Bike Sharing Assignment

Problem Statement

A bike-sharing system is a service in which bikes are made available for shared use to individuals on a short term basis for a price or free. Many bike share systems allow people to borrow a bike from a "dock" which is usually computer-controlled wherein the user enters the payment information, and the system unlocks it. This bike can then be returned to another dock belonging to the same system.

A US bike-sharing provider BoomBikes has recently suffered considerable dips in their revenues due to the ongoing Corona pandemic. The company is finding it very difficult to sustain in the current market scenario. So, it has decided to come up with a mindful business plan to be able to accelerate its revenue as soon as the ongoing lockdown comes to an end, and the economy restores to a healthy state.

In such an attempt, BoomBikes aspires to understand the demand for shared bikes among the people after this ongoing quarantine situation ends across the nation due to Covid-19. They have planned this to prepare themselves to cater to the people's needs once the situation gets better all around and stand out from other service providers and make huge profits.

They have contracted a consulting company to understand the factors on which the demand for these shared bikes depends. Specifically, they want to understand the factors affecting the demand for these shared bikes in the American market. The company wants to know:

- Which variables are significant in predicting the demand for shared bikes.
- How well those variables describe the bike demands Based on various meteorological surveys and people's styles, the service provider firm has gathered a large dataset on daily -bike demands across the American market based on some factors.

In [54]:

```
import warnings
warnings.filterwarnings('ignore')
import pandas as pd
# Data visualization
import matplotlib.pyplot as plt
import seaborn as sns
# Data splitting
from sklearn.model_selection import train_test_split
# Feature scaling
from sklearn.preprocessing import MinMaxScaler
# Building a model
import statsmodels.api as sm
# VIF calculation
from statsmodels.stats.outliers_influence import variance_inflation_factor
# Evaluation (finding R2)
from sklearn.metrics import r2_score
```

In [55]:

```
# Importing the data set
data = pd.read_csv("day.csv")
data.head()
```

Out[55]:

	instant	dteday	season	yr	mnth	holiday	weekday	workingday	weathersit	temp
0	1	01-01- 2018	1	0	1	0	6	0	2	14.110847
1	2	02-01- 2018	1	0	1	0	0	0	2	14.902598
2	3	03-01- 2018	1	0	1	0	1	1	1	8.050924
3	4	04-01- 2018	1	0	1	0	2	1	1	8.200000
4	5	05-01- 2018	1	0	1	0	3	1	1	9.305237
4										•

In []:

In [56]:

```
# Summarizing all the details of all variables.
data.describe()
```

Out[56]:

	instant	season	yr	mnth	holiday	weekday	workingday
count	730.000000	730.000000	730.000000	730.000000	730.000000	730.000000	730.000000
mean	365.500000	2.498630	0.500000	6.526027	0.028767	2.997260	0.683562
std	210.877136	1.110184	0.500343	3.450215	0.167266	2.006161	0.465405
min	1.000000	1.000000	0.000000	1.000000	0.000000	0.000000	0.000000
25%	183.250000	2.000000	0.000000	4.000000	0.000000	1.000000	0.000000
50%	365.500000	3.000000	0.500000	7.000000	0.000000	3.000000	1.000000
75%	547.750000	3.000000	1.000000	10.000000	0.000000	5.000000	1.000000
max	730.000000	4.000000	1.000000	12.000000	1.000000	6.000000	1.000000
4							>

In [57]:

Verifying whether there are null values.
data.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 730 entries, 0 to 729
Data columns (total 16 columns):

#	Column	Non-Null Count	Dtype						
0	instant	730 non-null	int64						
1	dteday	730 non-null	object						
2	season	730 non-null	int64						
3	yr	730 non-null	int64						
4	mnth	730 non-null	int64						
5	holiday	730 non-null	int64						
6	weekday	730 non-null	int64						
7	workingday	730 non-null	int64						
8	weathersit	730 non-null	int64						
9	temp	730 non-null	float64						
10	atemp	730 non-null	float64						
11	hum	730 non-null	float64						
12	windspeed	730 non-null	float64						
13	casual	730 non-null	int64						
14	registered	730 non-null	int64						
15	cnt	730 non-null	int64						
dtyp	es: float64(4), int64(11),	object(1)						
memo	memory usage: 88.5+ KB								

Data visualization

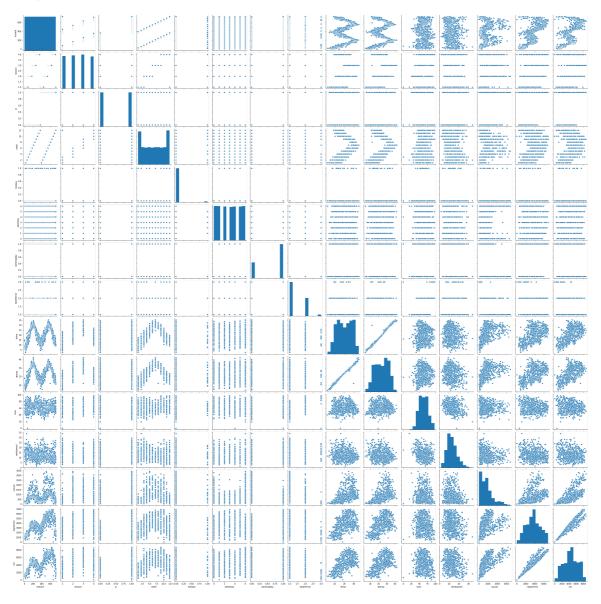
In [58]:

```
# Verifying the relation between all the variables using scatter plots.
plt.figure(figsize=[20,20])
sns.pairplot(data)
```

Out[58]:

