

Superposition of two harmonic oscillations with nearly the same frequency

→ Resulting effect are sound beats

→ the intensity of sound is modulated

$x(t)$  = displacement

$$x_1(t) = \hat{X}_1 \cos \omega_1 t$$

$$x_2(t) = \hat{X}_2 \cos \omega_2 t$$

$$x(t) = x_1(t) + x_2(t) = \hat{X} (\cos \omega_1 t + \cos \omega_2 t) = 2\hat{X} \left[ \cos \frac{1}{2}(\omega_1 - \omega_2)t \right] \left[ \cos \frac{1}{2}(\omega_1 + \omega_2)t \right]$$

→ Approximation: if  $\omega_1 \approx \omega_2$ , then  $\omega \approx \frac{\omega_1 + \omega_2}{2}$  and  $\Delta\omega \approx 0$

→  $x(t) = \left[ 2\hat{X} \cos \frac{\Delta\omega}{2} t \right] [\cos \omega t]$ , with  $2\hat{X} \cos \frac{\Delta\omega}{2} t$  is called modulated amplitude, and  $\cos \omega t$  is called basic oscillation.

on books.... lissajou figure

Fourier Coefficients

$$a_0 = \frac{1}{T} \int_0^T f(t) dt$$

$$a_n = \frac{2}{T} \int_0^T f(t) \cos(n\omega t) dt$$

$$b_n = \frac{2}{T} \int_0^T f(t) \sin(n\omega t) dt$$