

FIITJEE

ALL INDIA TEST SERIES

PART TEST – II

JEE (Main)-2025

TEST DATE: 01-12-2024

ANSWERS, HINTS & SOLUTIONS

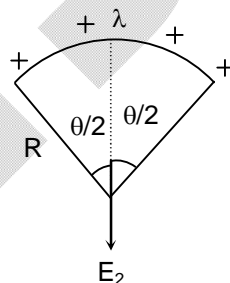
Physics

PART – A

SECTION – A

1. B
Sol. Use principle of superposition,

$$E_2 = \left(\frac{2K\lambda}{R} \right) \sin\left(\frac{\theta}{2}\right) \\ = \frac{2K\lambda}{R} \times \frac{1}{2} \hat{i} = \frac{K\lambda}{R} \hat{i}$$



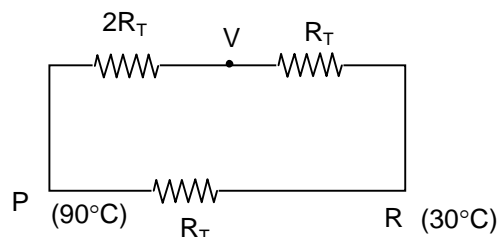
2. C
Sol. $dq = (2\pi x dx) \sigma$

$$di = \frac{dq}{dt} = \frac{2\pi x \sigma dx \times \omega}{2\pi} = \omega \sigma x dx$$

$$dB = \frac{\mu_0}{4\pi} \times \frac{2(\omega \sigma \pi x^3 dx)}{(y^2 + x^2)^{3/2}}$$

$$B = \frac{\mu_0 \sigma \omega}{2} \left(\frac{r^2 + 2y^2}{\sqrt{r^2 + y^2}} - 2y \right)$$

3. D
Sol. Equivalent circuit is



4. C
Sol. by solving

$$Q = KA \frac{dT}{dx} \Rightarrow \frac{Q}{A} \int_0^x dx = K_0 \int_0^T (1+T) dT$$

$$\Rightarrow \frac{Q}{A} x = K_0 \left(T + \frac{T^2}{2} \right)_0^T$$

By solving

$$\frac{Q}{A} x = K_0 \left(T + \frac{T^2}{2} \right)$$

$$\text{So, } \frac{Q}{A} x_0 = K_0 \left(300 + \frac{(300)^2}{2} \right)$$

So, at $x = 2x_0$ temperature $T \approx 425 \text{ K}$

5. B
Sol. $P = VI$

6. B
Sol. Let x be the temperature of block. In steady state

$$\frac{x-10}{R} + \frac{x-5}{R} + \frac{x-3}{R} = 0 \Rightarrow x = 6^\circ\text{C}$$

7. C

Sol. Now, $\frac{n_1(4)}{n_2(32)} = \frac{1}{4} \Rightarrow n_1 = 2n_2$

$$\text{Now, } C_v = \frac{n_1 \left(\frac{3}{2} R \right) + n_2 \left(\frac{5}{2} R \right)}{n_1 + n_2} = \frac{11}{6} R$$

$$C_p = C_v + R = \frac{17}{11} R$$

$$\therefore \gamma = \frac{C_p}{C_v} = \frac{17}{11} = 1 + \frac{6}{11}$$

8. D

Sol. $\frac{d\phi}{dt} = B \cdot \frac{\omega R^2}{2}$

Where, $\frac{\omega R^2}{2}$ is area swept in unit time perpendicular to the magnetic field.

9. D

Sol. The voltage across the resistor R is equal to the voltage across the coil

$$U_R = U_L$$

Voltage across the resistor

$$U_R = I_R \cdot R$$

Voltage across the inductor coil:

$$U_L = L \frac{dI_L}{dt}$$

Current through a resistor

$$I_R = \frac{dq_R}{dt}$$

Then

$$\frac{dq_R}{dt} R = L \frac{dI_L}{dt} \leftrightarrow R dq_R = L dI_L$$

According to Kirchhoff's second law

$$\varepsilon = I_{NCT} + I_R \cdot R$$

Then the current through the resistor at the moment of opening

$$I_R = \frac{\varepsilon - \frac{\varepsilon}{(2R)r}}{3r} = \frac{\varepsilon}{6r}$$

Then the current through the coil from Kirchhoff's first law:

$$I_L = I_{NCT} - I_R = \frac{\varepsilon}{2r} - \frac{\varepsilon}{6r} = \frac{\varepsilon}{3r}$$

We sum (integrate) (1)

$$R \int_0^{q_R} dq_R = L \int_0^{I_L} dI_L \Rightarrow R q_R = L I_L$$

Taking into account (2)

$$q_R = \frac{L}{R} \frac{\varepsilon}{3r} = \frac{\varepsilon L}{9r^2}$$

10. D

Sol. $i = \frac{2}{10}$

$$V_{BD} = 6 \left(\frac{2}{10} \right) = \frac{12}{10} = 1.2 \text{ V}$$

11. C

Sol. $\frac{X}{R_0} = \frac{40}{60} \Rightarrow R' = 6\Omega$

$$\text{and } 6 = \frac{78R_1}{R_t + 78} \Rightarrow R_t = 6.5 \Omega$$

$$\alpha = \frac{R_t - R_0}{R_0 t} = 8.3 \times 10^{-4} \text{ K}^{-1}$$

12. B

Sol. $R = 37 \times 10^2 \pm 5\%$
 $= (3700 \pm 185) \Omega$

13. D

Sol. Potential difference A and C = 4V

$$\text{Current in above circuit} = \frac{6}{5+1} = 1 \text{ A}$$

So, resistance of AD = 4Ω

Hence length = 80 cm

14. C

$$\text{Sol. } V_C = \frac{1}{4\pi\epsilon_0} \left[\frac{q}{R} - \frac{q}{2R} + \frac{q}{3R} \right] = \frac{1}{4\pi\epsilon_0} \left(\frac{5q}{6R} \right)$$