<seaborn.axisgrid.PairGrid at 0x12f6ca30>

<Figure size 1440x1440 with 0 Axes>



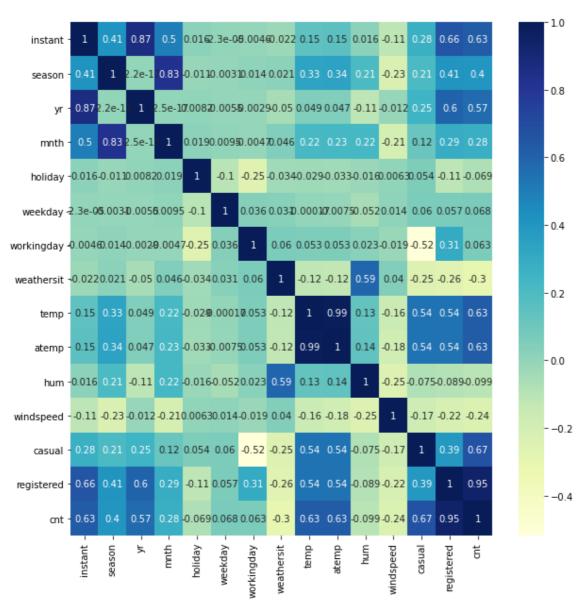
There are several variables that are categorical in nature when we observe in the plot. All the categorical variables plots are in straight lines. These variables need creating dummy variables.

In [59]:

```
# Finding the corrilation value of all the variables.
plt.figure(figsize=[10,10])
sns.heatmap(data.corr(), annot=True , cmap='YlGnBu')
```

Out[59]:

<AxesSubplot:>



Data Preparation

- Dropping unnecessory data
- Dropping highly corrilated data that are derived from the data visualization
- · Creating Dummy Variables for categorical variables

Dropping unnecessory data

There are some variables that does not add importance to the data for future predictions. They are instant, casual, registered, dteday. So dropping them wont effect the predictions.

```
Instant - Does not add any importence.
dteday - This feature is already explained by other features. So no need of it.
casual, registered - These are the type of customers using per day. They also do nt effect the future predictions
```

```
In [60]:

# Droping the unnecessary variables

data = data.drop(['instant', 'dteday', 'casual', 'registered'], axis=1)
```

Dropping highly corrilated data that are derived from the data visualization

In the given dataset we have two variables (atemp, temp) that are higly corrilated, i.e: corrilation value is nearly equal to zero. In this kind of situation considering only one variable will be enough. So drop one of them.

```
In [61]:
```

```
# Dropping atemp variable

data = data.drop(['atemp'], axis=1)
```

In [62]:

```
data.head()
```

Out[62]:

	season	yr	mnth	holiday	weekday	workingday	weathersit	temp	hum	windsp
0	1	0	1	0	6	0	2	14.110847	80.5833	10.749
1	1	0	1	0	0	0	2	14.902598	69.6087	16.652
2	1	0	1	0	1	1	1	8.050924	43.7273	16.636
3	1	0	1	0	2	1	1	8.200000	59.0435	10.739
4	1	0	1	0	3	1	1	9.305237	43.6957	12.522

→

Creating Dummy Variables for categorical variables

As we mentioned before in the pairplot section, we need to create dummy variables for some of the categorical variables. They are Season, month, weekday, weathersit.

In [63]:

```
# We first create categorical variables , replacing the numerics with actual data.

data.season = data.season.map({1:'spring', 2:'summer', 3:'fall', 4:'winter'})
data.weekday = data.weekday.map({0:'tuesdata', 1:'wednesdata', 2:'thursdata', 3:'fridat a',4:'saturdata',5:'sundata',6:'mondata'})
data.mnth = data.mnth.map({1:'Jan', 2:'Feb', 3:'Mar', 4:'Apr', 5:'May', 6:'Jun', 7:'Ju 1', 8:'Aug', 9:'Sep', 10:'Oct', 11:'Nov', 12:'Dec'})
data.weathersit = data.weathersit.map({1:'Clear',2:'Mist+cloudy',3:'Light snow',4:'Heav y snow'})
```

In [64]:

```
data.head()
```

Out[64]:

	season	yr	mnth	holiday	weekday	workingday	weathersit	temp	hum	winc
0	spring	0	Jan	0	mondata	0	Mist+cloudy	14.110847	80.5833	10.
1	spring	0	Jan	0	tuesdata	0	Mist+cloudy	14.902598	69.6087	16.
2	spring	0	Jan	0	wednesdata	1	Clear	8.050924	43.7273	16.0
3	spring	0	Jan	0	thursdata	1	Clear	8.200000	59.0435	10.
4	spring	0	Jan	0	fridata	1	Clear	9.305237	43.6957	12.
4										•

In [65]:

```
# Creating Dummy variables for Season, month, weekday, weathersit features.

dummies = pd.get_dummies(data[['season', 'mnth', 'weekday', 'weathersit']] , drop_first = True)
dummies.head()
```

Out[65]:

	season_spring	season_summer	season_winter	mnth_Aug	mnth_Dec	mnth_Feb	mnth_J
0	1	0	0	0	0	0	
1	1	0	0	0	0	0	
2	1	0	0	0	0	0	
3	1	0	0	0	0	0	
4	1	0	0	0	0	0	

5 rows × 22 columns

→

In [66]:

```
# Now concat these dummies with the actual dataset. And drop the categorical variables.
# Concating dummies to data (axis=1, i.e: adding columns) and dropng the categorical va lues at the same time.
data = pd.concat([data, dummies], axis=1).drop(['season', 'mnth', 'weekday', 'weathers it'], axis=1)
```

Splitting the data

In [67]:

```
data_train, data_test = train_test_split(data, train_size = 0.7, test_size = 0.3, rando
m_state = 100)
```

scaling the features

In [68]:

data_train.describe()

Out[68]:

	yr	holiday	workingday	temp	hum	windspeed	cnt
count	510.000000	510.000000	510.000000	510.000000	510.000000	510.000000	510.000000
mean	0.507843	0.025490	0.676471	20.102429	63.112926	12.831318	4486.382353
std	0.500429	0.157763	0.468282	7.431169	14.156632	5.291832	1952.158739
min	0.000000	0.000000	0.000000	2.424346	0.000000	2.834381	22.000000
25%	0.000000	0.000000	0.000000	13.606865	52.270825	9.041918	3120.000000
50%	1.000000	0.000000	1.000000	20.209597	63.437500	12.083182	4530.000000
75%	1.000000	0.000000	1.000000	26.615847	73.250025	15.750879	5973.500000
max	1.000000	1.000000	1.000000	35.328347	97.041700	34.000021	8714.000000

