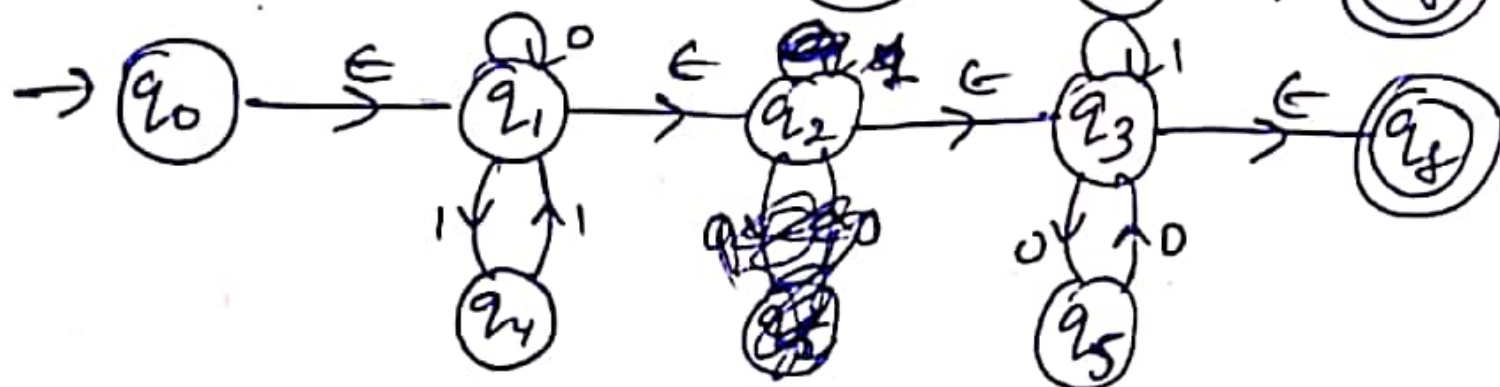
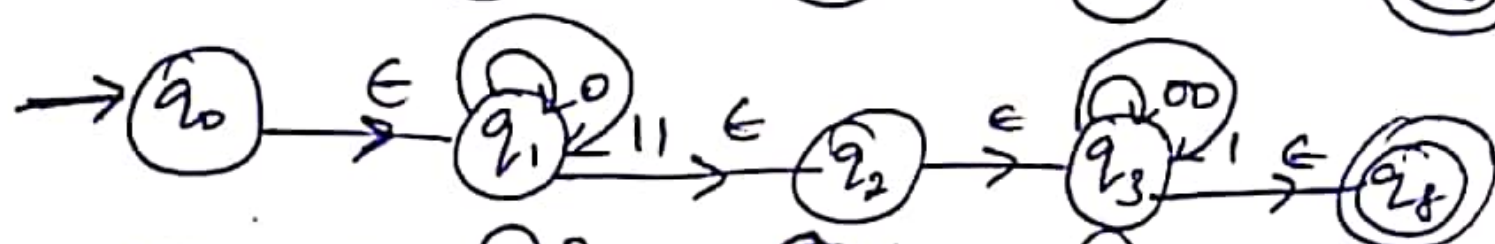
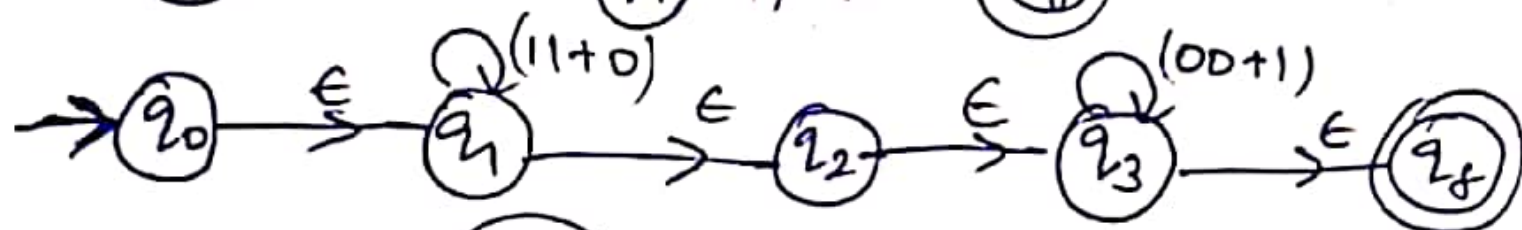
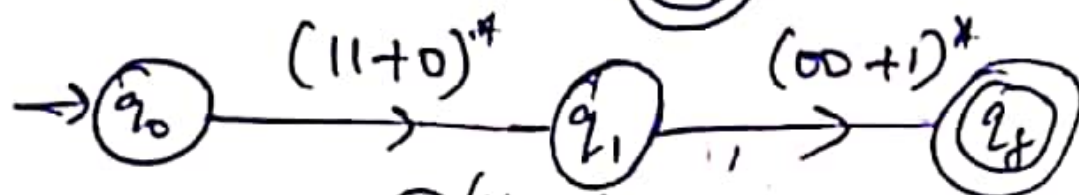
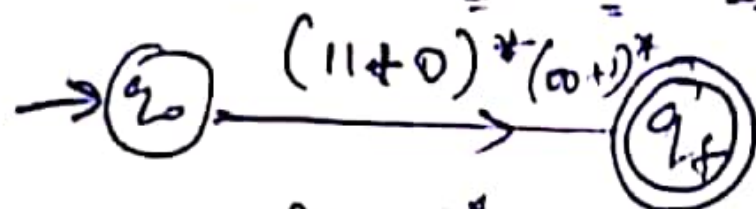