15. C

$$\text{Sol. } \frac{1}{R} = \frac{1}{20} + \frac{1}{20} + \frac{1}{30} + \frac{1}{30}$$

16. A

$$\text{Sol. } \vec{E}_q + \vec{E}_{8q} = \vec{0}$$

$$\Rightarrow \frac{Kqx}{(R^2 + x^2)^{3/2}} = \frac{K(8q)x}{(16R^2 + x^2)^{3/2}}$$

$$\Rightarrow x = 2R$$

$$\therefore \frac{1}{2}mv^2 = -\frac{Kq \times q}{\sqrt{(R^2 + x^2)}} + \frac{K(8q) \times q}{\sqrt{(16R^2 + x^2)}}$$

$$v = 20 \text{ m/s}$$

17. A

$$\text{Sol. } E_x = \frac{3}{\sqrt{\pi\epsilon_0}}, E_y = \frac{4}{\sqrt{\pi\epsilon_0}}$$

$$\therefore E_{\text{net}} = \frac{5}{\sqrt{\pi\epsilon_0}}$$

$$\therefore U = \frac{1}{2}\epsilon_0 E^2 \left(\frac{4}{3}\pi R^3 \right) = 0.45 \text{ J}$$

18. A

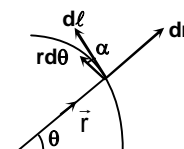
$$\text{Sol. } dB = \frac{\mu_0}{4\pi} \frac{id\ell \sin(90^\circ + \alpha)}{r^2}$$

$$dB = \frac{\mu_0 i}{4\pi r^2} d\ell \cos \alpha$$

$$dB = \frac{\mu_0 i}{4\pi r^2} r d\theta = \frac{\mu_0 i d\theta}{4\pi r}$$

$$dB = \frac{\mu_0 i d\theta}{4\pi \left(b + \frac{c}{\pi} \theta \right)}$$

$$\Rightarrow \int_0^B dB = \int_0^{\pi/2} \frac{\mu_0 i_0 d\theta}{4\pi \left(b + \frac{c}{\pi} \theta \right)} = \frac{\mu_0 i_0}{4c} \ln \left(1 + \frac{c}{2b} \right)$$

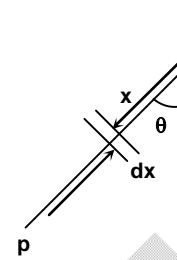


19. C

Sol. $d\varepsilon = B\omega \sin^2 \theta \int_0^\ell x dx$

$$\varepsilon = \int d\varepsilon = (B\omega \sin^2 \theta) \frac{\ell^2}{2}$$

$$= 4 \times 1 \times \frac{1}{2} \times \frac{1}{2} = 1$$



20. A

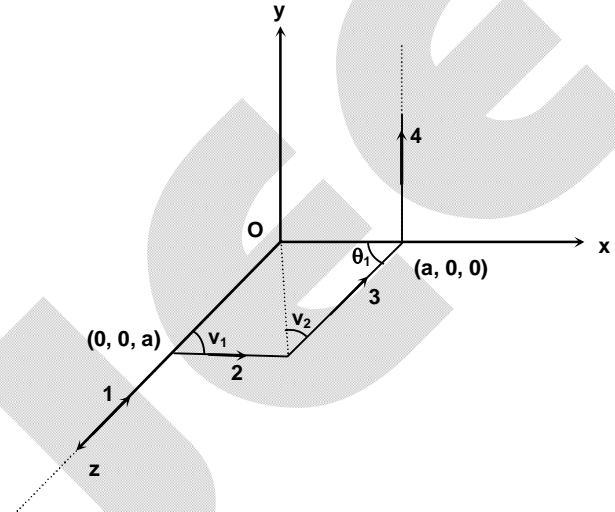
Sol. $\vec{B} = \vec{B}_1 + \vec{B}_2 + \vec{B}_3 + \vec{B}_4$

$$\vec{B}_2 = \vec{B}_3 = \frac{\mu_0 i}{4\pi a} (\cos \theta_1 + \cos \theta_2) \hat{j}$$

$$\vec{B}_2 = \vec{B}_3 = \frac{\mu_0 i}{4\sqrt{2}\pi a} \hat{j}$$

$$\vec{B}_4 = \frac{\mu_0 i}{4\pi a} \hat{k}$$

$$\Rightarrow \vec{B} = \frac{\mu_0 i}{4\pi a} (\sqrt{2}\hat{j} + \hat{k})$$



SECTION - B

21. 2

Sol. Let us consider a cube of double side length of same density. Also, $V \propto \frac{Q}{r}$ and V becomes 4 times on doubling the side length. Let the potential at center due to $\frac{1}{8}$ of this cube is V_1 . This point lies at corner of each of eight cubes of original size.

