

(3)

Scratch

nominal flow is translated to penstock flow

$$\Rightarrow 0.37 \text{ m}^3/\text{s} = A (1.8 \text{ m/s})$$

↳ this gives us d

↓

this gives us f

↓

this gives us Δp

$$A = \pi \left(\frac{d}{2}\right)^2 \quad d^2 = \frac{4A}{\pi} \quad d = \sqrt{\frac{4A}{\pi}}$$

get net head thru $\eta_t = \frac{\dot{W}_{\text{shaft}}}{\rho g \dot{V} H_{\text{net}}}$

and $\dot{W}_{\text{shaft}} = \eta_t \dot{W}_{\text{max}}, \quad \dot{W}_{\text{max}} = \rho g \dot{V} H_{\text{gross}}$

Work

$$(0.37 \text{ m}^3/\text{s})(1 - 0.15) = A (1.8 \text{ m/s})$$

$$\Rightarrow A = 0.17 \text{ m}^2$$

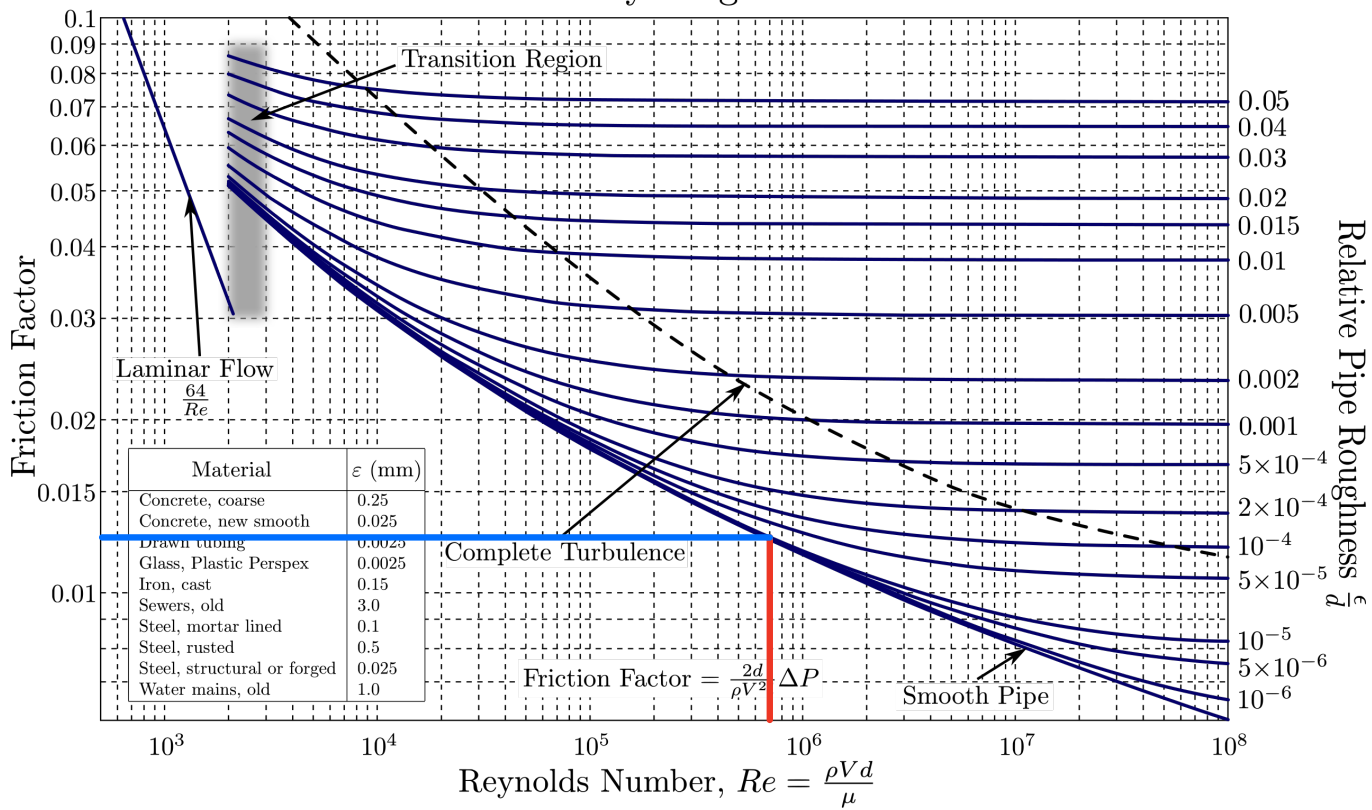
$$\Rightarrow \boxed{d = 0.47 \text{ m}}$$

$$\frac{\varepsilon}{d} = \frac{0.0025 \text{ mm}}{0.47 \text{ m}} \left| \frac{1 \text{ m}}{10^3 \text{ mm}} \right| = 5.3 \times 10^{-6}$$

$$Re = \frac{\rho v d}{\mu} = \frac{(1000 \text{ kg/m}^3)(1.8 \text{ m/s})(0.47 \text{ m})}{0.001 \text{ Pa}\cdot\text{s}} = 8.5 \times 10^5$$

$$\checkmark \frac{\text{kg}}{\text{m}^3} \frac{\text{m}}{\text{s}} \text{ m} \frac{1}{\text{Pa}\cdot\text{s}} = \frac{\text{kg}}{\text{m}\cdot\text{s}^2} \left(\frac{\text{m}^2}{\text{N}} \right) = \frac{\text{kg}\cdot\text{m}}{\text{s}^2} \frac{1}{\text{N}} = \frac{\text{N}}{\text{N}} = 1$$

