A Method of Metamorphic Relations Constructing for Object-oriented Software Testing

首先根据面向对象的软件程序构造蜕变关系标准

然后构造蜕变关系 最后根据蜕变关系标准提高蜕变关系

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Abstract—To solve the Oracle problem of methods sequence in object-oriented software testing, a method of metamorphic relations constructing for object-oriented software testing based on algebraic specification was proposed. Firstly, metamorphic relations constructing criteria for object-oriented testing was defined based on the characteristics of object-oriented software program. Then metamorphic relations were constructed based on GFT algorithm (Generating a Finite Number of Test Case). Finally the metamorphic relations were improved according to these criteria. The improved method was verified through constructing IntStrack class and SavAcc class metamorphic relations. The experiment results show that the metamorphic relations redundancy is decreased significantly. So the new method has a low metamorphic relations redundancy and improves the efficiency of software testing.

Keywords—Object oriented; metamorphic relation; algebraic specification 冗余

I. INTRODUCTION

Software testing is an important part in the process of software development, and the traditional testing technology is restricted by the Oracle problem[1], that in some situations, it is impossible or practically too difficult to decide whether the program outputs on the test cases are correct. So it is difficult to determine whether the program execution results are identical to the expected results. A metamorphic testing methods has been proposed by Chen et al[2]. It is an automated approach to allegiating the oracle program which can check correctness of the program by compare multiple executions.

It is obvious that metamorphic relations are the core part of the metamorphic testing, as they are not only used in test case generation, but also provide a mechanism for test result verification, and it is related to the efficiency of the test. There will be some problems, one of them is lacking necessary metamorphic relations constructing criteria[3-4]. Its negative influences lies in two aspects: 1) generate a large number of test cases that have similar function. 2) testing is inadequate because of low functional coverage.

Some construction methods of metamorphic relation have been presented. Upulee Kanewala[5] proposed a metamorphic relation constructing method using machine leaning techniques. Huai Liu[6] proposed composite metamorphic relation constructing method based on the already identified metamorphic relations. MURRHY[7] proposed seven general metamorphic relation constructing criteria, but it's only suitable for numerical procedure. Zhan-we Hui[8] construct a decomposition model for metamorphic relation with the formal model and provide three sub-relations for decrease complexity of metamorphic relation. Although Wang Rong[9] summed up a series of the basic guidelines for metamorphic relation on the basis of previous work, he did not give a specific construction method. When we test object-oriented programs all these methods mentioned above are not possible. So it is necessary to propose a object-oriented metamorphic relation construction method.

In object-oriented testing, when testing method sequence of the class, test case consists of a sequence method and the corresponding parameter values. Jinan University Professor Chen Huo-yen[10-12] proposed GFT algorithm to generate a limited number of base pairs as a test case based on algebraic specifications. In a given algebraic specification, replace class variables with normal form that its lengths less than positive integer k to generate a finite equivalence base pairs as the test case.

GTF算法的缺点

By examining the GFT algorithm, the following shortcomings are found: (1) the value K is difficult to determine. although the K value is determined by white-box information, metamorphic relation also contains a lot of redundancy. (2) Replace variables in axiom with normal form may generate wrong metamorphic relation because of not considering semantic errors, such as cross-border problems. (3) GFT only relies on axiom. Metamorphic relation constructed based on GFT is inadequate, because it's not

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verified the object state after method calling.

As for the drawback of the GFT, we makes the improvements for GFT. First, using white-box information to select normal form can reduce the redundancy of metamorphic relations; Secondly, proposed a method of metamorphic relations constructing for object-oriented software. This method ensure that the object state of all methods can be tested, and increase the adequacy of metamorphic relations. At last, when conducting a test, the metamorphic relation will be generated into a test case, thus the returned value of the object and the object's current state can be employed to judge the equivalence property of execution of results, which to a certain extent simplifies the Oracle problem of object-oriented class-level testing.

