

Allowing Responsive Web Modules

Ben Trovato
Institute for Clarity in
Documentation
1932 Wallamaloo Lane
Wallamaloo, New Zealand
trovato@corporation.com

G.K.M. Tobin
Institute for Clarity in
Documentation
P.O. Box 1212
Dublin, Ohio 43017-6221
webmaster@marysville-
ohio.com

Lars Thörvöld
The Thörvöld Group
1 Thörvöld Circle
Hekla, Iceland
larst@affiliation.org

ABSTRACT

Responsive Web Design (RWD) enables web application to adapt to the characteristics of different devices such as screen size which is important for mobile browsing. Today, the only W3C standard to support this adaptability is CSS media queries. However, using media queries it is impossible to create applications in a modular way, because responsive elements then always depend on the global context. Hence, responsive elements can only be reused if the global context is exactly the same, severely limiting their reusability. This makes it extremely challenging to develop large responsive applications, because the lack of true modularity makes certain requirement changes either impossible or expensive to realize.

In this paper we extend RWD to also include responsive modules, i.e., modules that adapt their design based on their local context independently of the global context. We present the ELQ project which implements our approach. ELQ is a novel implementation of so-called *element queries* which generalize media queries. Importantly, our design conforms to existing web specifications, enabling adoption on a large scale. ELQ is designed to be heavily extensible using plugins. Experimental results show speed-ups of the core algorithms of up to 37x compared to previous approaches.

Categories and Subject Descriptors

H.4 [Information Systems Applications]: Miscellaneous;
D.2.8 [Software Engineering]: Metrics—*complexity measures, performance measures*

General Terms

Theory

Keywords

ACM proceedings, L^AT_EX, text tagging

1. INTRODUCTION

Responsive Web Design (RWD) is an approach to make an application respond to the viewport size and device characteristics. This is currently achieved by using CSS media queries that are designed to conditionally design content by the media, such as using serif fonts when printed and sans-serif when viewed on a screen.

In order to reduce complexity and enable reusability applications are typically composed of modules, i.e., interchangeable and independent parts that have a single and well-defined responsibility [3]. In order for a module to be reusable it must not assume in which context it is being used.

In this paper we focus on the presentation layer of web applications. As it stands, using media queries to make the presentation layer responsive precludes modularity. The problem is that there is no way to make a module responsive without it being context-aware, due to media queries only being able to target the viewport. Thus, a responsive module using media queries is layout dependent and has therefore limited reusability. Therefore, media queries can only be used for RWD of non-modular static applications. In a world where no better solution than media queries exists for RWD, changing the layout of a responsive application becomes a cumbersome task.

1.1 The Problem Exemplified

Imagine an application that displays the current weather of various cities as widgets, by using a weather widget module. The module should be responsive, so that more information such as a temperature graph over time is displayed when the widget is big. When the widget is small it should only display the current temperature. Users should also be able to add, remove and resize widgets.

Such application cannot be built with media queries, since the widgets can have varying sizes independent of the viewport (e.g., the width of one widget is 30% while another is 40%). To overcome this problem we must change the application so that widgets always have the same sizes. This implies that the size of the module and the media query breakpoints are coupled/intertwined, i.e. they are proportional to each other. The problem now is that we have removed the reusability of the weather module, since it requires the specific width that is correctly proportional to the media query breakpoints.

Imagine a company working on a big application that uses media queries for responsiveness (i.e., each responsive module assumes to have a specific percentage of the viewport size). The ability to change is desired by both developers and stakeholders, but is limited by this responsive approach. The requirement of changing a menu from being a horizontal top menu to being a vertical side menu implies that all responsive modules break since the assumed proportionality of each module is changed. Even worse, if the menu is also supposed to hide on user input the responsiveness of the module breaks since the layout changes dynamically. The latter requirement is impossible to satisfy without element queries.