1. Convert RE $(11+0)^*(00+1)^*$ to NFA.

Sol: Conversion of RE - NFA - ϵ .



Conversion of NFA - ϵ to NFA.

| δ' | 0 | 1 | ϵ |
|-----------|-------------|-------------|-------------|
| q_0 | \emptyset | \emptyset | q_1 |
| q_1 | q_1 | q_4 | q_2 |
| q_2 | \emptyset | \emptyset | q_3 |
| q_3 | q_5 | q_3 | q_f |
| q_4 | \emptyset | q_1 | \emptyset |
| q_5 | q_3 | \emptyset | \emptyset |
| q_f | \emptyset | \emptyset | \emptyset |

ϵ -closure(q_0) = q_0, q_1, q_2, q_3, q_4

ϵ -closure(q_1) = q_1, q_2, q_3, q_f

ϵ -closure(q_2) = q_2, q_3, q_f

ϵ -closure(q_3) = q_5, q_f

ϵ -closure(q_4) = q_4

ϵ -closure(q_5) = q_5

ϵ -closure(q_f) = q_f

$$\begin{aligned}
 \delta'(q_0, 0) &= \epsilon\text{-closure}(\delta(\delta(q_0, \epsilon)), 0) = \epsilon\text{-closure}(\delta(q_1, 0)) \\
 &= \epsilon\text{-closure}(\delta(q_0, 0) \cup \delta(q_1, 0) \cup \delta(q_2, 0) \cup \delta(q_3, 0) \cup \delta(q_4, 0)) \\
 &= \epsilon\text{-closure}(\emptyset \cup q_1 \cup \emptyset \cup q_5, \emptyset) \\
 &= \epsilon\text{-closure}(q_1) \cup \epsilon\text{-closure}(q_5) = (q_1, q_2, q_3, q_4) \cup (q_5) \\
 &= q_1, q_2, q_3, q_4, q_5
 \end{aligned}$$

$$\begin{aligned}
 \delta'(q_0, 1) &= \epsilon\text{-closure}(\delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_2, 1) \cup \delta(q_3, 1) \cup \delta(q_4, 1)) \\
 &= \epsilon\text{-closure}(\emptyset \cup q_4 \cup \emptyset \cup q_3 \cup \emptyset) = \epsilon\text{-closure}(q_4) \cup \epsilon\text{-closure}(q_3) \\
 &= (q_4) \cup (q_3, q_4) = q_3, q_4, q_5
 \end{aligned}$$

$$\begin{aligned}
 \delta'(q_1, 0) &= \epsilon\text{-closure}(q_1, \emptyset \cup q_5 \cup \emptyset) \\
 &= \epsilon\text{-closure}(q_1) \cup \epsilon\text{-closure}(q_5) = (q_1, q_2, q_3, q_4) \cup q_5 \\
 &= q_1, q_2, q_3, q_4, q_5
 \end{aligned}$$

$$\begin{aligned}
 \delta'(q_1, 1) &= \epsilon\text{-closure}(q_4 \cup \emptyset \cup q_3 \cup \emptyset) = \epsilon\text{-closure}(q_4) \cup \epsilon\text{-closure}(q_3) \\
 &= (q_4) \cup (q_3, q_4) = q_3, q_4, q_5
 \end{aligned}$$

$$\delta'(q_2, 0) = \epsilon\text{-closure}(\emptyset \cup q_5 \cup \emptyset) = \epsilon\text{-closure}(q_5) = q_5$$

$$\delta'(q_2, 1) = \epsilon\text{-closure}(\emptyset \cup q_3 \cup \emptyset) = \epsilon\text{-closure}(q_3) = q_3, q_4$$

$$\delta'(q_3, 0) = \epsilon\text{-closure}(q_5 \cup \emptyset) = \epsilon\text{-closure}(q_5) = q_5$$

$$\delta'(q_3, 1) = \epsilon\text{-closure}(q_3 \cup \emptyset) = \epsilon\text{-closure}(q_3) = q_3, q_4$$

