



# Sri Chaitanya IIT Academy., India.

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*A right Choice for the Real Aspirant*

ICON Central Office - Madhapur - Hyderabad

SEC: Sr.S60\_Elite, Target &amp; LIIT-BTs

JEE-MAIN

Date: 01-01-2025

Time: 09.00Am to 12.00Pm

GTM-12/07

Max. Marks: 300%

## KEY SHEET

### MATHEMATICS

1	3	2	1	3	1	4	3	5	4
6	2	7	3	8	1	9	4	10	1
11	1	12	2	13	2	14	1	15	2
16	1	17	2	18	3	19	4	20	4
21	42	22	75	23	34	24	75	25	8

### PHYSICS

26	2	27	1	28	1	29	2	30	2
31	4	32	3	33	2	34	2	35	2
36	1	37	4	38	4	39	3	40	1
41	3	42	2	43	3	44	4	45	2
46	5	47	1	48	1	49	2	50	2

### CHEMISTRY

51	3	52	3	53	1	54	3	55	3
56	4	57	2	58	3	59	4	60	2
61	2	62	1	63	4	64	2	65	3
66	1	67	1	68	2	69	4	70	4
71	4	72	4	73	4	74	4	75	4



## SOLUTION

## MATHEMATICS

1. Given that  $PQ = kI$

$$|P| \cdot |Q| = k^3 \Rightarrow |P| = 2k \neq 0 \Rightarrow P \text{ is an invertible matrix}$$

$$\therefore PQ = kI \quad \therefore Q = kP^{-1}I \quad \left[ \because P^{-1}P = I \right]$$

$$\therefore Q = \frac{\text{adj.}P}{2} \quad \therefore q_{23} = -\frac{k}{8}$$

$$\therefore -\frac{(3\alpha+4)}{2} = \frac{k}{8} \Rightarrow 12\alpha + 16 \dots (i)$$

$$\therefore |P| = 2k \Rightarrow k = 10 + 6\alpha$$

From (i) and (ii) we get  $\alpha = -1, k = 4 \therefore \alpha^2 + k^2 = 17$

2.  $\alpha$  is 7<sup>th</sup> root of unity  $\Rightarrow 1 + \alpha + \alpha^2 + \dots + \alpha^6 = 0, p + q = -1$

$$pq = \alpha^4 + \alpha^6 + \alpha^5 + \alpha^7 + \alpha^8 + \alpha^7 + \alpha^9 + \alpha^{10} = 3 + (\alpha + \alpha^2 + \alpha^3 + \dots + \alpha^6) = 3 + (-1) = 2$$

$$\Rightarrow x^2 + x + 2 = 0$$

Both I and II are true and II is the correct explanation.

- 3.

M	A	N	K	I	N	D
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$$\left( \frac{4 \times 6!}{2!} \right) + (5 \times 0) + \left( \frac{4 \times 3}{2!} \right) + (3 \times 2) + (2 \times 1) + (1 \times 1) + (0 \times 0) + = 1492$$

$$\Rightarrow 1440 + 36 + 12 + 4 = 1492$$

4. (A) No. of such triangles =  $10^6 C_1 + = 60$   
 (B) No. of such triangles = 10  
 (C) No. of such quadrilaterals =  $10^5 C_1 + = 75$   
 (D) No. of such quadrilaterals = 10 (when four consecutive points are taken)

5. Let  $p(E_1) = x, p(E_2) = y$  and  $p(E_3) = z$

$$\alpha = p(E_1 \cap \overline{E_2} \cap \overline{E_3}) = p(E_1) \cdot p(\overline{E_2}) \cdot p(\overline{E_3})$$

$$\Rightarrow \alpha = x(1-y)(1-z) \quad \dots (i)$$

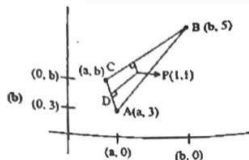
Similarly,

$$\beta = (1-x) \cdot y(1-z) \quad \dots (ii)$$

$$\gamma = (1-x)(1-y) \cdot z \quad \dots (iii)$$

$$p = (1-x)(1-y)(1-z) \quad \dots (iv) \text{ and solve equation.}$$

- 6.



