

HOMEWORK

EXERCICE 1

Determine the values of A, B, C, and D that makes this expression **false**:

!A and B and !C and D

- A. A = 1, B = 0, C = 0, D = 0
- B. A = 1, B = 0, C = 1, D = 0
- C. A = 0, B = 1, C = 0, D = 0
- D. A = 1, B = 0, C = 1, D = 1

| A | B | C | D | !A AND B AND !C NAD D |
|-------|-------|-------|-------|-----------------------|
| True | False | False | False | False |
| True | False | True | False | False |
| False | True | False | False | False |
| True | False | True | True | False |

EXERCICE 2

Determine the values of A, B, C, and D that makes this expression **true**:

!A . B . !C . D

- A. A = 0, B = 1, C = 0, D = 1
- B. A = 0, B = 0, C = 0, D = 1
- C. A = 1, B = 1, C = 1, D = 1
- D. A = 0, B = 0, C = 1, D = 0

| A | B | C | D | !A or B or !C or D |
|-------|-------|-------|-------|--------------------|
| False | True | False | True | True |
| False | False | False | True | True |
| True | True | True | True | True |
| False | False | True | False | True |

EXERCICE 3

True or false?

$$AC + ABC = AC$$

To solve this problem:

- 1- Try using a TRUTH table
- 2- Try using the 7 rules of simplification

| A | B | C | AC | AC +ABC |
|-------|-------|-------|-------|---------|
| True | True | False | False | False |
| False | True | False | False | False |
| True | False | True | False | False |
| False | False | True | False | False |

- 1- Try using the 7 rules of simplification

$$\begin{aligned} AC + ABC &= AC \text{ OR } (AC \text{ and } B) \\ &= AC \text{ and } (B \text{ or true}) \\ &= AC \text{ AND TRUE} \\ &= AC \end{aligned}$$

EXERCICE 5

True or false?

$$A + AB = A$$

To solve this problem:

- 1- Try using a TRUTH table
- 2- Try using the 7 rules of simplification

| A | B | AB | A+AB |
|-------|-------|-------|-------|
| True | False | False | True |
| False | False | False | False |
| False | True | False | False |
| True | True | True | True |

- 1- Try using the 7 rules of simplification

$$\begin{aligned} A + AB &= A \text{ or } (A \text{ and } B) \\ &= A \text{ and } (B \text{ or True}) \\ &= A \text{ and True} \\ &= A \end{aligned}$$

EXERCICE 6

True or false?

$$A + \neg AB = A + B$$

To solve this problem:

- 1- Try using a TRUTH table
- 2- Try using the 7 rules of simplification

| A | B | $\neg AB$ | $A + \neg AB$ |
|-------|-------|-----------|---------------|
| False | True | True | True |
| False | False | True | True |
| True | False | True | True |
| True | True | False | True |

- 1- Try using the 7 rules of simplification

$$\begin{aligned} A + \neg AB &= A \text{ or } \neg(A \text{ and } B) \\ &= A \text{ and } \neg(A \text{ or true}) \\ &= A \text{ or } \neg \text{true} \\ &= A \text{ or false} \\ &= A \end{aligned}$$

In the following exercises: you need to use the table of truth to simplify the expression as much as possible

EX-14

$$A == \text{True and } (B == \text{False or } A == \text{False}) \text{ and } B == \text{True}$$

| a | b | $a == \text{True and } (b == \text{False or } a == \text{False}) \text{ and } b == \text{True}$ |
|-------|-------|---|
| True | True | False |
| True | False | False |
| False | True | False |
| False | False | false |

The expression is equivalent to:

EX-15

| |
|---|
| $(A == \text{True} \text{ and } B == \text{False}) \text{ or } (A == \text{False} \text{ and } B == \text{True})$ |
|---|

| a | b | $(a == \text{True} \text{ and } b == \text{False}) \text{ or } (a == \text{False} \text{ and } b == \text{True})$ |
|-------|-------|---|
| True | True | False |
| True | False | True |
| False | True | True |
| False | False | False |

The expression is equivalent to:

EX-16

| |
|-------------------------------------|
| $(B \text{ or } !B) \text{ and } A$ |
|-------------------------------------|

| a | b | $(B \text{ or } !B) \text{ and } A$ |
|-------|-------|-------------------------------------|
| True | True | True |
| True | False | True |
| False | True | False |
| False | False | False |

The expression is equivalent to:

| |
|---|
| $ \begin{aligned} (B \text{ or } !B) \text{ and } A &= A \text{ and } (B \text{ or } !B) \\ &= A \text{ and } \text{False} \\ &= \text{false} \end{aligned} $ |
|---|