



Sri Chaitanya IIT Academy.,India.

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A right Choice for the Real Aspirant

ICON Central Office - Madhapur - Hyderabad

SEC: Sr.S60_Elite, Target & LIIT-BTs

JEE-MAIN

Date: 17-01-2025

Time: 03.00Pm to 06.00Pm

GTM-18/13

Max. Marks: 300*

KEY SHEET

MATHEMATICS

1	3	2	3	3	2	4	4	5	2
6	2	7	2	8	2	9	3	10	2
11	2	12	2	13	4	14	3	15	3
16	2	17	4	18	3	19	3	20	4
21	400	22	4	23	54	24	9	25	11

PHYSICS

26	4	27	2	28	4	29	2	30	1
31	2	32	4	33	3	34	4	35	1
36	1	37	2	38	2	39	2	40	2
41	3	42	2	43	2	44	4	45	4
46	750	47	6	48	10	49	9	50	2

CHEMISTRY

51	3	52	2	53	1	54	3	55	2
56	2	57	3	58	3	59	2	60	1
61	3	62	4	63	3	64	1	65	3
66	4	67	1	68	1	69	4	70	1
71	25	72	3	73	3	74	4	75	15



SOLUTION

MATHEMATICS

1. 1^∞ form
2. $4_{C_3} \cdot 4_{C_3} + (4_{C_2} \cdot 3_{C_1})^2 + (4_{C_1} \cdot 3_{C_2})^2 + 3_{C_2} \cdot 3_{C_2}$
3. $\vec{r} \times \vec{a} = \vec{b} \times \vec{r}$
 $\vec{r} \times (\vec{a} + \vec{b}) = 0, \vec{r} = \lambda (\vec{a} + \vec{b}) = \lambda (3\hat{i} - 3\hat{j})$
 $|\vec{r}| = 1 \Rightarrow \lambda \sqrt{18} = 1, \quad \lambda = \frac{1}{3\sqrt{2}}, \vec{r} \cdot (\hat{i} + \hat{j} + \hat{k}) = 0$
4. $0 \leq x \leq 1 \Rightarrow 0 \leq \frac{1-x}{1+x} \leq 1$
5. Point of intersection is $(2, -4, 7)$ $k = 69$
6. $g(x) = f(x) + f(1-x)$
 $g^1(x) = f^1(x) - f^1(1-x), x = \frac{1}{2}, g^1\left(\frac{1}{2}\right) = f^1\left(\frac{1}{2}\right) - f^1\left(\frac{1}{2}\right) = 0, g^1\left(\frac{1}{2}\right) = 0$
 $g^{11}(x) = f^{11}(x) + f^{11}(1-x) > 0$
 Concave upwards, $\therefore \alpha = \frac{1}{2}$
7. $a_i \times b_i$ is a multiple of 3 if at least one of a_i or b_i is a multiple of 3
 If $a_i = 3$ then $b_i = 1, 2, 3, 4, 5, 6, 7$
 If $b_i = 3$ or 6 then $a_i = 1, 2, 3, 4$
 \therefore total possibilities $= 7 + 4 + 4 - 2 = 13$ \therefore probability $= \frac{13}{4C_1 \times 7C_1} = \frac{13}{28}$
8. $y^2 \leq 8x$
 $4x - 3y + 4 \leq 0$ Area of shaded portion is equal to
 $\frac{1}{n} \int_{1/2}^2 \sqrt{8x} - \text{area of trapezium ABCD}$
 $2\sqrt{2} \int_{1/2}^2 \sqrt{x} - \frac{9}{2} = 2\sqrt{2} \left[\frac{3}{2} x^{3/2} \right]_{1/2}^2 - \frac{9}{2}$
 $= \frac{4\sqrt{2}}{3} \left(2\sqrt{2} - \frac{1}{2\sqrt{2}} \right) - \frac{9}{2} = \frac{4\sqrt{2}}{3} \left(\frac{8-1}{2\sqrt{2}} \right) - \frac{9}{2} = \frac{14}{3} - \frac{9}{2} = \frac{28-27}{6} = \frac{1}{6}$
9. sub : $t = x + y$
10. X must have 1, 2 remaining 3 elements can be selected in $2.2.2 = 8$
11. Conceptual
12. $\int \left(\frac{x}{2} \sec^2 \frac{x}{2} + \tan \frac{x}{2} \right) dx, \quad \int (x f^1(x) + f(x)) dx = x f(x) + c$
13. Conceptual