slope of  $AC = \infty$

Slope of  $PD = 0$

$$D\left(\frac{a+a}{2}, \frac{b+3}{2}\right) = D\left(a, \frac{b+3}{2}\right)$$



$$\frac{b+3}{2} - 1 = 0, b+3-2=0 \Rightarrow b = -1$$

$$b = -1$$

$$E\left(\frac{b+a}{2}, \frac{5+b}{2}\right) = \left(\frac{a-1}{2}, 2\right)$$

$$\text{slope of } BC \times \text{slope of } EP = -1$$

$$\left(\frac{5-b}{b-a}\right) \times \left(\frac{2-1}{\frac{a-1}{2}-1}\right) = -1 \Rightarrow \left(\frac{6}{-1-a}\right) \times \left(\frac{2}{a-3}\right) = -1 \Rightarrow 12 = (1+a)(a-3)$$

$$\Rightarrow 12 = a^2 - 3a + a - 3 \Rightarrow a^2 - 2a - 15 = 0$$

$$a = -3 \text{ accept}$$

$$\text{Equation of AP } A(-3,3), P(1,1)$$

$$y-1 = \left(\frac{3-1}{-3-1}\right)(x-1) \Rightarrow x+2y=3$$

$$\text{Equation of } BC \ B(-1,5), C(-3,-1)$$

$$Y+1 = \left(\frac{5+1}{-1+3}\right)(x+3) = 3x+9 \quad 3x-y+8=0$$

$$Q \equiv \left(\frac{-13}{7}, \frac{17}{7}\right)$$

7. Given equation is

$$e^{4x} + 4e^{3x} - 58e^{2x} + 4e^x + 1 = 0$$

$$\text{Take, } f(x) = \left(e^{2x} + \frac{1}{e^{2x}} + 4\left(e^x + \frac{1}{e^x}\right) - 58\right)$$

$$\text{Let } e^x + \frac{1}{e^x} = p (> 0) \quad \dots(i)$$

$$p^2 + 4p - 60 = 0 \quad p = 6 \text{ or } -10$$

$$\text{Only } p = 6 \text{ is allowed } e^x + \frac{1}{e^x} = 6$$

Two real and distinct value of x

8. Since, given  $\ell_1 + \ell_2 = 20 \Rightarrow \frac{d\ell_2}{d\ell_1} = -1$

$$\text{Now, } A_1 = \left(\frac{\ell_1}{4}\right) \text{ and } A_2 = \pi \left(\frac{\ell_2}{2\pi}\right)^2$$

$$\text{Let } S = 2A_1 + 3A_2 = \frac{\ell_1^2}{8} + \frac{3\ell_2^2}{4\pi}$$

For max or min

$$\frac{ds}{d\ell_1} = 0 \Rightarrow \frac{2\ell_1}{8} + \frac{6\ell_2}{4\pi} \cdot \frac{d\ell_2}{d\ell_1} = 0 \Rightarrow \frac{\ell_1}{4} = \frac{6\ell_2}{4\pi} \Rightarrow \frac{\pi\ell_1}{\ell_2} = 6$$

9. Let  $f(x) = 4x^3 - 11x^2 + 8x - 5 \forall x \in R$



$$\Rightarrow f'(x) = 12x^2 - 22x + 8 \quad \text{and} \quad f'(x) > 0$$

10. Since, we know  $\overline{AB} + \overline{BC} + \overline{CA} = \overline{0} \Rightarrow \alpha = 2, \beta = 4, \gamma - \delta = 3$

$$\text{Now, } \frac{1}{2} |\overline{AB} \times \overline{AC}| = 5\sqrt{6}$$

$$(\delta - 9)^2 + (2\delta + 12)^2 + 100 = 600 \Rightarrow \delta = 5, \gamma = 8$$

$$\text{Hence, } \overline{CB} \cdot \overline{CA} = 60$$

11. Given points and direction ratios are shown below.

$$a_1 = (1, 2, 3), a_2 = (2, 4, 5), \vec{b}_1 = 2\hat{i} + 3\hat{j} + \lambda\hat{k}$$

$$\vec{b}_2 = \hat{i} + 4\hat{j} + 5\hat{k}$$

Apply shortest distance formula,

12.  $15 \sin^4 \alpha + 10(1 - \sin^2 \alpha)^2 = 6, 25 \sin^4 \alpha - 20 \sin^2 \alpha + 4 = 0$

$$\Rightarrow 25 \sin^4 \alpha - 10 \sin^2 \alpha - 10 \sin^2 \alpha + 4 = 0$$

$$\Rightarrow (5 \sin^2 \alpha - 2) = 0 \Rightarrow \sin^2 \alpha = \frac{2}{5}$$

