FIITJEE ALL INDIA TEST SERIES

JEE (Advanced)-2025 <u>FULL TEST - VIII</u> PAPER -2

TEST DATE: 27-04-2025

ANSWERS, HINTS & SOLUTIONS

Physics

PART – I

SECTION - A

B
 Thermal resistance of the spherical shell,

$$R = \int_{a}^{3a} \frac{dr}{k4\pi r^{2}} = \int_{a}^{3a} \frac{dr}{\frac{\alpha}{r^{2}} 4\pi r^{2}} = \frac{2a}{4\pi\alpha} = \frac{a}{2\pi\alpha}$$

Now,
$$-mS\frac{d\theta}{dt} = \left(\frac{\theta - \theta_0}{R}\right)$$

$$-\mathsf{mSR} \int_{70}^{50} \frac{\mathsf{d}\theta}{(\theta - \theta_0)} = \int_{0}^{t} \mathsf{d}t$$

$$t = mSR \left[\ell n(\theta - \theta_0) \right]_{50}^{70}$$

$$t = mSR \ell n \left(\frac{70 - 30}{50 - 30} \right)$$

$$t = mSR\ell n2$$

$$t = \frac{mSa\ell n2}{2\pi\alpha}$$

2. B

Sol. Similar to gravitational force and orbital motion $\Rightarrow v_{\rm escape} = \sqrt{2} v_{\rm orbital}$

3. A

Sol. Potential at 'C' =
$$\frac{kQ}{R} = \frac{\sigma R}{2\epsilon_0}$$

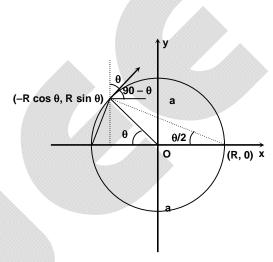
Flat surface of hemispherical shell is on equipotential surface.

Sol.
$$i = \frac{|E_1 + E_2 - E_3 - E_4|}{r_1 + r_2 + r_3 + r_4}$$

5. A, B, C
Sol.
$$v^2 = 800 + 100 t^2 - 200 t$$
 ...(i)
Magnitude of velocity of projectile of motion is
 $v^2 = u^2 + 100 t^2 - 2gtu \sin \theta$...(ii)
Comparing (i) and (ii)
 $u = 20\sqrt{2}$ m/s and $\theta = 45^\circ$

6. B. D

Sol.
$$\begin{split} Id\vec{\ell} &= IRd\theta \Big[sin\theta \hat{i} + cos\theta \hat{j} \Big] \\ r &= R(1 + cos\theta) \hat{i} - R sin\theta \hat{j} \\ |\vec{r}| &= R\sqrt{1 + cos^2\theta + 2cos\theta + sin^2\theta} \\ &= 2R cos \bigg(\frac{\theta}{2} \bigg) \\ Id\vec{\ell} \times \vec{r} &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ sin\theta & cos\theta & 0 \\ 1 + cos\theta & -sin\theta & 0 \end{vmatrix} IR^2 d\theta \\ &= IR^2 d\theta = \Big[-sin^2\theta - cos\theta - cos^2\theta \Big] \hat{k} \\ &= 2IR^2 cos^2 \bigg(\frac{\theta}{2} \bigg) (-\hat{k}) d\theta \end{split}$$



$$d\vec{B}_1 = \frac{\mu_0}{4\pi} \frac{Id\vec{\ell} \times \vec{r}}{|\vec{r}|^3} = \frac{\mu_0}{4\pi} \frac{2IR^2 \cos^2\left(\frac{\theta}{2}\right) d\theta}{8R^3 \cos^{3/2}\theta} (-\hat{k}) = \frac{\mu_0 I}{16\pi R} \sec\left(\frac{\theta}{2}\right) d\theta (-\hat{k})$$