Additionally, it is popular to define breakpoints relative to the font size. Media queries can only target the font size of the document root, limiting the functionality drastically. With element queries, breakpoints may be defined relative to the font size of the targeted element.

As we can see, even with limited requirements there still are significant flaws with using media queries for responsive modules.

1.2 Requirements

The desired behavior of a responsive module is having its inner design responding to the size of *its container* instead of the viewport. Only then is a responsive module independent of its layout context. Realizing responsive modules requires CSS rules that are conditional upon *elements*, instead of the global viewport.

- A solution must provide a possibility for an element to change depending on the properties of the parent element. Elements should automatically respond to changes of the parent size so that the correct design can be presented for each size.
- A solution must conform to the syntax of HTML, CSS, and JavaScript so that the compatibility of tools, libraries and existing projects is retained.
- A solution must have adequate performance for large applications that make heavy use of responsive modules.
- Extensibility
- Composability

1.3 Approach

In this paper we extend the concept of RWD to also include responsive modules. The W3C has discussed such a feature under the name of *element queries* given its analogy to media queries. This paper presents a novel implementation of element queries in JavaScript named ELQ, and discusses the new possibilities of GUI design that our implementation enables.

Our approach is implemented as a client side library to be included in applications. One could argue that a solution does not need to be executed on the client side, but instead generate media queries on the server side for all modules

with respect to the current application layout. However, this is insufficient due to the modules then being limited to applications with static layouts. Also, the generated media queries would not be able to respond to the user changing properties of elements such as layout and font size.

1.4 Contributions

This paper makes the following contributions:

- A new design that enables responsive modules while conforming to the syntax of HTML, CSS, and JavaScript.
- Our approach is the first to enable nested elements that are responsive in a modular way, i.e., styling required for RWD is fully encapsulated in the module. As a side effect, responsive modules may also be arbitrarily styled with CSS independently of their context.
- An extensible library architecture that enables plugins to significantly extend the behavior of the library. This makes it possible to create plugins in order to ease integration of ELQ into existing modules or libraries.
- A new implementation technique that offers substantially higher performance than previous approaches. Our technique batch processes DOM operations so that layout thrashing (i.e., forcing the layout engine to perform multiple independent layouts) is avoided.

The rest of the paper is organized as follows:

2. BACKGROUND

- Explain media queries really short (simple example). Maybe explain some terminology.

Media queries and element queries are similar in the sense that they both enable developers to define conditional style rules that are applied by specified criteria. The main difference is the type of criteria that can be used; in media queries device, document, and media criteria are used, while element criteria are used in element queries. It can somewhat simplified be described as that media queries target the document root and up (i.e., the viewport, browser, OS, device, input mechanisms, etc.) while element queries target the document root and down (i.e., elements of the document).

3. OVERVIEW OF ELQ

To enable element queries today, we have developed a novel JavaScript implementation named ELQ. Our implementation satisfied all requirements given in 1.1. The library have been designed to conform to the standards and specifications of the web languages while providing the features required of building advanced constellations of responsive modules. The novelty lies in having significantly improved performance by batch processing DOM operations, and providing an API that enables nesting of modules. ELQ also has excellent browser compatibility as it supports Internet Explorer 8 and upwards.

ELQ is designed to be plugin-based for increased flexibility and extensibility. By providing a good library foundation

and plugins it is up to developers to choose the right plugins for each project. In addition, by letting the plugins satisfy the requirements it is easy to extend the library with new plugins when new requirements arise.

An *element breakpoint* is defined as a point of an element property range which can be used to define conditional behavior, similar to breakpoints of media queries. For example, an element breakpoint of 500 pixels in width enables conditional styling depending on if the element is narrower or wider than 500 pixels. An element may have multiple breakpoints. An *element breakpoint state* is defined as the state of the element breakpoint relative to the current element property value. For example, if an element that is 300 pixels wide has two width breakpoints of 200 and 400 pixels the element breakpoint states are “wider than 200 pixels” and “narrower than 400 pixels”.

