

**Bài 1.**

$$x^2 + y^2 + z^2 = 0 \tag{I}$$

**Bài 2.**

$$F = \{F_x \in F_c : (|S| > |C|) \cap (M_{inPixels} < |S| < max_{inPixels}) \cap (|S_{connected}| > |S| - \epsilon)\} \tag{1}$$

**Bài 3.**

$x = 1$	$xy = 2$	$xyz = 3$
$xy = 23$	$xyz = 3$	$x = 11$
$xyz = 345$	$x = 1$	$xyz = 22$

**Bài 4.**

$$x_1x_2x_3 = \frac{-d}{a}$$

[2]

$$x_1x_2 + x_2x_3 + x_3x_1 = \frac{c}{a}$$

[3]

Đồng thời:

$$x_1 + x_2 + x_3 = \frac{-b}{a}$$

[4]

**Bài 5.**

Vế trái

$$\overbrace{A^+_+ + B^-_+ + A^{BC^2} + \frac{\omega}{\Phi}} = \underbrace{A^+_+ + B^*_+ + 12\frac{A^B}{C} + \frac{\Omega}{\varphi}}_{\text{Vế phải}}$$

(Pt.5)

Bài 6.

$$\frac{(\sqrt{3} + \sqrt{2})}{\sqrt{5} - \sqrt{7}} = \frac{(\sqrt{3} + \sqrt{2})(\sqrt{5} + \sqrt{7})}{(\sqrt{5} - \sqrt{7})(\sqrt{5} + \sqrt{7})} = \frac{(\sqrt{3} + \sqrt{2})(\sqrt{5} + \sqrt{7})}{(\sqrt{5} + \sqrt{7})} \quad (2)$$

Bài 7.

Listing 1: Mã nguồn Python

```
1 def factorial(n):
2     if n == 0 or n == 1:
3         return 1
4     else:
5         return n * factorial(n - 1)
6
7 num = 5
8 result = factorial(num)
9 print(f"The factorial of {num} is {result}.")
```

Bài 7.

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**Algorithm 1** QuickSort

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```
1: procedure QUICKSORT(arr, low, high)
2:   if low < high then
3:     pivot ← PARTITION(arr, low, high)
4:     QUICKSORT(arr, low, pivot - 1)
5:     QUICKSORT(arr, pivot + 1, high)

6: procedure PARTITION(arr, low, high)
7:   pivot ← arr[high]
8:   i ← low - 1
9:   for j ← low to high - 1 do
10:    if arr[j] ≤ pivot then
11:      i ← i + 1
12:      swap arr[i] and arr[j]
13:  swap arr[i + 1] and arr[high]
14:  return i + 1
```

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Now the exponent in the joint density in (4-11) can be simplified. By Result 4.9(a),

$$\begin{aligned} (\mathbf{x}_j - \boldsymbol{\mu})' \boldsymbol{\Sigma}^{-1} (\mathbf{x}_j - \boldsymbol{\mu}) &= tr[(\mathbf{x}_j - \boldsymbol{\mu})' \boldsymbol{\Sigma}^{-1} (\mathbf{x}_j - \boldsymbol{\mu})] \\ &= tr[\boldsymbol{\Sigma}^{-1} (\mathbf{x}_j - \boldsymbol{\mu}) (\mathbf{x}_j - \boldsymbol{\mu})'] \end{aligned} \quad (4-12)$$

Next,

$$\begin{aligned} \sum_{j=1}^n (\mathbf{x}_j - \boldsymbol{\mu})' \boldsymbol{\Sigma}^{-1} (\mathbf{x}_j - \boldsymbol{\mu}) &= \sum_{j=1}^n tr[(\mathbf{x}_j - \boldsymbol{\mu})' \boldsymbol{\Sigma}^{-1} (\mathbf{x}_j - \boldsymbol{\mu})] \\ &= \sum_{j=1}^n tr[\boldsymbol{\Sigma}^{-1} (\mathbf{x}_j - \boldsymbol{\mu}) (\mathbf{x}_j - \boldsymbol{\mu})'] \\ &= tr \left[ \boldsymbol{\Sigma}^{-1} \left( \sum_{j=1}^n (\mathbf{x}_j - \boldsymbol{\mu}) (\mathbf{x}_j - \boldsymbol{\mu})' \right) \right] \end{aligned} \quad (4-13)$$