$$\delta(q_4, 0) = \epsilon\text{-closure}(\emptyset) = \emptyset$$

$$\delta(q_4, 1) = \epsilon\text{-closure}(q_1) = q_1, q_2, q_3, q_4, q_5$$

$$\delta(q_5, 0) = \epsilon\text{-closure}(q_3) = q_3, q_4$$

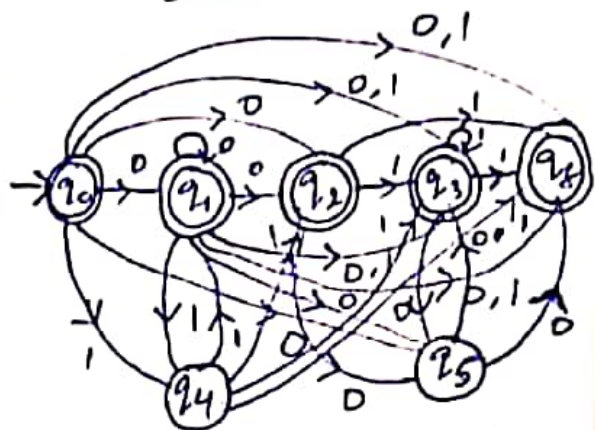
$$\delta(q_5, 1) = \epsilon\text{-closure}(\emptyset) = \emptyset$$

$$\delta'(q_f, 0) = \epsilon\text{-closure}(\emptyset) = \emptyset$$

$$\delta'(q_f, 1) = \epsilon\text{-closure}(\emptyset) = \emptyset$$

NFA

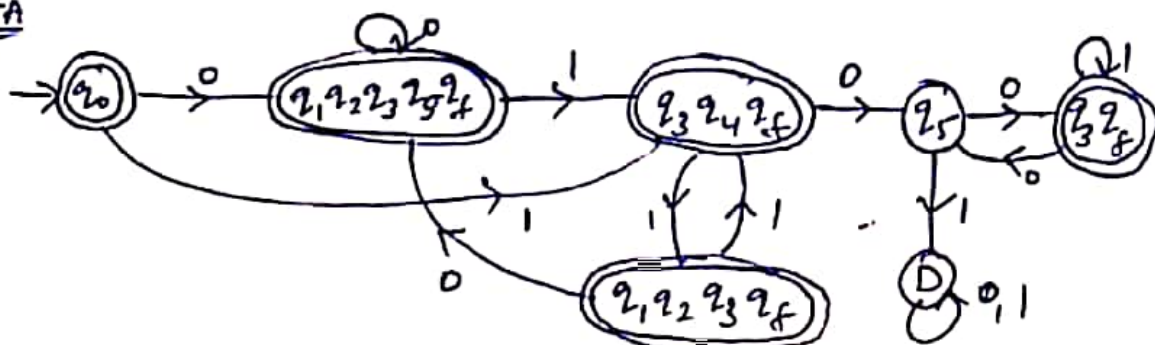
| δ' | 0 | 1 |
|-----------|-------------------------------|--------------------------|
| * q_0 | $\{q_1, q_2, q_3, q_5, q_f\}$ | $\{q_3, q_4, q_f\}$ |
| * q_1 | $\{q_1, q_2, q_3, q_5, q_f\}$ | $\{q_3, q_4, q_f\}$ |
| * q_2 | $\{q_5\}$ | $\{q_3, q_f\}$ |
| * q_3 | $\{q_5\}$ | $\{q_3, q_f\}$ |
| q_4 | $\{\emptyset\}$ | $\{q_1, q_2, q_3, q_f\}$ |
| q_5 | $\{q_3, q_f\}$ | $\{\emptyset\}$ |
| * q_f | $\{\emptyset\}$ | $\{\emptyset\}$ |



DFA-NT

| δ'' | 0 | 1 |
|-----------------------------|-------------------------------|--------------------------|
| * q_0 | $\{q_1, q_2, q_3, q_5, q_f\}$ | $\{q_3, q_4, q_f\}$ |
| * q_1, q_2, q_3, q_5, q_f | $\{q_1, q_2, q_3, q_5, q_f\}$ | $\{q_3, q_4, q_f\}$ |
| * q_3, q_4, q_f | $\{q_5\}$ | $\{q_1, q_2, q_3, q_f\}$ |
| q_5 | $\{q_3, q_f\}$ | $\{D\}$ |
| * q_1, q_2, q_3, q_5, q_f | $\{q_1, q_2, q_3, q_5, q_f\}$ | $\{q_3, q_4, q_f\}$ |
| * q_3, q_f | $\{q_5\}$ | $\{q_3, q_f\}$ |
| D | D | D |

DFA



DFA