II. CONCEPTS

Definition 1(metamorphic relation, MR)[13] Suppose that program P computes function f, which is also referred to as the specification that P must accord with. Let $x_1, x_2...x_n$ (n > 1) be n different inputs of function f, if their satisfaction of relation r implies that their corresponding outputs $f(x_1)$, $f(x_2), \dots, f(x_n)$ satisfy relation r_f that is

$$r(x_1, x_2, \dots, x_n) \Rightarrow r_f(f(x_1), f(x_2), \dots, f(x_n))$$

Then (r, r_f) is a MR of f. Because P is an implementation of

f, if f is correct, it should also satisfy this relation, that is

$$r(I_1, I_2, \dots, I_n) \Rightarrow r_f(P(I_1), P(I_2), \dots, P(I_n))$$

Where I_1, I_2, \dots, I_n are inputs of P that associate with x_1 x_1, x_2, \dots, x_n , and $P(I_1), P(I_2), \dots, P(I_n)$ are their outputs. So

 (r,r_f) is also an MR of P. When we test P with (r,r_f) , the

test cases originally given are original test cases, others which are deduced from relation r are follow-up test cases.

Definition 2 (algebraic specification)[10] The algebraic specification of class C can be denoted by C = (S, F, V). S is a subset of class C. E is a collection of method of class E. Each method E can be expressed as E. E is a collection of method of class E. Each method E can be expressed as E. E is a collection of method of class E. Each method E can be expressed as E. The right-hand side is output parameters. The algebraic specification consists of equational axioms that describe the behavioral properties of the operations expressed by E. The following example shows an algebraic

specification of the class IntStack of integer stacks:

module INTSTACK is

classes Int Bool IntStack

inheriting INT

operations

new: -->IntStack

_.empty: IntStack -->Bool

.push(): IntStack Int -->IntStack

_.pop: IntStack -->IntStack

.top: IntStack-->Int U{NIL}

variables

S: IntStack

N: Int

axioms

 a_1 : new.empty = true

 a_2 : S.push(N).empty = false

 a_3 : new.pop = new

 a_4 : S.push(N).pop = S

 a_5 : $S.top = NIL \ if \ S.empty$

 a_6 : S.push(N).top = N

In a given class C, operations or methods generating new objects of C are called creators. Operations or methods changing the values of attributes of object in C are called constructors or transformers. Operations or methods that only output the values of attributes of objects in C are called observers.

Definition 3 (term) A syntactically valid sequence of operations in a given algebraic specification is called a term. For example, *new.push.pop* is a term, but *new.empty.pop* is not in the class of integer stacks above.

Definition 4 (normal form) In algebraic specification, a term is in mormal form if and only if it cannot be further transformed by any axiom in the specification. For example, new.push(1).push(2) is in normal form, but new.push(1).push(2).pop is not.

Definition 5 (method sequence metamorphic relation) In testing of object-oriented software, let the equational sequence,

$$p_i, q_i \in F, (i = 1, 2...m, s = 1, 2...n), p_1().p_2()$$

 $\dots p_m() = \underline{q_1().q_2() \cdots q_n()}$ be method sequence of MR.

Definition 6 (single-value metamorphic relation) In testing of object-oriented software, let $_.p_1().p_2()..._.p_m()$ = $A_.p_i \in F$ ($i = 1,2,\cdots,m$), be single-value MR, if A is a

value rather than a sequence of operations.

III. CRITERION ANALYSIS

A. criterions of constructing metamorphic relations

Based on the characteristics of the object-oriented algebra specification, a large number of experiments and results analysis, criterions of constructing *MRs* were proposed as follows:

Criterion 1 Given a algebraic specification C = (S, F, V), the following formula can be deduced: $\forall f \in F, \exists \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), f() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, p_m(), g() = p_1(), q_2(), \dots, q_n()\} \lor \{p_1(), p_2(), \dots, q_n(), q_2$

Criterion 2 If a method $_.f() \in F$ is not a observer and only appear at the end of the MR, construct new MR in order to ensure that the current states after all methods except observers called can be tested. For method sequence MR, this method can appear in everywhere.

Criterion 3 Construct *MR* should combine white-box, for instance boundary conditions (the length of array). The more white-box informations we consider, the more fault detection MR we have.