8 rows × 29 columns

In [69]:

data_train.head()

Out[69]:

	yr	holiday	workingday	temp	hum	windspeed	cnt	season_spring	season_
653	1	0	1	19.201653	55.8333	12.208807	7534	0	
576	1	0	1	29.246653	70.4167	11.083475	7216	0	
426	1	0	0	16.980847	62.1250	10.792293	4066	1	
728	1	0	0	10.489153	48.3333	23.500518	1796	1	
482	1	0	0	15.443347	48.9583	8.708325	4220	0	

5 rows × 29 columns

→

In [70]:

```
# Creating the object for MinMaxScaler()
scaler = MinMaxScaler()

# Using the obj to access the method from MinMax and perform scaling
data_train[data_train.columns] = scaler.fit_transform(data_train[data_train.columns])
```

In [71]:

data_train.describe()

Out[71]:

	yr	holiday	workingday	temp	hum	windspeed	cnt
count	510.000000	510.000000	510.000000	510.000000	510.000000	510.000000	510.000000
mean	0.507843	0.025490	0.676471	0.537262	0.650369	0.320768	0.513620
std	0.500429	0.157763	0.468282	0.225844	0.145882	0.169797	0.224593
min	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
25%	0.000000	0.000000	0.000000	0.339853	0.538643	0.199179	0.356420
50%	1.000000	0.000000	1.000000	0.540519	0.653714	0.296763	0.518638
75%	1.000000	0.000000	1.000000	0.735215	0.754830	0.414447	0.684710
max	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000

8 rows × 29 columns

Building the model

In [72]:

```
# Splitting X and Y
y_train= data_train.pop('cnt')
X_train = data_train
```

In [73]:

```
# Building a model from statsmodel
X_train_lm = sm.add_constant(X_train)
model = sm.OLS(y_train, X_train_lm).fit()
print(model.summary())

# Calcilating VIF values
VIF = pd.DataFrame()
VIF['Features'] = X_train.columns
VIF['vif'] = [variance_inflation_factor(X_train.values, i) for i in range(X_train.shape
[1])]
VIF['vif'] = round(VIF['vif'],2)
VIF = VIF.sort_values(by = "vif", ascending = False)
print(VIF)
```

OLS Regression Results

========	======		=======			======
====						
Dep. Varial	ole:	С	nt R-sq	uared:		
0.853						
Model:		0	LS Adj.	R-squared:		
0.845			3	•		
Method:		Least Squar	es F-sta	atistic:		1
03.8						
Date:		Mon, 05 Oct 20	20 Prob	(F-statisti	c).	8.74e
-182		11011, 05 000 20	2000	(. 50001501	,.	01710
Time:		18:38:	24 Ing-	Likelihood:		52
7.95		10.50.	24 LOG	LIKCIIII00u.		32
No. Observa	ations:	5	10 AIC:			-9
99.9	actons.	,	10 AIC.			- 5
Df Residua	le•	1	82 BIC:			-8
81.3	15.	4	62 DIC.			-0
Df Model:			27			
Covariance	Typo:	nonrobu				
========						
		coof	ctd onn	t	P> t	
[0 025	0.0751	coei	Stu en	·	P> L	
[0.025	_					
const		0.2429	0.035	6.854	0.000	
	0 212	0.2429	0.033	0.034	0.000	
0.173	0.313	0 2221	0.000	20, 020	0.000	
yr	0.240	0.2321	0.008	28.820	0.000	
0.216	0.248	0.0067	0.024	0 270	0.701	
holiday	0.054	0.0067	0.024	0.278	0.781	-
0.041	0.054	0.0027	0.013	7 702	0.000	
workingday	0 117	0.0937	0.012	7.783	0.000	
0.070	0.117	0.4506	0.046	0.734	0.000	
temp	0 543	0.4506	0.046	9.734	0.000	
0.360	0.542	0 4543	0.020	2 022	0.000	
hum	0.076	-0.1513	0.038	-3.933	0.000	-
0.227	-0.076	0.1065	0.026	7 257	0.000	
windspeed	0.436	-0.1865	0.026	-7.257	0.000	-
0.237	-0.136	0.0403	0.030	1 607	0 100	
season_spr:	•	-0.0482	0.030	-1.607	0.109	-
0.107	0.011	0.0207	0.026	1 470	0 140	
season_sumr		0.0387	0.026	1.478	0.140	-
0.013	0.090	0 1050	0.000	2 704	0.000	
season_wint		0.1058	0.028	3.794	0.000	
0.051	0.161	0.0144	0.024	0 430	0.660	
mnth_Aug	0.001	0.0144	0.034	0.428	0.669	-
0.052	0.081	0.0456	0.024	1 250	0 175	
mnth_Dec	0.000	-0.0456	0.034	-1.358	0.175	-
0.112	0.020	0.0222	0.022	0.000	0 227	
mnth_Feb	0 022	-0.0323	0.033	-0.982	0.327	-
0.097	0.032	0.0630	0.024	1 073	0.063	
mnth_Jan	0.003	-0.0628	0.034	-1.873	0.062	-
0.129	0.003	0.0404	0 025	4 454	0.250	
mnth_Jul	0.000	-0.0404	0.035	-1.151	0.250	-
0.109	0.029	0.0000	0 00-	0 440	0.000	
mnth_Jun	0.046	-0.0030	0.025	-0.119	0.906	-
0.052	0.046	0.0040	0 00-	0.040	0.055	
mnth_Mar	0.040	0.0010	0.025	0.043	0.966	-
0.047	0.049	0.0000	0 001	4 440	0 255	
mnth_May	0.005	0.0239	0.021	1.140	0.255	-
0.017	0.065					