$$\vec{B}_1 = \frac{\mu_0 I}{16\pi R} \int\limits_{-\pi/2}^{\pi/2} sec\bigg(\frac{\theta}{2}\bigg) (-\hat{k}) \, d\theta = \frac{\mu_0 I}{8\pi R} In \bigg[sec\bigg(\frac{\theta}{2}\bigg) + tan\bigg(\frac{\theta}{2}\bigg) \bigg]_{-\pi/2}^{\pi/2} \left(-\hat{k}\right)$$

$$= \frac{\mu_0 I}{8\pi R} \left\{ ln\left(\sqrt{2} + 1\right) - ln\left(\sqrt{2} - 1\right) \right\} \left(-\hat{k}\right) = \frac{\mu_0 I}{8\pi R} ln\left(\frac{\sqrt{2} + 1}{\sqrt{2} - 1}\right) (-\hat{k}) = \frac{\mu_0 I}{4\pi R} ln\left(\sqrt{2} + 1\right) (-\hat{k})$$

$$\vec{B}=4\vec{B}_1=\frac{\mu_0I}{\pi R}In\Big(\sqrt{2}+1\Big)(-\hat{k})$$

Second Method

$$dB = \frac{\mu_0 I d\ell \sin \left(90 - \frac{\theta}{2}\right)}{4\pi \left[2R\cos\left(\frac{\theta}{2}\right)\right]^2} = \frac{\mu_0 I}{16\pi R} \sec\left(\frac{\theta}{2}\right) d\theta$$

$$\vec{M} = (4R^2 + 2\pi R^2)I(+\hat{k}) = 2R^2I(2+\pi)(+\hat{k})$$

7. A, B, C, D

Sol. From the frame of ring

$$V_{P} \cos 37^{\circ} = 20$$

$$V_P = 25 \text{ m/s}$$

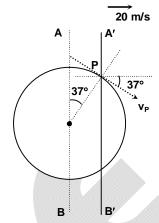
$$a_P \cos 37^\circ = a_R$$

$$a_P \sin 37^\circ = a_t$$

$$a_P = \frac{a_R}{\cos 30^\circ} = \frac{(20)^2 / 2}{4 / 5} = \frac{3125}{8} \text{ m/s}^2$$

$$a_P \sin 37^\circ = a_t$$





SECTION - B

$$4 \times 2.5 = 4 V_C + 4 V_1$$

$$\Rightarrow$$
 V_c + V₁ = 2.5 COAM

$$4 \times 2.5 \times \frac{1}{2} = 4 \times V_1 \times \frac{1}{2} + [2 \times 2 (\frac{1}{2})^2]\omega$$

$$\Rightarrow$$
 2.5 = V₁ + $\frac{\omega}{2}$

$$V_{sep} = e V_{app}$$

$$V_C + \omega \frac{1}{2} - V_1 = \frac{1}{2} \times 2.5$$

$$\Rightarrow$$
 $V_C + \frac{\omega}{2} = V_1 + \frac{2.5}{2}$

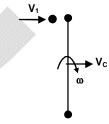
By solving equation, $\omega = 2.5 \text{ rad/s}$, $V_c = \frac{2.5}{2} \text{ m/s}$, $V_1 = \frac{2.5}{2} \text{ m/s}$

Loss of energy = $K_{e(i)} - K_{e(f)} = 3.12 J$

Sol.
$$e_{av} = \frac{\Delta \phi}{\Delta t} = \frac{2BA}{\Delta t}$$

$$\Rightarrow B = \frac{e_{av}\Delta t}{2A}$$

$$=\frac{20\times10^{-3}\times0.2}{2\times4\times10^{-4}}=5$$



Sol. For leaving the surface,
$$\cos\theta = 2/3$$

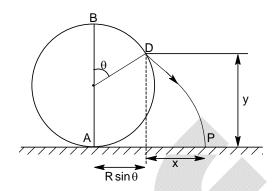
$$y = (v \sin \theta)t + \frac{1}{2} gt^2 = R(1 + \cos \theta)$$
 ... (1

and
$$x = (v \cos \theta)t$$
 ... (2)

and
$$v^2 = \frac{2}{3}gR$$
 ... (3)

On solving;

AP = R sin
$$\theta$$
 + x = $\frac{5}{27}(\sqrt{5} + 4\sqrt{2})R$



11.