When the breakpoint states of an element changes, ELQ performs cycle detection in order to detect and handle possible cyclic element queries. If a cycle is detected, the new element breakpoint states are not applied in order to avoid an infinite cycle. The cycle detection system is implemented as an conservative algorithm, and may detect false positives.

3.1 The API

As CSS 3 does not support custom at-rules/selectors, responsive elements are annotated in HTML by element attributes. The main idea is to annotate elements with breakpoints of interest so that children can be conditionally styled in CSS by targeting the different element breakpoint states. In this example, we will use the `elq-breakpoints` plugin that observes the element in order to automatically update the breakpoint classes. Although not written in the examples, the library also supports attributes defined with the `data-` prefix to conform to the HTML standard.

In listing 3.1 we see an element that has annotated two breakpoints at 300 and 500 pixels.

```
<div class="foo" elq elq-breakpoints
  elq-breakpoints-widths="300 500">
  <p>When in doubt, mumble.</p>
</div>
```

When ELQ has processed the element, it will always have two classes, one for each breakpoint, that tells if the size of the element is greater or lesser than each breakpoint. For instance, if the element is 400 pixels wide, the element has the two classes `elq-min-width-300px` and `elq-max-width-500`. Similarly, if the element is 200 pixels wide the element the classes are instead `elq-max-width-300px` and `elq-max-width-500`. So for each breakpoint only the min/max part changes. It may seem alien that the classes describe that the width of the element is both maximum 300 and 500 pixels. This is because we have taken a user-centric approach, so that when using the classes in CSS the API is similar to element queries. However, developers are free to change this API at will as ELQ is plugin-based.

Now that we have defined the breakpoints of the element, we can conditionally style it by using the classes. See listing 3.1 for an example of how the classes can be used.

```
.foo.elq-min-width-300px.elq-max-width-500px {
  background-color: green;
}

.foo.elq-min-width-500px {
  background-color: blue;
}

.foo.elq-max-width-500px p {
  color: white;
}
```

3.1.1 Nested modules

This API is sufficient for applications that do not need nested breakpoint elements, and similar features is provided by related libraries. However, using such API in responsive modules still limits the reusability since the modules then may not exist in an outer responsive context. Also, it is customary to compose large/complex modules by smaller modules that may also need to be responsive [3].

The reason this API is not sufficient for nested modules is because there is no way to limit the CSS matching search of the selectors. The selector of the last example given in listing 3.1 specifies that all paragraph elements should have white text if *any* ancestor breakpoints element is above 500 pixels wide. Since the ancestor selector may match elements outside of the module, such selectors are dangerous to use in the context of responsive modules. The problem may be somewhat reduced by more specific selectors and such, but it cannot be fully solved for arbitrary styling.

To solve this problem, we provide a plugin that let us define elements to “mirror” the breakpoints classes of the nearest ancestor breakpoints element. Then, the conditional style of the mirror element may be written as a combinatory selector that is relative to the nearest ancestor breakpoints element. See listing 3.1.1 for example markup of the mirror plugin to enable nested modules.

```
<div class="foo" elq elq-breakpoints
  elq-breakpoints-widths="300 500">
  <div class="foo" elq elq-breakpoints
    elq-breakpoints-widths="300 500">
    <p elq elq-mirror >...</p>
  </div>
  <p elq elq-mirror >...</p>
</div>
```

As the paragraph elements are mirroring the nearest `.foo` ancestor, we can now write CSS as shown in listing 3.1.1.

```
.foo {
  /* So that the nested module
     behaves differently */
  width: 50%;
}

.foo p.elq-max-width-500px {
  color: white;
}
```

Since we in the previous examples have annotated elements manually, the power and flexibility of the API have not been properly displayed. Only when combined with JavaScript, things get more interesting.