14. $1 = \alpha \left(\frac{\sqrt{3}}{2} - \frac{i}{2} \right) + \beta(1+i)$ equate real and imaginary parts $\alpha - 2\beta = 0$

15. Conceptual

16. Term independent of x is ${}^8C_3 a^3 = 448$ coefficient of x^4 $x^4 = {}^8C_5 \cdot 2^5 = 1792$

$$f'(x) = 3x^2 + 2x f'(1) + f''(2)$$

17. I: $f''(x) = 6x + 2f'(1)$

$$f'''(x) = 6 \quad \text{then } f(0) = 6$$

II:

$$f(g(x)) = x \quad f'(x) = 3x^2 + 6x - 33, f'(g(x) \cdot g'(x)) = 1$$

$$g'(2) = \frac{1}{f'(g(25))} \quad g(2) = -1, = \frac{1}{f'(-1)} = \frac{1}{-36}, k = -36$$

18. $AB = I \quad T_r(C_r) = r + (r-1) = (2r-1)$

19. $x \neq 0, y \neq 0, z \neq 0$

$$\Delta = 0, a+b+c=1$$

20. $I = -I \Rightarrow 2I = 0 \quad I = 0$

21. Conceptual

22. Let $x_i - 10 = y_i$ for $i=1,2,3,4,5$

$$6y = \sqrt{\frac{25}{5} - \left(\frac{5}{5}\right)^2} = 2$$

$$\text{S.D} = 1 - 21.6y = 4$$

23. Foci of ellipse $= (1 \pm 3, 1 \pm 0) = (4, 1)(-2, 1)$

$$e_E = \sqrt{1 - \frac{16}{25}} = \frac{3}{5}, e_H = \frac{5}{3} = \sqrt{1 + \frac{b^2}{a^2}}, \frac{b^2}{a^2} = \frac{16}{9}$$

$$\text{And } 2al = 6 \Rightarrow ae = 3 \Rightarrow a^2 + b^2 = 9, a^2 \cdot \frac{25}{9} = 9, a^2 = \frac{81}{25} b^2 = \frac{144}{25}$$

$$\text{Hyperbola: } \frac{25x^2}{81} - \frac{25y^2}{144} = 1$$

$$\frac{2a}{e} = \frac{54}{25}$$

24. $f(x) = \left(3 \left(\frac{3-x^2}{3} \right) (3+x^2) \right)^{\frac{1}{4}}$

$$= (9-x^4)^{\frac{1}{4}}, f(f(x)) = \left(9 - \left((9-x^4)^{\frac{1}{4}} \right)^4 \right)^{\frac{1}{4}}$$

$$f(f(x)) = (x)$$

$$f^{2n+1}(x) = (9-x^4)^{\frac{1}{4}} \quad f^{2n}(x) = x$$

$$f^{2025}(\sqrt{2}) = 5^{\frac{1}{4}} \quad f^{2024}(\sqrt{2}) = \sqrt{2}$$

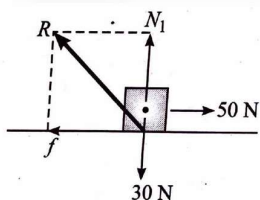
25. By using graph

**PHYSICS**

$$\begin{aligned}
 26. \quad U &= \frac{3}{2} PV \\
 &= \frac{3}{2} \times 3 \times 10^6 \times 2 \\
 &= 9 \times 10^6 \text{ J}
 \end{aligned}$$

$$\begin{aligned}
 27. \quad p_c &= p_0 - \frac{2S}{r_1}, p_D = p_0 - \frac{2S}{r_2} \\
 p_c + \rho g h_1 &= p_D + \rho g h_2 \\
 p_c - p_D &= \rho g (h_2 - h_1) \\
 h_2 - h_1 &= \frac{2S}{\rho g} \left(\frac{1}{r_2} - \frac{1}{r_1} \right) \\
 &= \frac{2S(r_1 - r_2)}{\rho g r_1 r_2}
 \end{aligned}$$

28.