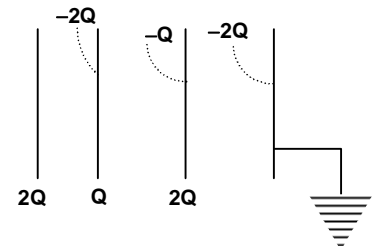
22. 8

Sol. Potential of plate 4 is zero

$$\Rightarrow (V_3 - V_4) = V_3$$

$$(V_3 - V_4) = \left(\frac{2Q}{A\epsilon_0} \right) 2d = 4 \left(\frac{Qd}{A\epsilon_0} \right)$$

$$V_3 = 8 \text{ volt}$$



23. 4

Sol. $H = i^2 R t$

$$200 = 2^2 \times R \times 1$$

$$\Rightarrow 200 = 4R$$

$$H_2 = 1^2 \times R \times 8 = 400 \text{ Joule}$$

24. 3

Sol. $B = \frac{\mu_0 J}{2} + \frac{\mu_0 J}{2} = \mu_0 J$

$$U = \frac{B^2}{2\mu_0} \times 6L^3 = 3\mu_0 J^2 L^3$$

25. 9

Sol. Hint: According to stefan's law, the power radiated by a black body at absolute temperature T is given by

$$\theta = \sigma A T^4 \quad \dots(i)$$

According to wein's displacement law

$$\lambda_m T = b \Rightarrow T = \frac{b}{\lambda_m}$$

From (1) and (2)

$$\theta = \sigma A \left(\frac{b}{\lambda_m} \right)^4 = \frac{\sigma A b^4}{\lambda_m^4}$$

For a sphere of radius r, $A = 4\pi r^2$

$$\text{Hence } \theta = \frac{\sigma b^4 4\pi r^2}{\lambda_m^4} = K \frac{r^2}{\lambda_m^4}$$

Where $K = 4\pi\sigma b^4$ is a constant.

$$\text{Hence } \theta_1 = K \frac{r_1^2}{(\lambda_m^4)_1}$$

$$\theta_2 = K \frac{r_2^2}{(\lambda_m^4)_2}$$

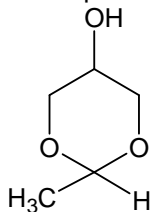
$$\frac{\theta_1}{\theta_2} = \left(\frac{r_1}{r_2} \right)^2 \cdot (\lambda_m^4)_2 = \left(\frac{3}{5} \right)^2 \times \left(\frac{500}{300} \right)^4 = (\lambda_m^4)_1 = \left(\frac{5}{3} \right)^2$$

Chemistry

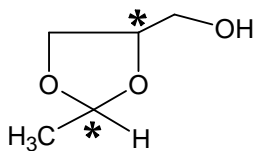
PART – B

SECTION – A

26. B
Sol. Possible products

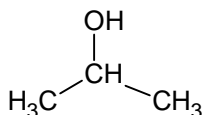


Plane of symmetry
(Optically inactive)



Two chiral centres
(4-isomers)

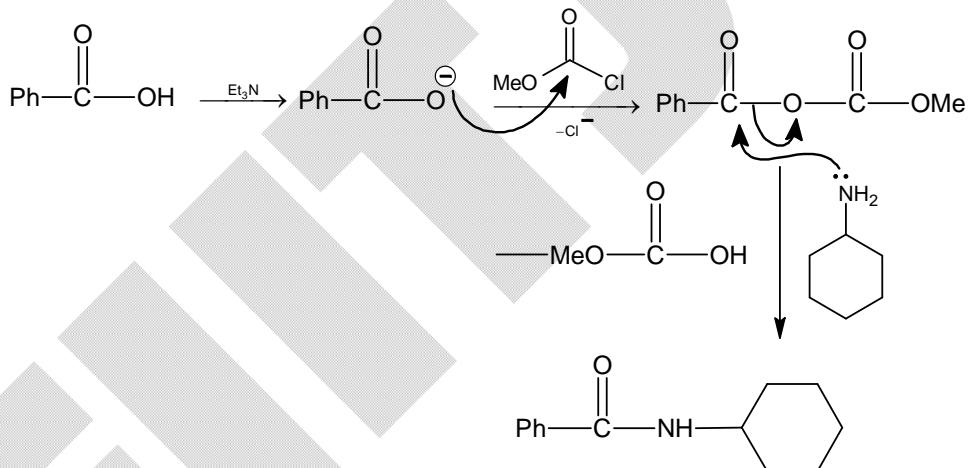
27. C
Sol.



Q
(2° alcohol)

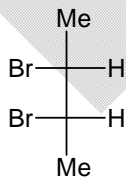
It gives yellow ppt. of CHI_3 with $\text{I}_2 + \text{NaOH}$.

28. C
Sol.

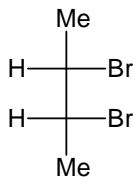


29. A
Sol. Factual

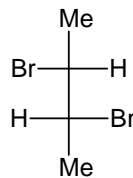
30. D
Sol.



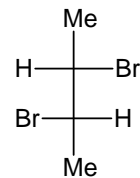
(i)



(ii)



(iii)

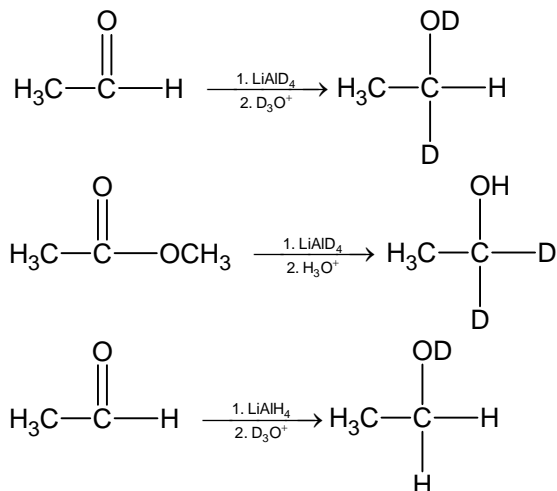


(iv)

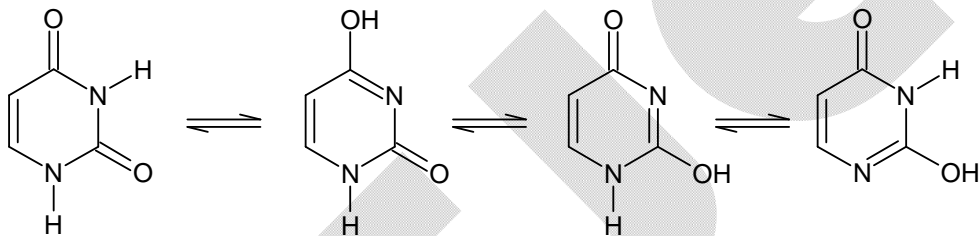
(iii) and (iv) are non-superimposable mirror image.

