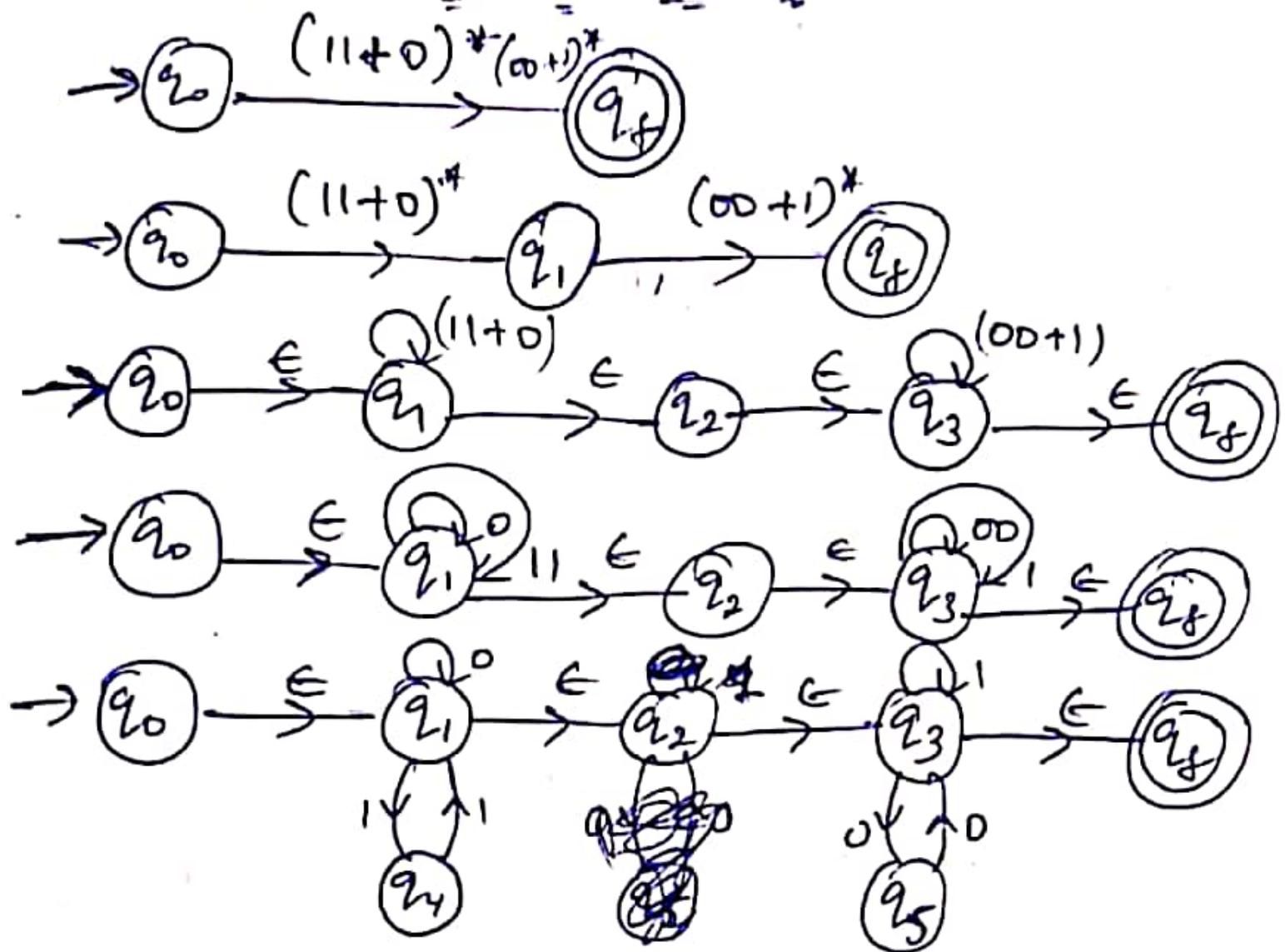


Q1. Convert RE $(11+0)^* (00+1)^*$ to NFA.