Criterion 4 The *MR* set which the length of *MRs* are more longer and the number of them are shorter is more effective. Construct compositional *MRs* is a effective way to reducing the number of *MRs*. The fault detection of Composite *MR* is better than its corresponding component *MRs*.

Criterion 5 The more difference between two sides of MR, the more likely their outputs are not equal. For the object-oriented MR, the concept of "difference between two sides of MR" involve difference in method sequence length and number of method type.

- B. Construction procedures of metamorphic relation Suppose that in algebraic specification of class C, each axiom a_i performs the following steps to construct MR sets.
 - 1) a_i is a MR, if variables of class C is not included in

axiom a_i .

- 2) If axiom a_i include variables of class C, according to guideline 3, take $RP = \{r_j, j=1,2,\cdots l\}$ as replacement sequences, l is the number of replacement sequences.
- 3) Construct new equation a_{ij} by replacing variables of class C in axiom a_i with r_i , a_{ij} is a MR deducted from axiom a_i .
- 4) Do semantic checking of MR constructed by previous step. Revise MR that doesn't conform to semantic.
- 6) According to criterion 1, traverse all the transformation relations, find the method that does not appear at the end of any method sequence, construct a new MR.
- 7) According to the criterion 2, new *MR* is constructed with the methods that only appear at the end of the sequence.

Construct MR of IntStack according to the steps below:

1) Replace variable S of class C, we generally use constructor to replace. According to white-box information, the length of array in stack is 100, so we can choose method sequence of one hundred push as the replacement. The $RP = \{r_1, r_2\}$ is as follows:

```
r_1: new r_2: new.push(N_1).push(N_2)···push(N_{100})
```

Replace object variable in axiom with r_i , the constructed MRs are as follows.

```
a<sub>1</sub>: new.empty=true
a<sub>21</sub>: new.push(N).empty=false
a<sub>22</sub>:
new.push(N<sub>1</sub>).push(N<sub>2</sub>)...push(N<sub>1</sub>)
```

 $new.push(N_1).push(N_2)...push(N_{100}).push(N).empty = false$ a_3 : new.pop = new,

 a_{41} : new.push(N).pop=new,

 a_{42} : $new.push(N_1).push(N_2)$ ···push(N_{100}). $push(N).pop = new.push(N_1)$. $push(N_{100})$

 a_{51} : new.top = NIL

 a_{61} : new.push(N).top=N

 a_{62} : $new.push(N_1)\cdots push(N_{100})push(N).top=N$

2) Carry out a semantic check on the above *MRs* and correct the one at variance with semanteme. For example, in terms of the stack operation, the maximum array length is 100, only 100 integers can be pushed on to the stacked. When push

the 101st integer, that integer fails to be pushed. What is on the stack are still the pushed 100 integers. Hence, a₄₂ should be modified as $new.push(N_1).push(N_2)\cdots push(N_{100}).push(N)$. $pop = new.push(N_1). push(N_{99}).$

3) According to criterion 5, a_{22} , a_{62} are more difference than a_{21} , a_{61} . Choose the first two MRs. Based on criterion 4, compose three MRs a_3 , a_{41} , a_{42} into $a_{3-41-42}$: new.pop.push(N) $pop.push(N_1)$. $push(N_2) \cdots push(N_{100}).push(N).pop = new.$ $push(N_1) \cdots push(N_{99})$ and $a_{3-41-42}$: new.pop.push(N).pop. $push(N_1)$. $push(N_2) \cdots push(N_{100}).push(N).pop = new.pop.$ $push(N).pop. push(N_1)\cdots push(N_{99})$. According to criterion 5, $a_{3-41-42}$ is more difference than $a_{3-41-42}$, put $a_{3-41-42}$ to MR set. MR set is as follows:

```
a_1: new.empty = true
 a_{22}: new.push(N_1).push(N_2)\cdots push(N_{100}).empty = false
 a_{3-41-42}: new.pop.push(N).pop.push(N_1).push(N_2) ··· push
(N_{100}) .push(N).pop= new.push(N_1)...push(N_{99})
 a_{51}: new.top = NIL
 a_{62}: new.push(N_1).push(N_2)\cdots push(N_{100}).push(N).top = N
```

4) Based on criterion1, the method new is not appear at the end of sequence method in any MR. Construct a MR that one side of it ends with new. Add a_{41} : new.push(N).pop=new in MRset.

The finally MR set is as follows:

```
a_1: new.empty = true
  a_{22}: new.push(N_1).push(N_2)\cdots push(N_{100}).empty = false
  a_{41}: new.push(N).pop=new
  a_{3-41-42}: new.pop.push(N).pop.push(N_1).push(N_2).push(N_3)
\cdots push(N_{100}) .push(N).pop = new.push(N_1) \cdots push(N_{99})
  a_{51}: new.top = NIL
  a_{62}: new.push(N_1).push(N_2)\cdots push(N_{100}).push(N).top = N
```

- A. Analysis on the constructed metamorphic relation set is as follows:
- 1) a_1 can verify the object state after new calling and the returned value after empty calling, in addition, it can also verify the mistakes of stack length correction in the last call of empty method, and stack array bound mistakes caused by the correction on stack length mistakes in the new method.
- 2) a_{22} can verify the object state after new and push and the returned value after empty calling, in addition, it can also verify the mistakes of stack length correction in the last call of empty method, and stack array bound mistakes caused by the

correction on stack length mistakes in the new and push methods.

- 3) a_{41} can verify the object state after new, push, pop calling. It can verify the returned value and object state caused by the mistakes of stack length correction.
- 4) $a_{3-41-42}$ can verify object state after new, pop and push calling. It can verify stack length of the two sides differ from each other, and stack array bound mistakes that caused by mistakes of stack length modification.
- 5) a_{51} can verify the object state after new, and the returned value after top calling. It can verify stack array bound mistakes that caused by mistakes of stack length modification. In addition, it can also verify the mistakes that returned value of top is not NIL.
- 6) a_{62} can verify the object state after new, push calling, and the returned value after top calling. It can verify stack array bound mistakes caused by the modification on stack length mistakes in the new, push and top methods. It can also verify the mistakes that returned value of top is not N.

In summary, the MRs constructed in this method can verify the consistency of executing results on both sides in method sequence; if both sides of the method sequence can't implement a certain defect point, the defect point can't be identified. Then construct a new MR. Generally speaking, as the variety for defects is in a wide range, so we usually set up a threshold value, if the failure-detecting rate reached this threshold, the test can be stopped.

IV. EXPRIMENT

B. Mutantion

In order to verify the effectiveness and efficiency of the MRs, we use mutation testing to analyze. Mutation testing (or Mutation analysis or Program mutation) is used to design new software tests and evaluate the quality of existing software tests. Mutation testing involves programs modified in small ways, each mutated version is called a mutant. Traditional mutation testing execute test cases in origin program and mutations respectively and the results are compared. If the results of mutations differ from origin program, it means the mutations are killed. It is usually appear three results when using mutation testing to verify the mutation detection capability of MRs[15]. (1) The test results do not satisfy MR. It shows that the MR killed mutations, namely the MR can detect

these mutations.(2) The test results satisfy MR. It shows that the MR did not kill mutants, namely the MR cannot detect such mutations. (3) When a mutation terminates due to the program execution fails, that means the MR killed mutation.

We use mujava to generate 122 mutations as shown in Table 1.

C. measurement criterion

The evaluation of *MRs* and test cases should be measured through multi-dimensional indicators. So the following three measurement criterions are proposed.

1) mutation score (MS)[16]

$$MS(T) = \frac{M_k}{M_t - M_a} \tag{1}$$

Where M_k is the number of mutants detected by the test case, M_t the total number of mutants, and M_q the number of equivalent mutants that cannot be detected by any set of test data. M_s is a macro-criterion that it doesn't care which mutation is tested.