$$\begin{aligned}
 N_1 &= 30 \text{ N} \\
 f &= \mu N_1 = 0.5 \times 30 = 15 \text{ N} \\
 \text{Contact surface} \\
 R &= \sqrt{N_1^2 + f^2} \\
 &= \sqrt{(30)^2 + (15)^2} \\
 &= 15\sqrt{5} \text{ N}
 \end{aligned}$$

$$\begin{aligned}
 29. \quad \frac{1}{\lambda} &\propto Z^2 \Rightarrow \lambda \propto \frac{1}{Z^2} \\
 \lambda_{He^+} : \lambda_{Li^{++}} : \lambda_{Be^{+++}} &= \frac{1}{2^2} : \frac{1}{3^2} : \frac{1}{4^2} \\
 &= 36 : 16 : 9
 \end{aligned}$$

$$\begin{aligned}
 30. \quad \vec{\tau} &= \vec{p} \times \vec{E} = (\alpha \hat{i} - \beta \hat{j}) \times (2\beta \hat{i} + 3\alpha \hat{j}) \\
 &= 3\alpha^2 \hat{k} + 2\beta^2 \hat{k} = (3\alpha^2 + 2\beta^2) \hat{k}
 \end{aligned}$$

$$31. \quad \vec{\tau} = \vec{M} \times \vec{B}$$

$$32. \quad [\text{Pressure}] = \left[\frac{\text{Force}}{\text{Area}} \right] = ML^{-1}T^{-2}$$

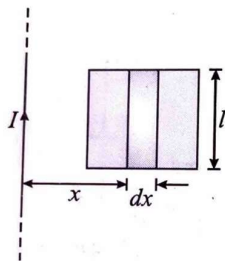
$$33. \quad K = K_0 \cos^2 \omega = \frac{K_0}{2} [1 + \cos 2\omega t]$$

For maximum value of $K = \cos 2\omega t = 1$



$$K_{\max} = K_0 = U_{\max} = E$$

34.



Magnetic fields due to long wire

$$B = \frac{\mu_0 I}{2\pi x}, dA = l dx$$

$$d\Phi = B dA$$

$$\Phi = \frac{\mu_0 I l}{2\pi} \int_a^{a+l} \frac{dx}{x}$$

$$= \frac{\mu_0 I l}{2\pi} \ln\left(1 + \frac{l}{a}\right) = MI$$

$$M = \frac{\mu_0 I l}{2\pi} \ln\left(1 + \frac{l}{a}\right)$$

35. Conceptual (gauss theorem)

$$36. R_{eq} = R_1 + R_2$$

$$R = \frac{l}{KA}$$

$$37. \vec{\tau} = \vec{r} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -1 & 1 \\ 7 & 3 & -5 \end{vmatrix}$$

$$= \hat{i}(5-3) - \hat{j}(-5-7) + \hat{k}(3+7) = 2\hat{i} + 12\hat{j} + 10\hat{k}$$

38. Planet's follow law of conservation of angular momentum

$$39. V = E - Ir$$

$$\text{When } I = 0, E = 2.0V$$

$$\text{When } I = 5A, 0 = 2 - 5r$$

$$r = 0.4\Omega$$

40. $\omega < \omega_0$ i.e. $X_C > X_L$, Current Leads $\omega > \omega_0$ i.e. $X_L > X_C$, Voltage Leads $\omega = \omega_0$ i.e. $X_L = X_C$, Same phase

$$\omega = \sqrt{2}\omega_0, \omega^2 = 2\omega_0^2 = \frac{2}{LC}, \omega L = \frac{2}{\omega C} \Rightarrow X_L = 2X_C.$$

41. First law of thermodynamics is based on law of conservation of energy and it can be written as $dQ = dU - dW$. Where dW is work done on the system.

$$42. \left(\frac{\Delta R}{R} \times 100\right)_{\max} = \frac{\Delta V}{V} \times 100 + \frac{\Delta I}{I} \times 100 \quad T^2 = \rho^a r^b \sigma^c, a=1, b=3, c=-1$$



43. $I = \frac{P}{A}$

44.



Energy loss will be maximum when collision will be perfectly elastic



(By momentum)

Maximum energy loss = $K_i - K_f$

$$= \frac{1}{2}mv^2 - \frac{1}{2}(m-M)v' = \frac{1}{2}mv^2 - \frac{1}{2}(m+M)\frac{m^2v^2}{(m+M)^2} = \frac{1}{2}mv^2 \left[1 - \frac{m}{3+M} \right] = \left(\frac{M}{m+M} \right) \frac{1}{2}mv^2$$

Statement 1 is false

45. work done on an object doesn't depend on the initial velocity of the object, Work done by a force is frame-dependent.

46. $n_1\lambda_1 = n_2\lambda_2$

47. $E = cB$

48. $x = 2t + 4t^2 \Rightarrow \frac{dx}{dt} = V_x = 2 + 8t \Rightarrow \frac{d^2x}{dt^2} = a_x = 8m/s^2$

$$\& y = 3t^2 \Rightarrow \frac{dy}{dt} = V_y = 6t \Rightarrow \frac{d^2y}{dt^2} = a_y = 6m/s^2$$

$$\therefore a = \sqrt{a_x^2 + a_y^2} = \sqrt{8^2 + 6^2} = 10m/s$$

49. $\frac{hc}{\lambda} = \phi + eV \dots\dots\dots(i)$

$$\frac{hc}{\lambda} = \phi + \frac{eV}{4} \dots\dots\dots(ii)$$

$$(i) - 4(ii) \Rightarrow -\frac{hc}{3\lambda} = -3\phi \Rightarrow \phi = \frac{hc}{9\lambda} = \frac{hc}{n\lambda}$$

$$n = 9$$

50. $y = 2\sin(100\pi t - 2\pi x)$

$$= A\sin(\omega t - kx)$$

$$\omega = 100\pi, k = 2\pi$$

$$\text{wave velocity } v = \frac{\omega}{k} = 50m/s$$

$$\mu = \frac{M}{L} = \frac{20 \times 10^{-3}}{50 \times 10^{-2}} = 0.04kg/m$$

$$v = \sqrt{\frac{T}{\mu}}$$

$$T = \mu v^2 = (0.04)(50)^2 = 100N = 50\lambda$$

$$\lambda = 2$$



CHEMISTRY

51. Key: 3

Sol: Bhore's model did not consider wave nature of electron.

52. Key: 2

Sol:

$$E_{cell} = E_{cell}^0 - \frac{0.0591}{2} \log \frac{[Zn^{2+}]}{[Cu^{2+}]}$$

$$1.1591 = 1.1 - \left(\frac{0.0591}{2} \right) \log(10^{-2})$$

53. Aldol condensation

54. Key: 3

Reaction is second order with respect to A and zero order with respect to B

55. Key: 2

i) BF_3 – trigonal planar – $\mu = 0$

ii) SO_3 – trigonal planar – $\mu = 0$

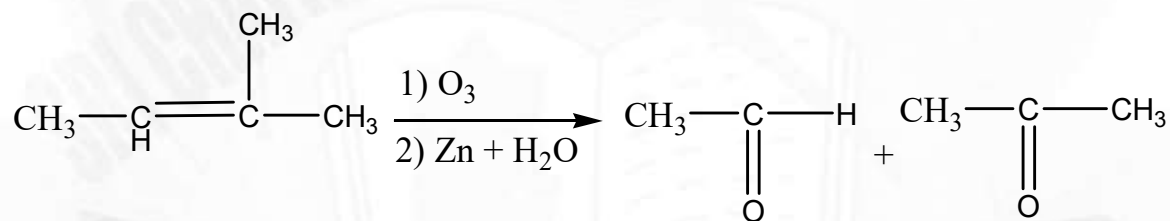
iii) CCl_4 – tetrahedral – $\mu = 0$

iv) H_2O – bent – $\mu \neq 0$

56. Key: 2

$$W = 0.5 \times 20 = 10 \text{ atm.ltr}$$

57.



58. KEY:3

$$K_c' = \sqrt{\frac{1}{K_c}} = 12.5.$$

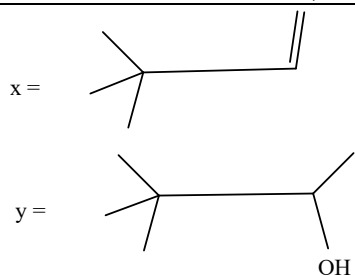
59. Key: 2

Sol: Greater the stability of conjugate base, more will be acidic strength

Equivalent resonance structures give more stability

60. Key: 1

Sol:



61. KEY: 3

Sol: For ideal behaviour

$$P_{total} = 0.25 \times 512 + 0.75 \times 344$$

$$= 386 \text{ mm Hg} < 600 \text{ mm Hg}$$

Hence, the solution shows positive deviation

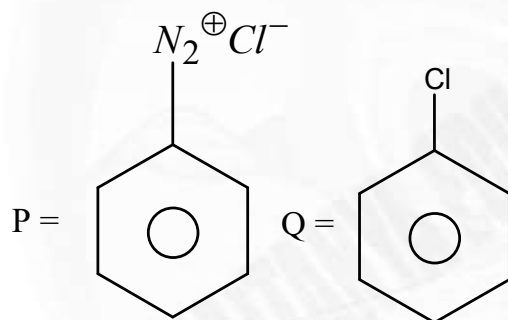
$$\Rightarrow \Delta H_{mix} = \text{positive}$$

62. Key: 4

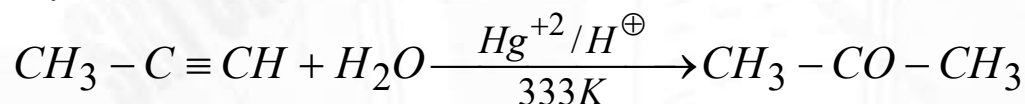
Sol: acetic acid is less acid than benzoic acid.

63. Key: 3

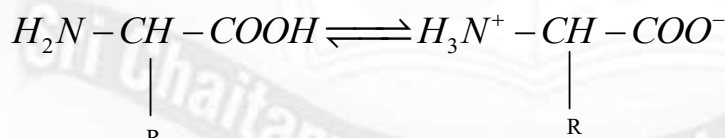
Sol:



64. Key: 1



65. Key: 3



Sol:

66. KEY: 4

$$\Delta H = [435 + 240] - [2 \times 430] = -185$$

67. KEY: 1

68. Key: 1

(i) $\text{Cl}_2 > \text{Br}_2 > \text{F}_2 > \text{I}_2$: BDE(ii) $(\text{H} - \text{O}) > (\text{H} - \text{S}) > (\text{H} - \text{Se})$: BDE(iii) $(\text{H} - \text{F}) > (\text{H} - \text{Cl}) > (\text{H} - \text{Br})$: BDE



(iv) $(N - H) > (P - H) > (As - H)$: BDE

69. Key: 4

$$\text{Sol: } [Al^{3+}]^1 [OH^-]^3 = 3 \times 10^{-34}$$

$$[OH^-] = 10^{-11}$$

\therefore minimum pH required to precipitate

$Al(OH)_3$ is 3

$$[Mg^{2+}][OH^-]^2 = 3 \times 10^{-12}$$

$$[OH^-] = 10^{-6}$$

\therefore Minimum pH required to precipitate

$Mg(OH)_2$ is 8

70. Key: 1

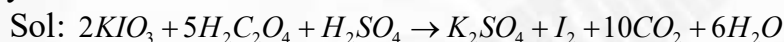
(i) In group 14, the stability of +2 oxidation state increases down the group due to inert pair effect

(ii) Stable oxidation state of Thallium is +1 due to inert pair effect

71. Key: 25

In first row of transition series, highest O.S is +7. (exhibited by Mn, Z= 25)

72. Key: 3



73. Key : 3

$$\text{Sol: (i) } [Co(NH_3)_6]^{3+} : d^6; d^2sp^3; \text{dia} : t_{2g}^6 e_g^0$$

$$\text{(ii) } [CoF_6]^{3-} : d^6; sp^3d^2; \text{para (4 unpaired electrons): } t_{2g}^4 e_g^2$$

$$\text{(iii) } [Cu(NH_3)_4]^{2+} : d^9 : \text{para : square planar : (one unpaired electron)}$$

$$\text{(iv) } [Zn(OH_2)_6]^{2+} : d^{10} : \text{dia : } sp^3d^2 : t_{2g}^6 e_g^4$$

$$\text{(v) } [Cr(CN)_6]^{3-} : d^3 : \text{Para : } d^2sp^3 : t_{2g}^3 e_g^0 \text{ (three unpaired electrons)}$$

74. II, III, IV, VIII gives tollen's test

75. KEY: 15

$$\text{Sol: Equivalent weight of metal} = 15 \text{ g.eq}^{-1}$$