Now,
$$Z_2 = R + \omega Li$$

$$Z_2 = 20 + 20i$$

The rms current through the inductor is

$$I_2 = \frac{80}{20\sqrt{2}} = 2\sqrt{2} A$$

$$I^2 = I_1^2 + I_2^2 + 2I_1I_2\cos\!\left(\frac{3\pi}{4}\right)$$

$$4 = I_1^2 + 8 + 2I_1 \times 2\sqrt{2} \Biggl(-\frac{1}{\sqrt{2}} \Biggr)$$

$$I_1^2 - 4I_1 + 4 = 0$$

$$\Rightarrow (I_1 - 2)^2 = 0 \Rightarrow I_1 = 2A$$

$$X_C = \frac{80}{l_1} = \frac{80}{2} = 40\Omega$$

$$X_C = 40 \Omega$$

$$X_C = 40 \ \Omega$$
$$\frac{1}{\omega C} = 40$$

$$C = \frac{1}{100 \times 40} = 250 \times 10^{-6} \text{ F}$$

$$C = 250 \, \mu F$$

$$\text{Sol.} \qquad \frac{4}{3}\pi R^3 \rho_{\scriptscriptstyle 1}, \frac{dv}{dt} + v \frac{d}{dt} \bigg(\frac{4}{3}\pi R^3 \rho_{\scriptscriptstyle 1} \bigg) = \frac{4}{3}\pi R^3 \rho_{\scriptscriptstyle 1} g \,.$$

$$R\frac{dv}{dt} + 3v\frac{dR}{dt} = Rg$$

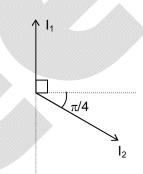
...(ii)

Also,
$$\pi R^2 v \rho_2 = \frac{dm}{dt}$$

$$v = \frac{4\rho_1}{\rho_2} \cdot \frac{dR}{dt}$$

$$\rho_2$$
 dt
After a long time when acceleration becomes constant $v = at$ will satisfy our differential equation.

$$v = at$$
 $v = \frac{4\rho_1}{\rho_2} \frac{dR}{dt}$



$$R = \frac{at^2 \rho_2}{8\rho_1}$$

From equation (i) and (ii)

$$\frac{at^{2}\rho_{2}a}{8\rho_{1}} + \frac{3\rho_{2}}{4\rho_{1}} (at)^{2} = \frac{at^{2}\rho_{2}g}{8\rho_{1}}$$

$$\frac{a}{8} + \frac{3a}{4} = \frac{g}{8}$$

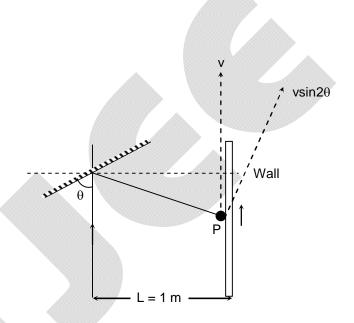
$$a = \frac{g}{7}$$

Sol.
$$\tan(2\theta - 90) = \frac{Y}{L}$$

$$y = -L \cot 2\theta$$

$$\frac{dy}{dt} = -L \times \left(-\cos ec^{2} 2\theta\right) \times 2\frac{d\theta}{dt}$$

$$= 2L\left(\cos ec^{2} 2\theta\right)\frac{d\theta}{dt}$$



SECTION - C

Sol. (for Q. 14-15).