Sol1. Conversion of RE-NFA-E.



Conversion of NFA-E to NFA.

δ'	0	1	E
q_0	\emptyset	\emptyset	q_1
q_1	q_1	q_4	q_2
q_2	\emptyset	\emptyset	q_3
q_3	q_5	q_3	q_f
q_4	\emptyset	q_1	\emptyset
q_5	q_3	\emptyset	\emptyset
q_f	\emptyset	\emptyset	\emptyset

ϵ -closure(q_0) = q_0, q_1, q_2, q_3, q_f
 ϵ -closure(q_1) = q_1, q_2, q_3, q_f
 ϵ -closure(q_2) = q_2, q_3, q_f
 ϵ -closure(q_3) = q_3, q_f
 ϵ -closure(q_4) = q_4
 ϵ -closure(q_5) = q_5
 ϵ -closure(q_f) = q_f

$$\begin{aligned}
 \delta'(q_0, 0) &= \epsilon\text{-closure}(\delta(\delta(q_0, \epsilon)), 0) = \epsilon\text{-closure}(\delta(q_{0,0}), 0) \\
 &= \epsilon\text{-closure}(\delta(q_0, 0) \cup \delta(q_1, 0) \cup \delta(q_2, 0) \cup \delta(q_3, 0) \cup \delta(q_{4,0})) \\
 &= \epsilon\text{-closure}(\emptyset \cup q_1 \cup \emptyset \cup q_5 \cup \emptyset) \\
 &= \epsilon\text{-closure}(q_1) \cup \epsilon\text{-closure}(q_5) = (q_1, q_2, q_3, q_4) \cup \{q_5\} \\
 &= q_1, q_2, q_3, q_5, q_4
 \end{aligned}$$

$$\begin{aligned}
 \delta'(q_0, 1) &= \epsilon\text{-closure}(\delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_2, 1) \cup \delta(q_3, 1) \cup \delta(q_4, 1)) \\
 &= \epsilon\text{-closure}(\emptyset \cup q_4 \cup \emptyset \cup q_3 \cup \emptyset) = \epsilon\text{-closure}(q_4) \cup \epsilon\text{-closure}(q_3) \\
 &= (q_4) \cup (q_3, q_5) = q_3, q_4, q_5
 \end{aligned}$$

$$\begin{aligned}
 \delta'(q_1, 0) &= \epsilon\text{-closure}(q_1 \cup \emptyset \cup q_5 \cup \emptyset \cup \emptyset) \\
 &= \epsilon\text{-closure}(q_1) \cup \epsilon\text{-closure}(q_5) = (q_1, q_2, q_3, q_4) \cup \{q_5\} \\
 &= q_1, q_2, q_3, q_5, q_4
 \end{aligned}$$

$$\begin{aligned}
 \delta'(q_1, 1) &= \epsilon\text{-closure}(q_4 \cup \emptyset \cup q_3 \cup \emptyset) = \epsilon\text{-closure}(q_4) \cup \epsilon\text{-closure}(q_3) \\
 &= (q_4) \cup (q_3, q_5) = q_3, q_4, q_5
 \end{aligned}$$

$$\delta'(q_2, 0) = \epsilon\text{-closure}(\emptyset \cup q_5 \cup \emptyset) = \epsilon\text{-closure}(q_5) = q_5$$

$$\delta'(q_2, 1) = \epsilon\text{-closure}(\emptyset \cup q_3 \cup \emptyset) = \epsilon\text{-closure}(q_3) = q_3, q_4$$

$$\delta'(q_3, 0) = \epsilon\text{-closure}(q_5 \cup \emptyset) = \epsilon\text{-closure}(q_5) = q_5$$

$$\delta'(q_3, 1) = \epsilon\text{-closure}(\emptyset \cup q_3 \cup \emptyset) = \epsilon\text{-closure}(q_3) = q_3, q_4$$