mnth_Nov		-0.0419	0.036	-1.152	0.250	-
0.113	0.030					
mnth_Oct		0.0075	0.036	0.211	0.833	-
0.063	0.078					
mnth_Sep		0.0811	0.032	2.533	0.012	
0.018	0.144					
weekday_mondata		0.0985	0.013	7.300	0.000	
0.072 0.125						
weekday_sat	urdata	-0.0038	0.015	-0.263	0.793	-
0.033	0.025					
weekday_sun	data	0.0054	0.015	0.362	0.718	-
0.024	0.035					
weekday_thu		-0.0135	0.015	-0.917	0.359	-
0.042	0.015					
weekday_tue		0.0440	0.014	3.213	0.001	
0.017	0.071					
weekday_wednesdata		-0.0155	0.015	-1.064	0.288	-
0.044	0.013					
weathersit_	•	-0.2574	0.026	-9.778	0.000	-
	-0.206					
weathersit_	_	-0.0611	0.010	-5.854	0.000	-
	-0.041					
==========	=========		======	=======	======	=====
Omnibus:		84.475	Durbin	-Watson:		
2.040						
Prob(Omnibu	s):	0.000	Jarque	-Bera (JB):		23
5.382	•		•	` ,		
Skew:		-0.804	Prob(J	B):		7.72
e-52			•	•		
Kurtosis:		5.914	Cond.	No.		1.05
e+15						
========			======		======	=====
====						

Notes:

- $\[1\]$ Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The smallest eigenvalue is 1.43e-27. This might indicate that there are

strong multicollinearity problems or that the design matrix is singular.

3 61 0116	marcreorrinear rey pr	ODICHIS	•
	Features	vif	
2	workingday	86.81	
20	weekday_mondata	19.72	
24	weekday_tuesdata	18.35	
6	season_spring	10.79	
8	season_winter	9.50	
7	season_summer	8.29	
3	temp	7.12	
17	mnth_Nov	6.80	
18	mnth_Oct	6.59	
9	mnth_Aug	6.43	
12	mnth_Jan	5.90	
10	mnth_Dec	5.68	
13	mnth_Jul	5.66	
19	mnth_Sep	4.94	
1	holiday	4.59	
11	mnth_Feb	4.39	
15	mnth_Mar	3.47	
14	mnth_Jun	2.83	
16	mnth_May	2.22	

```
4
                        hum
                              2.05
25
        weekday_wednesdata
                              1.78
21
         weekday saturdata
                              1.62
22
           weekday_sundata
                              1.61
23
         weekday thursdata
                              1.61
27
    weathersit_Mist+cloudy
                              1.60
26
     weathersit_Light snow
                              1.29
5
                  windspeed
                              1.24
0
                         yr
                              1.06
```

Here the no of variables to be eliminated are too high. So we use automated Feature selection method i.e: RFE

For that we need to build a model using Sklearn

In [74]:

```
from sklearn.feature_selection import RFE
from sklearn.linear_model import LinearRegression

sk_model = LinearRegression()
sk_model = sk_model.fit( X_train, y_train)

rfe = RFE(sk_model , 15)
rfe = rfe.fit( X_train, y_train)

list(zip(X_train.columns,rfe.support_,rfe.ranking_))
```

Out[74]:

```
[('yr', True, 1),
 ('holiday', True, 1),
 ('workingday', True, 1),
 ('temp', True, 1),
 ('hum', True, 1),
 ('windspeed', True, 1),
 ('season_spring', True, 1),
 ('season_summer', True, 1),
 ('season_winter', True, 1),
 ('mnth_Aug', False, 9),
 ('mnth_Dec', False, 4),
 ('mnth_Feb', False, 5),
 ('mnth_Jan', False, 2),
 ('mnth_Jul', True, 1),
 ('mnth_Jun', False, 13),
 ('mnth_Mar', False, 14),
 ('mnth_May', False, 6),
 ('mnth_Nov', False, 3),
 ('mnth_Oct', False, 11),
 ('mnth_Sep', True, 1),
 ('weekday_mondata', True, 1),
 ('weekday_saturdata', False, 12),
 ('weekday_sundata', False, 10),
 ('weekday_thursdata', False, 8),
 ('weekday_tuesdata', True, 1),
 ('weekday_wednesdata', False, 7),
 ('weathersit_Light snow', True, 1),
 ('weathersit_Mist+cloudy', True, 1)]
```

```
In [75]:
```

```
# The selected features from the RFE process are
X_train = X_train[X_train.columns[rfe.support_]]
```

Re-Build the model using the new training set using statsmodel

In [76]:

```
# Building a model from statsmodel
X_train_lm = sm.add_constant(X_train)
model = sm.OLS(y_train, X_train_lm).fit()
print(model.summary())

# Calcilating VIF values
VIF = pd.DataFrame()
VIF['Features'] = X_train.columns
VIF['vif'] = [variance_inflation_factor(X_train.values, i) for i in range(X_train.shape
[1])]
VIF['vif'] = round(VIF['vif'],2)
VIF = VIF.sort_values(by = "vif", ascending = False)
print(VIF)
```