In steady state photo current =
$$\frac{IAe}{hf} = \frac{V}{R}$$

Sol. Path difference =
$$\frac{\lambda}{2}$$

Here
$$\lambda = \frac{1}{2}m$$

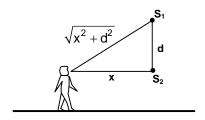
$$\sqrt{x^2 + d^2} - x = \frac{\lambda}{2}$$

$$(x^2 + d^2) = \left(x + \frac{\lambda}{2}\right)^2 = x^2 + \frac{\lambda^2}{4} + x\lambda$$

$$\therefore x = \frac{d^2}{\lambda} - \frac{\lambda}{4} = \frac{3^2}{1/2} - \frac{1/2}{4} = 17.875 \text{ m}$$



Sol. Total number of minima heard will be 6.



Chemistry

PART - II

SECTION - A

18. D

Sol. Na – Hg + H₂O
$$\longrightarrow$$
 NaOH + Hg + $\frac{1}{2}$ H₂

19. C

Sol.
$$\operatorname{Au} + 4\operatorname{HNO}_3 + 4\operatorname{Cl}^- \longrightarrow \left[\operatorname{AuCl}_4^-\right] + \operatorname{NO} + 2\operatorname{H}_2\operatorname{O}$$
$$\operatorname{3Pt} + 16\operatorname{H}^+ + 4\operatorname{HNO}_3^- + 18\operatorname{Cl}^- \longrightarrow \operatorname{3}\left[\operatorname{PtCl}_6\right]^{2^-} + 4\operatorname{NO} + 8\operatorname{H}_2\operatorname{O}$$

20. A

Sol. Concentration of $|H^+|$ at anode = 10^{-8} M

 \therefore concentration of $|H^+|$ at cathode = 10^{-7} M

because pH =
$$\frac{1}{2} [pkw + pka - pkb] = \frac{1}{2} [14 + 4.74 - 4.74] = 7.$$

so $|H^+| = 10^{-7} M$

$$E = 0 - \frac{0.059}{1} \log \frac{10^{-8}}{10^{-7}} = E = 0.059 \text{ V}$$

21. B

Sol.

$$Ph - C \longrightarrow Ph - N = C = O \xrightarrow{KOH} PhNH_2 + K_2CO_3$$

Intramolecular rearrangement takes place.

22. A, C, D

Sol. (A) T undergoes an ester hydrolysis in hot aqueous alkali as

- (B) LiAlH₄ reduces ester to alcohol as 'U' no chiral carbo, optically inactive
- (C) U on treatment with excess of acetic anhydride form a diester
- (D) U on treatment with CrO₃ / H⁺ undergo oxidation to diacid which gives effervescence with NaHCO₃

$$U + CrO_3 \xrightarrow{H^+} COOH \xrightarrow{NaHCO_3} CO_2 \uparrow$$

Sol. Compounds containing C,S & N gives blood red colour in Lassaigne's test

Sol. For NaA,
$$K_h = \frac{K_W}{K_a} = \frac{10^{-14}}{10^{-8}} = 10^{-6}$$

For NaB,
$$K_h = \frac{K_W}{K_a} = \frac{10^{-14}}{10^{-6}} = 10^{-8}$$

For NaC,
$$K_h = \frac{K_W}{K_a} = \frac{10^{-14}}{2 \times 10^{-8}} = \frac{10^{-6}}{2}$$

For NaD,
$$K_h = \frac{K_W}{K_a} = \frac{10^{-14}}{10^{-10}} = 10^{-4}$$

For NaE,
$$K_h = \frac{K_W}{K_a} = \frac{10^{-14}}{10^{-7}} = 10^{-7}$$

Since, K_h of NaD is the highest, therefore, NaD is most extensively hydrolysed.

For NaB,
$$pH = \frac{1}{2} (pK_W + pK_a + log C)$$

or pH =
$$\frac{1}{2} \left(14 + 6 + \log \frac{1}{10} \right) = \frac{1}{2} \left(20 - 1 \right) = \frac{1}{2} \times 19$$

or
$$pH = 9.5$$

For isohydric solution, $K_{a_1}C_1 = K_{a_2}C_2$

$$10^{-7} \times 0.1 = 10^{-6} \times 0.01 = 10^{-8}$$

Hence, 0.1 (M) HE is isohydric to 0.01 (M) HB solution.