3.1.2 A high-level API

To further prove the potential of ELQ, we have created a plugin that enables a high-level API for responsive modules. The API enables developers to use responsive grids and utility classes very similar to the ones defined by the CSS Bootstrap framework. See listing 3.1.2 for an example grid that uses the Bootstrap API. The example grid is defined to be single columned for small viewports, triple columned for medium viewports, and double columned for large viewports. It should be noted that the last column is hidden for large viewports.

```
<div class="container">
  <div class="row">
    <div class="col-md-4 col-lg-6">
      ...
    </div>
    <div class="col-md-4" col-lg-6">
      ...
    </div>
    <div class="col-md-4 hidden-lg-up">
      ...
    </div>
  </div>
</div>
```

This API uses media queries and supports a fixed set of breakpoints that can be used to determine when the grid should change layout (depending on the viewport size). The column classes defines the behaviour of the grid, and has the syntax `col-[breakpoint]-[size]`. The predefined breakpoints are `xs`, `sm`, `md`, `lg` and the size may be between 1 and 12.

The syntax of our API does not differ much from the Bootstrap API, but the behavior does. The columns of our API responds to the parent `row` instead of the viewport. Therefore, we have altered the column classes to also accept custom breakpoints so that developers have full control of the grid behavior. The `breakpoint` part of the column class can be any positive number, and may optionally be postfix with a unit. Currently, the supported units are `px`, `em`, `rem`. If the units is omitted, `px` is assumed. See listing 3.1.2 for an example grid that uses our API. The example grid is defined to be single columned when the width of the grid is below 500 pixels, triple columned when the width is between 500 and 700 pixels, and double columned for when the width is above 700 pixels. It should be noted that the last column is hidden when the width is above 700 pixels.

```
<div class="container">
  <div class="row">
    <div class="col-500-4 col-700-6">
      ...
    </div>
    <div class="col-500-4" col-700-6">
      ...
    </div>
    <div class="col-500-4 hidden-700-up">
      ...
    </div>
  </div>
</div>
```

This enables developers to define grid behaviors by pixel precision in nestable modules, while maintaining the familiar Bootstrap API style.

4. EXTENSIONS VIA PLUGINS

One of our contributions is to allow ELQ to be easily extended with plugins. For example, if annotating HTML is undesired it is possible to create a plugin that instead parses CSS. Likewise, if adding breakpoint classes to element is undesired it is possible to create a plugin that does something else when an element breakpoint state of an element has changed. In order to enable such powerful behavior alterations by plugins, extensibility has been the main focus when designing the ELQ architecture.

A plugin is defined by a *plugin definition object* and has the structure shown in listing 4.

```
var myPluginDefinition = {
  getName: function () {
    return "my-plugin";
  },
  getVersion: function () {
    return "0.0.0";
  },
  isCompatible: function (elq) {
    return true;
  },
  make: function (elq, options) {
    return {
      // Implement plugin instance methods.
      ...
    };
  }
};
```

All of the methods are invoked when registered to an ELQ instance. The `getName` and `getVersion` methods tell the name and version of the plugin. The `isCompatible` tells if the plugin is compatible with the ELQ instance that it is registered to. In the `make` method the plugin may initialize itself to the ELQ instance and return an object that defines the API accessible by ELQ and other plugins.

When necessary, ELQ invokes certain methods of the plugin API, if implemented, to let plugins decide the behavior of the system. Those methods are the following:

- **activate(element)** Called when an element is requested to be activated, in order for plugins to initialize listeners and element properties.
- **getElements(element)** Called in order to let plugins reveal extra elements to be activated in addition to the given element.
- **getBreakpoints(element)** Called to retrieve the current breakpoints of an element.
- **applyBreakpointStates(element, breakpointStates)** Called to apply the given element breakpoint states of an element.

In addition, plugins may also listen to the following ELQ events:

- **resize(element)** Emitted when an ELQ element has changed size.
- **breakpointStatesChanged(element, breakpointStates)** Emitted when an element has changed element breakpoint states (e.g., when the width of an element changed from being narrower than a breakpoint to being wider).