Moody Diagram



$$f \sim 0.013$$

$$\Delta p = f \frac{L}{d} \frac{\rho v^2}{2} = (0.013) \frac{(300 \text{ m})}{(0.47 \text{ m})} \frac{(1000 \text{ kg/m}^3)(1.8 \text{ m/s})^2}{2}$$

$$\frac{\text{kg}}{\text{m}^3} \frac{\text{m}^2}{\text{s}^2} = \text{Pa}$$

$$\sim 13 \text{ kPa}$$

To account for this pressure drop with \dot{W}_{\max} (maximum power supposing no irreversibilities), convert this pressure drop to power by using

$$\Delta p A v = 4.2 \text{ kW}$$

and then subtract it from the maximum power to obtain a new maximum power with this particular irreversibility

$$\begin{aligned}\dot{W}_{\max} - \Delta p A v &= \\ &= \rho g \dot{V} H_{\text{gross}} - \Delta p A v = \rho g A v H_{\text{gross}} - \Delta p A v \\ &= (\rho g H_{\text{gross}} - \Delta p) A v = 104 \text{ kW}\end{aligned}$$

$$\frac{\frac{\text{kg}}{\text{m}^3} \frac{\text{m}}{\text{s}^2} \frac{\text{m}^3}{\text{s}} \text{m}}{\text{m}^2} = \frac{\text{kg m}^2}{\text{s}^3} = \frac{\text{Nm}}{\text{s}} = \text{W}$$

$$\frac{\text{N}}{\text{m}^2} \frac{\text{m}}{\text{s}} \text{m}$$

$$\dot{W}_{\text{shaft}} = \eta_t \dot{W}_{\max} = 83 \text{ kW}$$

$$\eta_t = \frac{\dot{W}_{\text{shaft}}}{\rho g \dot{V} H_{\text{net}}} \rightarrow \rho g \dot{V} H_{\text{net}} = \frac{\dot{W}_{\text{shaft}}}{\eta_t} \rightarrow H_{\text{net}} = \frac{\dot{W}_{\text{shaft}}}{\eta_t \rho g \dot{V}} = 33.6 \text{ m}$$

$$\frac{\frac{\text{kg}}{\text{hr}^3}}{\frac{\text{m}}{\text{s}^2}} \frac{\text{m}^3}{\text{s}} = \frac{\text{N}}{\text{s}} \quad \frac{\text{S}}{\text{N}} \frac{\text{J}}{\text{s}} = \text{m}$$

$$0.9 \cdot 0.9 \underset{\substack{\downarrow \\ \eta_g}}{W_{\text{shaft}}} = 67 \text{ kW} =: W_{\text{electric}}$$

additional loss

Assuming this is run all day (24 hrs) and starts from

midnight (00:00),

		demand per hour	total demand (600 hours)
6h	00:00 - 06:00	0.1 kW	60
* 3h	06:00 - 09:00	0.5	300
8h	09:00 - 17:00	0.1	60
* 2h	17:00 - 19:00	1.5	900
5h	19:00 - 00:00	0.1	60

$$\begin{aligned}
 (\text{daily } E \text{ needed}) &= 60 \text{ kW} \cdot 6\text{h} + 300 \text{ kW} \cdot 3\text{h} + 60 \text{ kW} \cdot 8\text{h} + 900 \text{ kW} \cdot 2\text{h} \\
 &\quad + 60 \text{ kW} \cdot 5\text{h} \\
 &= 3840 \text{ kWh} \\
 (\text{daily } E \text{ provided}) &= 67 \text{ kW} \cdot 24\text{h} = 1632 \text{ kWh}
 \end{aligned}$$

$3840 > 1632 \Rightarrow$ Daily E cannot be met

3.4

$68 > 60$ so for normal hrs req is met but peak times we need 4-13 times more efficient ones.
Possible mitigation: store energy somewhere to use it for peak hours.

$$\text{Extra } E (0-6) : (68 \text{ kW} - 60 \text{ kW})(6 \text{ hr}) = 48 \text{ kWh}$$

$$\text{Lacking } E (6-9) : (300 \text{ kW} - 68 \text{ kW})(3 \text{ hr}) = 696 \text{ kWh}$$

So even if we store all residue E from 0-6 we still cannot last the morning peak.

$$\text{Extra } E (9-17) : 64 \text{ kWh}$$

$$\text{Lacking } E (17-19) : 1664 \text{ kWh}$$

$$\text{Extra } E (19-24) : 40 \text{ kWh}$$

Every day:

$$\text{Debt} : 696 + 1664 = 2360 \text{ kWh}$$

$$\text{Extra Earning} : 48 + 64 + 40 = 152 \text{ kWh}$$

Debt is ~ 15 times more even if we store all

unused energy so you should not move forward
with this plant. Design better-performing power plants
or use less.

As For Which Turbines Are Allowed

red green or blue all allowed (^{within} ~~on~~ the range)