SECTION - B

Sol. LiAlH₄ and Zn + NaOH / MeOH reduces nitrobenzene into azobenzene.

Sol.
$$r_n \propto n^2$$

But $r_n + 1 - r_n = r_n - 1$
 $(n+1)^2 - n^2 = (n-1)^2$
 $n = 4$

Sol.
$$\Delta E = \Delta H = \Delta T = q = P_{ext} = \Delta S_{surr} = 0$$

$$\Delta S_{sys} = \Delta S_{total} = +ve$$

$$\Delta G_{sys} = -Ve$$

Sol.
$$P_4 + 20HNO_3 \longrightarrow 4H_3PO_4 + 20NO_2 + 4H_2O_3$$

Sol.
$$i = 1.25$$

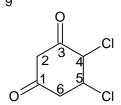
original mole fraction =
$$\frac{1}{n} = \frac{1}{1 + (n-1)}$$

Now
$$\frac{1.25}{1.25 + (n-1)} = \frac{1}{5}$$

$$6.25 = 1.25 + (n - 1)$$

n = 6

30. Sol.



SECTION - C

$$\frac{P_{_{A}}^{0}}{2}\!+\!\frac{P_{_{B}}^{0}}{2}\!=\!1\ \ \, \Longrightarrow P_{_{A}}^{0}+P_{_{B}}^{0}=2$$

$$\frac{P_A^0}{4} + \frac{3P_B^0}{4} > 1 \text{ atm} \quad P_A^0 + 3P_B^0 > 4 \text{ atm}$$

$$\text{and} \quad \frac{P_{A}^{0}}{8} + \frac{3P_{B}^{0}}{8} + \frac{4P_{C}^{0}}{8} = 1 \quad \Rightarrow P_{A}^{0} + 3P_{B}^{0} + 4P_{C}^{0} = 8 \text{ atm.}$$

$$\Rightarrow \quad P_A^0 + 3P_B^0 = (8-4\times0.8) \text{ atm} = 4.8 \text{ atm}.$$

Distance between nearest neighbour = $\frac{\sqrt{3}a}{2}$

Distance between next nearest neighbour = a.

Mathematics

PART - III

SECTION - A

Sol. Number of ways = Coefficient of
$$x^{30}$$
 in $[(x^{\circ} + x^{2} + x^{3}) + x^{4}(x + 1)]^{7} = 420$

$$\begin{split} \text{Sol.} & \text{ Let } S = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \left[\frac{mn}{3^n} \times \frac{n \cdot 3^m + m \cdot 3^n - n \cdot 3^m}{3^m \left(n \cdot 3^m + m \cdot 3^n \right)} \right] \\ & = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \left[\frac{m^2 n \cdot 3^n}{3^n \cdot 3^m \left(n \cdot 3^m + m \cdot 3^n \right)} \right] = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \left[\frac{m^2 n}{3^m \left(n \cdot 3^m + m \cdot 3^n \right)} \right] \end{split}$$

$$\begin{split} S &= \sum_{n=1}^{\infty} \sum_{m=1}^{\infty} \frac{n^2 m}{3^n \left(m \cdot 3^n + n \cdot 3^m \right)} \\ \Rightarrow & 2S = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{m n}{3^m \cdot 3^n} = \left(\sum_{m=1}^{\infty} \frac{m}{3^m} \right)^2 = \frac{9}{16} \\ \Rightarrow & S = \frac{9}{32} = \frac{p}{q} \Rightarrow q - 3p = 32 - 27 = 5 \end{split}$$

Sol. Sum of elements =
$$\sum_{r=0}^{3} \left(\frac{4\pi}{3} + 2r\pi \right) = \frac{52\pi}{3}$$