There are two main flows of the ELQ system; activating an element and updating an element. When ELQ is requested to activate an element, the following flow occurs:

1. Initialize the element by installing properties and a system that handles listeners.
2. Call the `getElements` method of all plugins to retrieve any additional elements to activate. Perform an activation flow for all additional elements.
3. Call the `activate` method of all plugins so that plugin-specific initializations may occur.
4. If any plugin has requested ELQ to detect resize events of the element, install an resize detector to the element.
5. Pass the element through the update flow.

The update flow is as follows:

1. Call the `getBreakpoints` method of all plugins to retrieve all breakpoints of the element.
2. Element breakpoint states are calculated.
3. If any state has changed since the previous update:
 - (a) Perform cycle detection. If a cycle is detected, then abort the flow and emit a warning.
 - (b) Call the `applyBreakpointStates` method of all plugins in order for plugins to apply the new element breakpoint states.
 - (c) Emit an `breakpointStatesChanged` event.

Of course, there are options to disable some of the steps such as cycle detection and applying breakpoint states. In addition to being triggered by the activation flow and plugins, it is also triggered by element resize events.

TODO: Explain that plugins may set properties of `element.elq`, and also use the `elq` plugin API.

4.1 Example Plugin Implementation

The `elq-breakpoints` API that enables developers to annotate breakpoints in HTML, as described in section ??, is implemented as two plugins. This shows that even the core functionality of ELQ is implemented in terms of plugins. The first plugin parses the breakpoints of the element attributes. The second plugin applies the breakpoint states as classes.

The simplified code of the `make` method of the parsing plugin is presented in listing ??.

TODO: Write that the following is the implementation of the `make` method of the previous shown plugin definition (line number reference).

```
function activate(element) {
  if (!element.hasAttribute("elq-breakpoints")) {
    return;
  }
}
```

```
element.elq.resizeDetection = true;
element.elq.updateBreakpoints = true;
element.elq.applyBreakpointStates = true;
element.elq.cycleCheck = true;
// TODO: Use Detection instead of Check,
// to be consistent.
}

function getBreakpoints(element) {
  // Parse the "elq-breakpoints-*" attributes
  // and retrieve their breakpoints.
  return ...;
}

// Return the plugin API
return {
  activate: activate,
  getBreakpoints: getBreakpoints
};
```

The applying plugin simply implements the `applyBreakpointStates` method to alter the `className` property of the element by the given element breakpoint states.

TODO: Explain the code a bit more, what's happening?

5. IMPLEMENTATION

Batching. Resize listening.

6. EMPIRICAL EVALUATION

6.1 Performance

The following tests were performed on a computer with a 2.5 GHz processor and 16 GB of memory¹. The library has been tested in the following browsers: Chrome 42.0.2311.152, Firefox 37.0.1 and Safari 8.0.6. Measurements and graphs show evaluations performed in Chrome unless stated otherwise.

inline]Include evaluation about the cycle detector? inline]Write about the new "noclasses" option, and maybe flesh out the interplugin API section? inline]Write that as ELQ is plugin-based, it makes sense to measure the core subsystems by themselves and the plugins enabling element queries in different setups. inline]Have to measure how `elq-breakpoints` handles large amount of elements. It might suffer from layout thrashing since might read/write the DOM at invalid stages of the `erd` subsystem. inline]Actually since `elq-breakpoints` is batch-processed, no layout thrashing occurs. However, two disjunct layouts are performed (one for the `erd` system and one for the plugin) which could theoretically be merged. inline]Philipp: If possible, show graphs for other browsers than Chrome. inline]Write about Bootstrap performance here.

This section evaluates the performance of the object-based and scroll-based solutions to detecting element resize events described in Section ???. The optimized ELQ version of the scroll-based solution is also evaluated. Since the element resizing detection subsystem performs the heaviest tasks, only the performance of that subsystem is evaluated. The other subsystems entail no significant performance penalties.

