

GRAVITATIONAL INSTABILITY IN IRRADIATED DISCS

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When are Discs Gravitationally Unstable?

- In their youth, discs can be massive enough that the *disc's self-gravity is important*.
- When the disc mass is comparable to its host star ($\gtrsim 10\% M_\star$), *gravitational instabilities (GI) can occur resulting in spiral arms*.





When are Discs Gravitationally Unstable?

Sound speed

$$Q = \frac{c_s \Omega}{\pi G \Sigma} \lesssim 1.7$$

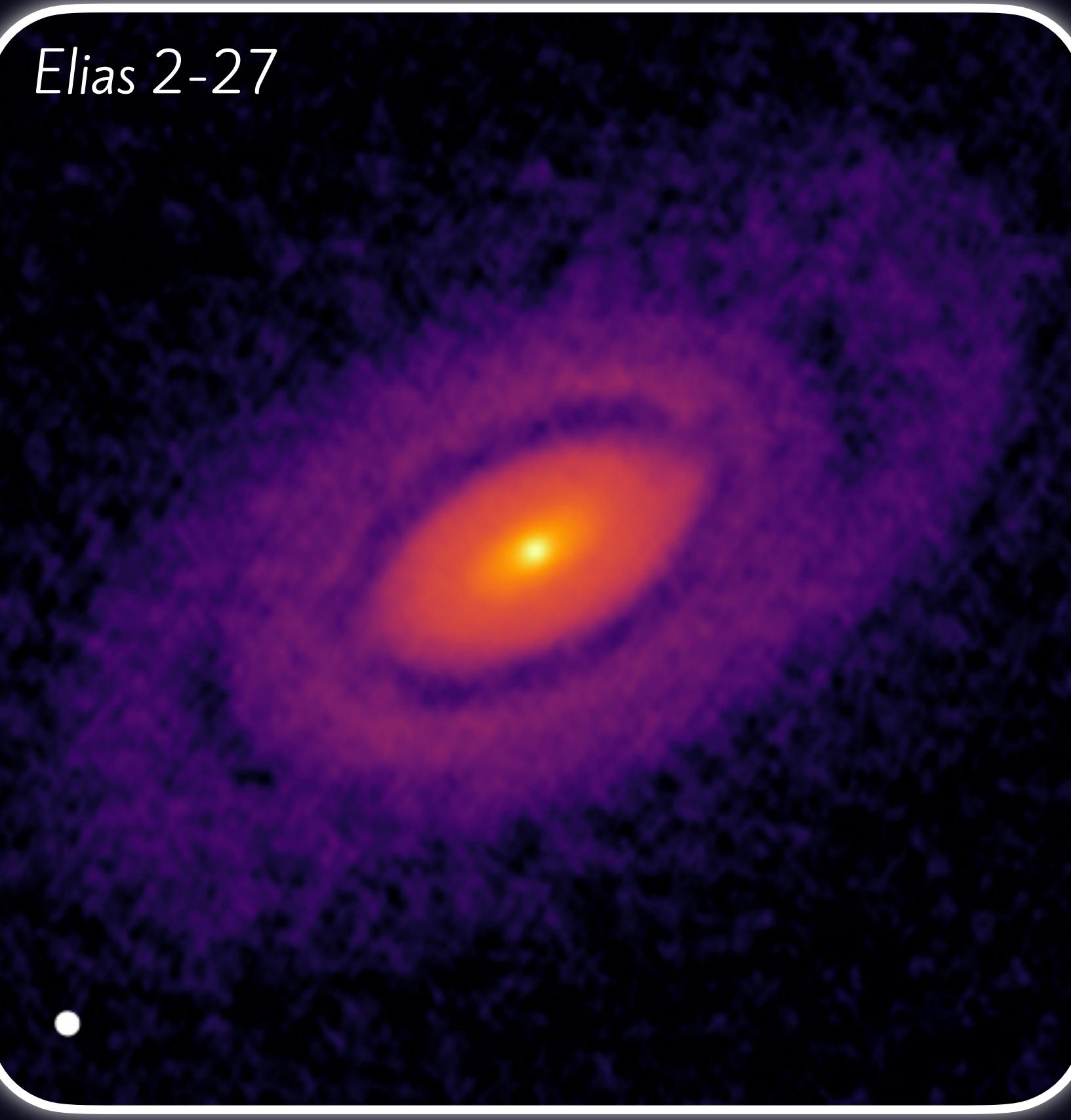
Surface Density

Toomre 1964

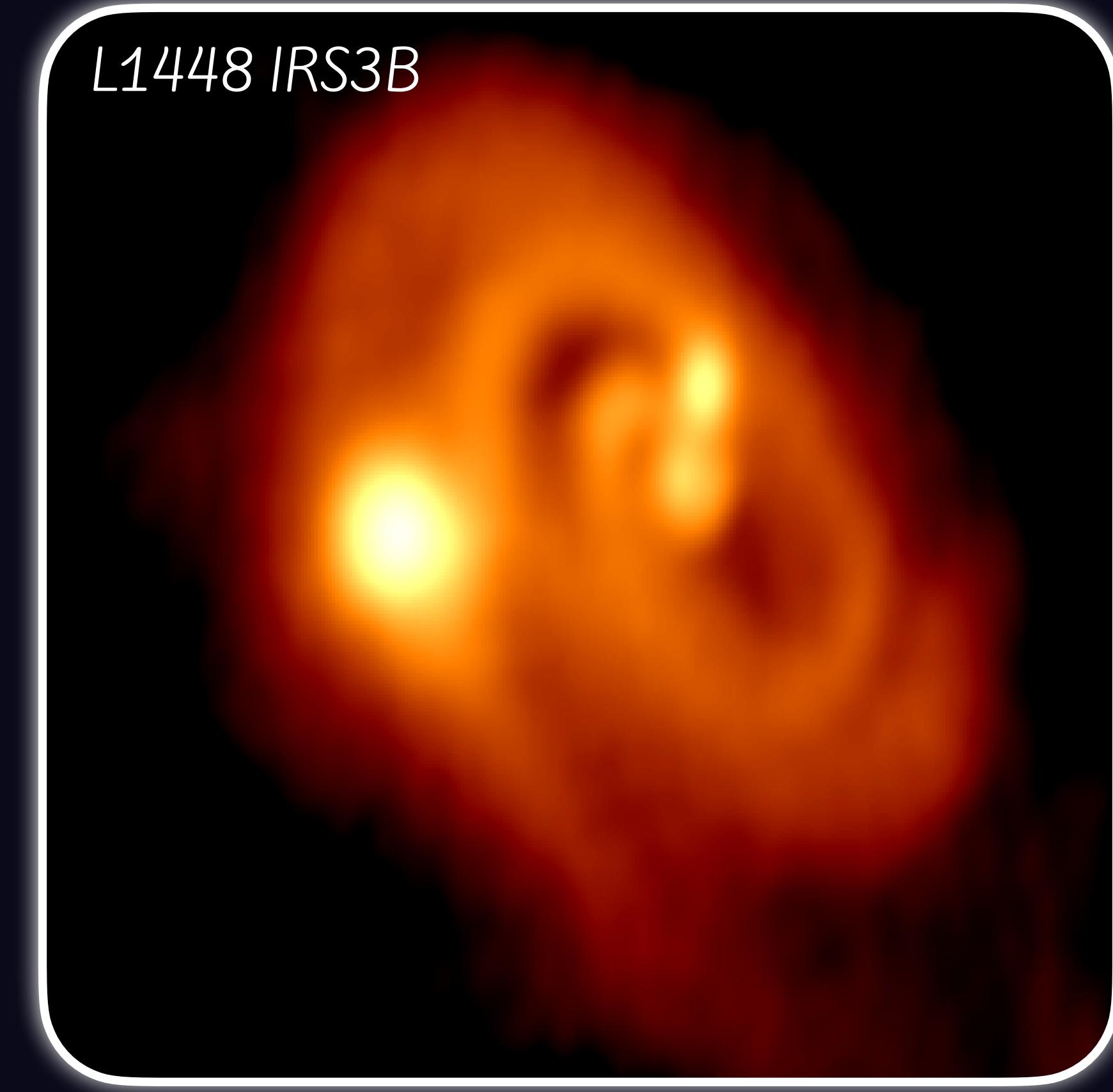




Observations of Gravitationally Unstable Discs



Andrews+ 2018, Huang+ 2018



Tobin+ 2016, Reynolds+ 2020

Thermodynamics

Radiative Transfer

β cooling

- + Models the disc realistically.
- Slow and computationally expensive.
- + Fast and computationally inexpensive.
- Disc model is not consistent with expectations.



SIMULATING GRAVITATIONALLY UNSTABLE DISCS WITH β COOLING



The Internal Energy Equation

$$\frac{du}{dt} = -\frac{P}{\rho}(\nabla \cdot v) + \Lambda_{\text{shock}} - \frac{\Lambda_{\text{cool}}}{\rho}$$



PdV
Heating



Shock
Heating

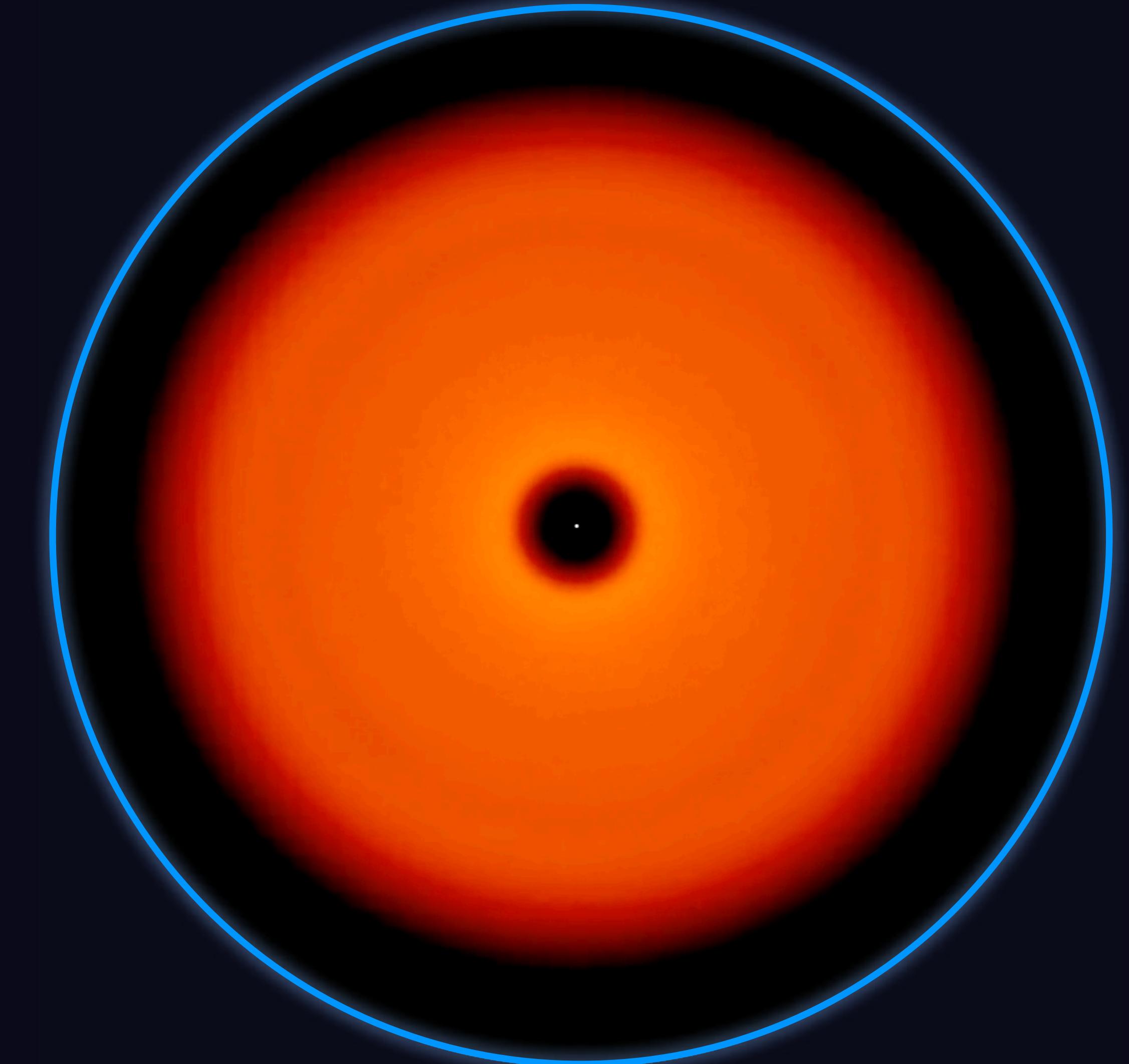


Cooling
Term



High Toomre Q

- *Very little PdV or shock heating.*
- *The disc is free to cool until gravitational instabilities develop.*





Low Toomre Q

- *Dense spiral structures have formed.*
- *PdV and shock heating become more important.*





Heating and Cooling in Balance

- *PdV and shock heating balance the cooling in the disc.*
- *The disc cannot fragment. Or become stable.*
- *It will remain gravitationally unstable with spiral arms.*





SIMULATING GRAVITATIONALLY UNSTABLE DISCS WITH RADIATIVE TRANSFER



CALCULATES THE TEMPERATURES

- Using the luminosity of the star,
- Particle data from PHANTOM,
- PdV and Shock heating from PHANTOM.

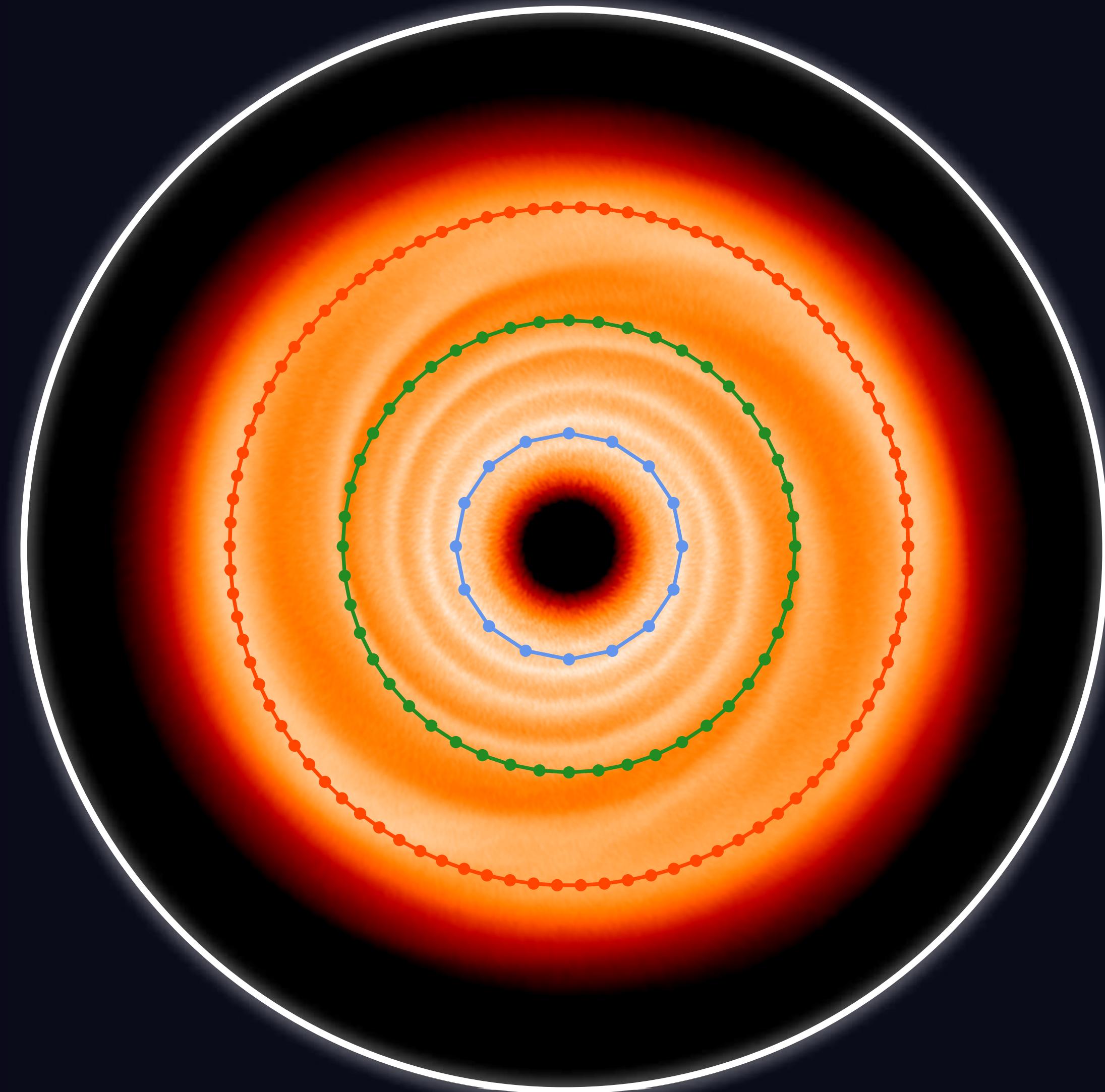
MOVES THE PARTICLES

- Energy is constant between time-steps.
- At the end of each time-step, MCFOST updates the temperatures.



Frequency of calculations

- The temperature is updated every 7.071 years.
- Ensures that particles do not evolve too much between temperature calculations regardless of where they are in the disc.

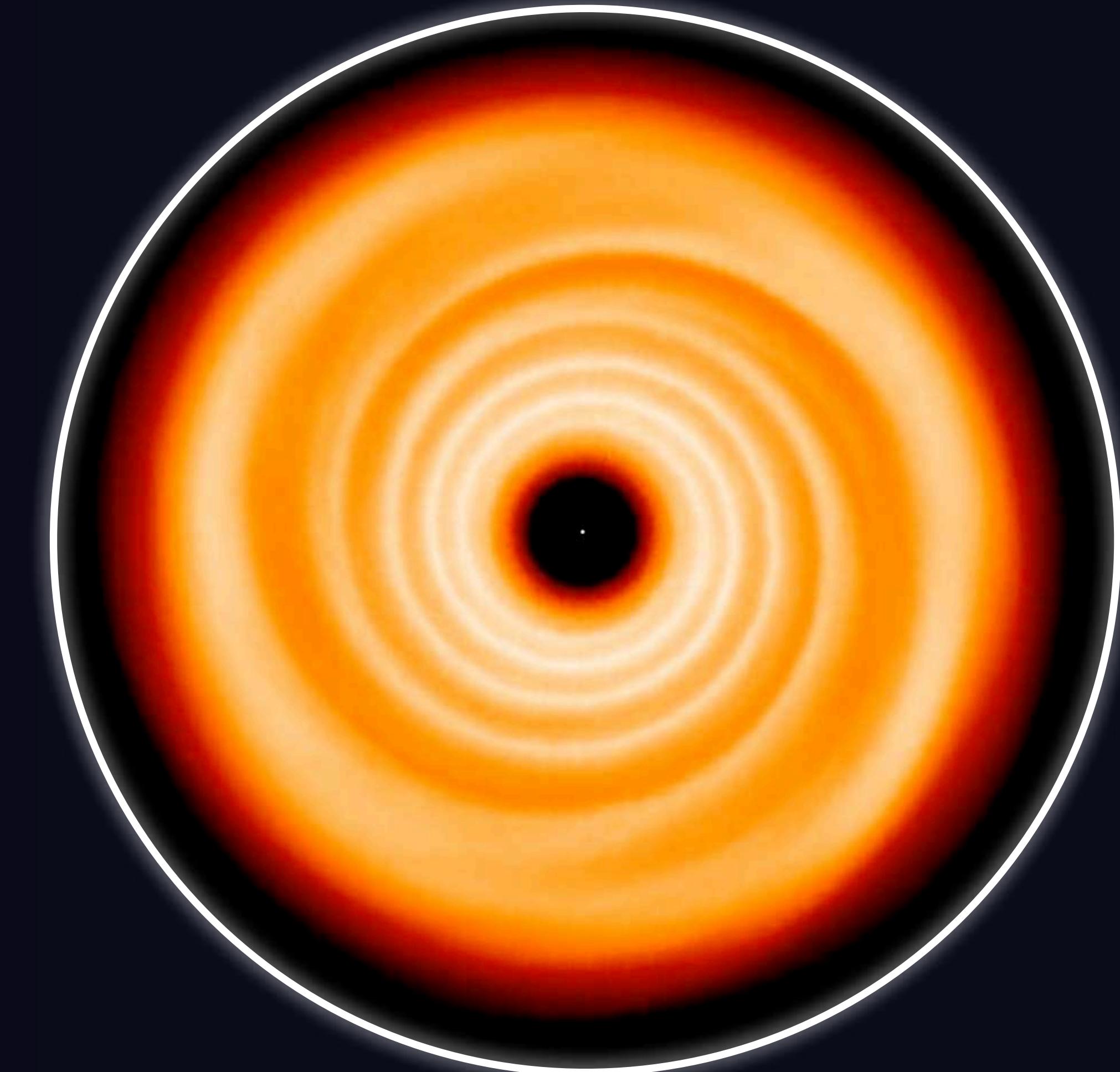


How Many Photons?