13. For,  $S_1$  we have  $\Rightarrow \frac{(x+1)(x^2+3x+5)}{x^2-3x+2} \leq 0$

$$\Rightarrow x \in (-\infty, -2) \cup (1, 2)$$

For  $S_2$ , we have

$$3^x(3^x - 3) - 3^2(3^x - 3) \leq 0$$

$$\text{For } S_2, x \in [1, 2] \Rightarrow (-\infty, -2) \cup [1, 2]$$

14.  $\int \frac{x^2}{(x \sin x + \cos x)} dx \quad \because \frac{d}{dx}(\sin x + \cos x) = x \cos x$

$$\int \frac{x \cos x}{(x \sin x + \cos x)^2} \left( \frac{x}{\cos x} \right) dx = \frac{x}{\cos x} \left[ \frac{-1}{x \sin x + \cos x} \right]$$

Use by parts method

15. Area:  $\int_1^4 (2\sqrt{2}\sqrt{x} - \sqrt{2}x) dx$

16. Given,  $(1 + x^2) dy = y(x - y) dx$

$$\text{Where, } y(0) = 1, y(2\sqrt{2}) = \beta$$

$$dy = \left( \frac{yx - y^2}{1 + x^2} \right) dx$$



$$\frac{dy}{dx} + y \left( \frac{-x}{1+x^2} \right) = \left( \frac{-1}{1+x^2} \right) y^2, \text{ divide by } y^2 \text{ both sides and proceed}$$

17. First common term of both the series is 23 and common difference is  $7 \times 4 = 28$

$$\therefore \text{Last term} \leq 407 \Rightarrow 23 + (n-1) \times 28 \leq 407 \Rightarrow (n-1) \times 28 \leq 384$$

$$\Rightarrow n \leq \frac{384}{28} + 1 \Rightarrow n \leq 14.71$$

Hence, number of terms common are 14

18.  $N = (26 + a + b)$ ,  $f_i x_i = (504 + 3a + 9b)$

$$19. \sum_{i=1}^{50} X_i = \sum_{i=1}^{50} Y_i = T; \therefore n(X_i) = 10, n(Y_i) = 5$$

$$\text{So, } \sum_{i=1}^{50} X_i = 500, \sum_{i=1}^{50} Y_i = 5n \Rightarrow \frac{500}{20} = \frac{5n}{6} \Rightarrow n = 30$$

20. Given function is

$$\lim_{x \rightarrow 0} \frac{(5x + \dots) - \ln(1 + \alpha x)}{x} = 0$$

$$f(x) = \begin{cases} \frac{\ln(1 + 5x) - \ln(1 + \alpha x)}{x} & : x \neq 0 \\ 10 & : x = 0 \end{cases}$$

Applying expansion of  $\ln(1+x)$ .

$$\lim_{x \rightarrow 0} (5 - \alpha) = 10 \quad 5 - \alpha = 10 \Rightarrow \alpha = -5$$

21. Given matrix is  $A = \begin{pmatrix} \alpha & \beta & \gamma \\ \alpha^2 & \beta^2 & \gamma^2 \\ \beta + \gamma & \lambda + \alpha & \alpha + \beta \end{pmatrix}$

$$R_3 \rightarrow R_3 + R_1$$

$$\Rightarrow |A| = |\alpha + \beta + \gamma| \begin{vmatrix} \alpha & \beta & \gamma \\ \alpha^2 & \beta^2 & \gamma^2 \\ 1 & 1 & 1 \end{vmatrix}$$

$$\Rightarrow |A| = (\alpha + \beta + \gamma)(\alpha - \beta)(\beta - \gamma)(\gamma - \alpha) \therefore |adj A| = |A|^{n-1}$$

$$|adj(adj A)| = |A|^{(n-1)^2}$$

$$|adj(adj(adj(adj A)))| = |A|^{(n-1)^4} = |A|^{2^4} = |A|^{16} \therefore (\alpha + \beta + \gamma) = 2^{32} \cdot 3^{16}$$