OLS Regression Results

=======	.======		-			=======	=====		
====									
Dep. Varia	ıble:	C	cnt	R-squared:					
0.847									
Model:		(DLS	Adj.	R-squared:				
0.843									
Method:		Least Squar	res	F-STa	atistic:		1		
96.3		Man OF Oct 20	220	Doob	/F statistic	١.	1 120		
Date: -191		Mon, 05 Oct 20	020	Prob	(F-Statistic):	1.13e		
Time:		18:38:	• 25	Log-L	_ikelihood:		51		
7.87		10.50	. 23	LUG-L	ikeiinood.		71		
No. Observ	ations:		510	AIC:			-1		
006.	46101131	•		,,			_		
Df Residua	als:	4	195	BIC:			-9		
42.2									
Df Model:			14						
Covariance	Type:	nonrobu	ust						
=======	:=======	.=======			-=======	=======			
=======	=====								
		coef	sto	d err	t	P> t			
[0.025	0.975]								
const		0.1989	,	0.028	7.181	0.000			
0.144	0.253	0.1000	,	0.020	7.101	0.000			
yr	0.233	0.2297	(0.008	28.660	0.000			
0.214	0.245	0.2257	,	3.000	20.000	0.000			
holiday		-0.0190	(0.021	-0.892	0.373	_		
0.061	0.023								
workingday	1	0.0837	(0.010	8.672	0.000			
0.065	0.103								
temp		0.5278	(0.033	15.897	0.000			
0.463	0.593								
hum		-0.1595	(0.037	-4.268	0.000	-		
0.233	-0.086	0.1006			- 440				
windspeed	0 424	-0.1806	(0.025	-7.110	0.000	-		
0.231	-0.131	0.0554	,	2 021	2 604	0.007			
season_spr 0.096	-0.015	-0.0554	,	0.021	-2.694	0.007	-		
season_sum		0.0526	(0.015	3.553	0.000			
0.024	0.082	0.0320	,	0.015	3.333	0.000			
season_win		0.1003	(0.017	5.890	0.000			
0.067	0.134								
mnth_Jul		-0.0549	(0.018	-3.035	0.003	_		
0.090	-0.019								
mnth_Sep		0.0818	(0.016	4.956	0.000			
0.049	0.114								
weekday_mc		0.0937	(0.012	8.045	0.000			
0.071	0.117								
weekday_tu		0.0405	(0.012	3.304	0.001			
0.016	0.065	. 0.0463			0.440	0.000			
	Light snow	-0.2463	(0.026	-9.449	0.000	-		
0.298	-0.195 Mistaloue	ly 0 0570	,	2 212	E FFO	0 000			
weathersit 0.078	_Mist+cloud -0.037	ly -0.0578	,	0.010	-5.559	0.000	-		
		.=======	====	=====			=====		
====									
Omnibus		CA 6	270	Dunk	in Watson:				

Omnibus: 64.879 Durbin-Watson:

2.065

```
      Prob(Omnibus):
      0.000 Jarque-Bera (JB):
      15

      8.454
      5kew:
      -0.661 Prob(JB):
      3.91

      e-35
      5.390 Cond. No.
      1.00

      e+15
      ----
      ----
```

Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The smallest eigenvalue is 1.5e-27. This might indicate that there are strong multicollinearity problems or that the design matrix is singular.

```
Features
                             vif
2
               workingday 50.69
          weekday_mondata 12.20
11
         weekday_tuesdata 11.79
12
            season_spring
6
                          5.02
3
                    temp
                          3.62
                          3.49
8
            season_winter
1
                  holiday 2.91
7
                           2.61
            season_summer
4
                          1.91
                      hum
14
   weathersit_Mist+cloudy
                            1.57
9
                 mnth_Jul
                           1.49
10
                 mnth Sep
                           1.30
13
    weathersit_Light snow
                           1.25
5
                windspeed
                            1.20
0
                            1.03
                       yr
```

The holiday variable has high p value and low VIF value. So, lets eliminate it andsee the changes.

In [77]:

```
# Dropping the extra feature
X_train.drop('holiday', inplace = True, axis=1)

# Building a model from statsmodel
X_train_lm = sm.add_constant(X_train)
model = sm.OLS(y_train, X_train_lm).fit()
print(model.summary())

# Calcilating VIF values
VIF = pd.DataFrame()
VIF['Features'] = X_train.columns
VIF['vif'] = [variance_inflation_factor(X_train.values, i) for i in range(X_train.shape
[1])]
VIF['vif'] = round(VIF['vif'],2)
VIF = VIF.sort_values(by = "vif", ascending = False)
print(VIF)
```

OLS Regression Results

=======	=======	015 KC	•	======		.=======	======
====							
Dep. Variab	ble:		cnt	R-squ	uared:		
0.847							
Model:		OLS		Adj.	R-squared:		
0.843					·		
Method:		Least Squa	res	F-sta	atistic:		1
96.3		·					
Date:		Mon, 05 Oct 2	020	Prob	(F-statistic	:):	1.13e
-191		•			•	•	
Time:		18:38	3:25	Log-L	ikelihood:		51
7.87				J			
No. Observa	ations:		510	AIC:			-1
006.							
Df Residual	ls:		495	BIC:			-9
42.2							
Df Model:			14				
Covariance	Type:	nonrob	ust				
========			=====				======
========	=====						
		coef	st	td err	t	P> t	
[0.025	0.975]						
const		0.1799		0.042	4.276	0.000	
0.097	0.263				20.550		
yr 2011	0.245	0.2297		0.008	28.660	0.000	
0.214	0.245	0.4027		0 005	4 047	0.000	
workingday	0.453	0.1027		0.025	4.047	0.000	
0.053	0.152	0 5270		0 000	45 007	0.000	
temp 0.463	0.593	0.5278		0.033	15.897	0.000	
hum	0.595	-0.1595		0.037	-4.268	0.000	
0.233	-0.086	-0.1393		0.037	-4.200	0.000	_
windspeed	-0.000	-0.1806		0.025	-7.110	0.000	_
0.231	-0.131	0.1000		0.023	7.110	0.000	
season_spri		-0.0554		0.021	-2.694	0.007	_
0.096	-0.015	0.0554		0.021	2.054	0.007	
season_sumr		0.0526		0.015	3.553	0.000	
0.024	0.082	0.0320		0.013	3.333	0.000	
season_wint		0.1003		0.017	5.890	0.000	
0.067	0.134	0.1200			2.020		
mnth Jul		-0.0549		0.018	-3.035	0.003	_
0.090	-0.019						
mnth_Sep		0.0818		0.016	4.956	0.000	
0.049	0.114						
weekday_mor	ndata	0.1126		0.027	4.202	0.000	
0.060	0.165						
weekday_tu	esdata	0.0594		0.027	2.206	0.028	
0.006	0.112						
weathersit_	_Light snow	v -0.2463		0.026	-9.449	0.000	-
0.298	-0.195						
weathersit_		dy -0.0578		0.010	-5.559	0.000	-
0.078	-0.037						
	=======		=====			=======	======
====			070	ь	Co. 11-2		
Omnibus:		64.	879	Durbi	in-Watson:		
2.065 Prob(Omnibu	ue).	a	000	Jana	ue-Bera (JB):		15
8.454	us).	0.	999	Jarqu	ie-pei.a (JD);		15
U. TJ T							

```
-0.661
Skew:
                                       Prob(JB):
                                                                     3.91
e-35
                                       Cond. No.
Kurtosis:
                                5.390
25.2
Notes:
[1] Standard Errors assume that the covariance matrix of the errors is cor
rectly specified.
                  Features
                            vif
3
                      hum 32.14
2
                     temp 18.98
1
               workingday 18.41
10
          weekday_mondata
                            4.91
4
                windspeed
                           4.90
5
            season_spring
                           4.80
11
                           4.76
         weekday_tuesdata
7
            season_winter 3.71
6
            season_summer
                           3.03
                            2.31
13 weathersit_Mist+cloudy
0
                       yr
                            2.09
8
                 mnth_Jul
                            1.60
9
                 mnth_Sep
                            1.38
12
    weathersit_Light snow
                            1.25
```