31. A
Sol. Factual

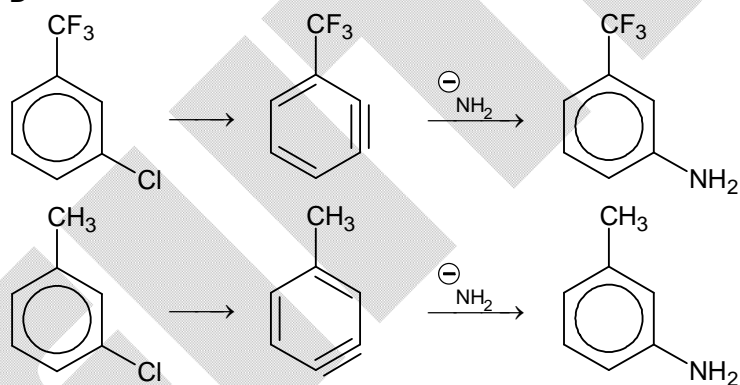
32. B
Sol.



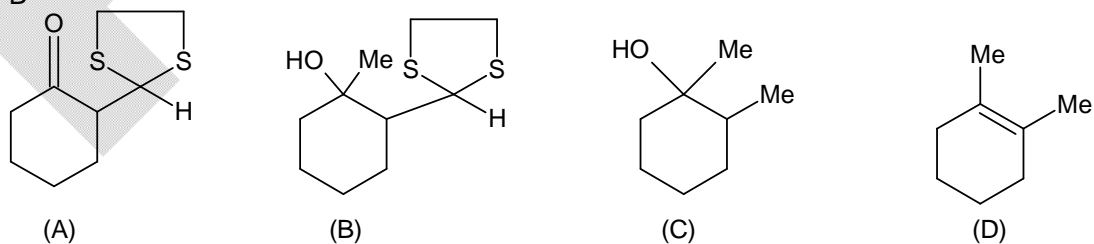
33. C
Sol.

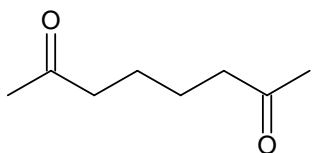


34. D
Sol.

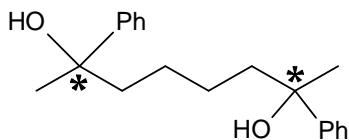


35. B
Sol.





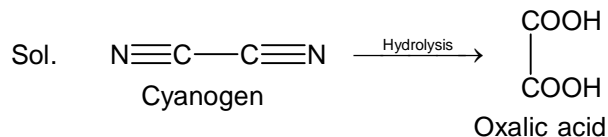
(E)



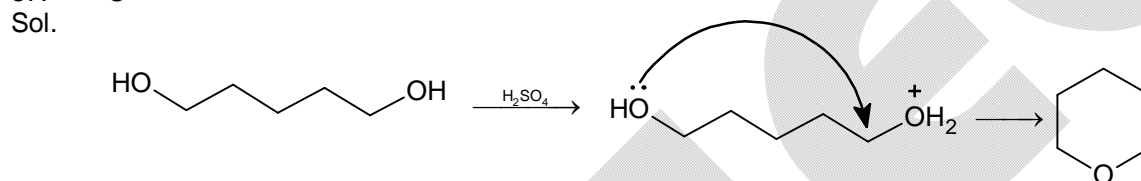
(F)

Symmetrical (3-isomers)

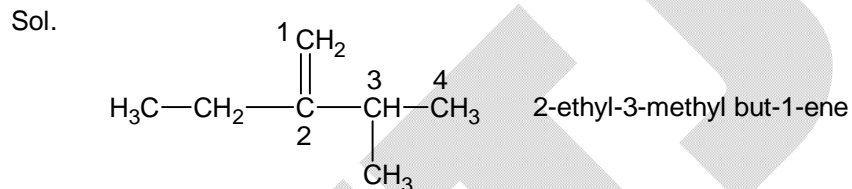
36. C



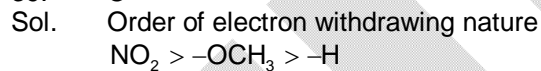
37. C



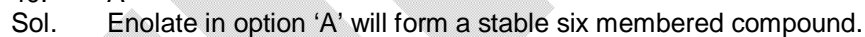
38. D



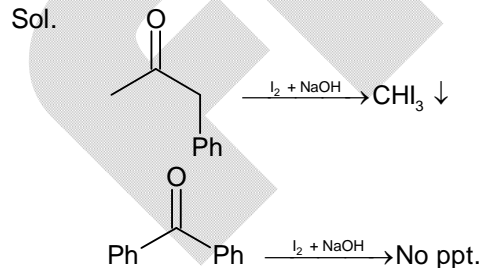
39. C



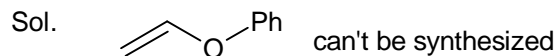
40. A



41. C

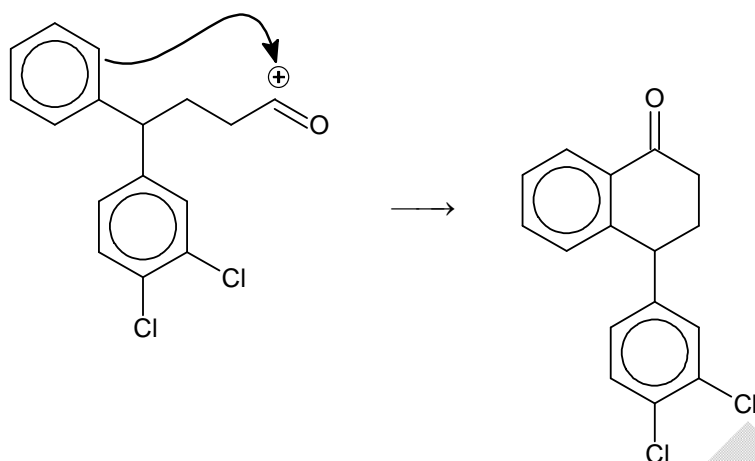


42. B

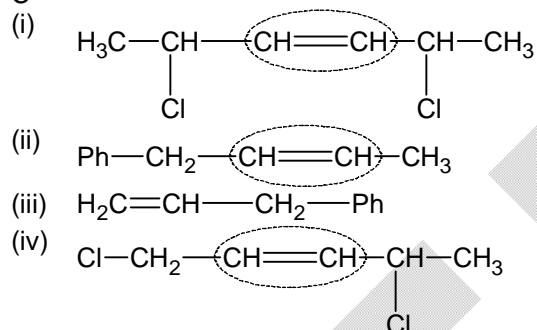


43.
Sol.

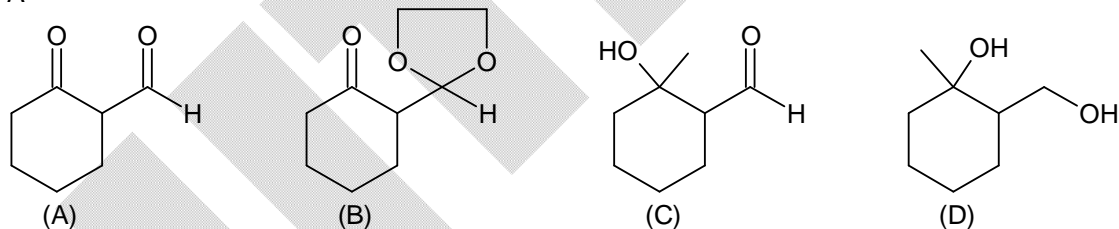
C


 44.
Sol.

C


 45.
Sol.

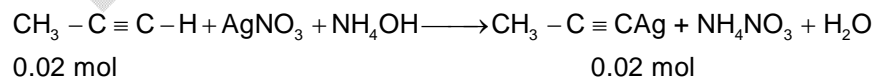
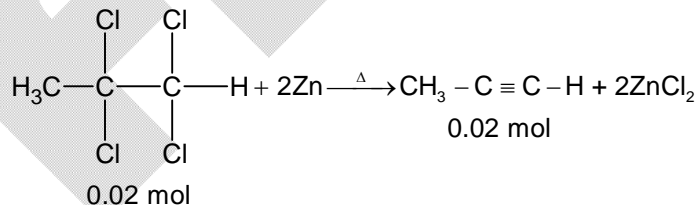
A



SECTION – B

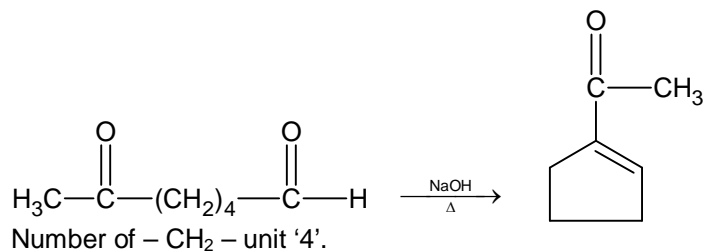
 46.
Sol.

3


 Moles of $\text{CH}_3-\text{C}\equiv\text{CAg} = 0.02$

 Mass of $\text{CH}_3-\text{C}\equiv\text{CAg} = 0.02 \times 147 = 2.94 \approx 3 \text{ g}$

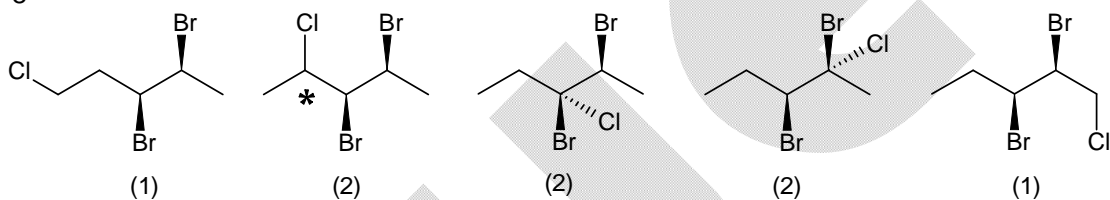
47. 4
Sol.



48. 20
Sol. Number of H-bond between A and T are 2.
Number of H-bond between G and C are 3.
The complimentary strand is "TATACGCG"
Total H-bond = $4 \times 2 + 4 \times 3 = 20$

49. 4
Sol. Copolymers are Bakelite, Buna-S, Melamine, Terylene.

50. 8
Sol.