Sol. Put
$$e^{\frac{y^2}{x}} = t \Rightarrow y(y - x) = x \log_e(ce^y - 1)$$

Sol. Here,
$$\Delta'(x) = Ax + B$$

 $\Delta''(x) = A$
 $\Delta'''(x) = 0$

Sol.
$$p'(x) = \lambda[(x - \beta)^2 + \gamma^2 + 2(x - \alpha)(x - \beta)]$$

41. A, D
Sol.
$$A^4 - 7A^3 + 15A^2 - 9A = 0$$
 (Null matrix)
 $\Rightarrow B + C = 4A$

SECTION - B

111111, 888888 and numbers formed by (8, 8, 8, 1, 1, 1) are only the 6 digit numbers which are Sol. divisible by 21 \Rightarrow n₃ = 20, n₂ = 11, n₁ = 2

Sol.
$$\int \frac{(e^{x} - 1)\sin x - (e^{x} - 1 - x)\cos x}{1 + (e^{x} - 1 - x - \cos x)(e^{x} - 1 - x + \cos x)} dx$$

$$= \int \frac{(e^{x} - 1)\sin x - (e^{x} - 1 - x)\cos x}{\sin^{2} x + (e^{x} - 1 - x)^{2}} dx$$

$$= \int \frac{(e^{x} - 1)\sin x - (e^{x} - 1 - x)\cos x}{\sin^{2} x \left[1 + \left(\frac{e^{x} - 1 - x}{\sin x}\right)^{2}\right]} dx$$
Let
$$\frac{e^{x} - 1 - x}{\sin x} = t$$

$$I = tan^{-1} \left(\frac{e^{x} - 1 - x}{\sin x}\right) + c$$

- 44.
- Sol. Image of B in the crease always lies on line AD. Thus the parabola formed has the focus at B and directrix AD
- 45. 4
- Sol. Number of favourable cases = 7788
- 46. 5

Sol.
$$I = \int_{0}^{1} \frac{x^{15} - x^{11} + x^{7}}{\left(3x^{16} - 4x^{12} + 6x^{8}\right)^{\frac{3}{4}}} dx \implies I = \frac{1}{48} \int_{0}^{5} \frac{dt}{t^{\frac{3}{4}}} = \frac{5^{\frac{1}{4}}}{12}$$

- 47. 2
- Sol. Let $\cot^{-1}(2x-1) = \theta$; $0 < \theta < \pi$ $\Rightarrow \sin 2\theta = \frac{1+\cot \theta}{2} \Rightarrow \frac{2t}{1+t^2} = \frac{t+1}{2t} \Rightarrow t^3 3t^2 + t + 1 = 0$ $\Rightarrow t = 1, 1 \pm \sqrt{2} \text{ ; } t = 1 \sqrt{2} \text{ does not satisfy}$

$$\therefore x = 1, \frac{1}{\sqrt{2}}$$

SECTION - C

- 48. 12.00
- 49. 2.00
- Sol. (for Q. 48 to 49)

x + 2y + a = 0, 12x - 6y - 41 = 0 and radical axis of the given circles will be concurrent $\Rightarrow a = 2$

Now for required circle S = 0

$$x^2 + y^2 - 4 + \lambda(x + 2y + 2) = 0$$

(Equation of family of circles passing through the intersection points of x + 2y + a = 0 and $x^2 + y^2 = 4$)

Now, common chord with C_2 is $(\lambda + 4)x + 2(\lambda + 1)y + 2\lambda - 5 = 0$

Which is same as
$$12x - 6y - 41 = 0 \Rightarrow \lambda = -\frac{8}{5}$$

1.00 50.

51. 3.00

Sol. f(x + y + z) = f(x) f(y) f(z)

Putting y = z = -1

f(x-2) = f(x) f(-1) f(-1)

Putting x = 2

Futility x = 2 $f(0) = 4(f(-1))^2 \Rightarrow f(0)$ is positive Now, putting x = 0 = y = z $f(0) = f(0)^3 \Rightarrow f(0) = 1$ Again, putting y = 2 and z = 0 f(x + 2) = f(x) f(2) f(0)

 \Rightarrow f(x + 2) = 4f(x)

 \Rightarrow f'(x + 2) = 4f'(x)

 \Rightarrow f'(2) = 12