Now all the P-values are set but the VIF value of the variable "hum" > 10 which is a bad sign. So, drop it.

In [78]:

```
# Dropping the extra feature
X_train.drop('hum', inplace = True, axis=1)

# Building a model from statsmodel
X_train_lm = sm.add_constant(X_train)
model = sm.OLS(y_train, X_train_lm).fit()
print(model.summary())

# Calcilating VIF values
VIF = pd.DataFrame()
VIF['Features'] = X_train.columns
VIF['vif'] = [variance_inflation_factor(X_train.values, i) for i in range(X_train.shape
[1])]
VIF['vif'] = round(VIF['vif'],2)
VIF = VIF.sort_values(by = "vif", ascending = False)
print(VIF)
```

OLS Regression Results

========			====:	======			======
====							
Dep. Variab	ole:		cnt	R-squ	ıared:		
0.842							
Model:			OLS	Adj.	R-squared:		
0.838							
Method:		Least Squa	ares	F-sta	ntistic:		2
03.0							
Date:		Mon, 05 Oct 2	2020	Prob	(F-statisti	c):	5.73e
-189							
Time:		18:38	3:25	Log-L	ikelihood:		50
8.65							
No. Observa	itions:		510	AIC:			-9
89.3			406	DTC.			0
Df Residual 30.0	.5:		496	BIC:			-9
Df Model:			13				
Covariance	Typo:	nonrol	_				
=========							
		coef	S.	td err	t	P> t	
[0.025	0.9751	202.		CG C		. , , , ,	
	_						
const		0.1005		0.038	2.618	0.009	
0.025	0.176						
yr		0.2336		0.008	28.839	0.000	
0.218	0.250						
workingday		0.1034		0.026	4.008	0.000	
0.053	0.154						
temp		0.4920		0.033	15.056	0.000	
	0.556						
windspeed		-0.1491		0.025	-6.032	0.000	-
0.198	-0.101	0.0653		0 004	2 420	0.000	
season_spri	_	-0.0653		0.021	-3.139	0.002	-
0.106	-0.024	0.0465		0.015	3.101	0.002	
season_summ 0.017	0.076	0.0403		0.013	3.101	0.002	
season_wint		0.0859		0.017	5.058	0.000	
0.053	0.119	0.0055		0.017	3.030	0.000	
mnth_Jul	0.115	-0.0500		0.018	-2.723	0.007	_
0.086	-0.014	0.0300		0.010	2.,23	0.007	
mnth_Sep		0.0758		0.017	4.532	0.000	
0.043	0.109						
weekday_mor	ndata	0.1152		0.027	4.225	0.000	
0.062	0.169						
weekday_tue	esdata	0.0571		0.027	2.085	0.038	
0.003	0.111						
weathersit_	Light sno	w -0.2904		0.024	-11.931	0.000	-
0.338	-0.243						
weathersit_	_	ıdy -0.0835		0.009	-9.669	0.000	-
0.100	-0.067						
========	=======	=========	-===:	======	.=======	=======	======
====				<u> </u>			
Omnibus:		66.	.977	purbi	n-Watson:		
2.059		^	000	7	10 Pows /3D\		10
Prob(Omnibu 3.728	15):	0.	.000	Jarqu	ıe-Bera (JB)	•	16
Skew:		_A	681	Prob('IR)·		2.80
e-36		-0.	.001	F1 00(, JU) .		2.00
2 30							

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
Features
                         vif
1
              workingday 16.19
                    temp 12.73
2
3
               windspeed 4.75
9
         weekday_mondata 4.45
         weekday_tuesdata 4.21
10
4
           season_spring 3.82
6
           season_winter 2.80
5
            season_summer 2.75
                      yr
                         2.07
0
7
                mnth_Jul
                         1.60
12
  weathersit_Mist+cloudy
                          1.58
                          1.35
8
                mnth_Sep
11
    weathersit_Light snow
                          1.09
4
```

Still there are 2 features 'workingday' and 'temp' that has VIF>10. So, drop them one by one checking the changes in VIF.

In [79]:

```
# Dropping the extra feature
X_train.drop('workingday', inplace = True, axis=1)

# Building a model from statsmodel
X_train_lm = sm.add_constant(X_train)
model = sm.OLS(y_train, X_train_lm).fit()
print(model.summary())