¹The serial number of the computer is C02N4G9TG3QD and the vendor is Apple Inc. CPU: 2.5 GHz Intel Core i7. Memory: 16 GB 1600 MHz DDR3. GPU: Intel Iris Pro 1536 MB.

The object-based solution performs well when detecting resize events. However, injecting **object** elements is quite a heavy task. See figure 1 for graphs that show the performance of the object-based solution. As shown by the graphs, the injection can be performed with adequate performance as long as the number of elements is low. The solution does not scale well as the number of elements increases.

The scroll-based solution also performs well when detecting resize events. As no **object** element are injected the memory footprint is reduced significantly, which improves the injection performance. See figure ?? for graphs that show how both solutions perform compared to each other. It is clear that the scroll-based solution both performs and scales better than the object-based solution during injection. The amount of memory used by the scroll-based solution is so low that reliable measurements could not be gathered, as the number of element was not high enough to affect the memory usage noticeably.

Recall that the scroll-based solution was rewritten and optimized, which is referred to as the ELQ scroll-based solution. By avoiding layout thrashing, the injection performance was improved significantly. See figure 2 for graphs that show how it performs compared to the other solutions. As evident in the figure, the optimized ELQ solution has significantly reduced injection times compared to the other two. It achieves a 32-fold speedup compared to the object-based solution and a 13-fold speedup compared to the scroll-based solution when preparing 500 element for resize detection. The ELQ solution also scales better, as more clearly shown in figure 3 that includes polynomial regression graphs for all three solutions. Both scroll-based solutions have the same memory footprint (i.e., too low for reliable measurements).

Firefox and Safari. As shown, great performance can be achieved with the optimized ELQ scroll-based solution in Chrome. Unfortunately, there is no silver bullet to observing element resize events; as the other browser behave differently. See table 1 for the performance of the object-based and scroll-based solutions operating on 100 element in different browser. The ELQ scroll-based solution is preferred for Chrome, as the injection is 32-fold faster (when operating on 500 element) than the object-based solution while the resize detection performance is the same for both solutions. In Firefox, the object-based solution detects resize events 2-fold faster than the ELQ scroll-based solution when operating on 100 element (still, 100 ms for detecting resize events is acceptable). However, the injection time needed for the object-based solution is 5.5-fold of the time needed for the ELQ scroll-based solution. The ELQ scroll-based solution is therefore probably desired in Firefox for the general use case (as described in Section ??). In Safari, the ELQ scroll-based solution detects resize events in 800 ms while the object-based solution detects them in 25 ms, which of course is unacceptable. Unfortunately, the injection time needed for the object-based solution is 3-fold slower than the ELQ scroll-based solution. Since a delay of 800 ms when detecting resize events is undesired in most use cases, the object-based solution is preferred for Safari. Recall from Section ?? that this is due to WebKit and Gecko not being able to queue the scroll mutation operations as Blink does.

Layout engine	Injection		Resize detection	
	scroll	object	scroll	object
Blink	30 ms	600 ms	30 ms	30 ms
Gecko	200 ms	1100 ms	100 ms	50 ms
WebKit	100 ms	300 ms	800 ms	25 ms

Table 1: Performance of the object-based and ELQ scroll-based solutions in different layout engine when operating on 100 element.

inline]Present perf statistics of other browsers? Firefox still seems to favor the scroll solution (but less performant) while Safari seems to favor the object solution. inline]Show graph for resize detection also. inline]Graphs for Firefox, IE and Safari?

6.2 Case studies

Plugins makes it easy to integrate.

7. DISCUSSION

- Performance, APIs, Features.
- The mirror functionality of ELQ makes it uniquely suitable for nested modules.

7.1 Limitations

(Drawbacks) No good alternative. Mention RICG (perhaps standard that solves the issue in the future).

7.2 Standardization

It is stated on the W3C's www-style mailing list [4] by Zbarsky of Mozilla, Atkins of Google and Sprehn of Google that element queries are infeasible to implement without restricting them. By limiting element queries to specially separated container elements that can only be queried by child elements, many of the problems are resolved [2, 1]. Therefore, the Responsive Issues Community Group (RICG) is currently investigating the possibility of standardizing *container* queries.

Unfortunately, even such limited container queries requires significant effort to implement [1]. Atkins argues that a correct and full implementation is unlikely to be implemented, and therefore it might be wiser to pursue sub-standards that aids third-party solutions instead.

In the future, we hope that Elq may use the aiding sub-standards pushed by RICG, to achieve greater flexibility and performance.

We want RICG to standardize the following: bla bla bla

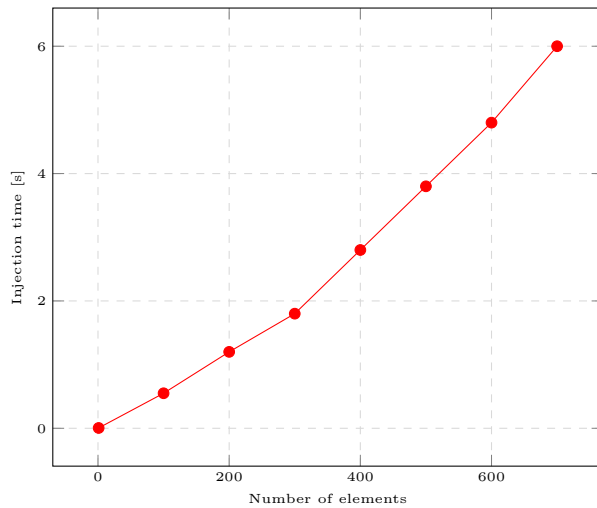
8. RELATED WORK

9. CONCLUSIONS

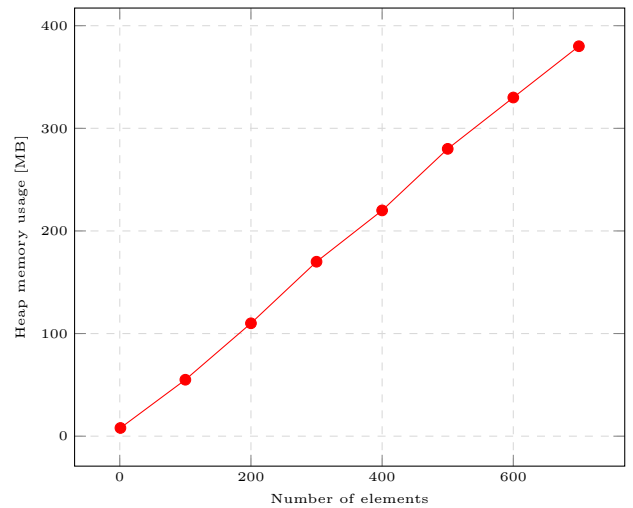
- Production ready.
- Probably no standard (or not in a long time).

10. ACKNOWLEDGMENTS

This section is optional; it is a location for you to acknowledge grants, funding, editing assistance and what have you. In the present case, for example, the authors would like to thank Gerald Murray of ACM for his help in codifying this *Author's Guide* and the **.cls** and **.tex** files that it describes.



—●— Object-based solution



—●— Object-based solution

Figure 1: The injection performance of the object-based solution. The left graph shows the injection time. The right graph shows the heap memory used when all object element have been injected.