22.  $0 \leq \frac{1-d}{4} \leq 1 \Rightarrow -3 \leq d \leq 1 \quad \dots(i)$

$$0 \leq \frac{1+2d}{4} \leq 1 \Rightarrow -\frac{1}{2} \leq d \leq \frac{3}{2} \quad \dots(ii)$$

$$0 \leq \frac{1-4d}{4} \leq 1 \Rightarrow -\frac{3}{4} \leq d \leq \frac{1}{4} \quad \dots(iii)$$

$$0 \leq \frac{1+3d}{4} \leq 1 \Rightarrow -\frac{1}{3} \leq d \leq 1 \quad \dots(iv)$$

From (i), (ii), (iii) and (iv)



$$-\frac{1}{3} \leq d \leq \frac{1}{4} \text{ minimum value of } d = -\frac{1}{3}$$

$$\text{Mean} = 0 + \frac{1+2d}{4} + \frac{2(1-4d)}{4} + \frac{3(1+3d)}{4}$$

$$X = \frac{6+3d}{4} = \frac{1}{4} \left( 6 - 3 \times \frac{1}{3} \right) = \frac{5}{4} \Rightarrow 60\bar{X} = 60 \times \frac{5}{4} = 75$$

23. It has infinitely many solutions.

24. we have  $x^2 + 4y^2 + 2x + 8y - \lambda = 0$

$$\Rightarrow \frac{(x+1)^2}{\lambda+5} + \frac{(y+1)^2}{\frac{\lambda+5}{4}} = 1 \quad \therefore \frac{2b^2}{a} = 4$$

$$\frac{2(\lambda+5)}{4} = 4(\sqrt{\lambda+5})$$

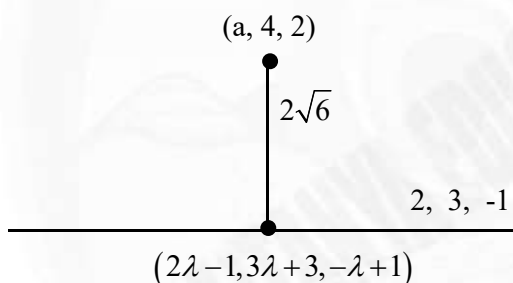
On solving  $\Rightarrow \lambda = 59$

$$\lambda = -5$$

$$1 = 2a = 2\sqrt{\lambda+5} = 2\sqrt{65} = 16$$

$$\Rightarrow \lambda + l = 59 + 16 + 75$$

25.



Given line  $\frac{X+1}{2} = \frac{Y-3}{3} = \frac{Z-1}{-1} = \lambda$

$$X = 2\lambda - 1, Y = 3\lambda + 3, Z = -\lambda + 1$$

$$(2\lambda - 1 - a)2 + (3\lambda - 1)3 + (-\lambda - 1)(-1) = 0$$

$$\Rightarrow 4\lambda - 2 - 2a + 9\lambda - 3 + \lambda + 1 = 0$$

$$14\lambda - 4 - 2a = 0 \Rightarrow 7\lambda - 2 - a = 0$$

$$\Rightarrow (5\lambda - 1)^2 + (3\lambda - 1)^2 + (\lambda - 1)^2 = 24$$

$$35\lambda^2 - 14\lambda - 21 = 0 \Rightarrow (\lambda - 1)(35\lambda + 21) = 0$$