2) Metamorphic relations Failure-detecting Capability (MRFS)[16]:

$$MRFC(a_i) = \frac{M_{a_i}}{M_i - M_a} \tag{2}$$

Where M_{ai} is the number of mutants detected by a_i , M_t is the total number of mutants, and M_{\P} is the number of equivalent mutants that cannot be detected by any set of test data. This

Table 1 122mutations of IntStack

Mutation Operation	Operation Description	Number
AORB	Arithmetic Operators	
	Replacement (binary	4
	arithmetic operator)	
AORS	Arithmetic Operators	
	Replacement (unary	3
	arithmetic operator)	
AOIS	Arithmetic Operator	
	Insertion (short-cut	40
	arithmetic operator)	
COI	Conditional Operator	4
	Insertion	
SDL	Statement Deletion	6
AODU	Arithmetic Operator	1
	Deletion(unary)	

AOIU	Arithmetic Operator	
	Insertion(unary	5
	arithmetic operator)	
ROR	Relation Operation	27
	Replacement	
LOI	Logical Operation Insert	14
VDL	Variable Deletion	8

measurement criterion evaluate the failure- detecting capability of *MRs*.

3) Mutation Metamorphic Relations Failure-detecting Capability (*MMRFC*) [16]:

$$MMRFC(m) = \frac{N_m}{N} \tag{3}$$

Where N is the number of MRs, N_m is the number of MRs that can kill mutation m.

D. Experimental results analysis

During the experimental execution, variables that in the generated *MR* shall be replaced with actual values. The selection of actual values can base on the equivalence class classifying criteria in black-box testing and path-coverage criterion in white-box testing. The replaced method sequence and corresponding parameter values constitute original test cases and follow-up test cases. Execute original e test cases

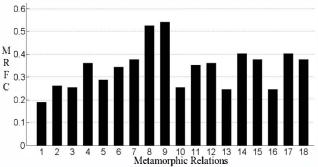


Figure 1 Error-detecting capacity of MRs in Paradigm

0.6
0.5
M 0.4
R
F 0.3
C
0.2
0.1
0
1 2 3 4 5 6

Figure 2 Error-detecting capacity of *MRs* in improved method and follow-up test cases respectively, and then determine

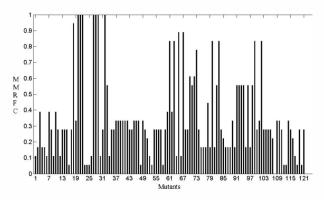


Figure 3 Mutation MRs Failure-detecting Capability

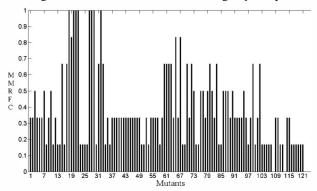


Figure 4 Mutation MRs Failure-detecting Capability

whether the executed results are equal. In the determination of the equivalence of the executing results, the following two conditions need to be considered: (1) if it is single-valued MR, we only need to determine whether the returned value in method sequence is equal to the specific value of the other side. (2) If it is the method sequence MR, we have to compare whether the returned value and object state equals to the other side.

Let's take the integer stack for an example, according to GFT algorithm, replace variables in axiom with the normal forms which length are 1, 2, 3 and 100 to construct eighteen MRs; and then construct six MRs according to the new algorithm. As the parameter values are merely values of pushed stack, so equivalence class division is not required; therefore, we can set $N_1 = 1$, $N_2 = 2$, ... $N_{101} = 101$, that is to obtain eighteen pairs and six pairs of test cases, and act them to the above 122 mutations. Set the threshold for mutation detection error rate to be 95%, after the test, calculate the measure index.

Mutation detection rate:

 $MS_{GFT}(T) = 118/122 = 96.7\%$

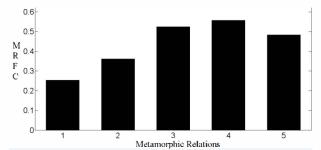


Figure 5 failure-detecting capability of composite MR and its corresponding component MRs

 $MS_{NFW}(T) = 116/122 = 95.6\%$

Through mutation detection rate, it can be seen that the mutation-detecting capacities of the six *MRs* constructed under new guidelines and the eighteen *MRs* constructed by GFT algorithm have reached to a set threshold, while the *MR* redundancy has reduced by 66.7%, which verified the effectiveness of *MRs* constructed based on the above criteria.

2) mutants-detecting capacity MRFC of MR 122 variants.

As can been seen from Figure 1 and Figure 2, *MR* constructed by GFT contains large *MR* redundancy, the Failure-detecting Capability of most *MRs* constructed by improved method is better than MRs constructed by GFT. In the *MR* constructed by GFT, mutation detection rate in 2, 3 and 4 *MRs*, in 10, 11 and 12 MRs, in 13, 14 and 15 MRs, and in 16, 17 and 18 *MRs* are basically similar, as the difference of normal form replaced class variables with the length of 1, 2 and 3 are not insignificant, verifying that the *MR* redundancy constructed by GFT normal form is significant. The 7, 8 and 9 MRs in figure 1 and the 6 *MR* in figure 2 have higher mutation detection rate, it is because the three MRs have considered the white-box information array bounds issue and verified the Guideline 3.

As can been seen from Figure 2, the mutation-detecting capacity of the third MR $a_{3-41-42}$ is much higher than other MRs, as it contains all methods except observers in IntStack class, and it also verify the object state after new, push and pop calling, moreover, it has the ability to detect that both sides of stack length is inconsistent after the correction of new, pop and push methods, and the stack array bound mistakes caused by the correction on stack length mistakes. Compared to other MRs, it comprises the most complete methods, and takes the white box information, such as array bounds issue into account, verifies the guideline 4.

3) Metamorphic relations Failure-detecting Capability

MMRF

As can been seen from Figure 3 and Figure 4, in Figure 4 the mutation *MRs* failure-detecting capability of most mutations is better than mutations in Figure 3. In addition, mutation number 22 \, 23 \, 24 \, 29 \, 30 \, 31 \, 34, can be verified by all the constructed *MRs*. Because those mutants caused by object state mistakes or stack array bound mistakes after new calling. All *MRs* start with new, thus those mutations can be verified.

4) Comparative study of composite MR and its corresponding component MR

In Figure 5, the first three MRs are a_3 , a_{41} , a_{42} respectively. The later two are composite MRs constructed by the first three. The fouth MR is $a_{3-41-42}$: $new.pop.push(N).pop.push(N_1)$ $push(N_2)...push(N_{100}).push(N).pop=new.push(N_1)$ \cdots $push(N_{99})$ and the fifth MR is $a_{3-41-42}$: $new.pop.push(N).pop.push(N_1)$ $push(N_2)$ \cdots $push(N_{100}).push(N).pop = new.pop.push(N).pop.$ $push(N_1)$ \cdots $push(N_{99})$. We find that the difference between two sides of $a_{3-41-42}$ is more larger than $a_{3-41-42}$, and in Figure 5 the failure-detecting capability of $a_{3-41-42}$ is much better than $a_{3-41-42}$, verifies the guideline 5. We can also find that the failure-detecting capability of $a_{3-41-42}$ is better than its corresponding component MRs, but $a_{3-41-42}$ is not. Because of similarity between the two sides of $a_{3-41-42}$, some failure-detecting capabilities of $a_{3-41-42}$ are hidden. It verifies the guideline 4 and 5.

Experiment is also conducted on SavAcc class according to the same methods and procedures. Experimental results showed that, under the similar mutation detection rate, the constructed number of *MRs* by new method is significantly less than the number constructed by GFT algorithm; after recombination, the mutation-detecting rate of *MR* has improved significantly, and verified the effectiveness of guidelines constructed *MR* proposed in this paper.

V. CONCLUSION

To solve the Oracle problem of methods sequence in object-oriented software testing, a method of *MRs* constructing for object-oriented software testing basted on algebraic specification was proposed. In metamorphic testing, we use returned value and object state to verify the equivalence between two execution results. Finally the improved method was verified through constructing *MRs* of IntStack and SavAcc class. The experiment results show that *MRs* redundancy is reduced by 66.7% at the same mutation score. So the new method has a low *MRs* redundancy and improves the efficiency of software testing.

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