11. REFERENCES

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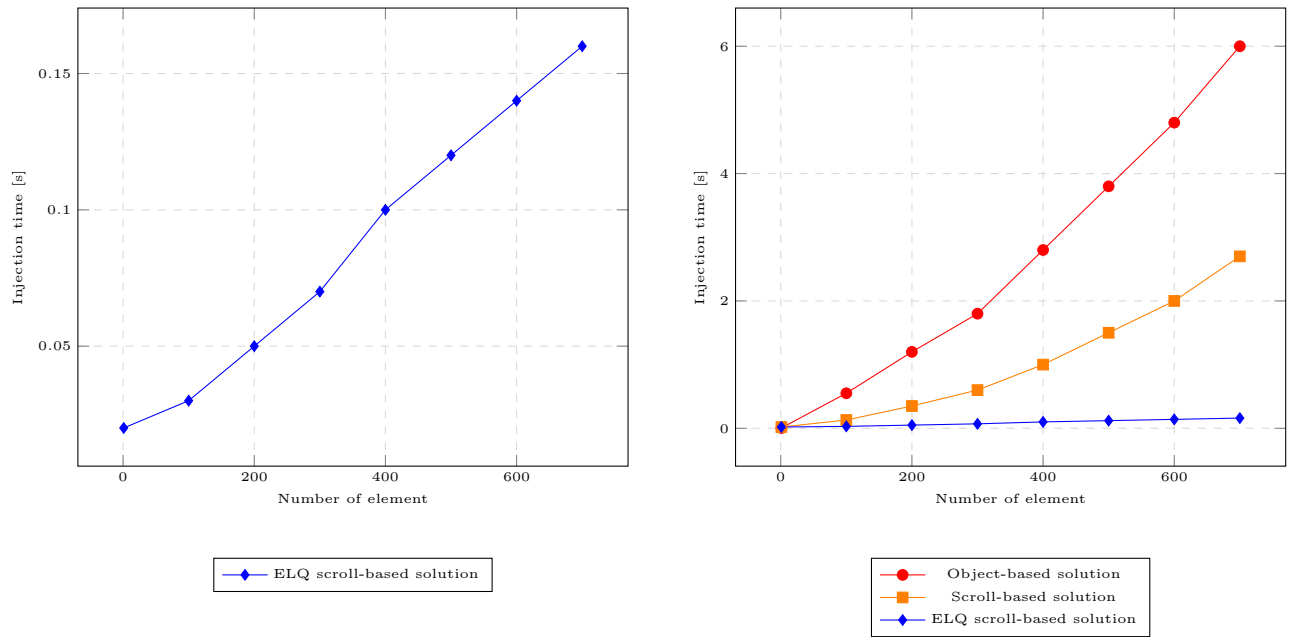


Figure 2: The injection performance of the optimized ELQ scroll-based element resizing detection solution. The left graph shows the injection time of the ELQ scroll-based solution. The right graph shows all three solutions for comparison. The heap memory usage graph has been omitted as the memory usage of the scroll-based solutions is too low for reliable measurements.

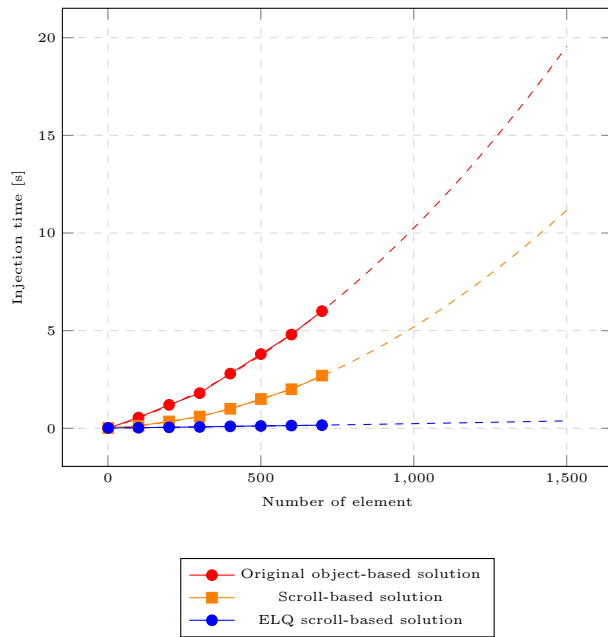


Figure 3: The injection performance of all three solutions including graph predictions by polynomial regression.