$$\delta(q_4, 0) = \epsilon\text{-closure}(\emptyset) = \emptyset$$

$$\delta(q_4, 1) = \epsilon\text{-closure}(q_1) = q_1, q_2, q_3, q_4$$

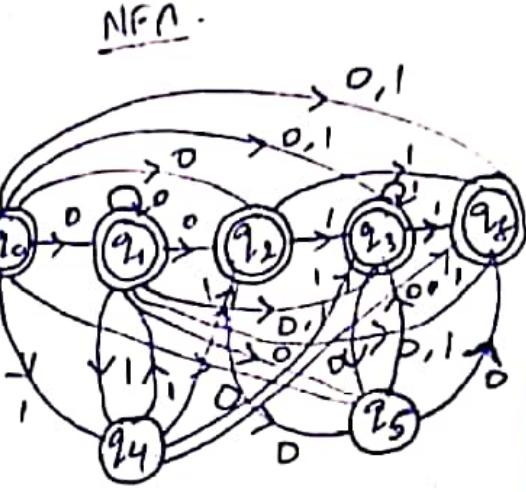
$$\delta(q_5, 0) = \epsilon\text{-closure}(q_3) = q_3, q_4$$

$$\delta(q_5, 1) = \epsilon\text{-closure}(\emptyset) = \emptyset$$

$\epsilon\text{-closure}(\emptyset) = \epsilon\text{-closure}(\emptyset) = \emptyset$

$\delta'(\{q_f\}, 1) = \epsilon\text{-closure}(d) = \emptyset$

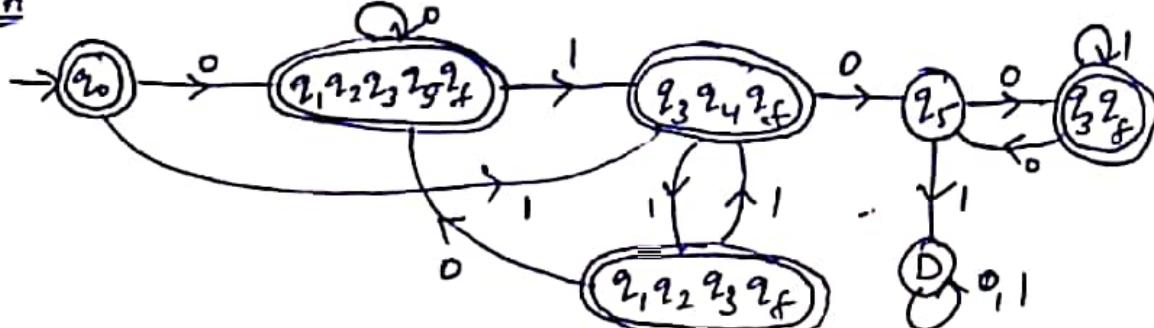
<u>NFA</u> δ'	0	1
* q_0	$\{q_1, q_2, q_3, q_5, q_f\}$	$\{q_3, q_4, q_f\}$
* q_1	$\{q_2, q_3, q_5, q_f\}$	$\{q_3, q_4, q_f\}$
* q_2	$\{q_5\}$	$\{q_3, q_5\}$
* q_3	$\{q_5\}$	$\{q_3, q_4\}$
* q_4	$\{\emptyset\}$	$\{q_3, q_4\}$
* q_5	$\{q_3, q_4\}$	$\{\emptyset\}$
* q_f	$\{\emptyset\}$	$\{\emptyset\}$



DFA - TT

δ''	0	1
* q_0	$\{q_1, q_2, q_3, q_5, q_f\}$	$\{q_3, q_4, q_f\}$
* q_1, q_2, q_3, q_5, q_f	$\{q_1, q_2, q_3, q_5, q_f\}$	$\{q_3, q_4, q_f\}$
* q_3, q_4, q_f	$\{q_5\}$	$\{q_1, q_2, q_3, q_f\}$
q_5	$\{q_3, q_f\}$	$\{\emptyset\}$
* q_1, q_2, q_3, q_f	$\{q_1, q_2, q_3, q_5, q_f\}$	$\{q_3, q_4, q_f\}$
* q_3, q_f	$\{q_5\}$	$\{q_3, q_f\}$
D	D	D

DFA



DFA

