 Future Work

The topic of RDF compression covered in this thesis can be divided into two aspects: Graph and dictionary compression. Therefore, these aspects are presented separately in the following list:

- Graph Compression
  - **More sophisticated implementation of GRP:** The GRP implementation used in the thesis is only a proof of concept, i.e., it is not performing well in terms of its run time. Also, the whole graph has to be loaded into the main memory. A faster and more space-efficient variant is needed in order to compete with the more mature HDT.
  - **Node-based compression:** GRP is an edge-based compressor, which means that it replaces edges of a graph by non terminal edges. However, there are also grammar-based compressors which are edge- and node-based, thus also replacing nodes by non terminal nodes. It would be interesting to see whether they can outperform GRP for RDF graphs. Currently, such a compressor is under development as an extension of [Dü16].
  - **Better grammar encoding:** In Ch. 2.3.2, it has already been stated that the grammar encoding method of GRP is not always working well (especially the  $k^2$ -tree for storing the start rule). Therefore, a different method can be chosen which maybe delivers better results.
  - **Compress multiple graphs together:** As already mentioned in Ch. 3.4.1, it is possible to compress multiple graphs at once. Then, properties or entities can be replaced by equal properties or entities, respectively. This would enable  $Graph_{GRP}$  to produce a better compression.
  - **Query evaluation:** This thesis did not investigate the query run times for GRP. The authors of [MP18] have already proven that neighborhood queries are very slow on graphs compressed by GRP. However, according to [MP18], reachability queries are faster on compressed graphs than on original ones. Therefore, it could be worse comparing those query run times to HDT's query speeds.
- Dictionary Compression
  - **More compression methods for literals:** As explained in Ch. 3.4.2, the thesis focused on string compression via Huffman Coding. But in literals there can be many other data types. It would be sensible to have a separate compression technique for each of those data types. That would probably result in a better compression ratio.
  - **Compress multiple dictionaries together:** This task is similar to compressing multiple graphs together. It can also make a difference with respect to the dictionary. If multiple RDF files have similar dictionaries (many overlapping URIs or literals) those could be merged into one main dictionary which would then be compressed. Of course, this is no trivial task, because it is necessary to differentiate the different smaller dictionaries, but there can be an elegant solution for that.

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## List of Acronyms

<b>RDF</b>	Resource Description Framework
<b>HDT</b>	Header Dictionary Triples
<b>GRP</b>	GraphRePair
<b>OWL</b>	Web Ontology Language
$CR_C$	Compression Ratio for Compressor $C$
$CT_C$	Compression Run Time for Compressor $C$
$DCT_C$	Decompression Run Time for Compressor $C$
$ELR$	Edge Label Ratio
$SPS$	Star Pattern Similarity
$IER$	Input Edge Ratio
$OER$	Output Edge Ratio
$SR$	Size Ratio





## Todo list

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