Mathematics

PART – C

SECTION – A

51. D

Sol. $x_1^2 + (x_2 + 1)^2 = 0$
 $x_1 = 0, x_2 = -1$
 $(y_1 + 1)^2 + (y_2 + 1)^2 = 0$
 $y_1 = -1, y_2 = -1$

52. A

Sol. Since $B_i C_i$ is parallel to $B_0 C_0$ triangles $AB_i C_i$ are similar to $\Delta AB_0 C_0$. So area of $\Delta AB_i C_i$ is $\left(\frac{41-i}{41}\right)^2$ of the area $\frac{1}{41-i}$ of the area of $\Delta AB_i C_i$. So the area of $\Delta B_i C_i C_{i+1}$ is $\frac{1}{41-i} \left(\frac{41-i}{41}\right)^2 = \frac{41-i}{41^2}$.

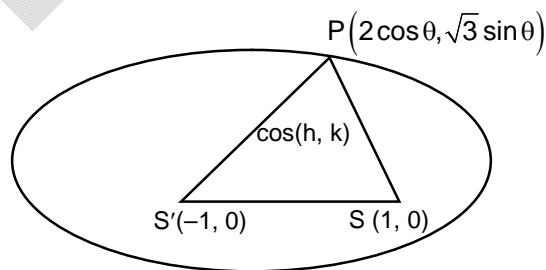
The sum of all triangles $\Delta B_i C_i C_{i+1}$ is then $\sum_{i=1}^{41} \frac{i}{41^2} = \frac{41 \times 42}{2} = \frac{21}{41}$. The height of $\Delta AB_0 C_0$ is

$$\sqrt{41^2 - 9^2} = 40, \text{ so its area is } \frac{1}{2} \times 40 \times 18 = 360.$$

$$\text{Hence total area } \frac{21}{41} \times 360 = \frac{7560}{41}.$$

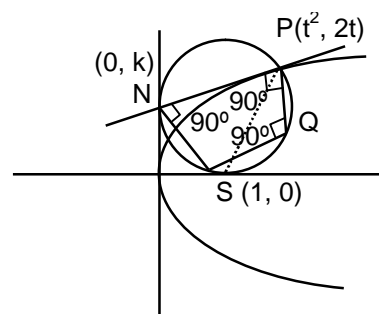
53. D

Sol. $\frac{x^2}{4} + \frac{y^2}{3} = 1$
 $\therefore 3h = 2\cos\theta, 3k = \sqrt{3}\sin\theta$
 $\frac{x^2}{4} + \frac{y^2}{1/3} = 1.$
 $\frac{9}{9}$



54. C

Sol. $yt = x + t^2$
 $l_{PQ} = l_{SN} = \sqrt{1+t^2} = \sqrt{10}$
 $\Rightarrow t = 3, -3.$



55.

B

Sol.

$$y^2 = 8x \Rightarrow y^3 = -8 \Rightarrow y = -2, x = \frac{1}{2}$$

equation of tangent is $y + 2 = -2(x - \frac{1}{2})$
 y intercept = -1
 $y' = \cos(x + y)(1 + y')$
 $-2 = \cos(x + y)(-1)$
 $\cos(x + y) = 2$ not possible.

56.

C

Sol.

$$x^2 + y^2 - 25 + \lambda y = 0$$

$$\left| \frac{0 + \frac{\lambda}{2} + c}{\sqrt{1 + 2}} \right| = \sqrt{\frac{\lambda^2}{4} + 25}$$

$$\Rightarrow \lambda^2 - 2\lambda c + 150 - 2c^2 = 0$$

 λ_1 and λ_2 are the roots of equation

$$2\left(0 + \frac{\lambda_1 \lambda_2}{4}\right) = -50, \lambda_1 \lambda_2 = -100$$

$$\Rightarrow 2c^2 = 250 \Rightarrow c^2 = 125 \Rightarrow c = 5\sqrt{5} \Rightarrow [c] = 11.$$

57.

D

Sol.

$$x^2 + y^2 = 8$$

$$x(3\cos\theta) + y(3\sin\theta) = 8$$

... (i)

$$\text{Also, } hx + ky = h^2 + k^2$$

... (ii)

$$\frac{3\cos\theta}{h} = \frac{3\sin\theta}{k} = \frac{8}{h^2 + k^2}$$

$$\Rightarrow \cos\theta = \frac{8h}{3(h^2 + k^2)}, \sin\theta = \frac{8k}{3(h^2 + k^2)}$$

$$\text{Locus is } S: x^2 + y^2 = \left(\frac{8}{3}\right)^2$$

The given line must pass through centre of circle

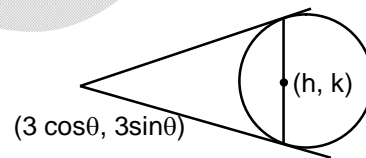
$$\therefore c = 2$$

 $hx + ky = 1$ touches the ellipse

$$\therefore \frac{1}{k^2} = \frac{h^2}{k^2} + 8$$

$$\text{The locus is } x^2 + 8y^2 = 1$$

Eccentricity of conjugates hyperbola 3.



58.

A

Sol. The equation of tangent at (x_1, y_1) is $\frac{xx_1}{a^2} - \frac{yy_1}{b^2} = 1$ It passes through $(0, -b)$, so

$$0 + \frac{y_1}{b} = 1 \Rightarrow y_1 = b$$

$$\text{Normal at } (x_1, y_1) \text{ is } \frac{a^2 x}{x_1} + \frac{b^2 y}{y_1} = a^2 e^2$$

It passes through $(2\sqrt{2}a, 0)$ so

$$x_1 = \frac{2\sqrt{2}a}{e^2}$$

Now x_1, y_1 lies on hyperbola

$$\therefore \frac{8a^2}{e^4 a^2} - \frac{b^2}{b^2} = 1$$

$$\Rightarrow e^4 = 4, \Rightarrow e^2 = 2.$$

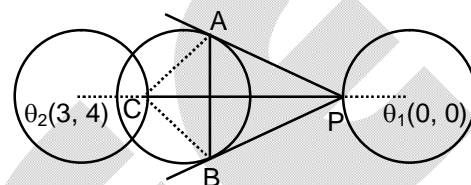
59.

C
Sol. Quadrilateral PACB is cyclic and PC will be the diameter of any circle passing through any of given 4 points.

\therefore diameter will be PC

Locus of C is $(x-3)^2 + (y-4)^2 = 1$

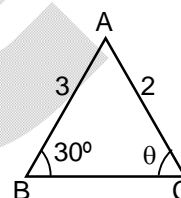
Minimum distance $O_1O_2 - r_1 - r_2 = 3$.



60.

B
Sol. By using cosine formula we get,

$$a^2 - 3\sqrt{3}a + 5 = 0 \Rightarrow \frac{a_2}{a_1} = \frac{17 + 3\sqrt{21}}{10}$$



61.

D
Sol. Let the variable line be $lx + my + n = 0$

$$P_1 = \frac{\frac{3a\alpha_1}{a+b+c} + \frac{3m\beta_1}{a+b+c} + n}{\sqrt{l^2 + m^2}}$$

$$P_2 = \frac{\frac{3b\alpha_2}{a+b+c} + \frac{3m\beta_2}{a+b+c} + n}{\sqrt{l^2 + m^2}}$$

$$P_3 = \frac{\frac{3c\alpha_3}{a+b+c} + \frac{3m\beta_3}{a+b+c} + n}{\sqrt{l^2 + m^2}}$$

$$P_1 + P_2 + P_3 = 0$$

$$\Rightarrow \frac{3l(a\alpha_1 + b\alpha_2 + c\alpha_3)}{a+b+c} + \frac{3m(a\beta_1 + b\beta_2 + c\beta_3)}{a+b+c} + 3n = 0$$

62.

B
Sol. Let $\sqrt{768} = 32\cos\theta$

$$16\sqrt{3} = 32\cos\theta$$

$$\cos\theta = \frac{\sqrt{3}}{2} \Rightarrow \theta = \frac{\pi}{6}$$

$$\sqrt{4 + \sqrt{8 - \sqrt{32 + 32\cos\frac{\pi}{6}}}}$$

$$\begin{aligned}
 &= \sqrt{4 + \sqrt{8 - 8 \cos \frac{\pi}{12}}} \\
 &= \sqrt{4 + 4 \sin \frac{\pi}{24}} \\
 &= \sqrt{4 + 4 \cos \frac{11\pi}{24}} \\
 &= 2\sqrt{2} \cos \frac{11\pi}{48} \therefore \frac{b}{a} = 24
 \end{aligned}$$

63. D

Sol. The tangent $3x + 4y - 25 = 0$ is tangent at vertex and axis is $4x - 3y = 0$
 so PS = a = 5
 L.R = 20

64. D

Sol. $m^3 + (2p + 5)m^2 - 6m - 2p = 0$
 $m_1 + m_2 + m_3 = -(2p + 5)$
 $\Sigma m_1 m_2 = -6$
 $m_1 m_2 m_3 = 2p$
 For A

$$P + \sum_{i=1}^3 m_i = -1$$

$$\Rightarrow P - 2P - 5 = -1 \Rightarrow P = -4$$

$$\Rightarrow m_1 m_2 m_3 = -8$$

$$\Rightarrow m_1 = 1, m_2 = -2, m_3 = 4$$

For B

$$\Rightarrow P - 2P - 5 = -5 \Rightarrow P = 0$$

$$\Rightarrow m_1 m_2 m_3 = 0$$

$$\Rightarrow m_1 = 1, m_2 = 0, m_3 = -6$$

For D

$$P + 2P = 32 \text{ not possible.}$$

65. A

Sol. $2x^2 + 2xy + 3y^2 - \left(\frac{3x+6y}{P}\right)^2 = 0$
 $\Rightarrow 2P^2 - 9 + 3P^2 - 36 \Rightarrow P^2 = 9$

66. B

Sol. $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$

Tangent at $P(a \sec \theta, b \tan \theta)$

$$\frac{x \sec \theta}{a} - \frac{y \tan \theta}{b} = 1$$

$$y = \pm \frac{b}{a} x$$

$$M = [a(\sec \theta - \tan \theta), -b(\sec \theta - \tan \theta)]$$

$$N = [a(\sec \theta + \tan \theta), b(\sec \theta + \tan \theta)]$$

$$\Rightarrow ON = \sqrt{a^2 + b^2} (\sec \theta + \tan \theta) = ae(\sec \theta + \tan \theta) \text{ and } OM = ae(\sec \theta - \tan \theta)$$

$$\Rightarrow OM + ON = 2ae \sec \theta$$

$$SP + S'P = e \left(a \sec \theta - \frac{a}{e} \right) + e \left(a \sec \theta + \frac{a}{e} \right) = 2ae \sec \theta$$

