

Microelectronic Circuits Assignment 1

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February, 2022

Question 1

Value of components (resistor/capacitor) present in the circuit:

Table 1: Calculated values for question 1

Sl. No.	Component Name	Value
1	R1(k Ω)	15k Ω
2	C1 (nF)	1nF

Circuit as on LT SPICE

Graphs

Miscellaneous calculations

Question 2

Value of components (resistors/gain) present in the circuit

Table 2: Calculated values for question 2

Sl. No.	Component Name	Value
1	$R_1(k\Omega)$	$30k\Omega$
2	$R_2(k\Omega)$	$17k\Omega$
3	$R_3(k\Omega)$	$30k\Omega$
4	$R_4(k\Omega)$	$50k\Omega$
5	k	18 V/V

Circuit as on LT SPICE

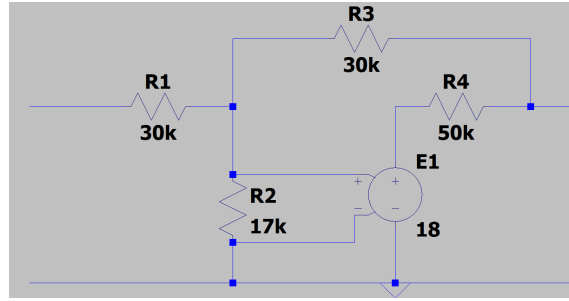


Figure 1: Original 2 port network simulated on LT SPICE

Z, Y and h Parameters

Z parameters

Z parameters as obtained from LT SPICE

$$Z = \begin{bmatrix} 23.492822k\Omega & -4.0669856k\Omega \\ -47.99043k\Omega & -11.24402k\Omega \end{bmatrix}$$

Y parameters

$$Y = \begin{bmatrix} 0.0k\Omega & 0.0k\Omega \\ 0.0k\Omega & 0.0k\Omega \end{bmatrix}$$

H parameters

$$H = \begin{bmatrix} 0.0k\Omega & 0.0 \\ 0.0 & 0.0k\Omega \end{bmatrix}$$

Calculations

Z parameters

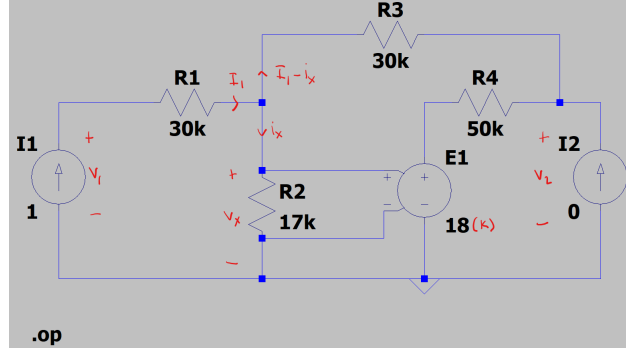


Figure 2: Z parameter circuit 1 (for z_{11} and z_{21})

Assume the convention in the above circuit for the calculations that follow

$$\begin{aligned}
 &-(I_1 - i_x)(R_3 + R_4) - kV_x + V_x = 0 \\
 &(i_x - I_1)(R_3 + R_4) = V_x(k - 1) \\
 &(i_x - I_1)(R_3 + R_4) = i_x R_2(k - 1) \\
 &i_x(R_3 + R_4 - R_2(k - 1)) = I_1(R_3 + R_4) \\
 &\implies i_x = I_1 \frac{(R_3 + R_4)}{R_3 + R_4 - R_2(k - 1)} \\
 &V_1 = I_1 R_1 + V_x \\
 &V_1 = I_1 R_1 + i_x R_2 \\
 &V_1 = I_1 \left(R_1 + \frac{R_2(R_3 + R_4)}{R_3 + R_4 - R_2(k - 1)} \right) \\
 &\implies \frac{V_1}{I_1} = \boxed{z_{11} = R_1 + \frac{R_2(R_3 + R_4)}{R_3 + R_4 - R_2(k - 1)}}
 \end{aligned}$$

Also :

$$\begin{aligned}
 &V_2 = (I_1 - i_x)R_4 + kV_x \\
 &V_2 = (I_1 - i_x)R_4 + k i_x R_2 \\
 &V_2 = i_x(kR_2 - R_4) + I_1 R_4 \\
 &V_2 = I_1 \left(R_4 + \frac{(kR_2 - R_4)(R_3 + R_4)}{R_3 + R_4 - R_2(k - 1)} \right) \\
 &\implies \frac{V_2}{I_1} = \boxed{z_{21} = R_4 + \frac{(kR_2 - R_4)(R_3 + R_4)}{R_3 + R_4 - R_2(k - 1)}}
 \end{aligned}$$

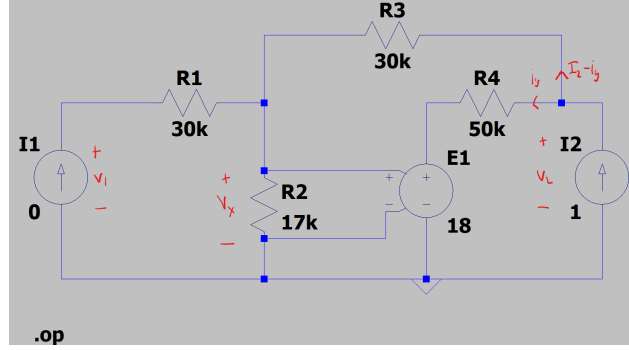


Figure 3: Z parameter circuit 2 (for z_{12} and z_{22})

Assume the convention in the above circuit for the calculations that follow

$$\begin{aligned}
 -R_3(I_2 - i_y) - V_x + kV_x + i_y R_4 &= 0 \\
 i_y R_4 - R_3(I_2 - i_y) &= (1 - k)V_x \\
 i_y R_4 - R_3(I_2 - i_y) &= (1 - k)(I_2 - i_y)R_2 \\
 i_y R_4 &= (I_2 - i_y)[(1 - k)R_2 + R_3] \\
 (R_4 + R_3 + (1 - k)R_2)i_y &= I_2[(1 - k)R_2 + R_3] \\
 \implies i_y &= I_2 \frac{(1 - k)R_2 + R_3}{(1 - k)R_2 + R_3 + R_4} \\
 V_2 &= i_y R_4 + kV_x \\
 V_2 &= i_y R_4 + k(I_2 - i_y)R_2 \\
 V_2 &= i_y [R_4 - kR_2] + KI_2 R_2 \\
 V_2 &= I_2 \left[\frac{(R_4 - kR_2)[(1 - k)R_2 + R_3]}{(1 - k)R_2 + R_3 + R_4} + kR_2 \right] \\
 \implies \frac{V_2}{I_2} &= \boxed{z_{22} = \frac{(R_4 - kR_2)[(1 - k)R_2 + R_3]}{(1 - k)R_2 + R_3 + R_4} + kR_2}
 \end{aligned}$$

Also :

$$\begin{aligned}
 V_1 &= V_x = (I_2 - i_y)R_2 \\
 V_1 &= I_2 R_2 \left[1 - \frac{(1 - k)R_2 + R_3}{(1 - k)R_2 + R_3 + R_4} \right] \\
 \implies \frac{V_1}{I_2} &= \boxed{z_{12} = R_2 \left[1 - \frac{(1 - k)R_2 + R_3}{(1 - k)R_2 + R_3 + R_4} \right]}
 \end{aligned}$$

Using the corresponding values taken from [2](#) into the above equations, we get the matrix for the Z parameters:

$$Z = \begin{bmatrix} 23.49282297k\Omega & -4.066985646k\Omega \\ -47.99043062k\Omega & -11.244041914k\Omega \end{bmatrix}$$

Which is in accordance with the values obtained from the simulation.

Load resistance value at port 2