For,  $\lambda = 1 \Rightarrow a = 5$

Let  $(\alpha_1, \alpha_2, \alpha_3)$  be reflection point P

$$\alpha_1 + 5 \quad \alpha_2 + 4 = 12 \quad \alpha_3 + 2 = 0$$

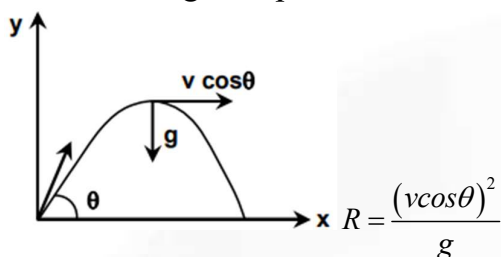
$$\alpha_1 = -3 \quad \alpha_2 = 8 \quad \alpha_3 = -2$$

$$a + \alpha_1 + \alpha_2 + \alpha_3 = 8$$

**PHYSICS**

26.  $M^1 L^{-3} T^0 = (M^1 L^1 T^{-2})^a (L T^{-1})^b T^c$   $a=1, b=-4, c=-2$

27. Rate of change of speed is minimum at highest point. Since at highest position.



28. Inside a closed Guassian surface  $Q_{enc} = 0$

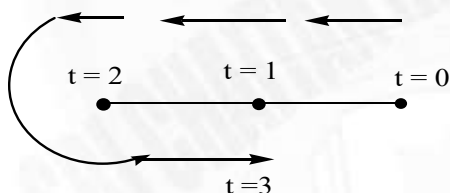
29. In 1D collisions formula for  $v_1 = \frac{m_1 - m_2}{m_1 + m_2} v_1 + \frac{2m_2}{m_1 + m_2} v_2$ , when  $m_1 \ll m_2, \vec{v}_1 = -\vec{u}_1 + 2\vec{u}_2$ .

30.  $\vec{E} \times \vec{B}$  gives direction of  $\vec{V}$

31. Time period becomes  $2\pi\sqrt{\frac{R}{g}}$  in statement 1. We can't neglect roundness of earth for pendulum of infinite length.

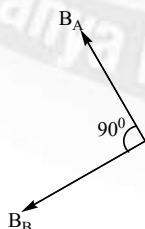
32.  $V_T = \frac{2}{9} \frac{r^2 g (\rho_B - \rho_l)}{\eta}$ ,  $Power = \vec{F} \cdot \vec{V}$

33.  $T = 4\text{sec}$ , Body starts at extreme position and ends at mean position as shown



34. For dropped body  $L - x = \frac{1}{2} g t^2$ , for pulse  $t = 2\sqrt{\frac{x}{g}}$ .  $x$  is the distance from bottom free end of row.

35. For infinitely long wire  $B = \frac{\mu_0 I_0}{2\pi r}$ ,  $r = a\sqrt{2}$ ,  $B_{Res} = \sqrt{2}B$



36. Above curie temperature ferro becomes para.

37. Distance between any two points when only increase.

38.  $V_{avg}$ ,  $V_{rms}$ ,  $V_{mp}$  will all exist at a particular temperature.



39. IN resonance  $V_L = V_C, V_{res} = V_R, Z = R$   $i_{Rms} = \frac{V_{Rms}}{Z}$
40.  $emf \in = A \frac{dB}{dt}, i = \frac{\in}{R}$ .
41.  $E_n = -13.6 \frac{Z^2}{n^2} eV, r_n = 0.529 \frac{n^2}{Z} A^0, V_n = 2.2 \times 10^6 \frac{Z}{n} m/s, T = \frac{2\pi r_n}{v_n}$ .
42.  $\frac{R_{Ge}}{R_{Be}} = \left(\frac{X}{9}\right)^{1/3}$   $X = 72$ , Number of neutron =  $72 - 32 = 40$
43. Zener current will be maximum, when  $V = 15V, 15 - (i \times 2.5k) = 5, i = 4 \text{ mA}, i_z = 3 \text{ mA}$
44. In uniform pure rolling, the linear velocity is constant. If no external force or torque is applied, the body will remain in a state of uniform pure rolling. In this case, the friction force is always zero, so there will not be any effect of the frictional force on the body.
45.  $\frac{I_{coherent}}{I_{incoherent}} = \frac{4I}{2I} = 2$
46.  $\frac{1}{2}mv_0^2 = \frac{1}{2}mv^2 + mgl(1 - \cos \theta)$   $T - mg \cos \theta = \frac{mv^2}{R}$ .
47.  $E = \frac{KQx}{(R^2 + x^2)^{3/2}}, \frac{dE}{dx} = 0$  is maximum  $x = \frac{R}{\sqrt{2}}$ .
48.  $\frac{E}{2} = E - ir, 2E = i(3+r), r = 1$ .
49.  $(1)\sin 90^\circ = \mu \sin 30^\circ$
50.  $I = \frac{ML^2}{3} \sin^2 \theta$ , angle is with vertical