67. C

Sol. Orthocentre lies on the rectangular hyperbola and

$$\begin{array}{c} \text{---} \xrightarrow{2} \bullet \xrightarrow{1} \bullet \text{---} \\ H(\alpha, \beta) \qquad G(h, k) \qquad O(3x_1, 3y_1) \end{array}$$

$$\therefore h = \frac{2 \times 3x_1 \times \alpha}{3}, k = \frac{2 \times 3y_1 \times \beta}{3}$$

$$\alpha = 3h - 6x_1, \beta = 3k - 6y_1$$

$$9(h - 2x_1)^2 - 9(k - 2y_1)^2 = 36 \therefore \lambda = 4$$

68. C

 Sol. $l_1 l_2 = 2$ and $t_1 + t_2 + t_3 = 0$ and $a = 2$

 Let the circumcentre be (h, k)

$$h = \frac{at_1 t_2 + at_3^2}{2} \Rightarrow h = 2 + t_3^2$$

$$k = \frac{a(t_1 + t_2) + 2at_3}{2} \Rightarrow k = t_3$$

$$\therefore h = 2 + k^2$$

$$y^2 = x - 2$$

69. D

Sol. Let A be the vertex

$$AR = \sqrt{a^2 t_2^4 + 4a^2 t_2^2} = |at_2| \sqrt{t_2^2 + 4}$$

$$a = 1$$

$$|t_2| = \left| -t_1 - \frac{2}{t_1} \right| \geq 2\sqrt{2}$$

$$AR \geq 4\sqrt{6}$$

70. B

 Sol. $\triangle ATC$ is isosceles, BHFC is cyclic
 $\angle BFH = \angle BHC$. Then $\triangle TBF \sim \triangle THC$
 Since $\triangle TBF$ is isosceles, so $\triangle THC$

$$\text{Area} = \frac{1}{2} \times 10 \times \sqrt{63} = 15\sqrt{7}$$

SECTION - B

71. 0

 Sol. Let $\theta = \frac{\pi}{28}$

$$\frac{\cos 2\theta}{\sin 3\theta} + \frac{\cos 6\theta}{\sin 9\theta} + \frac{\cos 18\theta}{\sin 27\theta}$$

$$= \frac{1}{2} \left[\frac{2\cos 2\theta \cdot \sin \theta}{\sin \theta \cdot \sin \theta} + \frac{2\cos 6\theta \cdot \sin 3\theta}{\sin 9\theta \cdot \sin 3\theta} + \frac{2\cos 18\theta \cdot \sin 9\theta}{\sin 27\theta \cdot \sin 9\theta} \right]$$

$$= \frac{1}{2} \left[\frac{\sin 3\theta - \sin \theta}{\sin \theta \cdot \sin \theta} + \frac{\sin 9\theta - \sin 3\theta}{\sin 9\theta \cdot \sin 3\theta} + \frac{\sin 27\theta - \sin 9\theta}{\sin 27\theta \cdot \sin 9\theta} \right]$$

$$= \frac{1}{2} [\operatorname{cosec} \theta - \operatorname{cosec} 3\theta + \operatorname{cosec} 3\theta - \operatorname{cosec} 9\theta + \operatorname{cosec} 9\theta - \operatorname{cosec} 27\theta]$$

$$= \frac{1}{2} [\operatorname{cosec} \theta - \operatorname{cosec} 27\theta] = 0$$

72. 2

Sol. $\frac{\sin x}{\sin y} = \frac{1}{2} \Rightarrow \frac{\sin x + \sin y}{\sin x - \sin y} = \frac{3}{-1}$

$$\Rightarrow \frac{2 \sin\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right)}{2 \cos\left(\frac{x+y}{2}\right) \sin\left(\frac{x-y}{2}\right)} = -3$$

$$\frac{\cos x}{\cos y} = \frac{3}{2}$$

$$\Rightarrow \frac{\cos x + \cos y}{\cos x - \cos y} = \frac{3+2}{3-2}$$

$$\Rightarrow \frac{2 \cos\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right)}{2 \sin\left(\frac{x+y}{2}\right) \sin\left(\frac{x-y}{2}\right)} = -5$$

$$\Rightarrow \tan^2\left(\frac{x+y}{2}\right) = \frac{3}{5}$$

$$k = 2$$

73. 2

Sol. $m^2 \sin^2 \theta - 2m \tan \theta + \tan^2 \theta + \cos^2 \theta = 0$

$$m_1 + m_2 = \frac{2 \tan \theta}{\sin^2 \theta}$$

$$m_1 m_2 = \frac{\tan^2 \theta + \cos^2 \theta}{\sin^2 \theta}$$

$$m_1 - m_2 = \sqrt{(m_1 + m_2)^2 - 4m_1 m_2}$$

$$= \sqrt{\frac{4 \tan^2 \theta}{\sin^4 \theta} - \frac{4 \tan^2 \theta + 4 \cos^2 \theta}{\sin^2 \theta}}$$

$$= \frac{2}{\sin^2 \theta} \sqrt{\tan^2 \theta - (\tan^2 \theta + \cos^2 \theta) \sin^2 \theta} = 2$$

74. 1

Sol. $\frac{1}{\sin 1^\circ} \left[\frac{\sin(46^\circ - 45^\circ)}{\sin 45^\circ \sin 46^\circ} + \frac{\sin(48^\circ - 47^\circ)}{\sin 49^\circ \sin 48^\circ} + \frac{\sin(50^\circ - 49^\circ)}{\sin 49^\circ \sin 50^\circ} + \dots + \frac{\sin(134^\circ - 133^\circ)}{\sin 133^\circ \sin 134^\circ} \right]$

$$= \frac{1}{\sin 1^\circ} [\cot 45^\circ - \cot 46^\circ + \cot 47^\circ - \cot 48^\circ + \cot 49^\circ - \cot 50^\circ + \dots + \cot 133^\circ - \cot 134^\circ] = \frac{1}{\sin 1^\circ}$$

75. 0

Sol. Perpendicular distance = 2
 Now $\sec^2 \theta + 2 \operatorname{cosec}^2 \theta = 2$
 No value of θ is possible.