# Calcilating VIF values
VIF = pd.DataFrame()
VIF['Features'] = X_train.columns
VIF['vif'] = [variance_inflation_factor(X_train.values, i) for i in range(X_train.shape
[1])]
VIF['vif'] = round(VIF['vif'],2)
VIF = VIF.sort_values(by = "vif", ascending = False)
print(VIF)
```

OLS Regression Results

=======================================		=======	=========		=====
====					
Dep. Variable:	С	nt R-squ	ared:		
0.837					
Model:	0	LS Adj.	R-squared:		
0.833		J	•		
Method:	Least Squar	es F-sta	tistic:		2
12.1					
Date:	Mon, 05 Oct 20	20 Proh	(F-statistic)		1.01e
-186	11011, 05 000 20		(. 500015010)	•	2.020
Time:	18:38:	25 Log-L	ikelihood:		50
0.52	10.50.	25 LOG L	IKCIIIIOOU.		50
No. Observations:	Ε.	10 AIC:			-9
75.0	.ر	io Aic.			-)
Df Residuals:	1	97 BIC:			-9
20.0	4	97 BIC.			- 3
Df Model:	,	12			
Covariance Type:					
=======================================	==========	=======	=========	=======	=====
==========	C		<u>.</u>	D. [4]	
	coet	sta err	t	P> T	
[0.025 0.975]					
const	0.2005	0.030	6.771	0.000	
0.142 0.259					
yr	0.2341	0.008	28.476	0.000	
0.218 0.250					
temp	0.4934	0.033	14.874	0.000	
0.428 0.559					
windspeed	-0.1513	0.025	-6.031	0.000	-
0.201 -0.102					
season_spring	-0.0679	0.021	-3.217	0.001	-
0.109 -0.026					
season_summer	0.0469	0.015	3.081	0.002	
0.017 0.077					
season_winter	0.0829	0.017	4.818	0.000	
0.049 0.117					
mnth_Jul	-0.0492	0.019	-2.639	0.009	-
0.086 -0.013					
mnth_Sep	0.0721	0.017	4.257	0.000	
0.039 0.105					
weekday_mondata	0.0157	0.011	1.371	0.171	_
0.007 0.038					
weekday_tuesdata	-0.0422	0.012	-3.562	0.000	_
0.066 -0.019					
weathersit_Light sn	ow -0.2858	0.025	-11.578	0.000	_
0.334 -0.237					
weathersit_Mist+clo	udy -0.0816	0.009	-9.323	0.000	_
0.099 -0.064	,	3,332	2,022	0.000	
=======================================					=====
====					
Omnibus:	80.7	63 Durhi	n-Watson:		
2.010	30.7				
Prob(Omnibus):	0.0	aa Tandu	e-Bera (JB):		21
0.920	0.0	oo bar qu	C DC1 a (3D).		4 1
Skew:	-0.7	91 Prob(TR)·		1.58
e-46	-0.7)	30).		1.50
Kurtosis:	5.7	25 Cond.	No		
17.5	J. 7.				
±1.0					

====

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
vif
                 Features
1
                    temp 5.17
2
                windspeed 4.62
4
            season_summer 2.23
3
            season_spring 2.11
0
                      yr 2.07
            season_winter 1.82
5
                 mnth_Jul 1.59
6
11 weathersit_Mist+cloudy 1.55
7
                 mnth_Sep 1.33
8
          weekday_mondata 1.22
9
         weekday_tuesdata 1.21
10
    weathersit_Light snow 1.08
```

Now weekday_mondata has high p value. drop it

In [80]:

```
# Dropping the extra feature
X_train.drop('weekday_mondata', inplace = True, axis=1)

# Building a model from statsmodel
X_train_lm = sm.add_constant(X_train)
model = sm.OLS(y_train, X_train_lm).fit()
print(model.summary())

# Calcilating VIF values
VIF = pd.DataFrame()
VIF['Features'] = X_train.columns
VIF['vif'] = [variance_inflation_factor(X_train.values, i) for i in range(X_train.shape
[1])]
VIF['vif'] = round(VIF['vif'],2)
VIF = VIF.sort_values(by = "vif", ascending = False)
print(VIF)
```

OLS Regression Results

=======	=======	========	:====:	======		=======	======
====							
Dep. Varia 0.836	ble:		R-squ				
Model:			Adj.	R-squared:			
0.832 Method:		Least Squa	ares	F-sta	ntistic:		2
30.8 Date:		Mon, 05 Oct 2				c):	1.65e
-187 Time:		18:38	2.25	Log-L	ikelihood:	·	49
9.56		10.50	0.23	_	ikeiinood.		
No. Observ 75.1	ations:		510	AIC:			-9
Df Residua 24.3	ls:		498	BIC:			-9
Df Model:			11				
Covariance		nonrob	oust				
		========	:====:	======			======
		coef	s [.]	td err	t	P> t	
[0.025	-						
const		0.2036		0.030	6.889	0.000	
0.146	0.262	0.2030		0.030	0.003	0.000	
yr	0,101	0.2338		0.008	28.423	0.000	
0.218	0.250						
temp		0.4923		0.033	14.832	0.000	
	0.557	0 1400		0 005	F 070	0.000	
windspeed 0.199	-0.100	-0.1498		0.025	-5.970	0.000	-
season_spr		-0.0680		0.021	-3.219	0.001	-
0.109	-0.026						
season_sum	mer 0.077	0.0467		0.015	3.067	0.002	
0.017 season_win		0.0831		0.017	4.824	0.000	
0.049	0.117	0.0031		0.017	4.024	0.000	
mnth_Jul		-0.0486		0.019	-2.607	0.009	-
0.085 mnth_Sep	-0.012	0.0721		0.017	4.253	0.000	
0.039	0.105	0,0,21		0.017	55	0.000	
weekday_tu 0.068	esdata -0.022	-0.0451		0.012	-3.862	0.000	-
weathersit	_Light sno	w -0.2856		0.025	-11.560	0.000	-
0.334 weathersit	-0.237 _Mist+clou	dy -0.0816		0.009	-9.311	0.000	-
0.099	-0.064						
	======	========	:====:	======		=======	======
==== Omnibus:		76	151	Dunhi	in-Watson:		
2.009		70.	1)1	נט וטט	in-watson.		
Prob(Omnib	us):	0.	000	Jarqu	ue-Bera (JB)	:	20
7.716 Skew:		-0.	733	Prob((JB):		7.85
e-46 Kurtosis:		E	762	Cond.	No		
17.4		٥.	702	conu.	110.		
	=======			=====	:=======	=======	======
====							