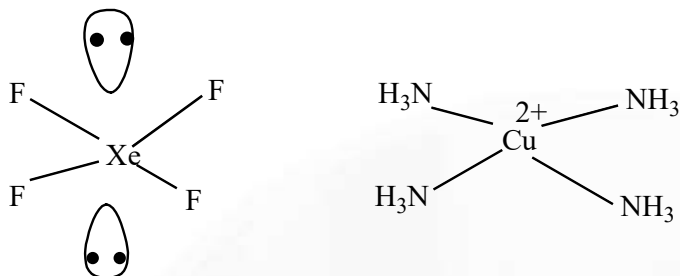




## CHEMISTRY

51. Stability of complex  $\propto$  chelation

52.



53. Statement 2 is the reason for statement 1

54. Oxidation power order :  $F_2 > Cl_2 > Br_2 > I_2$ 55. Energy  $\propto (n+l)$ 

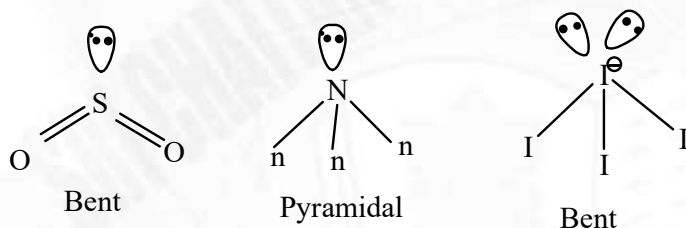
$$(n+l) \begin{bmatrix} e_3 > e_2 > e_4 > e_1 \\ 3+2 & 4+0 & 3+1 & 3+0 \\ 5 & 4 & 4 & 3 \end{bmatrix}$$

56.  $S_R + O_2 \longrightarrow SO_2 \Delta H, = -70960 \text{ Cal } \_\_\_\_\_\_ (i)$  $S_M + O_2 \longrightarrow SO_2 \Delta H, = -71030 \text{ Cal } \_\_\_\_\_\_ (ii)$ 

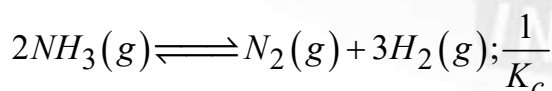
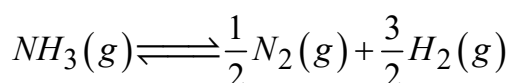
Subtracting eqn (II) from (i) we get ,

$$\Delta H = \Delta H_1 - \Delta H_2 = (-70960) - (-71030) = +70 \text{ Cal}$$

57.



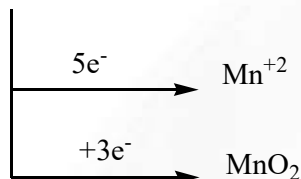
58. The correct statement for B is 5f electrons have much lower shielding effect as compared to 4f electrons because 5f- orbitals more diffused than 4f-orbitals

59. **Correct assertion** The bond enthalpies of the two O-H bonds in H-O-H are not equal.**Correct reason** This is because electronic environment around O is not same after breakage of one O-H bond.60.  $N_2(g) + 3H_2(g) \rightleftharpoons 2NH_3(g); K_c$ Multiplying by  $\frac{1}{2}$ , reaction becomes



$$\therefore \text{New } K_c = \left( \frac{1}{K_c} \right)^{\frac{1}{2}} = \left( \frac{1}{64} \right)^{\frac{1}{2}} = \frac{1}{8}$$

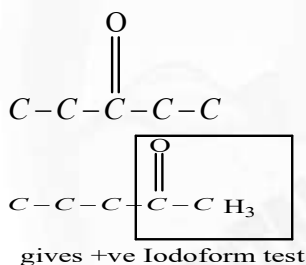
61. Both assertion and reason are true but reason is not correct explanation of assertion. Ammonium acetate is a salt of weak acid ( $\text{CH}_3\text{COOH}$ ) and weak base ( $\text{NH}_4\text{OH}$ ).
62.  $\text{C}_6\text{H}_{12}\text{O}_6$  (**GLUCOSE**) monosaccharide.
63. Ethanol and hexane forms positively deviated non-ideal solution.
64.  $\text{MnO}_4^- + e^- \longrightarrow \text{MnO}_4^{2-}$



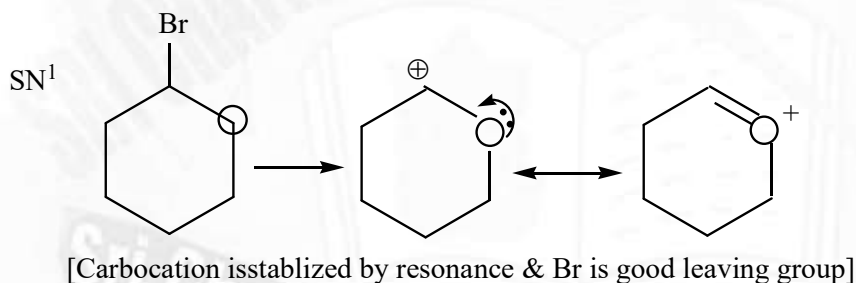
65.  $n_m = \frac{k \times 1000}{m}$

Specific conductance =  $\frac{1}{\text{specific resistance}} = \left( \frac{1}{x} \right) \quad n_m = \frac{1}{x} \times \frac{1000}{y}$

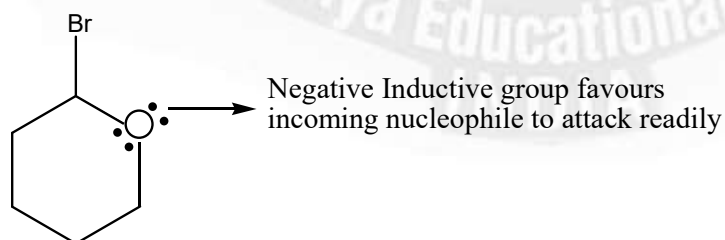
66.



67.



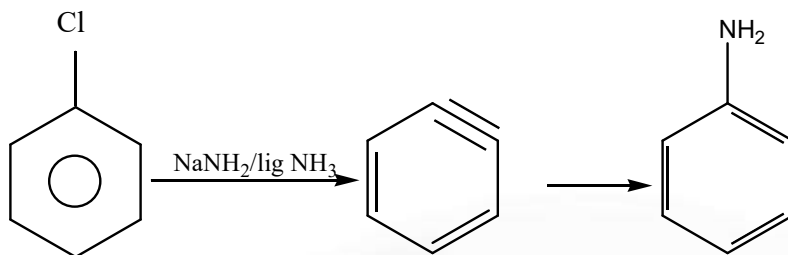
$\text{S}_{\text{N}}^2$



68. Compound (Y) is  $1^\circ$ -amine.
69. Basic strength  $\propto \frac{1}{\text{stability of Anion}}$



70.



71.

$$\frac{4mL}{M} = \left( \frac{\% (w/w) \times d \times 10}{\text{molar mass}} \right) = \frac{(29.2) \times 1.25 \times 10}{36.5} = 10M$$

According to dilution, eqn,  $M_i V_i = M_f V_f$ 

$$V_f = \frac{0.4 \times 100}{10} = 4mL$$

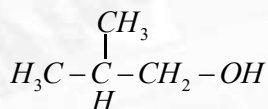
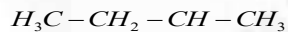
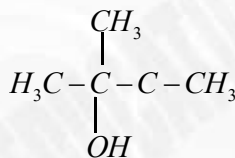
72.

$$\frac{16/3}{4/3} = 4$$

73.

(i),(ii),(iv),(vi)

74.

 $C_4H_{10}O$ 

75.

(i),(iii),(iv),(v)