- Previous works (Nealon+ 2020, Borchert+ 2022a,b) have used 100 photons for every SPH particle. However, those discs were not as massive.
- Gravitationally unstable discs are much more massive, and hence very optically thick.
- Need a much higher number of photons to ensure every SPH particle is reached. If no photons reach, the temperature of the particle. is set to 2.73K. This results in a negative feedback loop resulting in artificial fragmentation.
- We use 5000 photons for every SPH particle.



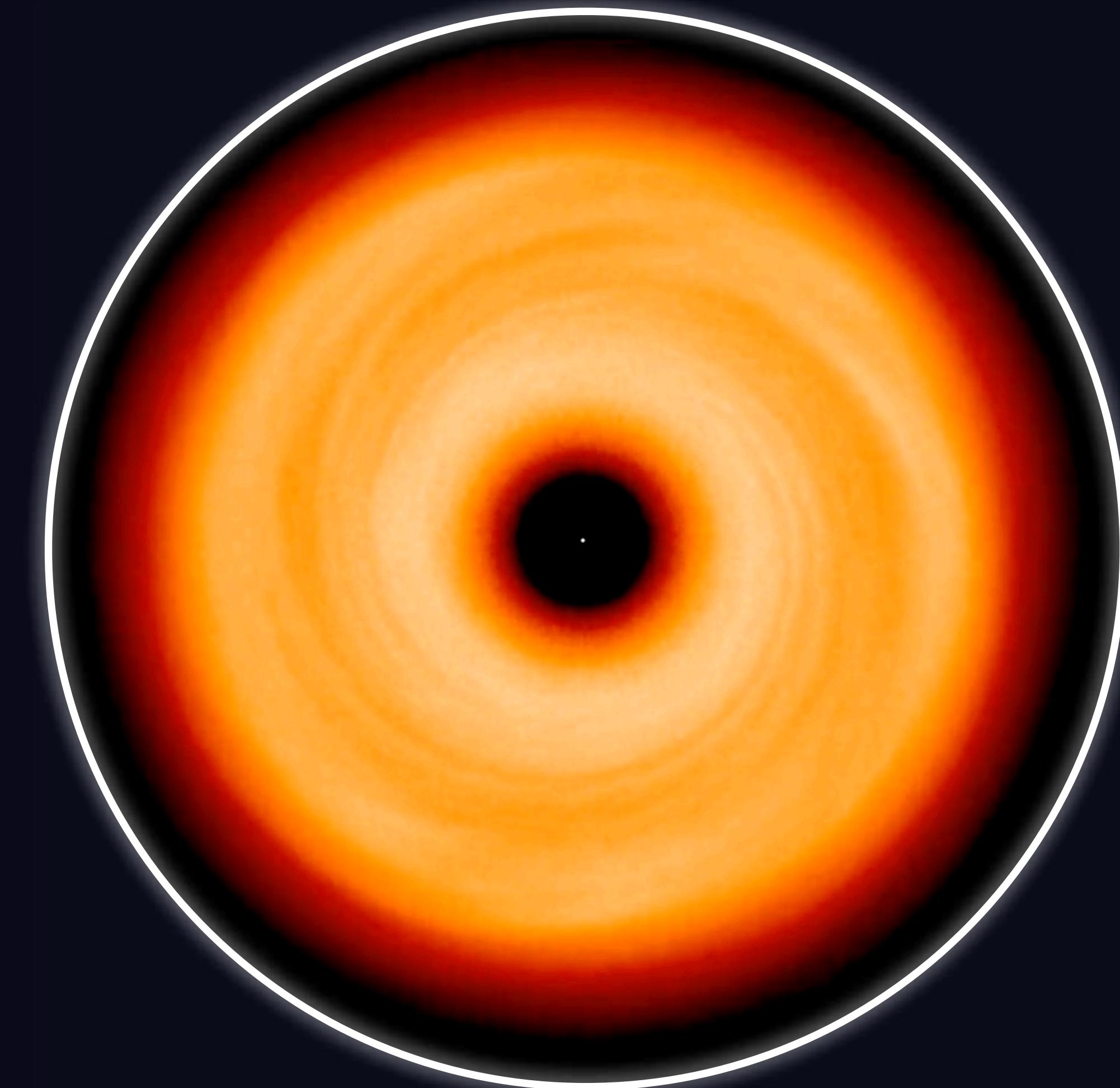
*Evolution of a
 $0.1M_{\odot}$ disc with
Radiative Transfer*



Rowther+ (in prep)



*Evolution of a
 $0.1M_{\odot}$ disc with
Radiative Transfer*

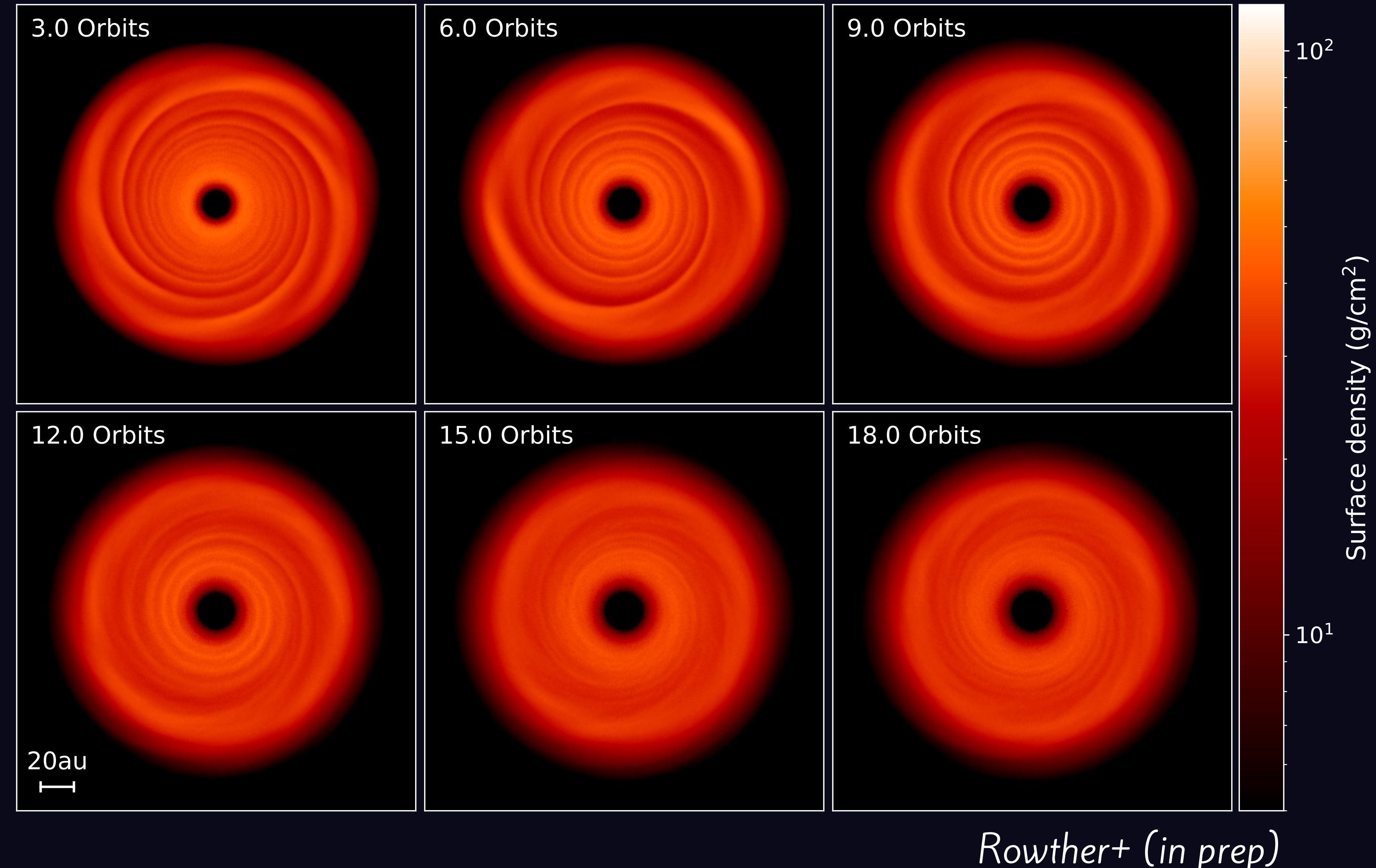


Rowther+ (in prep)

Gravitational instabilities become weaker over time.

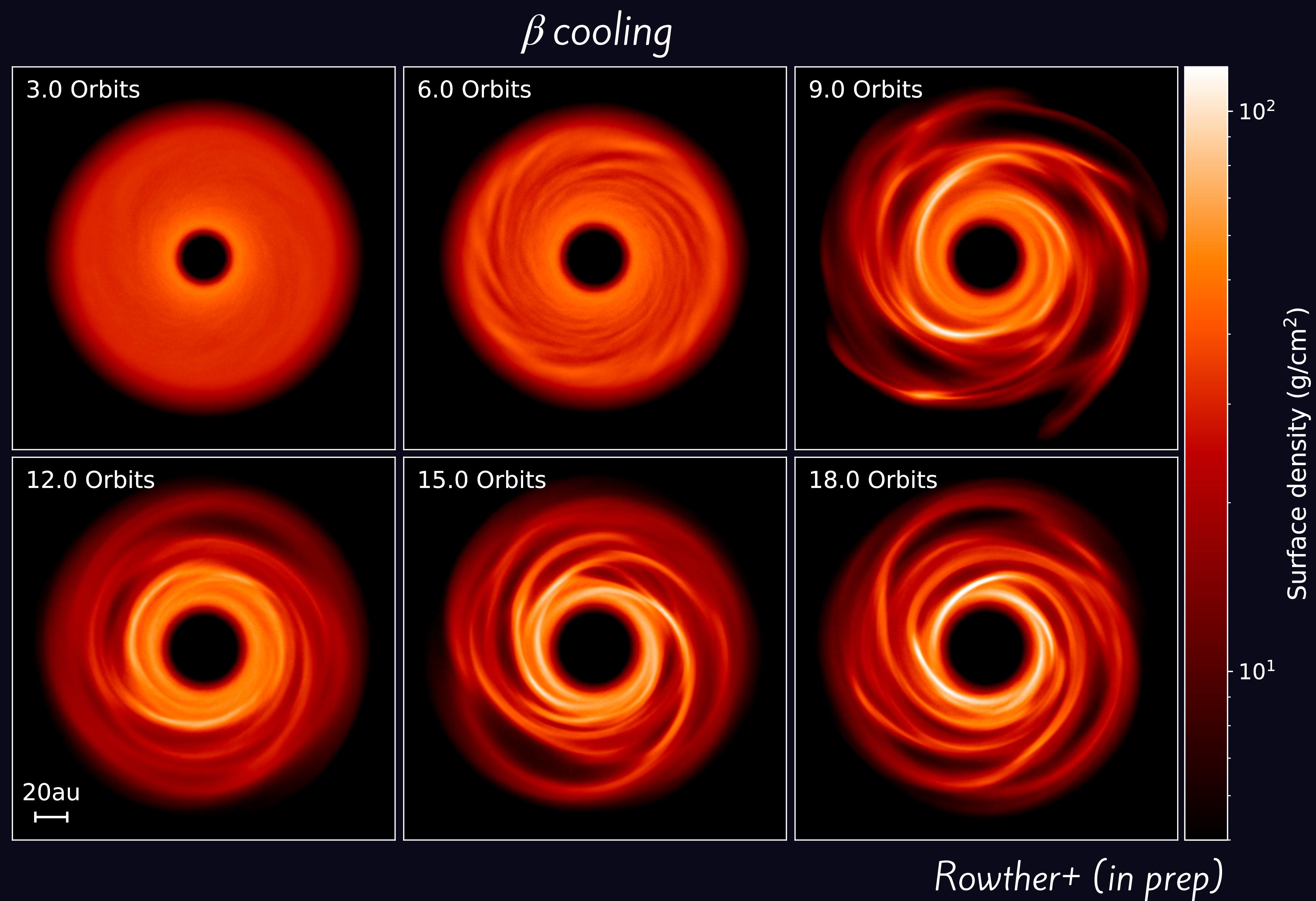


- *Spiral structures are weaker.*
- *Disc becomes more stable over time.*





- *Spiral structures are stronger.*
- *Disc is in a steady state with spiral structures.*



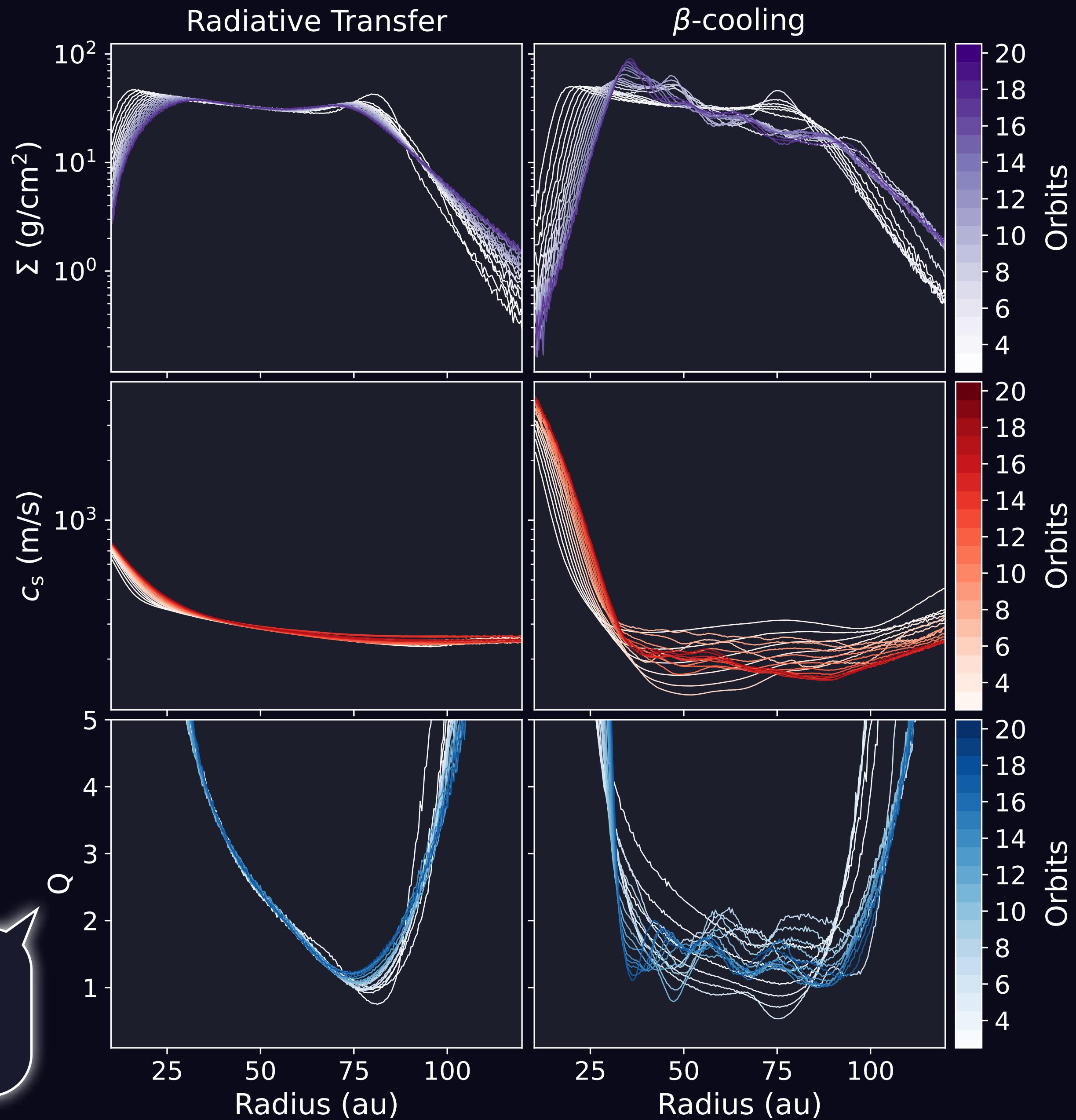


Evolution of Disc Instability

Radiative Transfer

- Disc is warmer.
- Temperature is fairly constant.
- Q has a steady increase.

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$



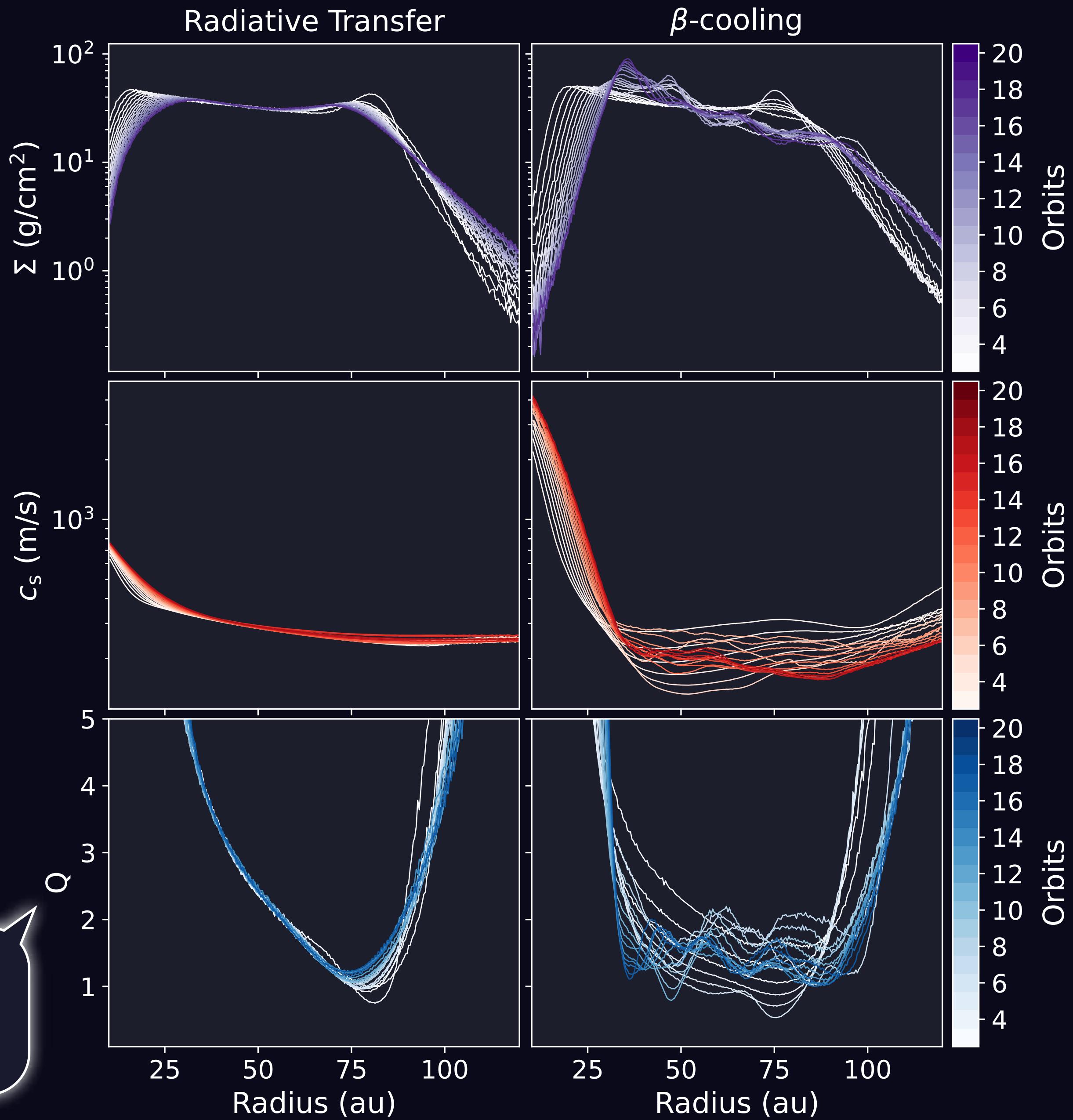


Evolution of Disc Instability

β cooling

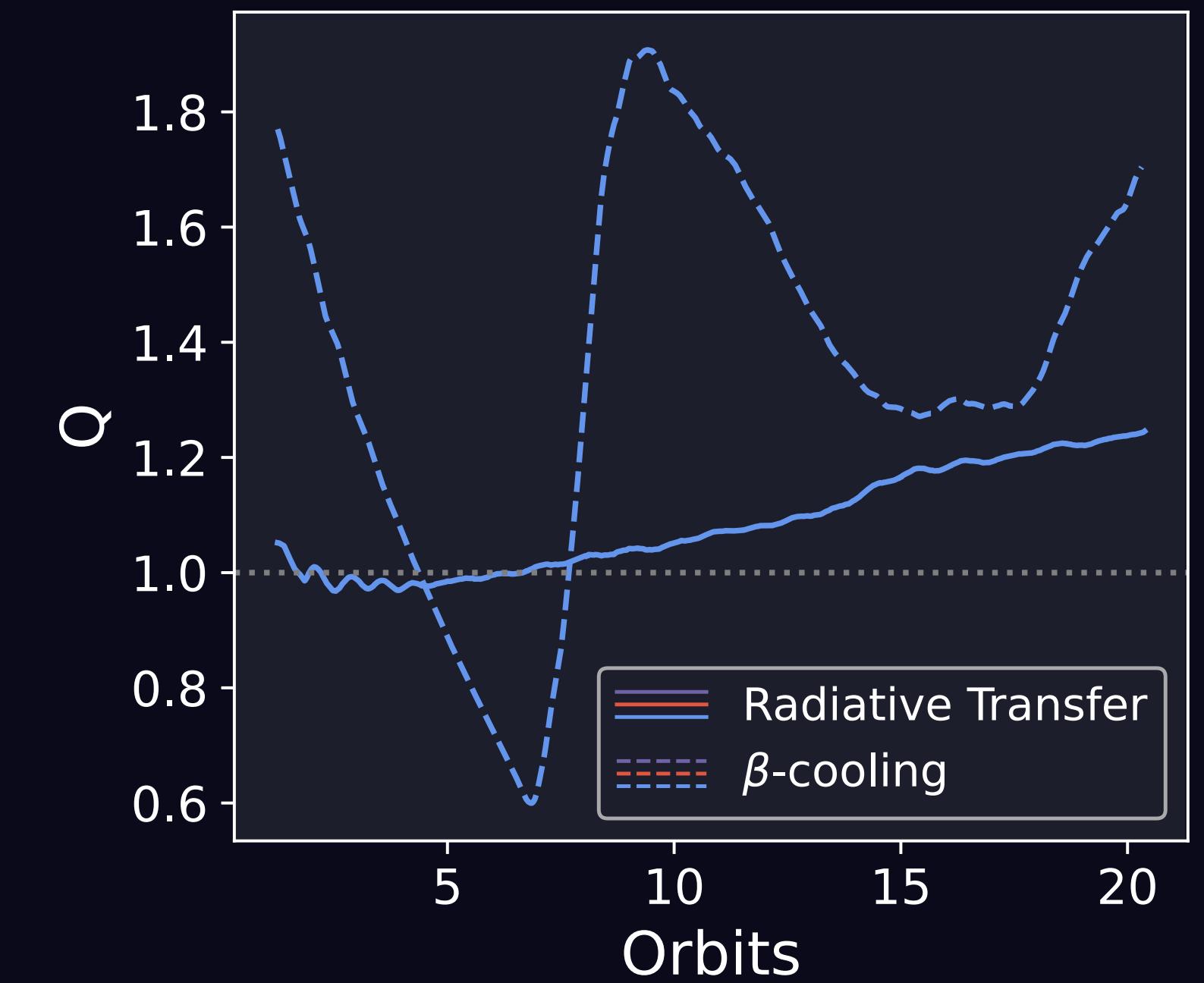
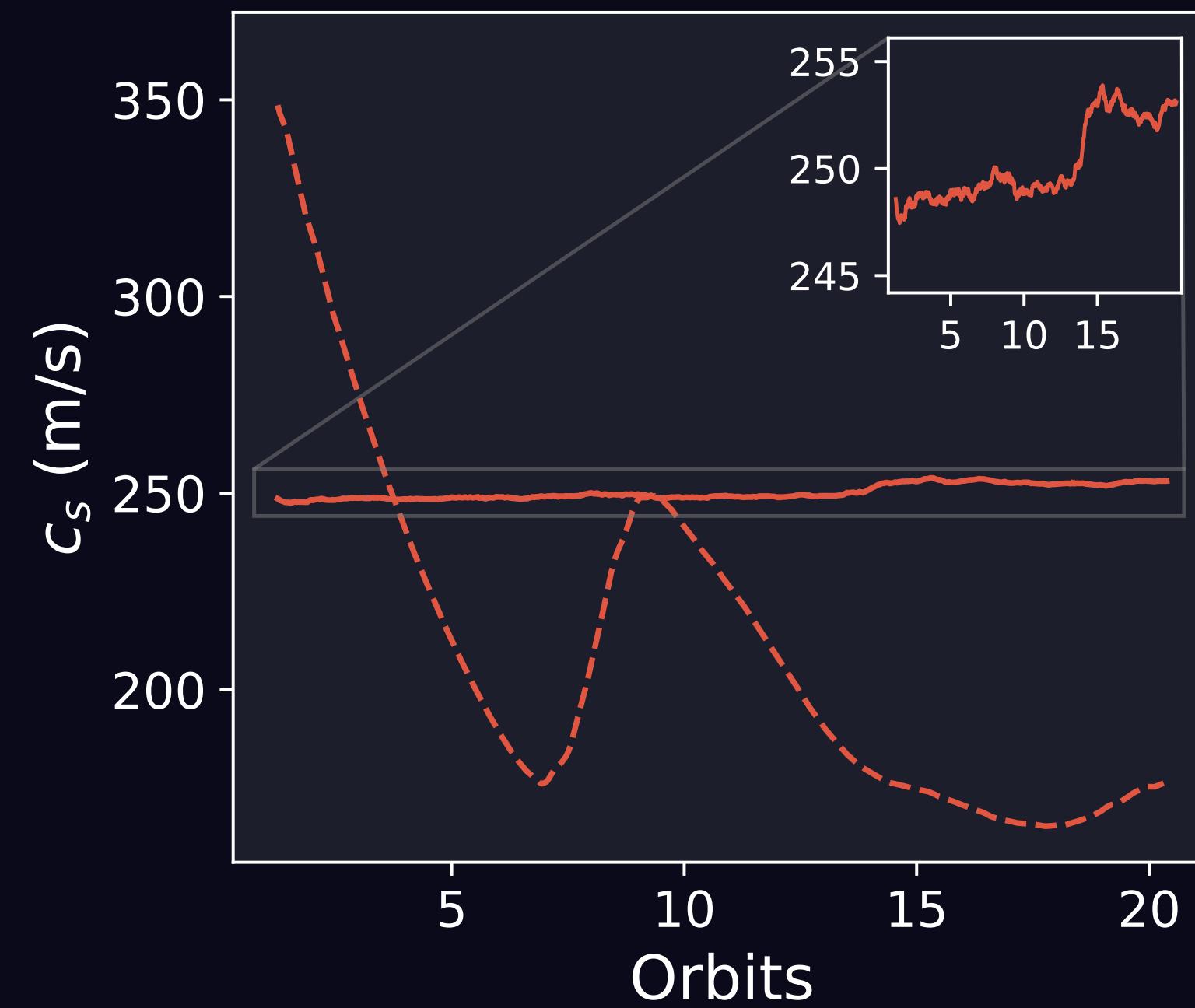
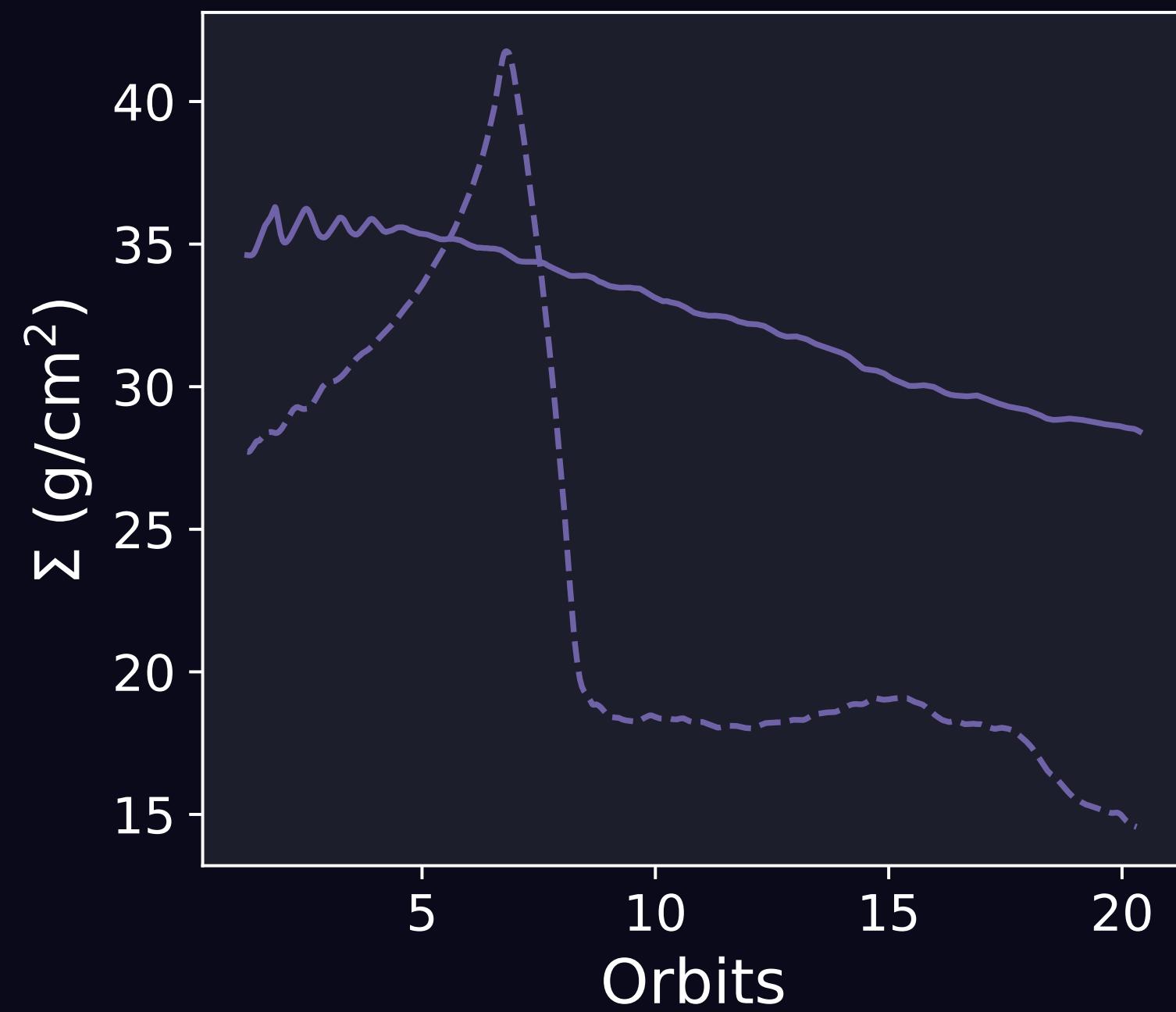
- Both surface density and sound speed evolve.
- Q eventually stabilises when heating and cooling are in balance.

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$



Evolution of Disc Instability (At $R=77\text{AU}$)

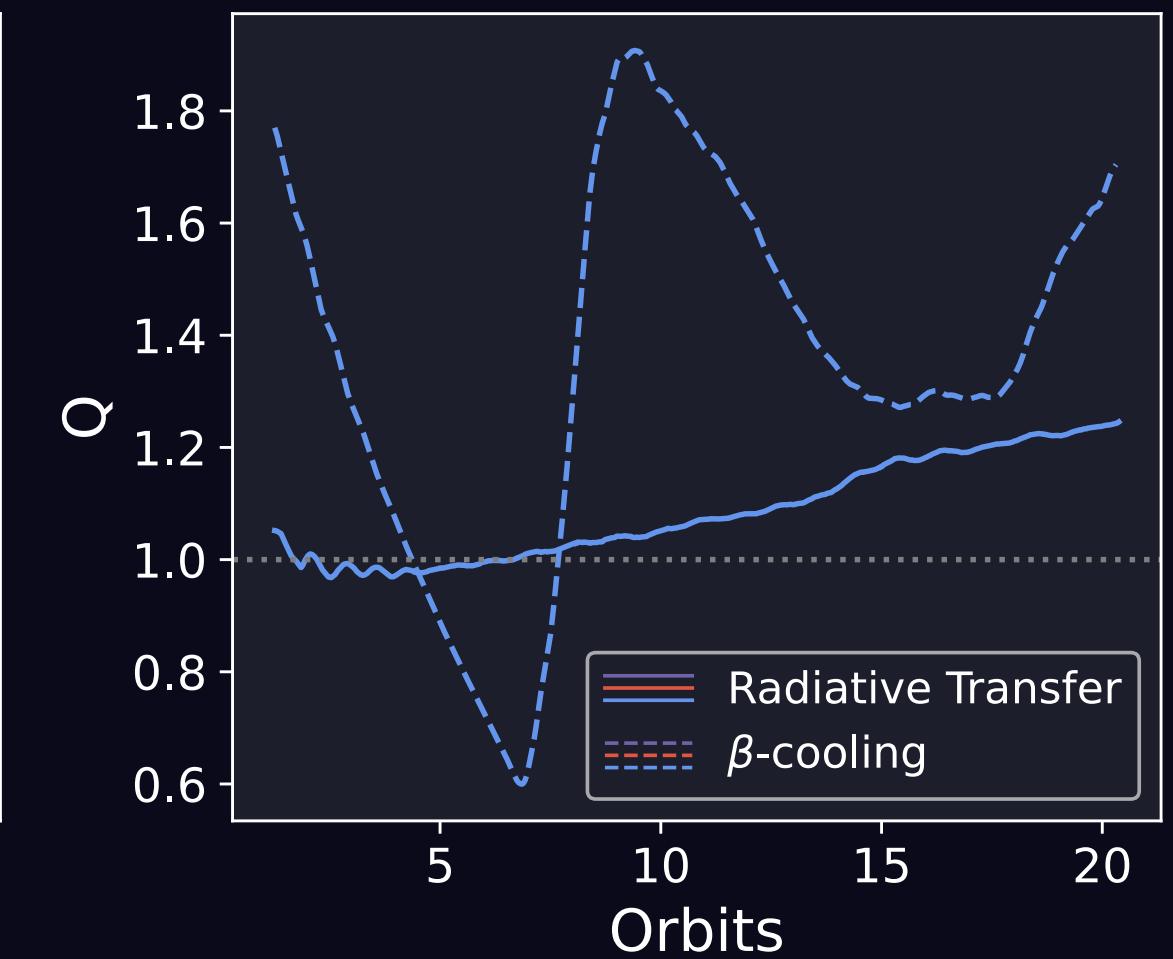
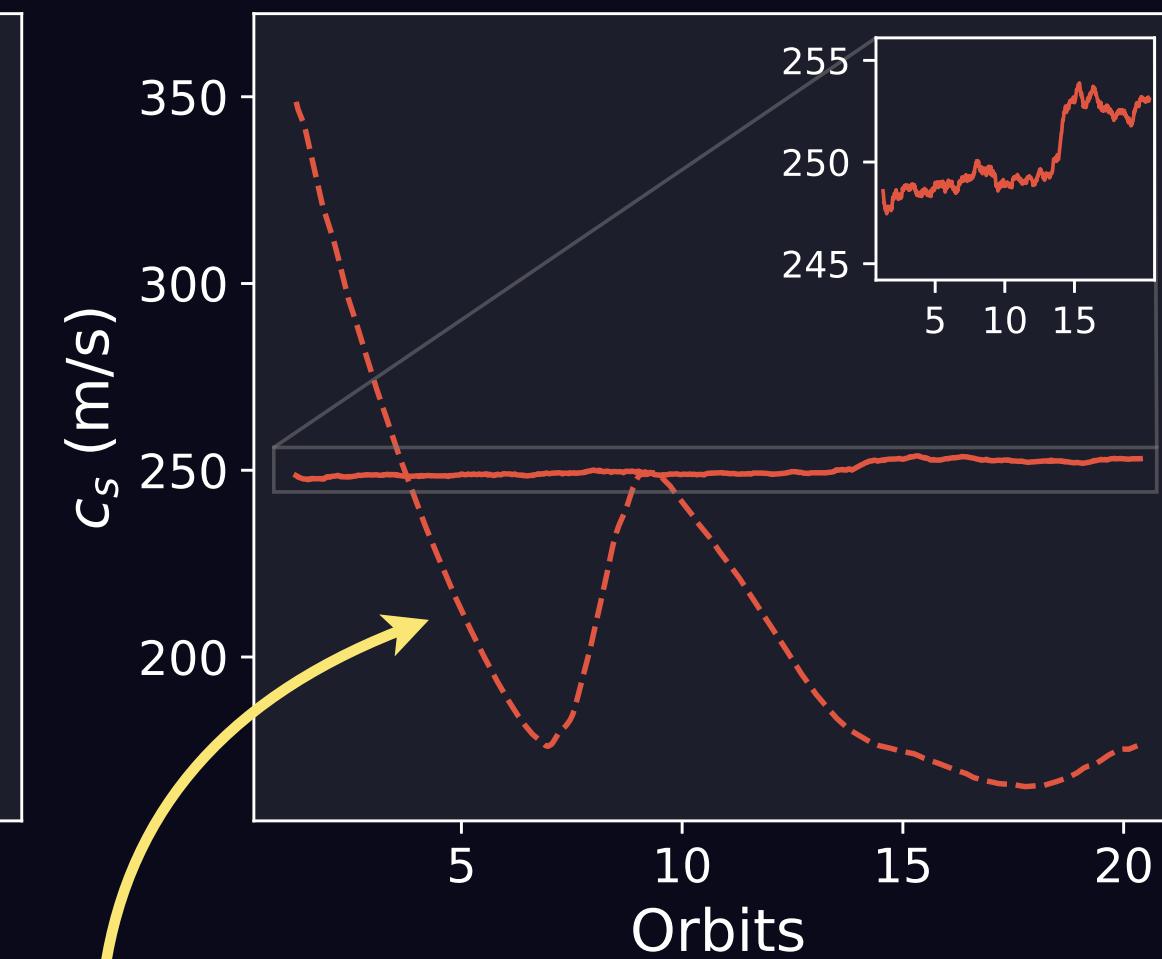
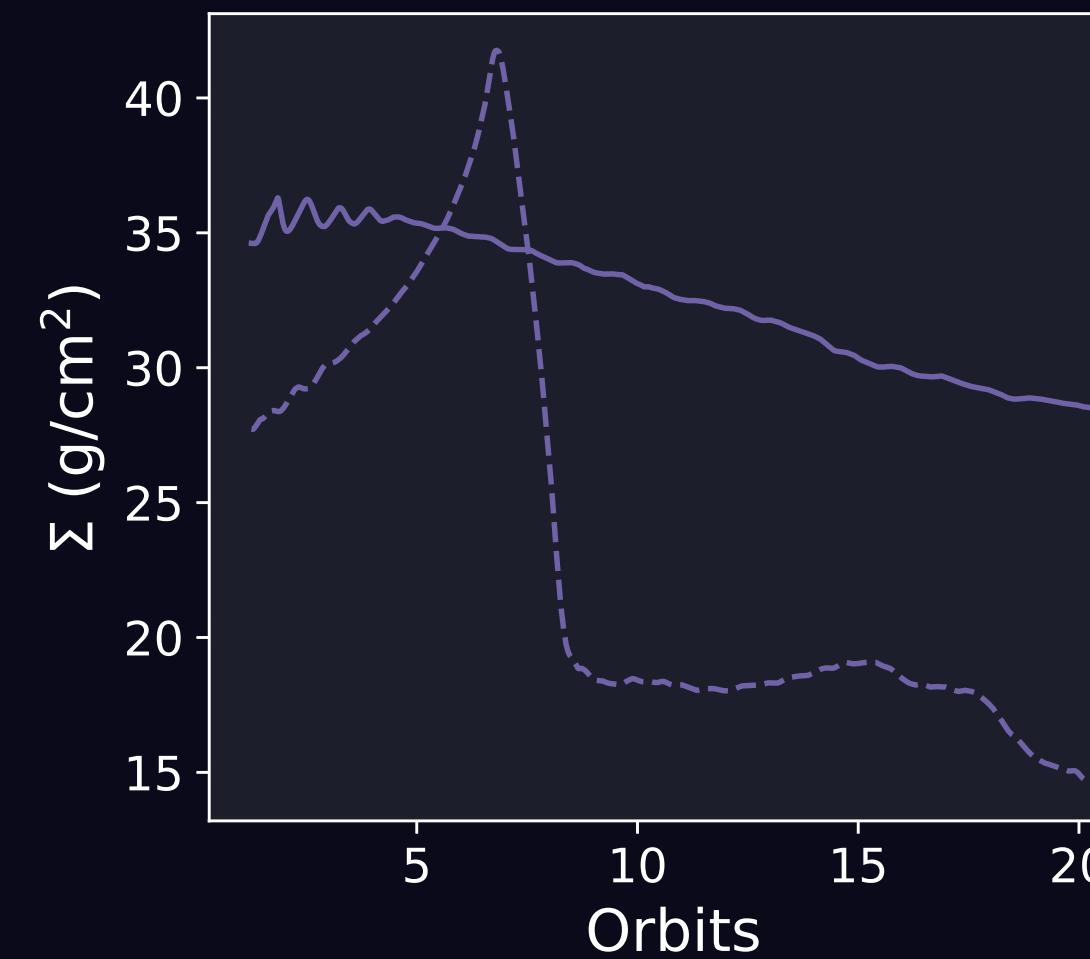
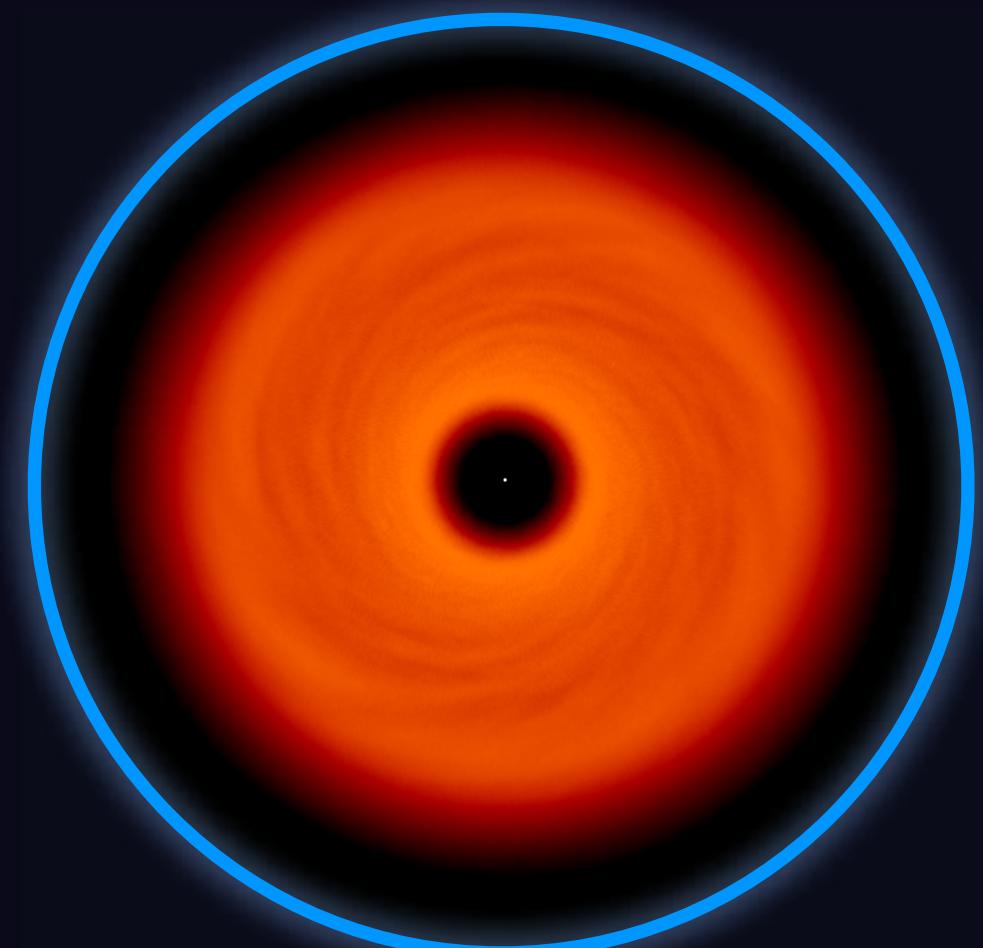
$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$





Evolution of Disc Instability (At $R=77\text{AU}$)

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$

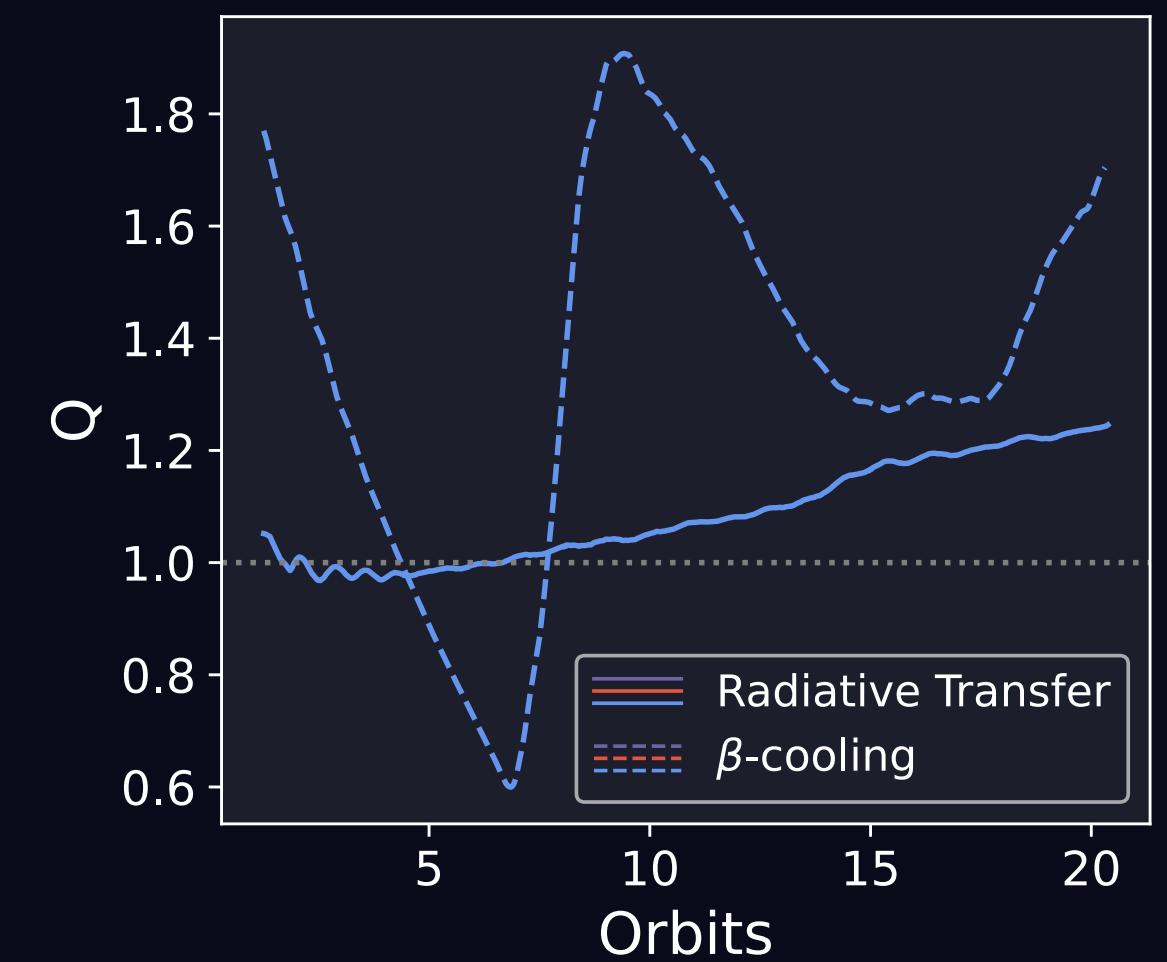
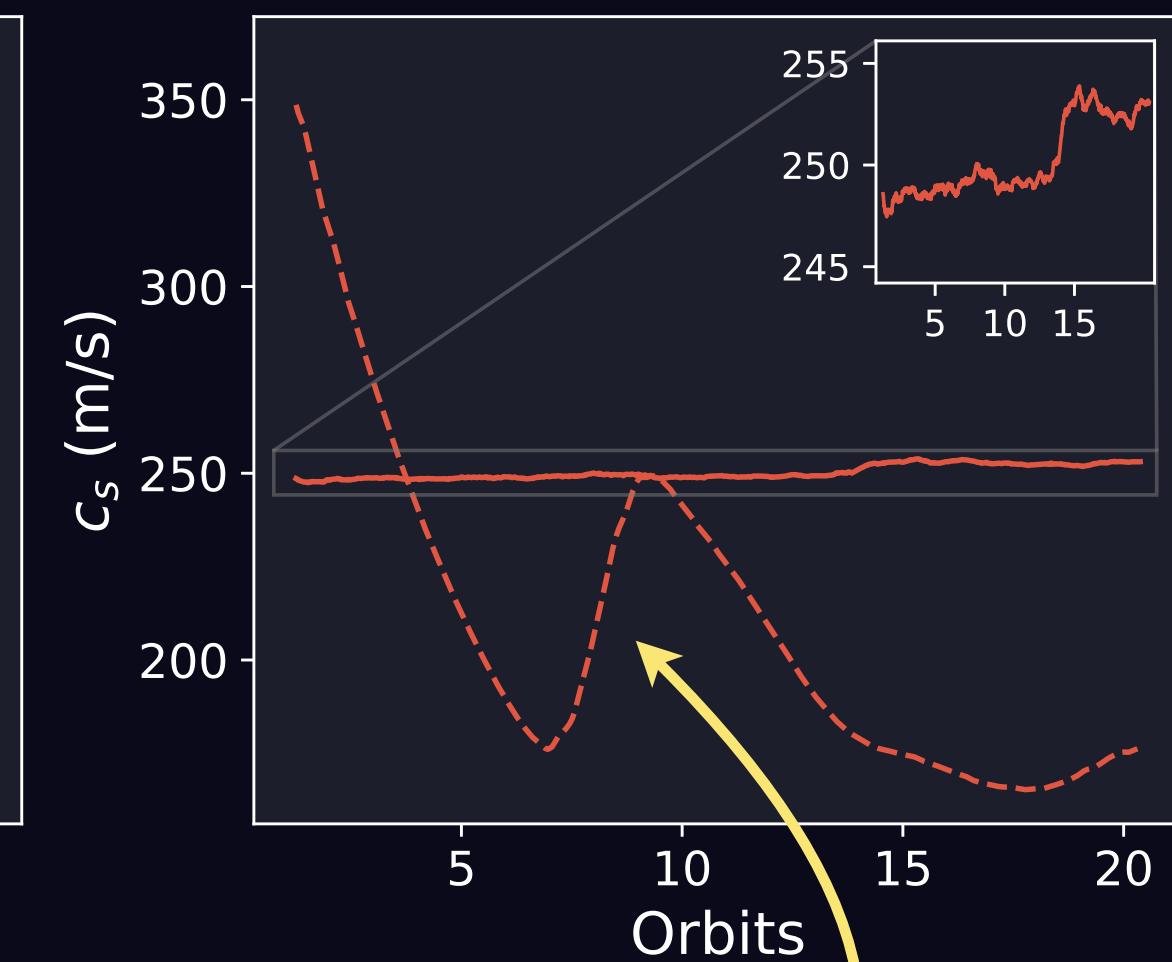
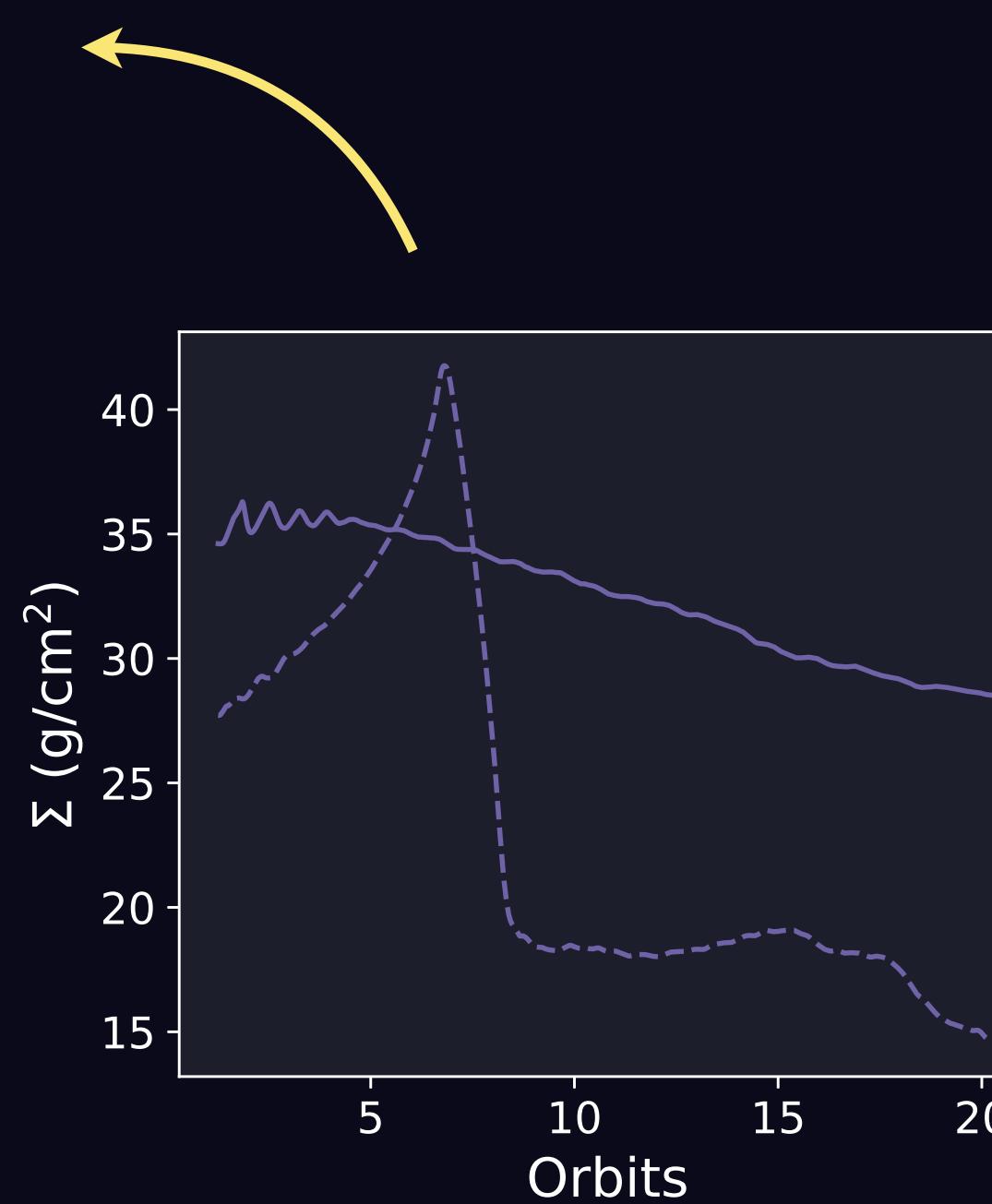
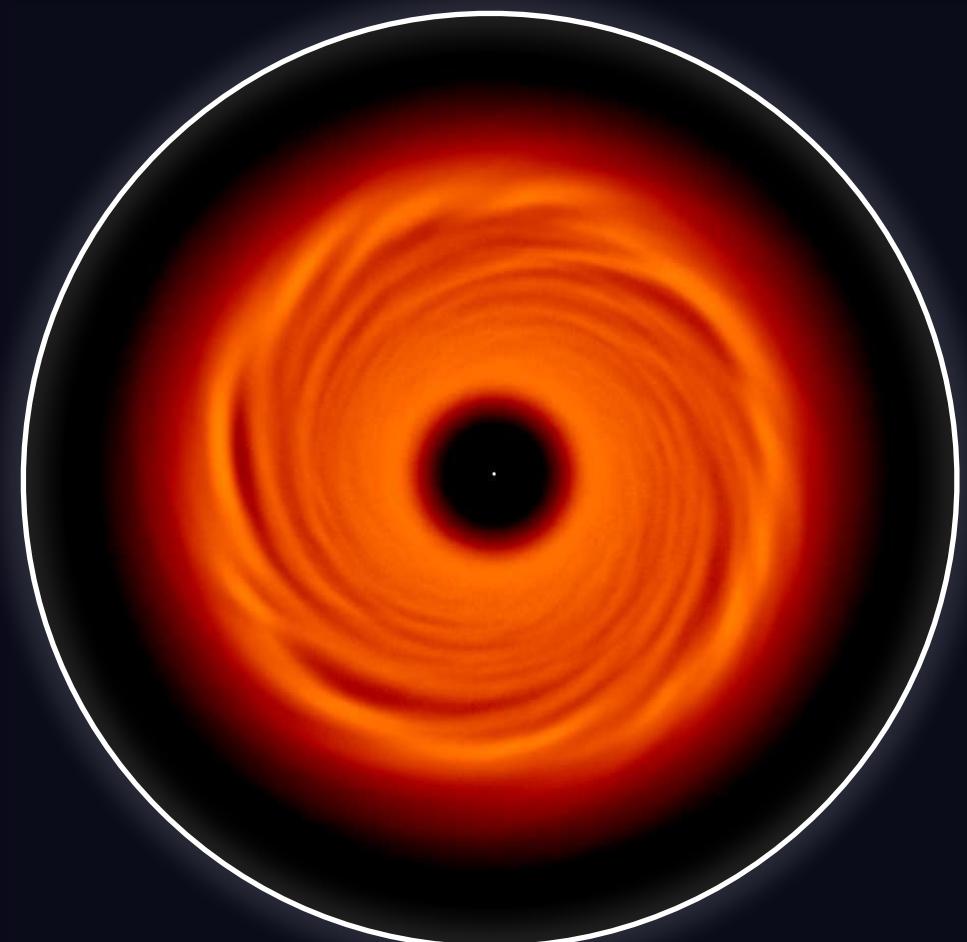


Initially, very little PdV and shock heating,
so the disc just cools.



Evolution of Disc Instability (At $R=77\text{AU}$)

*Disc has cooled enough to
form dense spirals.*



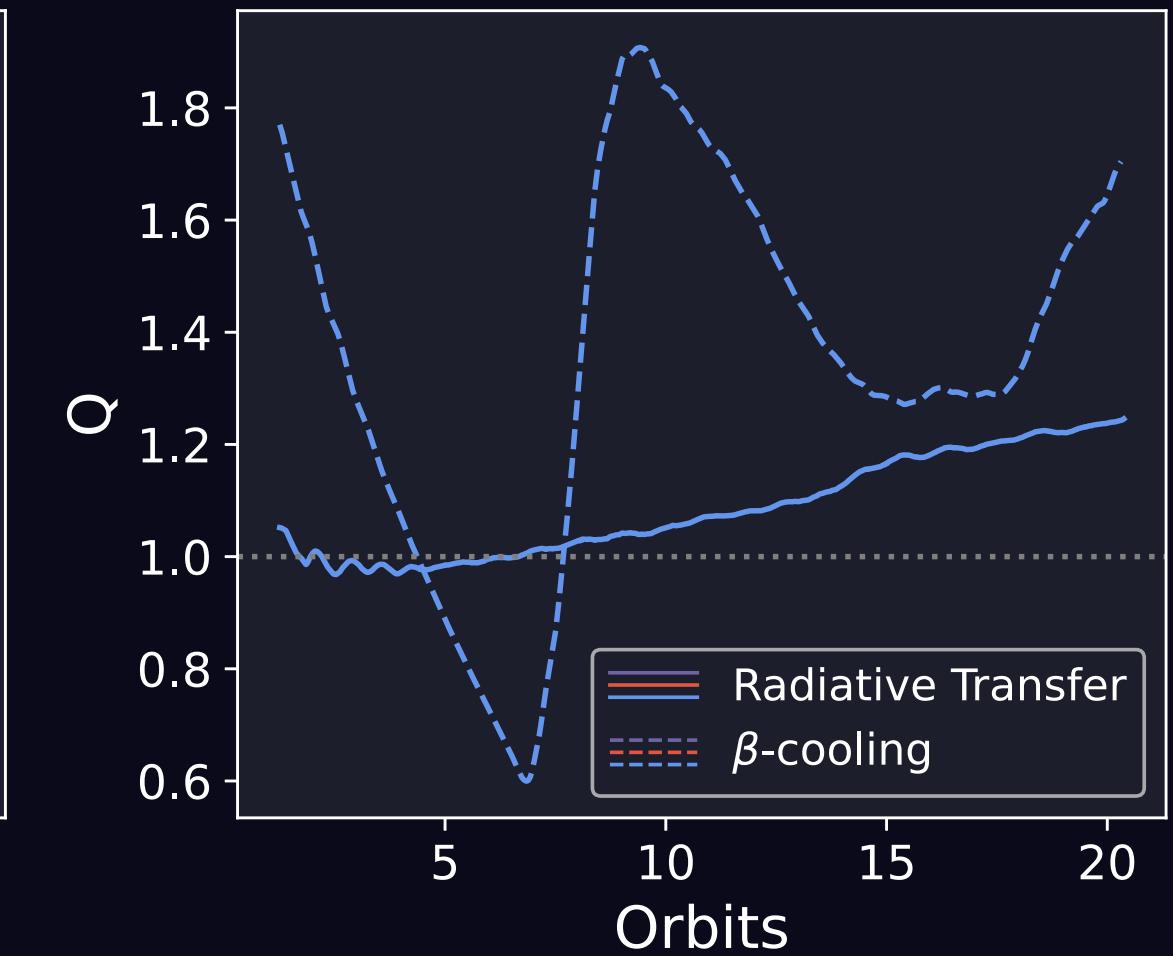
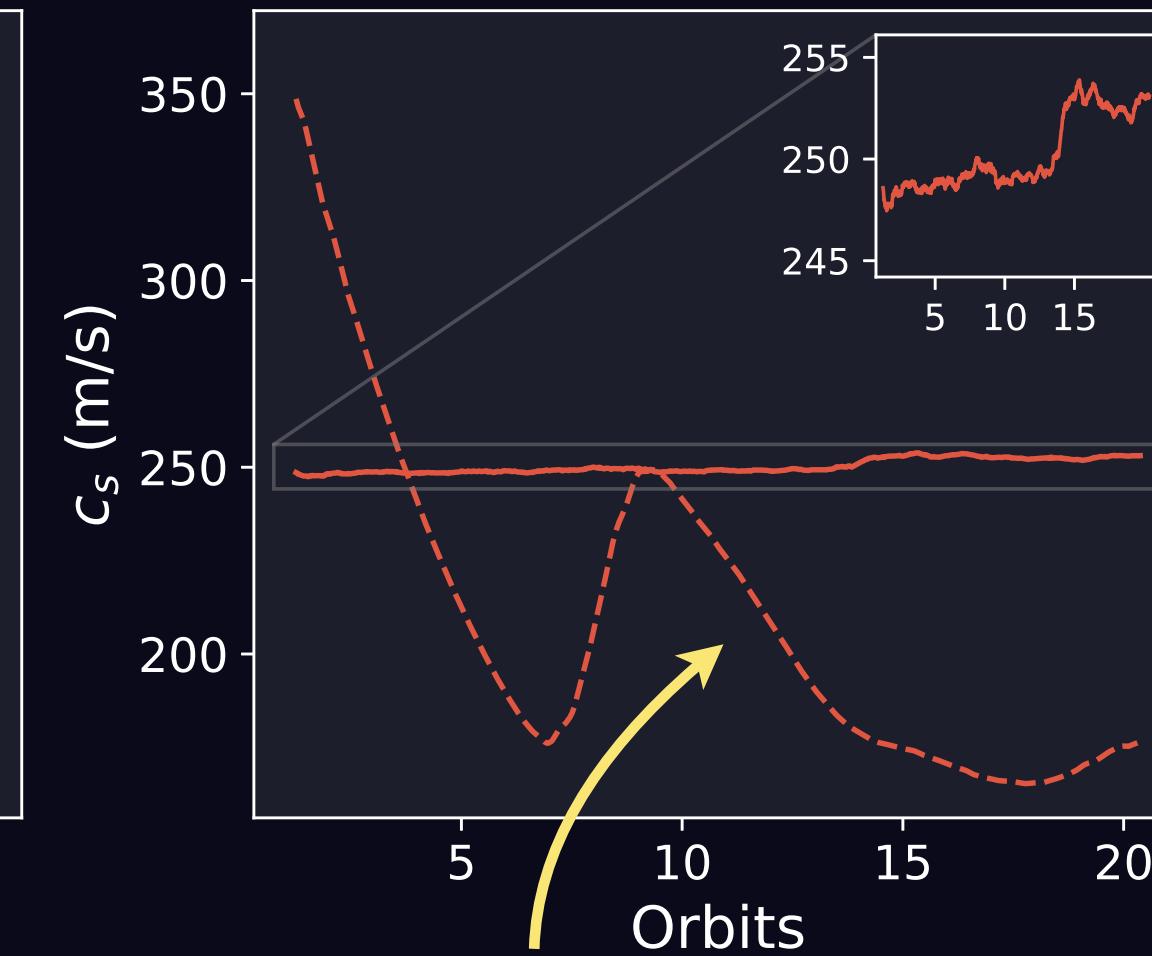
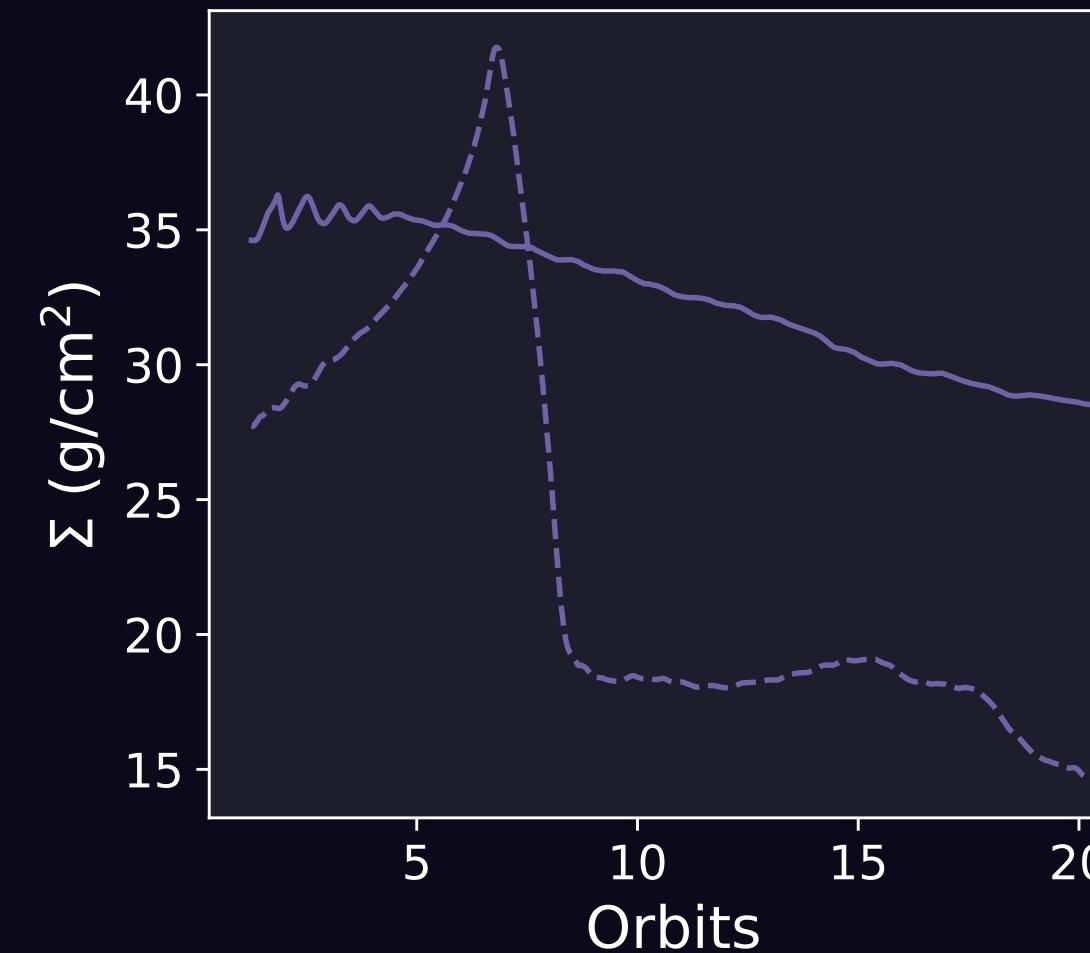
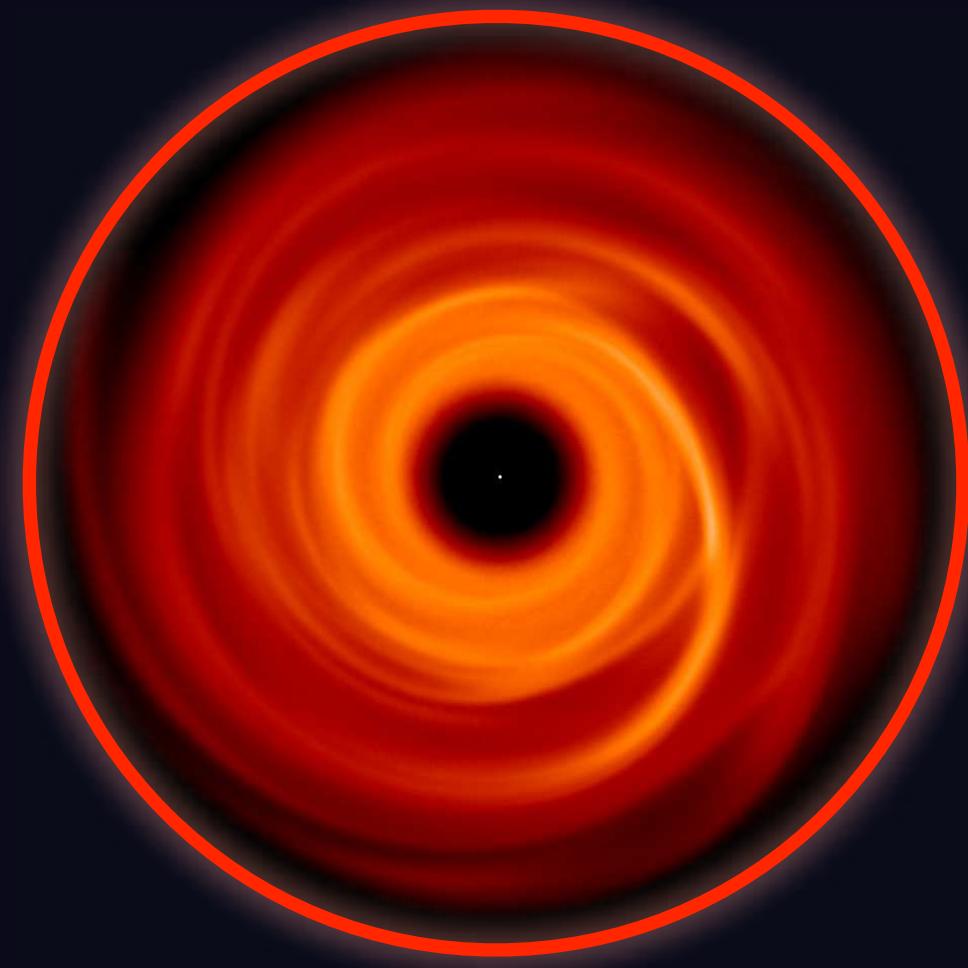
$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$

*Spirals are strong enough to stabilise the
disc through PdV and shock heating*



Evolution of Disc Instability (At $R=77\text{AU}$)

Spirals weaken as the disc
heats up.



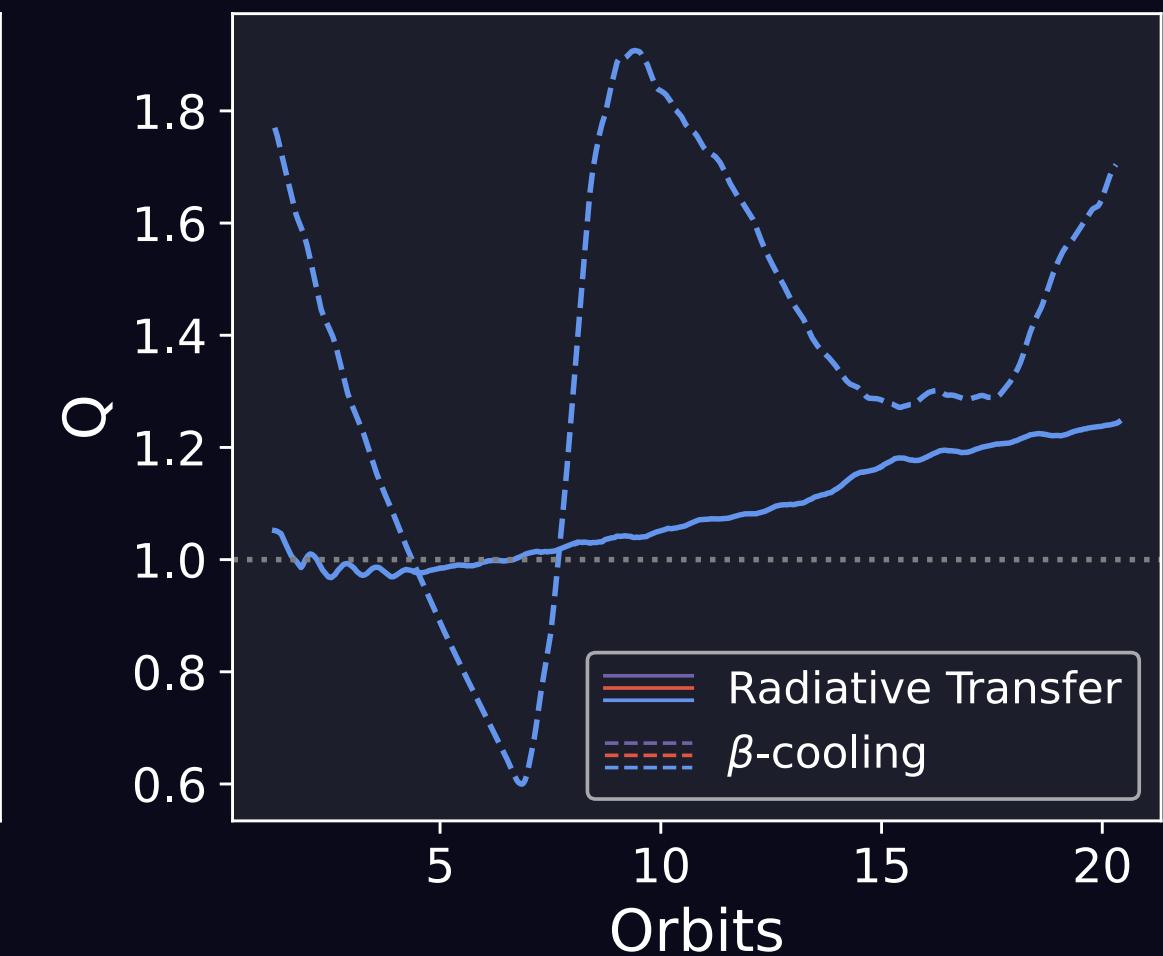
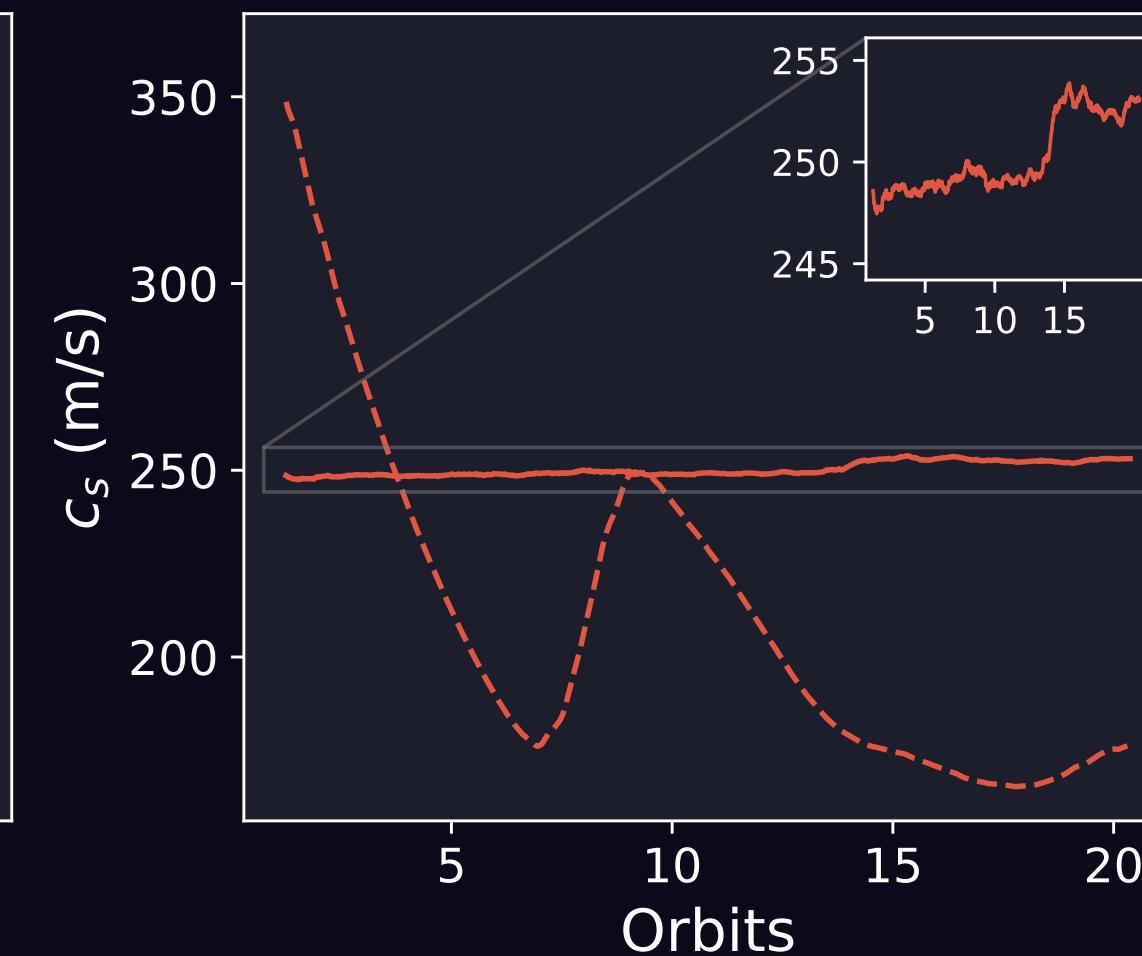
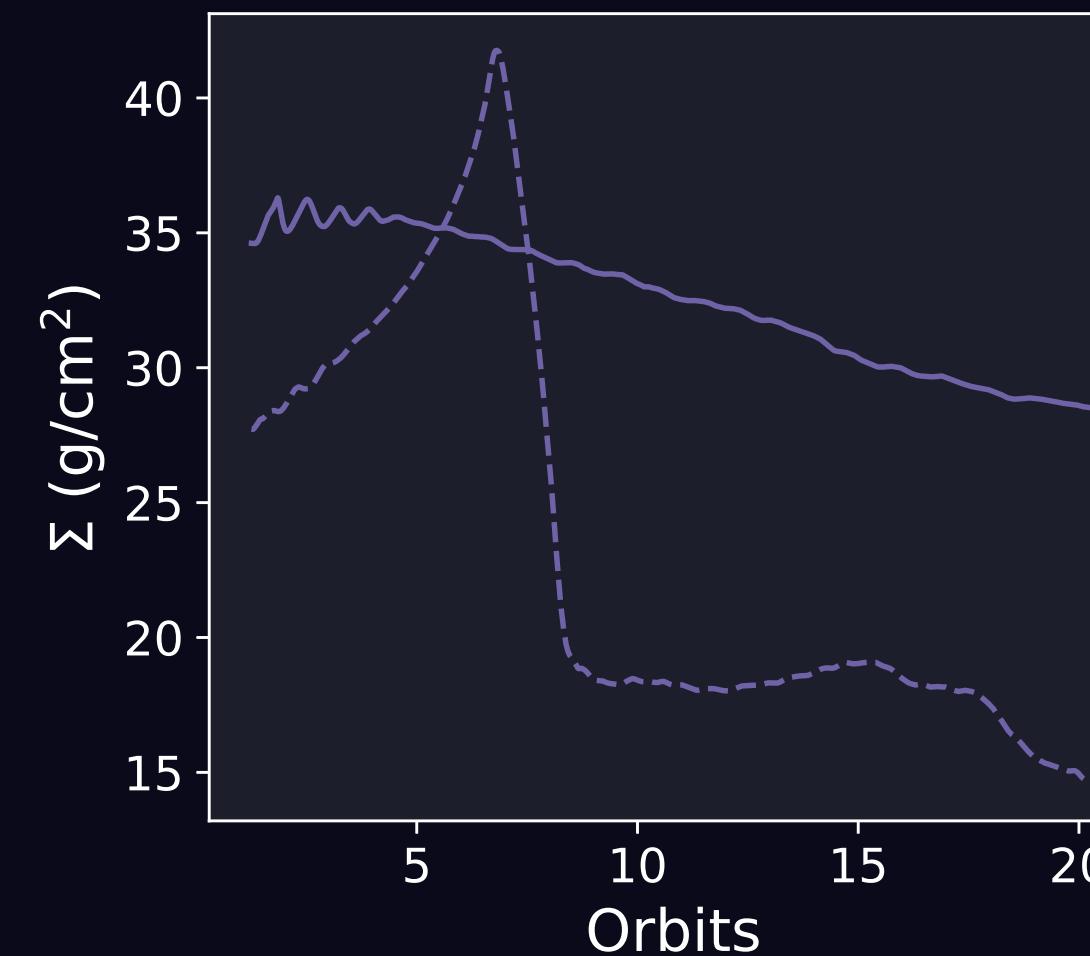
Cooling takes over once more as PdV and
shock heating lessen

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$



Evolution of Disc Instability (At $R=77\text{AU}$)

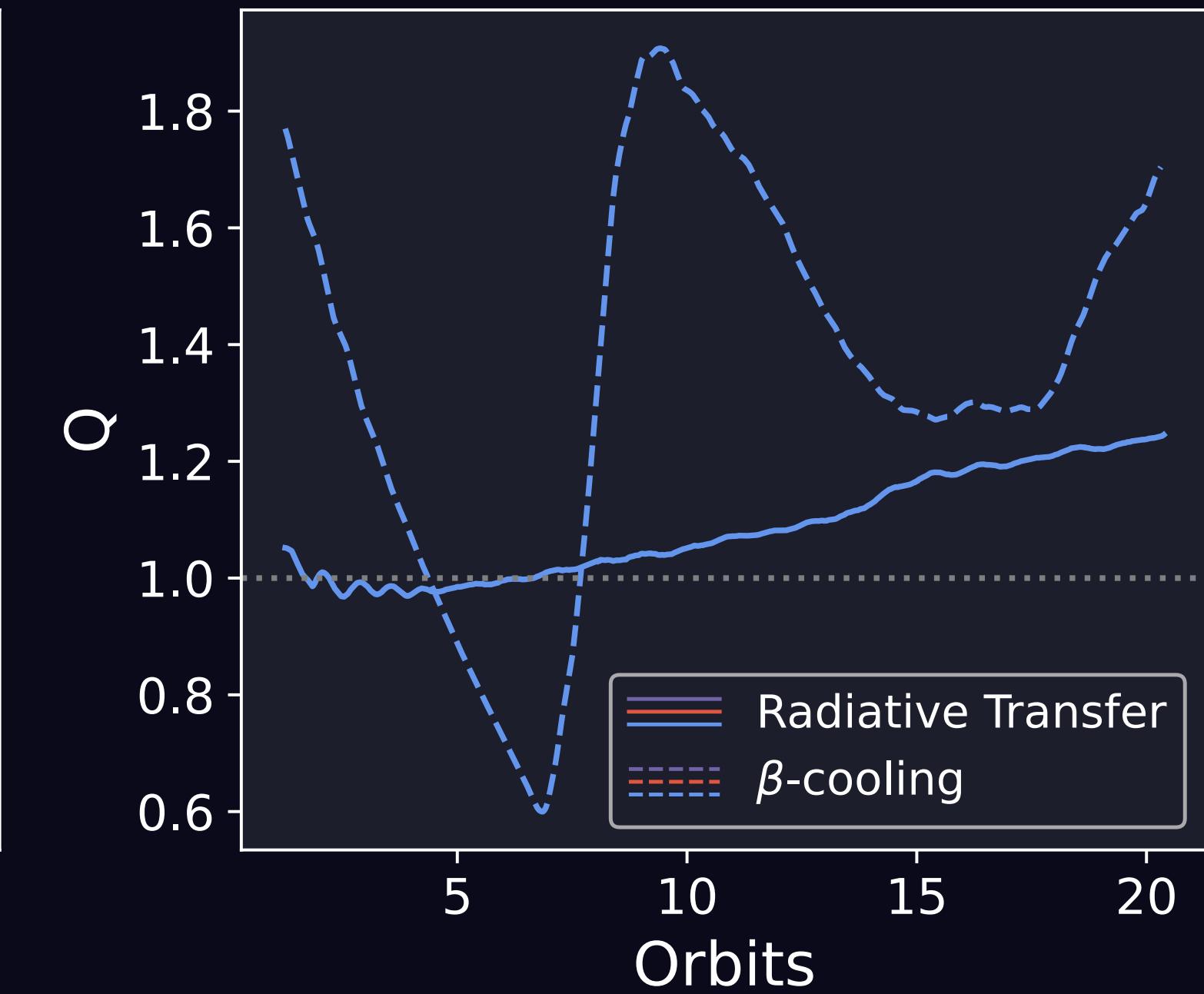
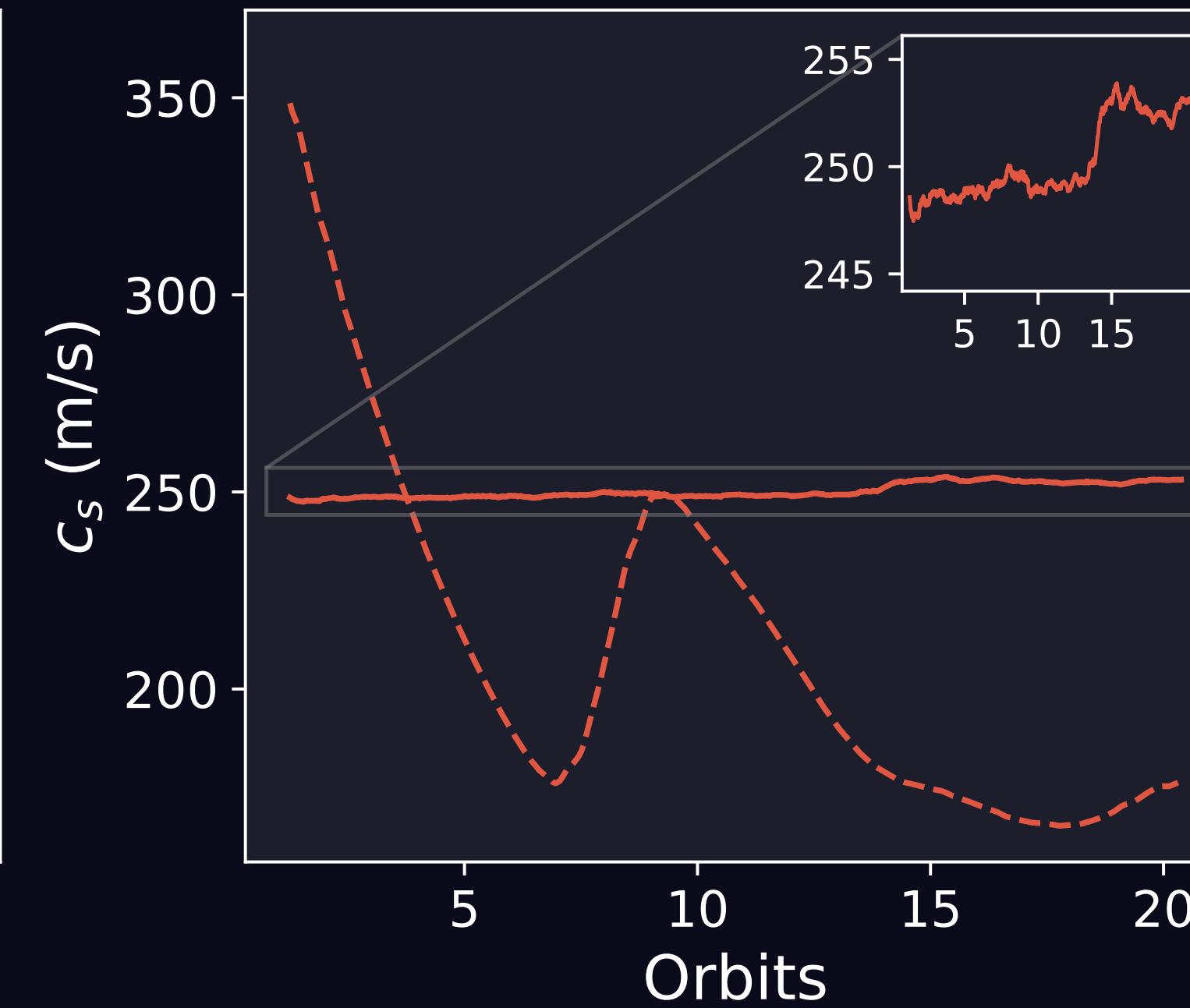
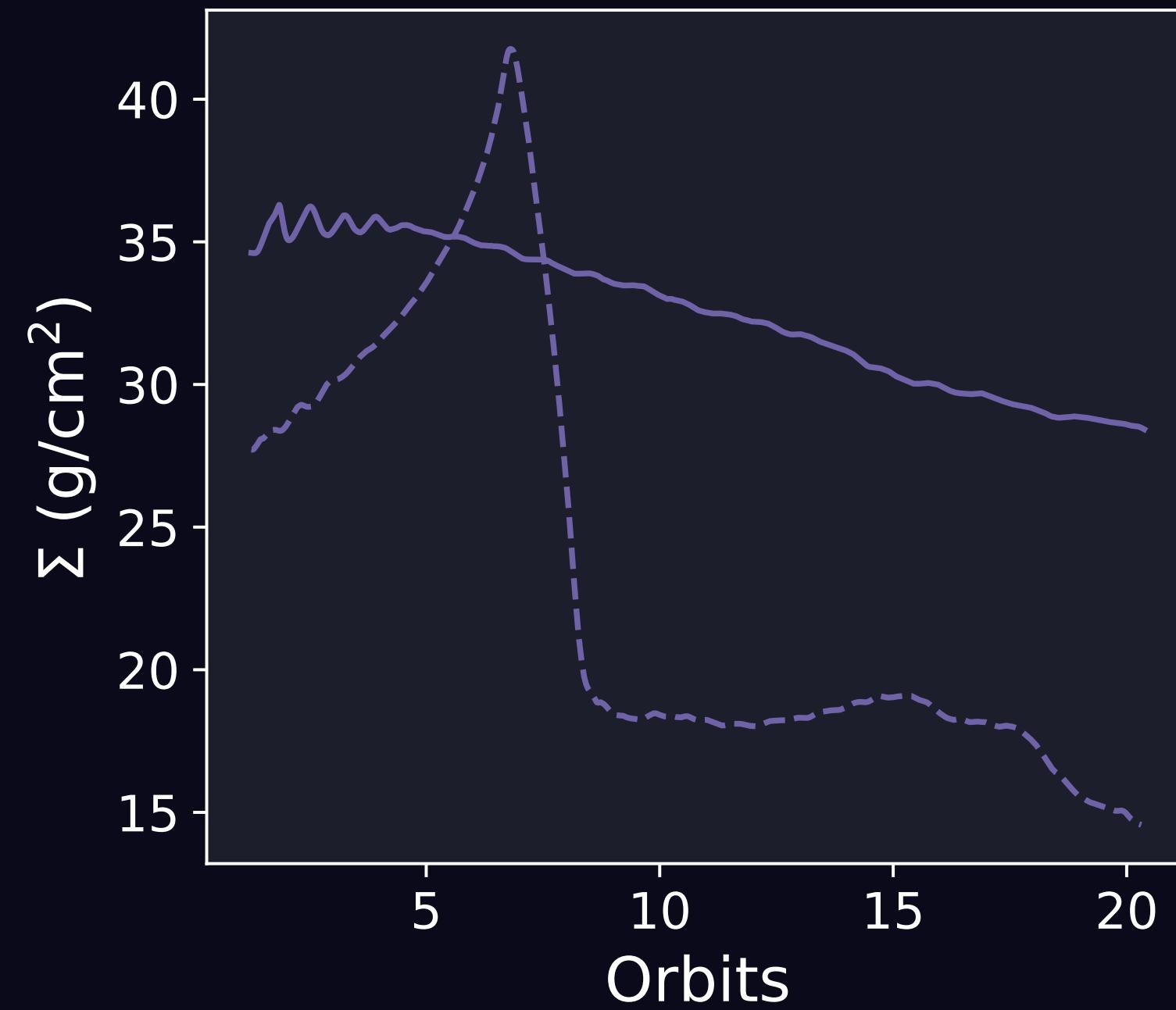
Steady spiral structures as cooling is balanced by PdV and shock heating



$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$

Evolution of Disc Instability (At $R=77\text{AU}$)

$$Q = \frac{c_s \Omega}{\pi G \Sigma}$$





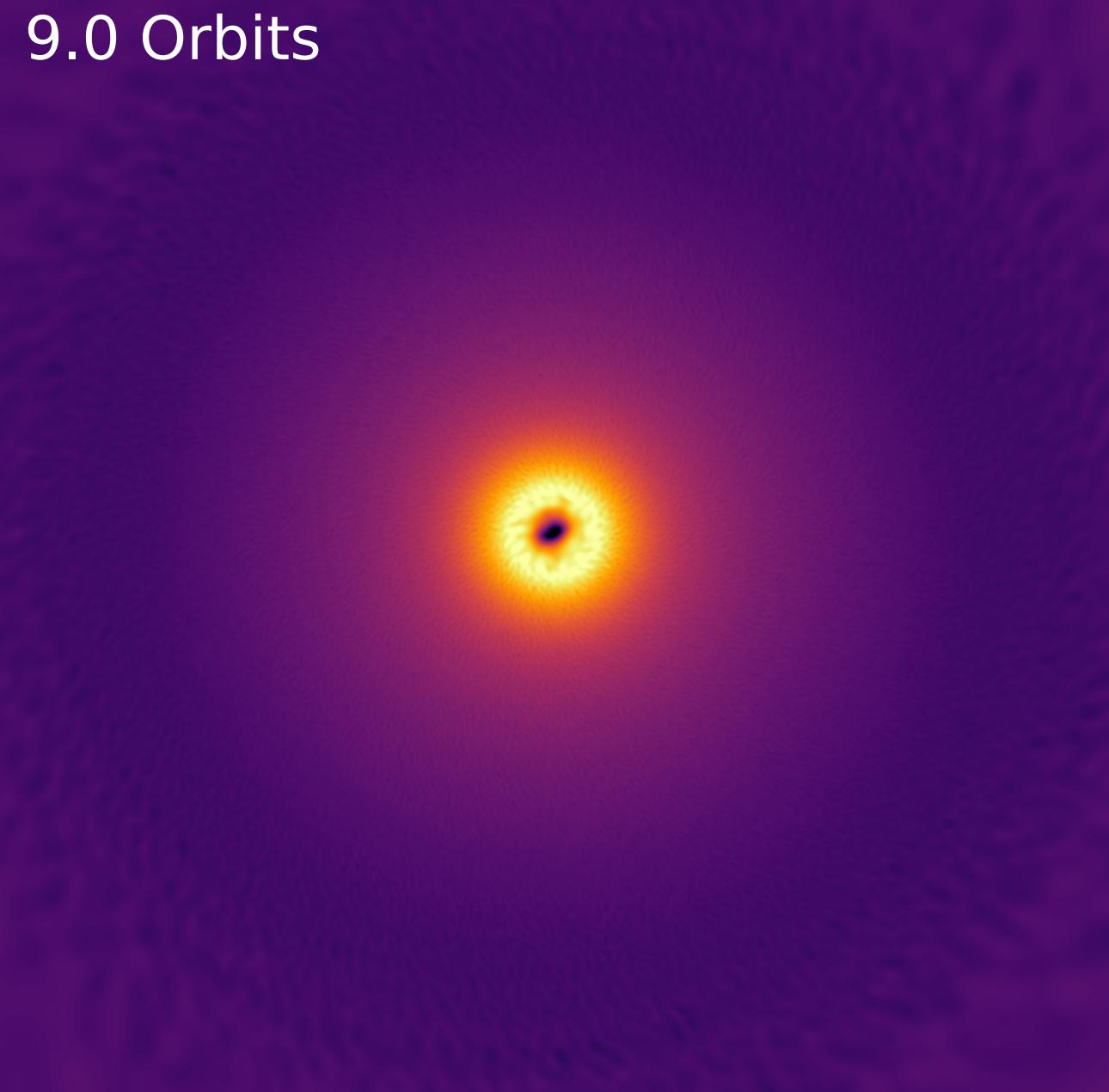
WHY IS PdV AND SHOCK HEATING MORE IMPORTANT FOR β COOLING?

Temperature Structure

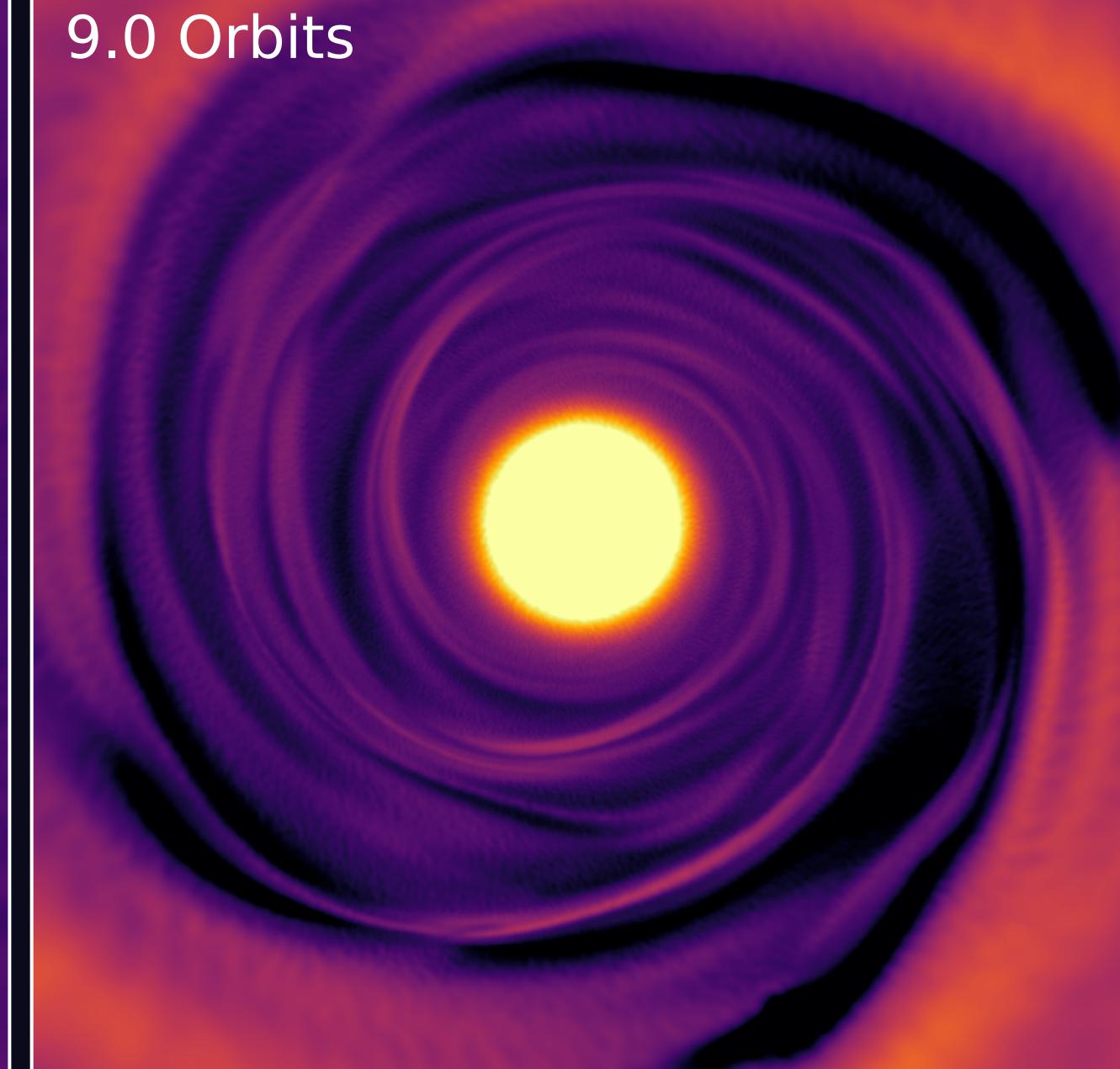
β cooling

- A colder disc.
- PdV and shock heating from the spirals are the source of heating.

Radiative Transfer



β -cooling

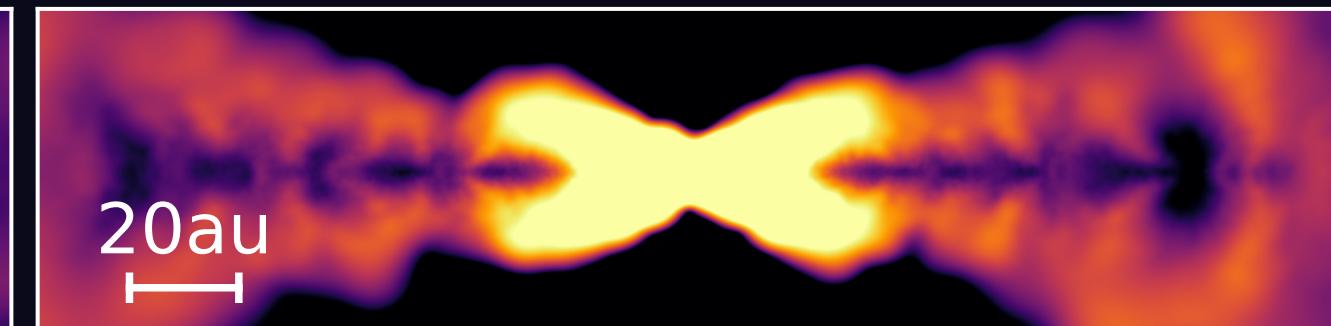
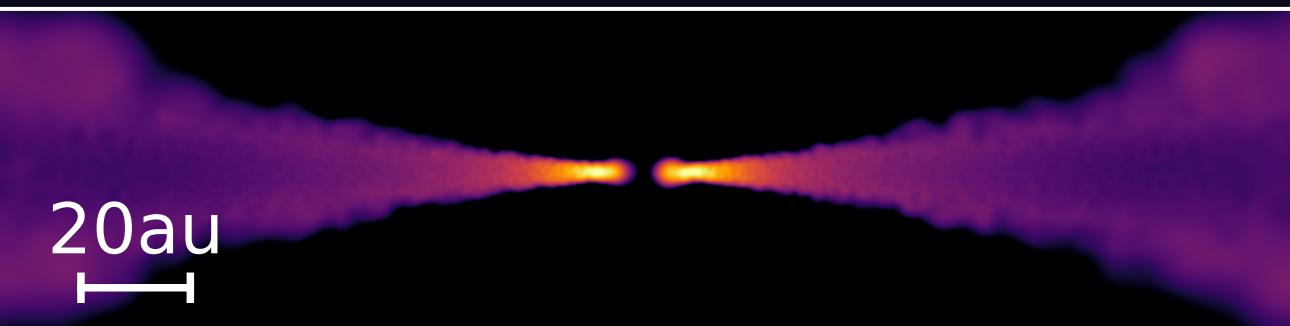


100

30

10

Temperature (K)

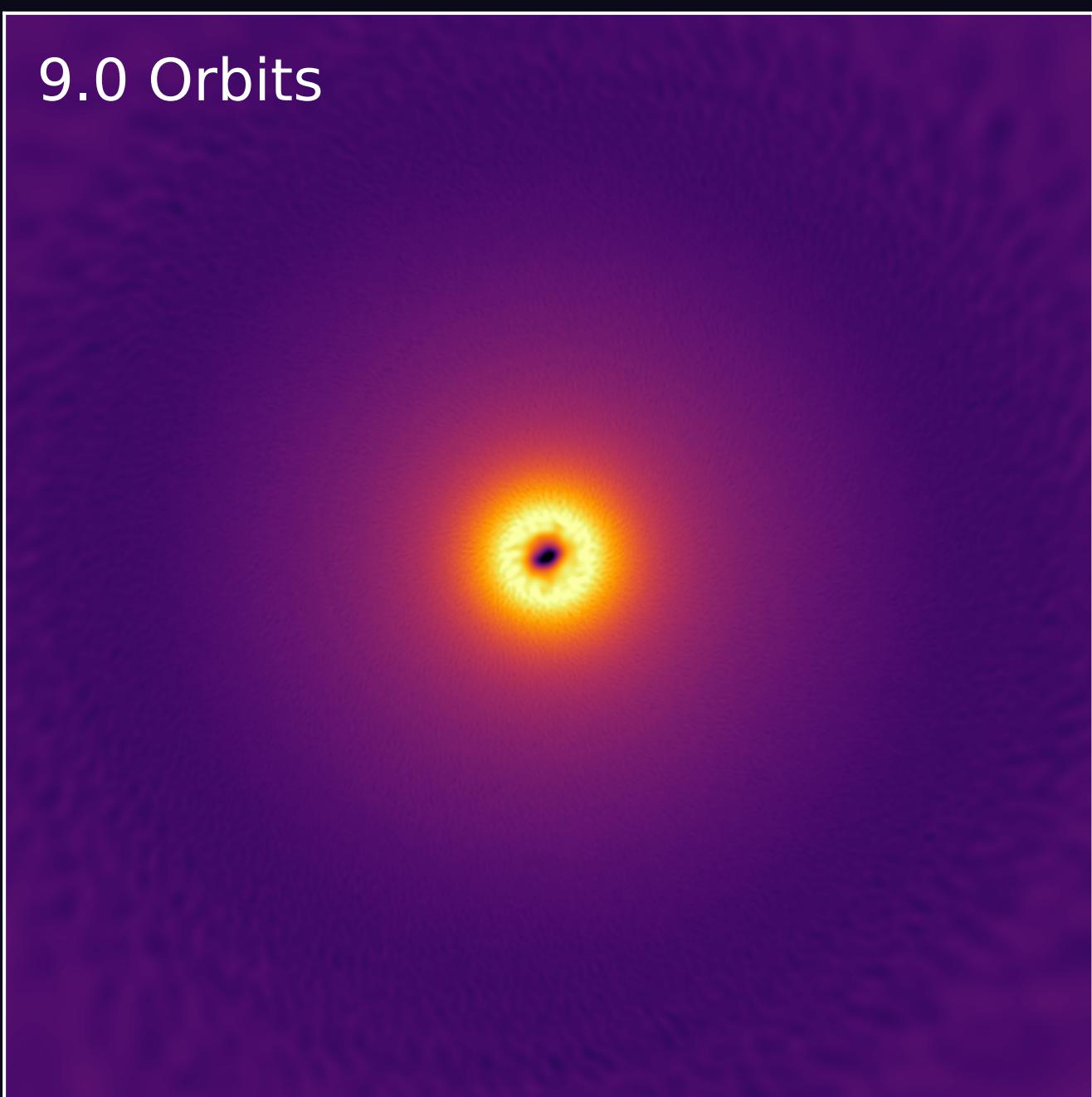


Temperature Structure

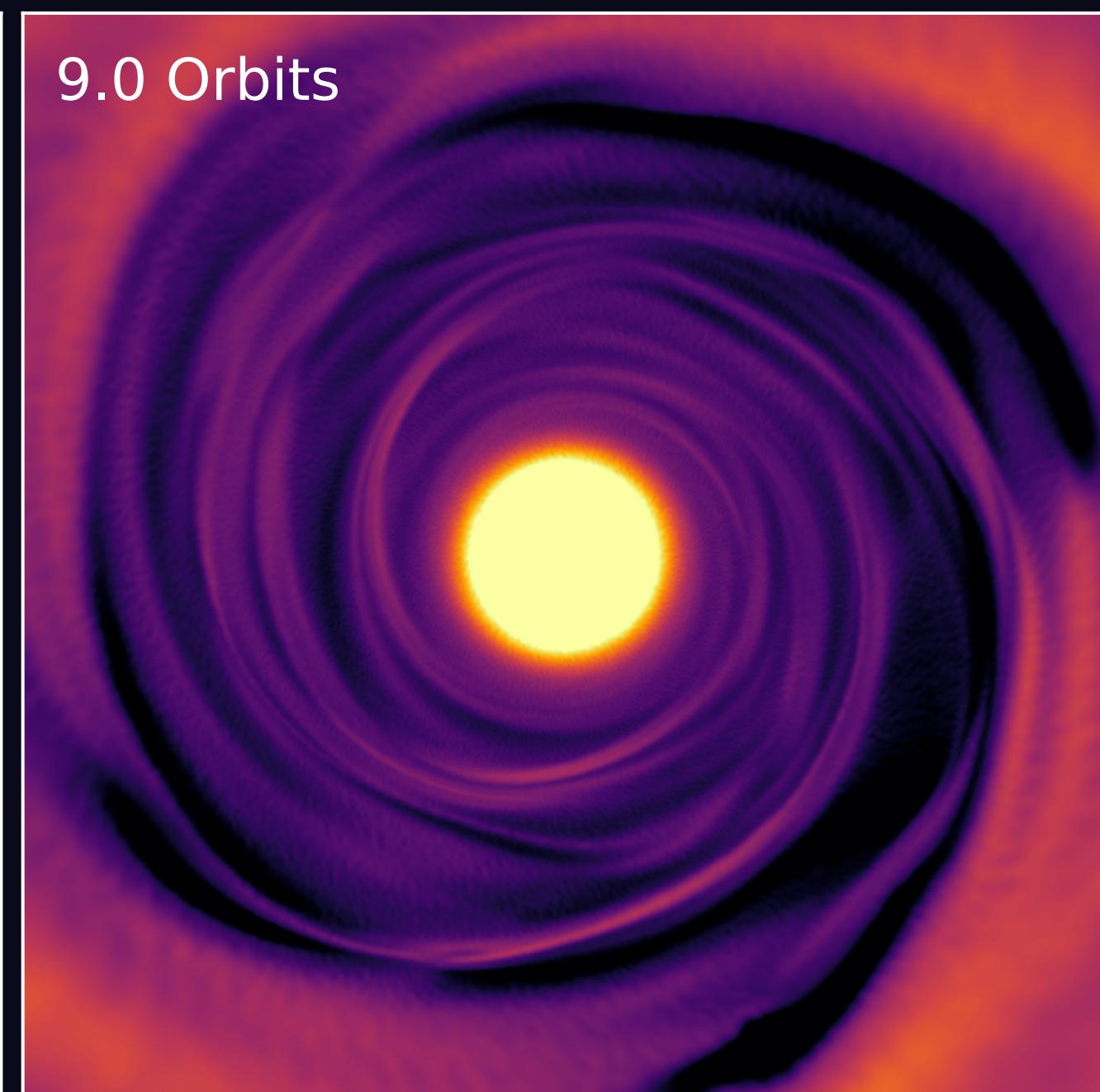
Radiative Transfer

- Disc is warmer.
- Stellar irradiation is the dominant source of heating.

Radiative Transfer



β -cooling



100

30

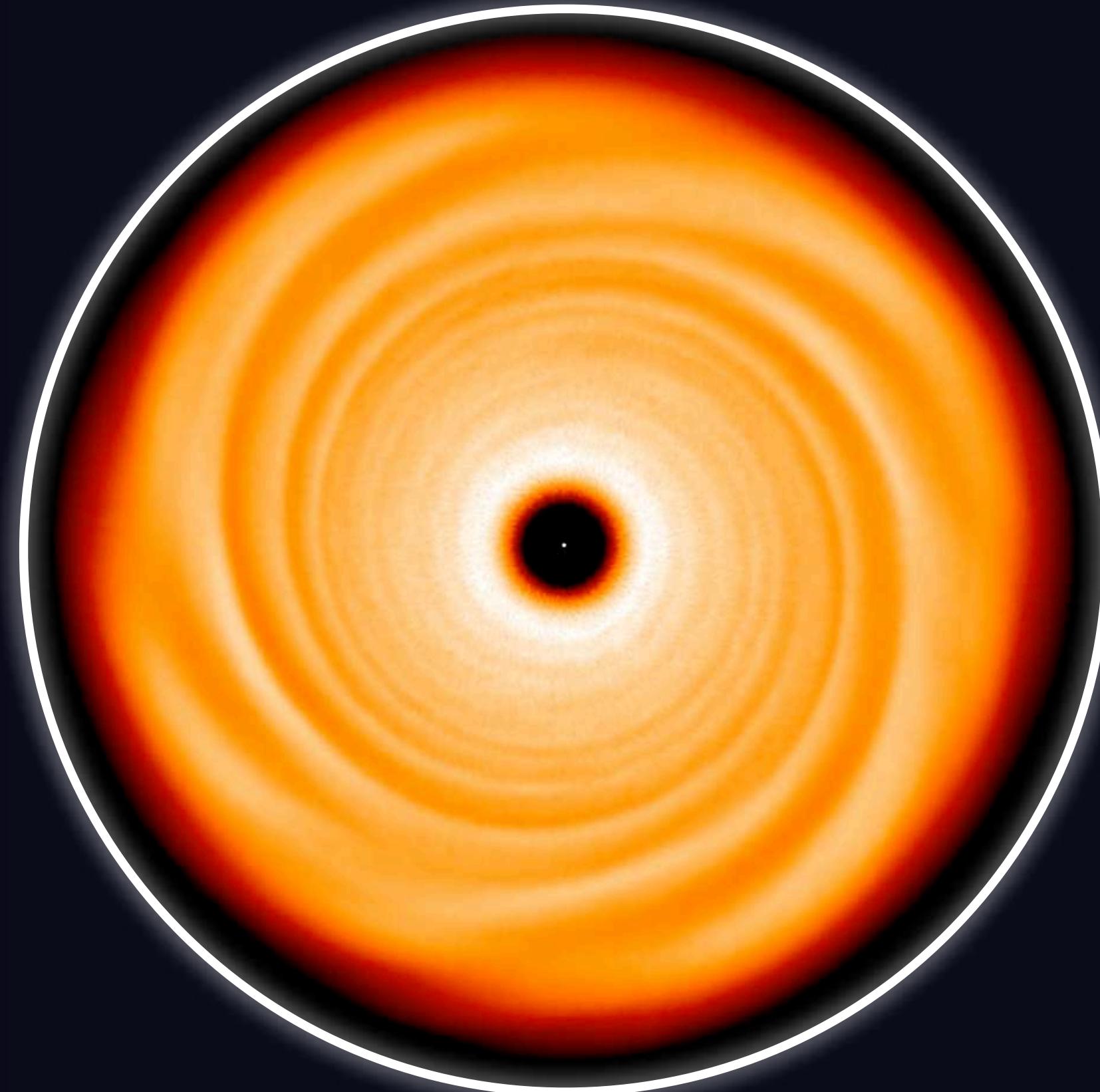
10

Temperature (K)



The Computational Cost

Radiative Transfer - $3e8$ CPU seconds



β cooling - $3e6$ CPU seconds



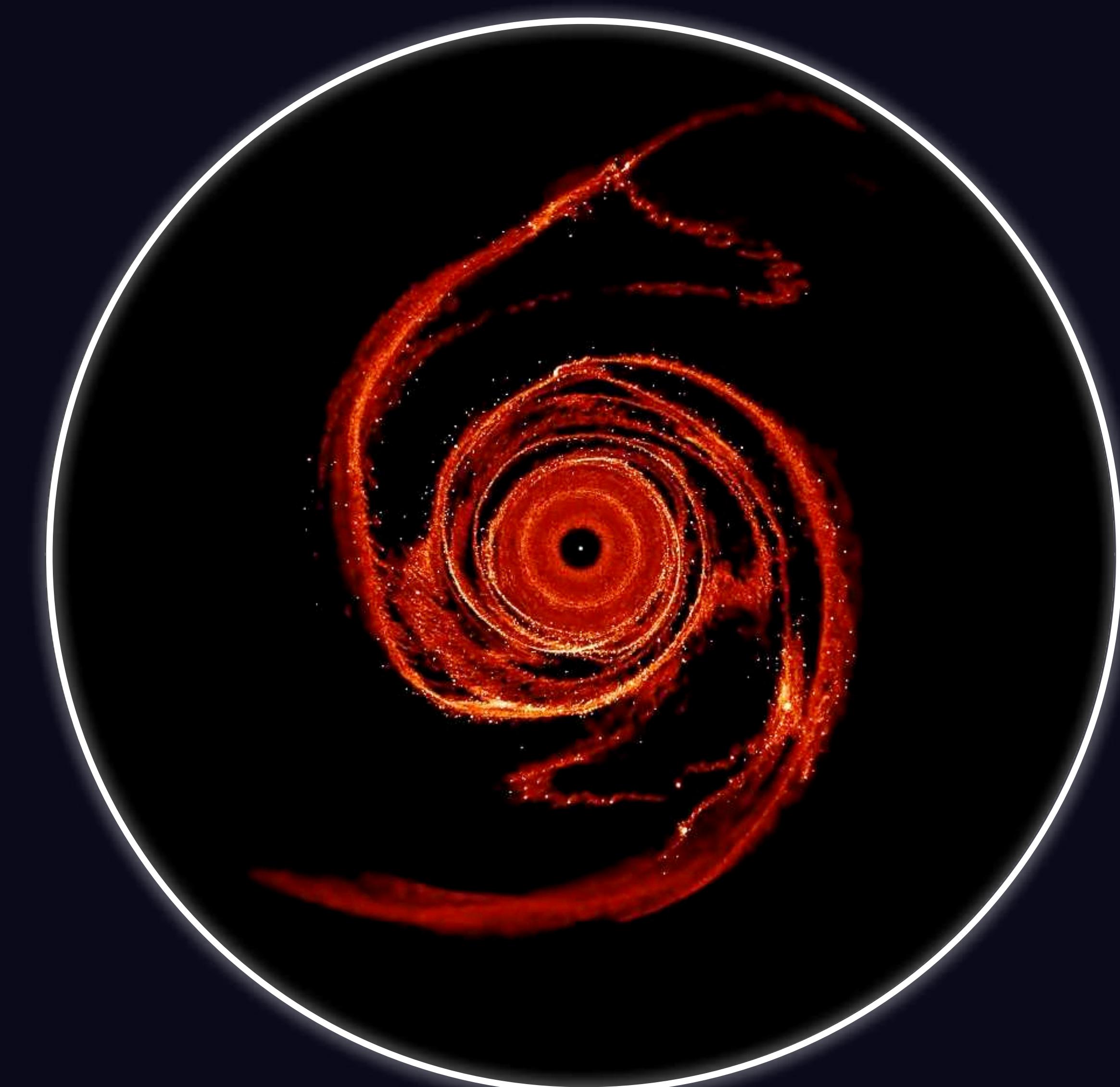


WHY BOTHER SIMULATING FOR MONTHS?



Dust Dynamics

- *The spirals are regions of pressure maxima where dust can be efficiently trapped and grow to form planetesimals.*

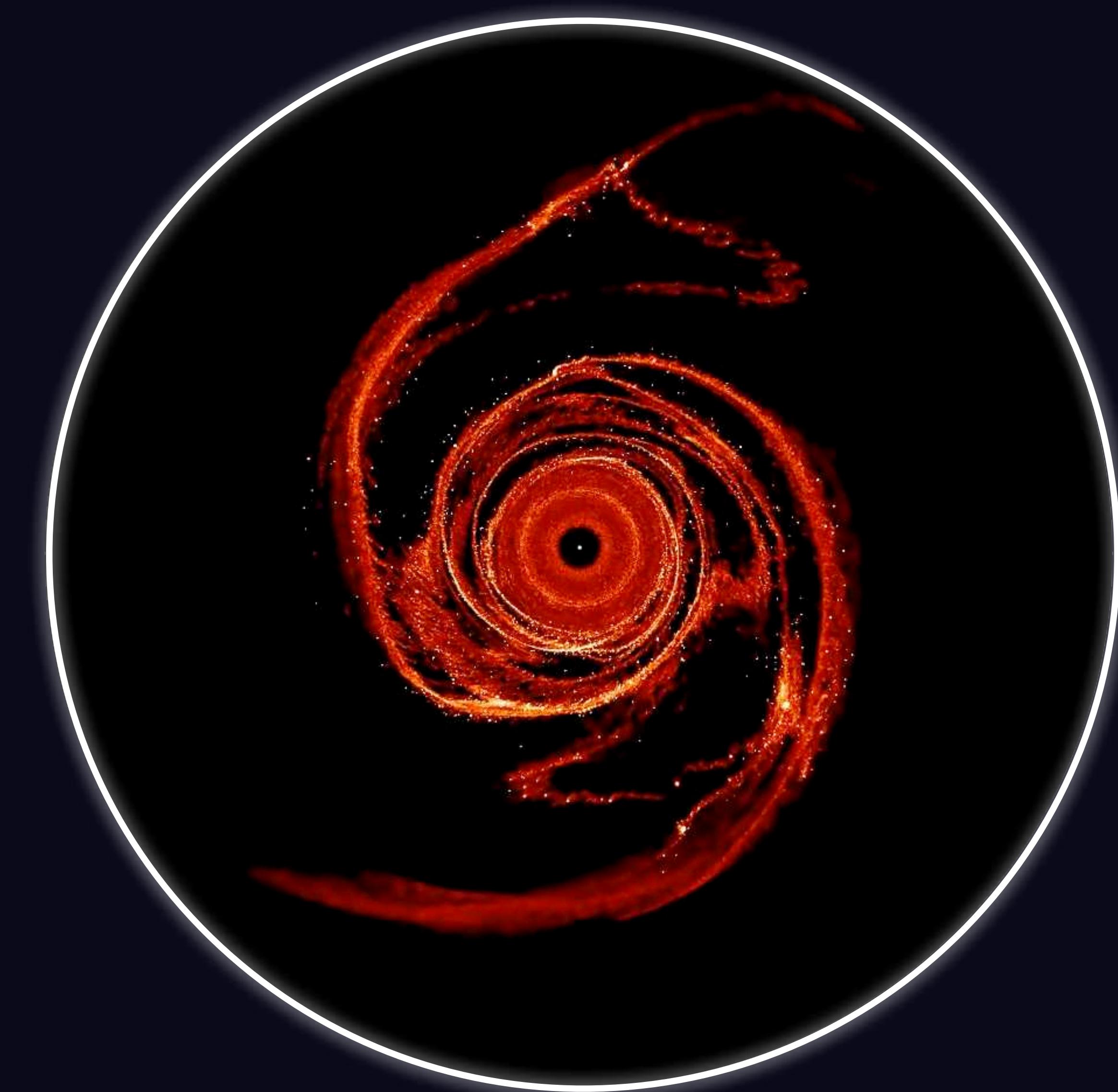


Rowther+ 2024



Dust Dynamics

- Dust is kicked around by high amplitude spirals (Longarini+ 2023b).

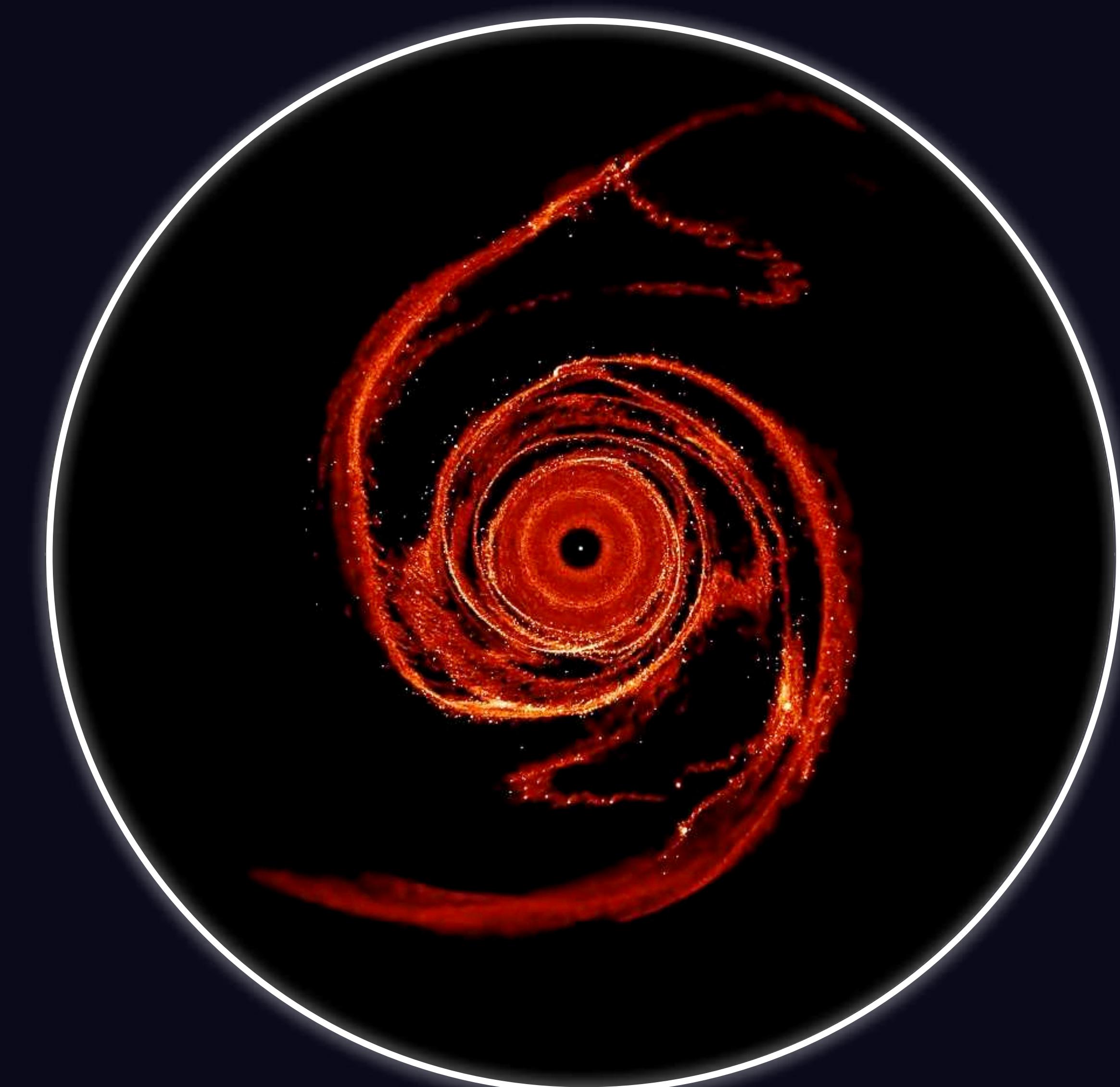


Rowther+ 2024



Dust Dynamics

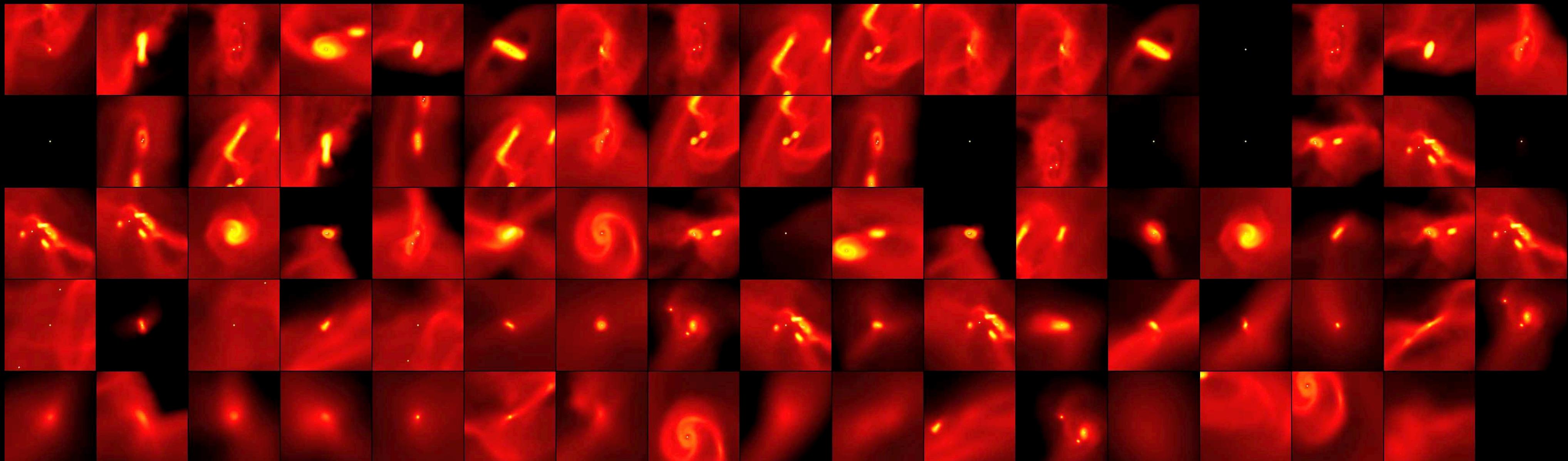
- *The weaker spirals with radiative transfer could be more favourable to forming planetesimals.*



Rowther+ 2024

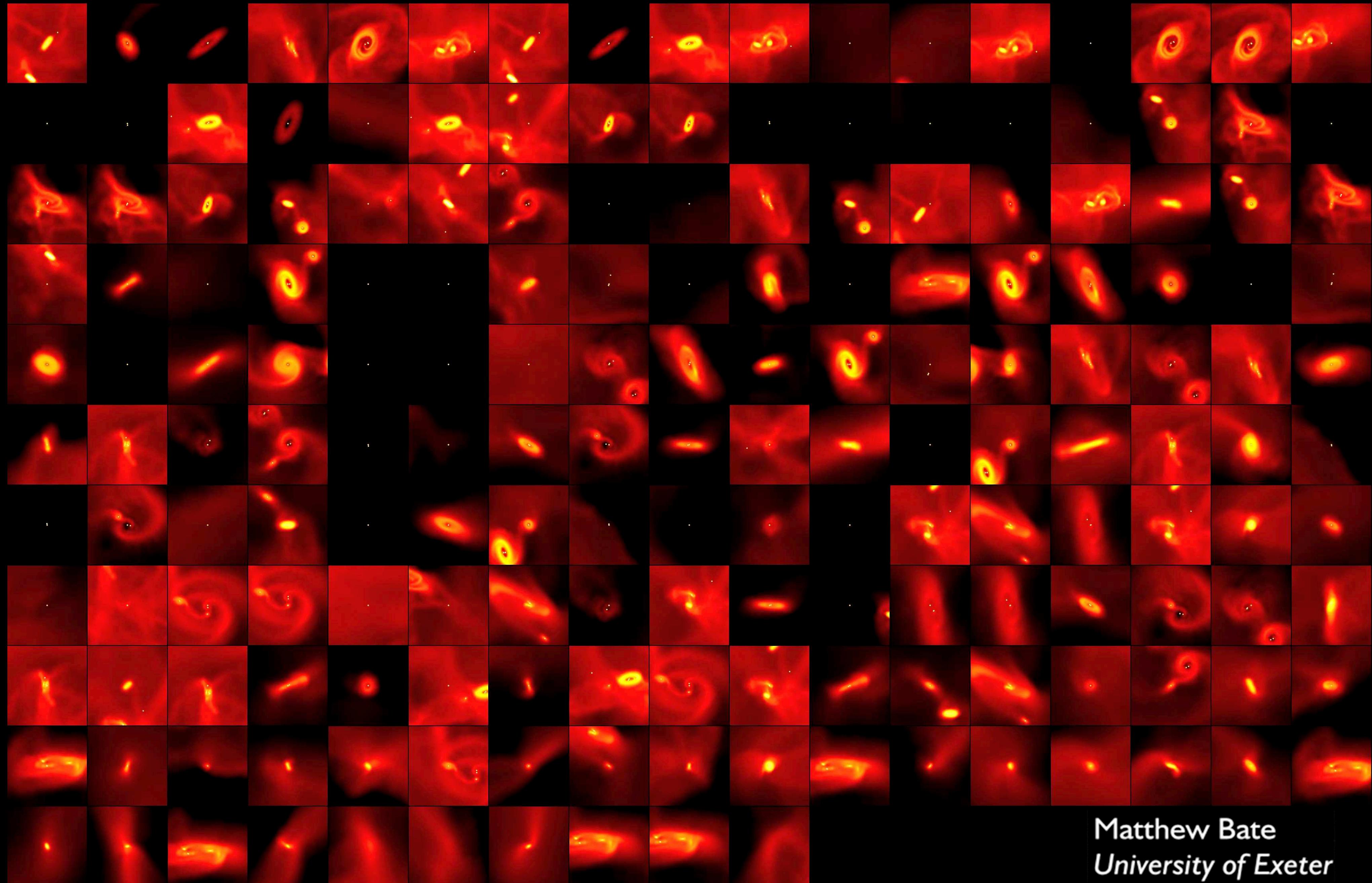


*Discs do
not evolve
in isolation*



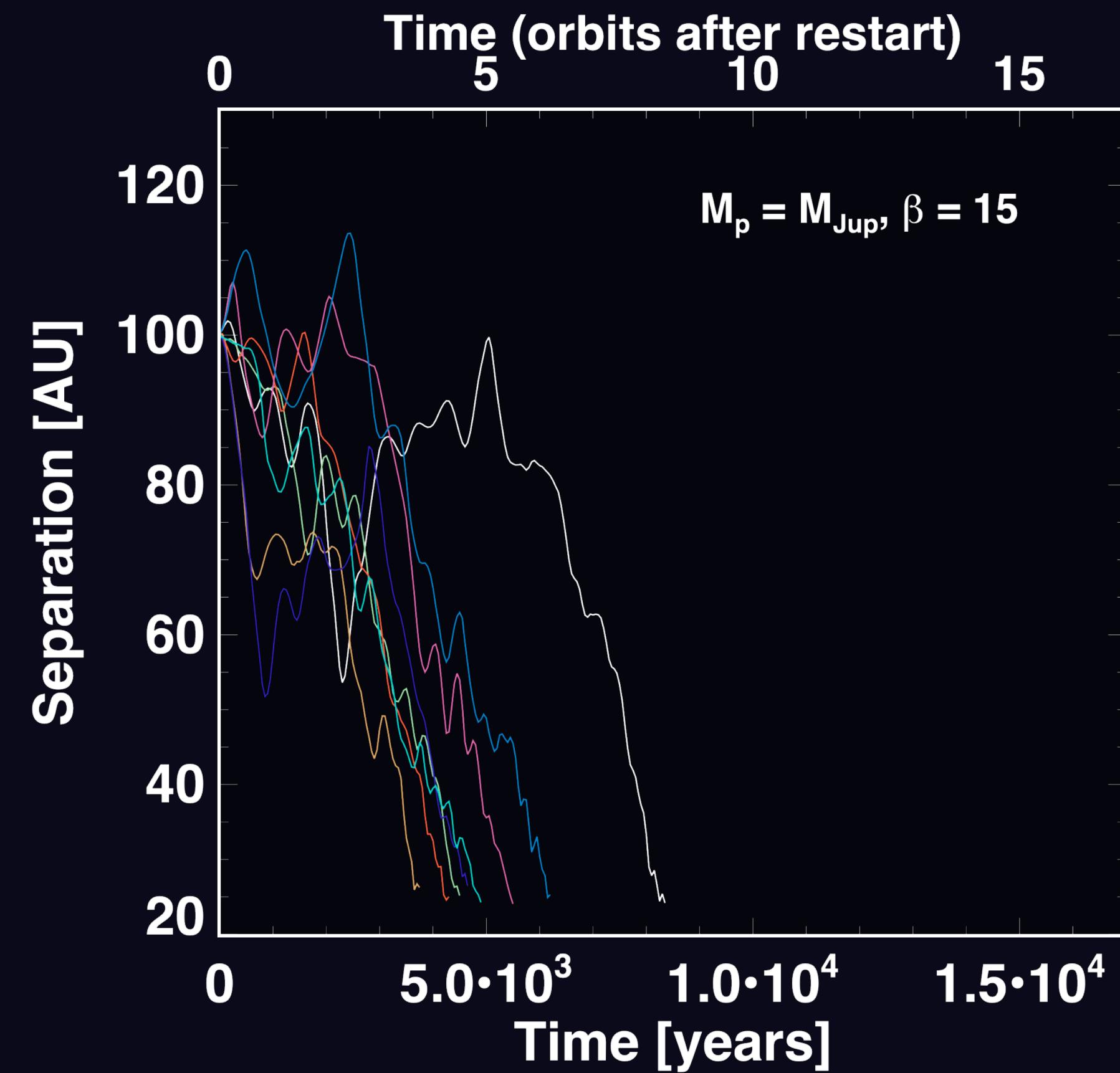
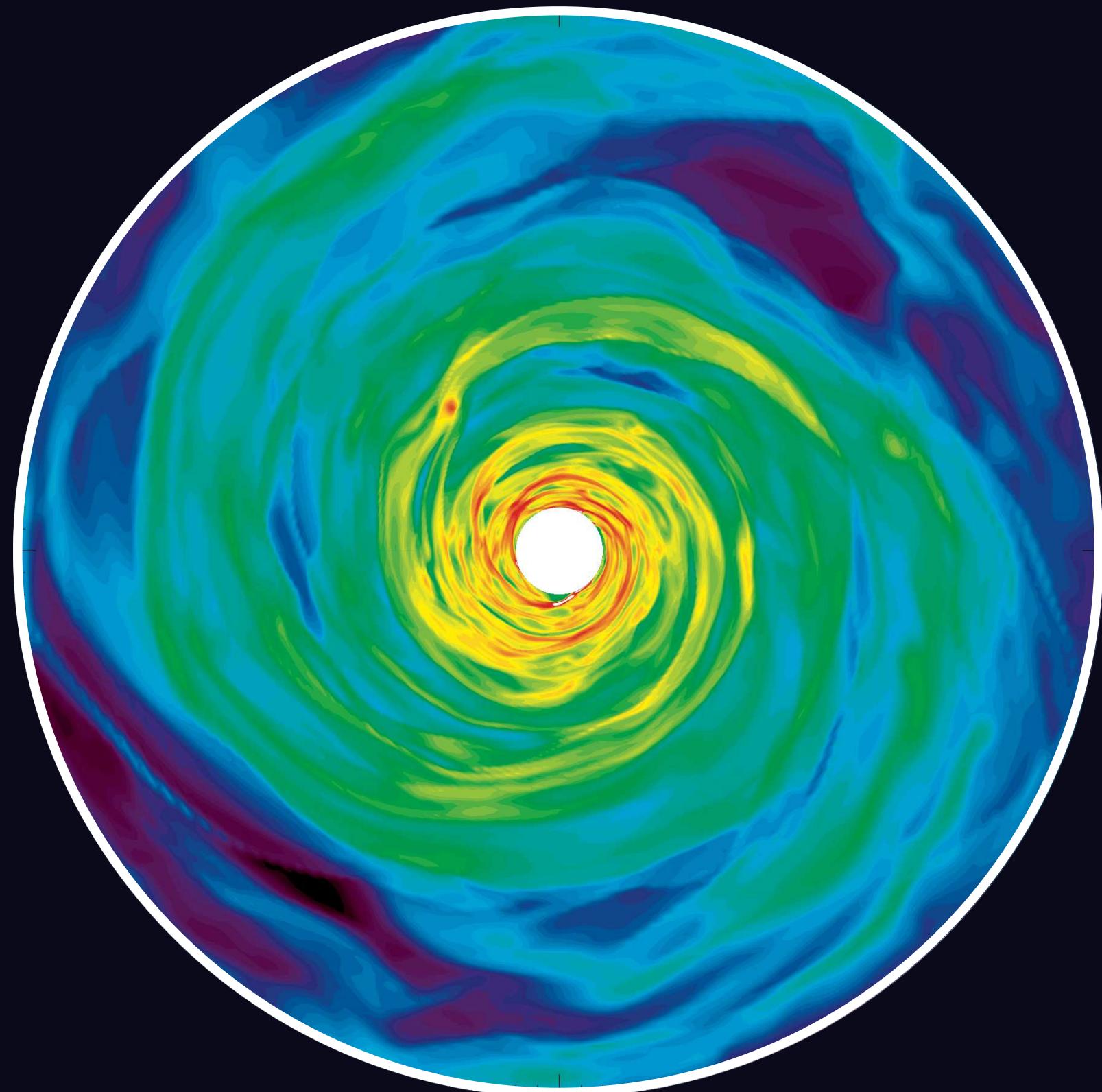


*Neighbours,
companions, and
chaotic accretion
episodes all can
alter the evolution
of the disc*



Matthew Bate
University of Exeter

The Doom of Giant Planets

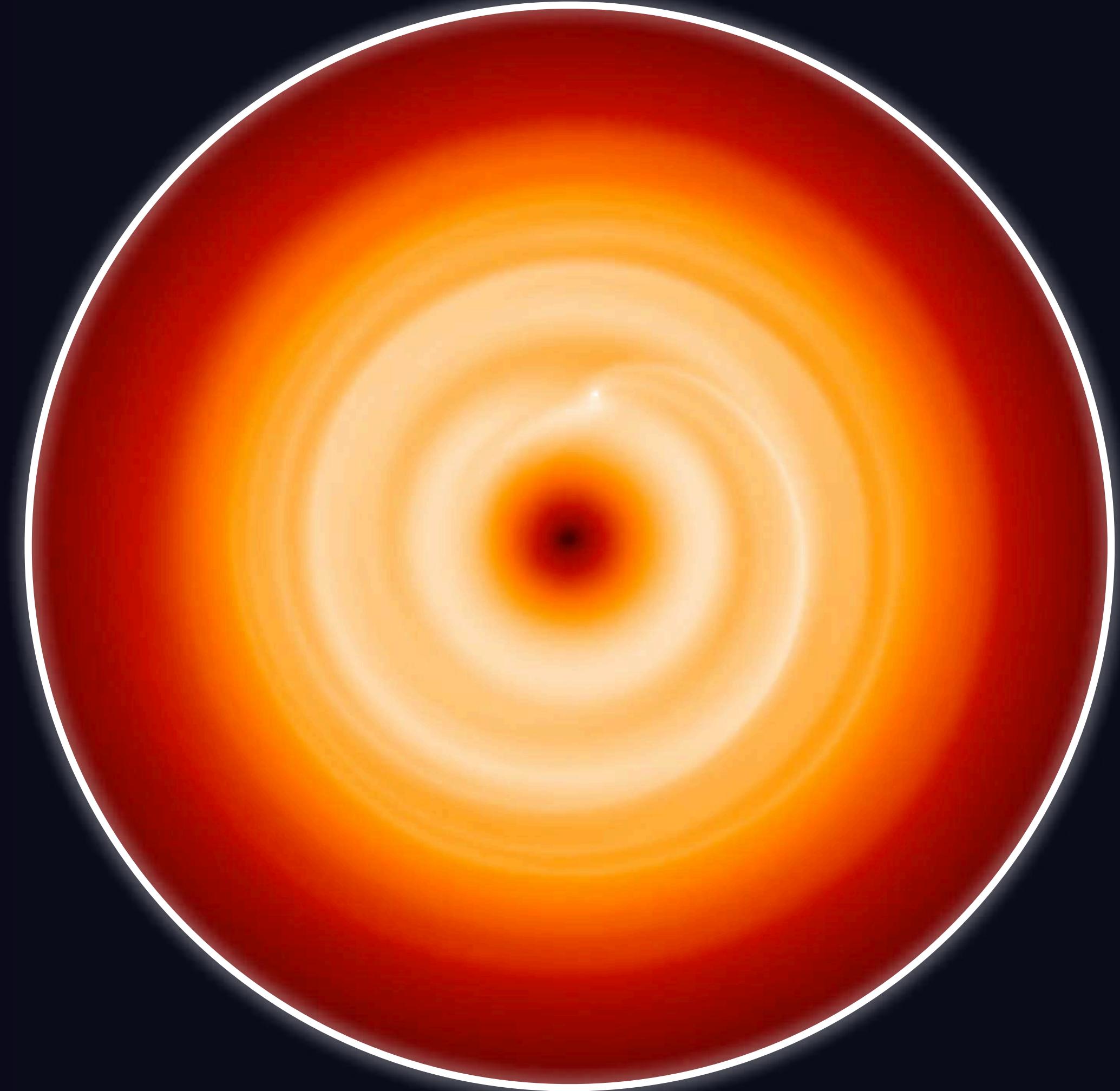


Planets migrate inwards rapidly within a few orbits in discs modelled with simple thermodynamics (Baruteau+ 2011)



Survival of Giant Planets

- Spirals with radiative transfer are weaker.
- Could be easier for planets to open up gaps, slowing their migration.



Rowther+ 2020, 2023



Conclusions

- Discs can become gravitationally unstable with stellar irradiation.
- The contribution from PdV and shock heating is tiny. the temperature of the disc is instead set by the star, and is fairly constant. This is in contrast to β -cooling where disc is very cold and the spirals set the temperature.
- Hence, the morphology of the spiral structures is different. They are weaker, and less numerous. Additionally, the disc becomes more stable over time as the surface density of the disc decreases.