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
Features
                          vif
1
                     temp 5.13
                windspeed 4.60
2
4
            season_summer 2.22
3
            season_spring 2.09
                       yr 2.07
0
            season_winter 1.80
5
6
                 mnth_Jul 1.59
10 weathersit_Mist+cloudy 1.55
                 mnth_Sep 1.33
7
8
         weekday_tuesdata 1.17
9
    weathersit_Light snow 1.08
```

Now lets calculate the ${\cal R}^2$ value for the actual and predicted values for the training set.

In [81]:

```
# Predicted value of the training data.
y_train_pred = model.predict(X_train_lm)
```

In [82]:

```
# Calculating the R2 value for the
from sklearn.metrics import r2_score
r2_score(y_true=y_train , y_pred=y_train_pred)
```

Out[82]:

0.8360233701515918

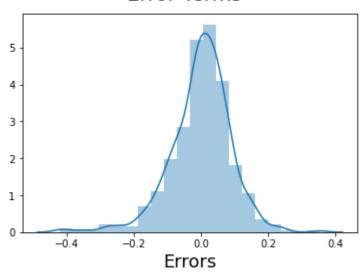
In [83]:

```
# Plot the histogram of the error terms
fig = plt.figure()
sns.distplot((y_train - y_train_pred), bins = 20)
fig.suptitle('Error Terms', fontsize = 20)  # Plot heading
plt.xlabel('Errors', fontsize = 18)
```

Out[83]:

Text(0.5, 0, 'Errors')

Error Terms

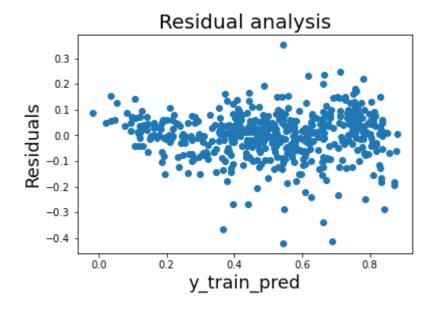


In [99]:

```
# Error terms are independent of each other
residuals = y_train - y_train_pred
plt.scatter( y_train_pred,residuals)
plt.title('Residual analysis', fontsize = 20)  # Plot heading
plt.xlabel('y_train_pred', fontsize = 18)
plt.ylabel('Residuals', fontsize = 18)
```

Out[99]:

Text(0, 0.5, 'Residuals')



In []:

Testing and Evaluation

```
In [84]:
```

```
data_test[data_test.columns] = scaler.transform(data_test[data_test.columns])
```

```
In [85]:
```

```
data_test['yr']
Out[85]:
       0.0
184
535
       1.0
299
       0.0
221
       0.0
152
       0.0
400
      1.0
702
       1.0
127
       0.0
640
       1.0
72
       0.0
Name: yr, Length: 219, dtype: float64
In [86]:
# Splitting X,y
```

X_test = data_test

y_test = data_test.pop('cnt')

```
In [87]:

X_test_lm = sm.add_constant(X_test)

X_test_lm = X_test_lm[X_train_lm.columns]
```

Out[87]:

 $X_{test_{m}}$

	const	yr	temp	windspeed	season_spring	season_summer	season_winter	mnth
184	1.0	0.0	0.831783	0.084219	0.0	0.0	0.0	
535	1.0	1.0	0.901354	0.153728	0.0	1.0	0.0	
299	1.0	0.0	0.511964	0.334206	0.0	0.0	1.0	
221	1.0	0.0	0.881625	0.339570	0.0	0.0	0.0	
152	1.0	0.0	0.817246	0.537414	0.0	1.0	0.0	
400	1.0	1.0	0.257562	0.287411	1.0	0.0	0.0	
702	1.0	1.0	0.519232	0.283397	0.0	0.0	1.0	
127	1.0	0.0	0.584649	0.069510	0.0	1.0	0.0	
640	1.0	1.0	0.745598	0.052115	0.0	0.0	1.0	
72	1.0	0.0	0.331557	0.203418	1.0	0.0	0.0	

219 rows × 12 columns

4

In [88]:

```
y_test_pred = model.predict(X_test_lm)
r2_score(y_true = y_test, y_pred = y_test_pred)
```

Out[88]:

0.805407680173852

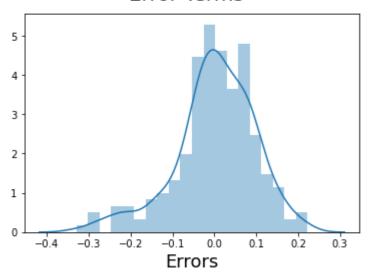
In [101]:

```
# Plot the histogram of the error terms
fig = plt.figure()
sns.distplot((y_test - y_test_pred), bins = 20)
fig.suptitle('Error Terms', fontsize = 20)  # Plot heading
plt.xlabel('Errors', fontsize = 18)
```

Out[101]:

Text(0.5, 0, 'Errors')

Error Terms



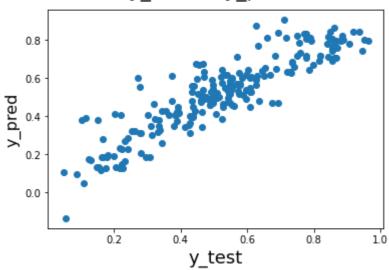
In [90]:

```
fig = plt.figure()
plt.scatter(y_test, y_test_pred)
fig.suptitle('y_test vs y_pred', fontsize = 20)  # Plot heading
plt.xlabel('y_test', fontsize = 18)  # X-label
plt.ylabel('y_pred', fontsize = 16)
```

Out[90]:

Text(0, 0.5, 'y_pred')





Ι	n]	:						

In []: