

FIITJEE

ALL INDIA TEST SERIES

CONCEPT RECAPITULATION TEST – IV

JEE (Main)-2025

TEST DATE: 21-03-2025

ANSWERS, HINTS & SOLUTIONS

Physics

PART – A

SECTION – A

1. C

Sol. For the sector, $y_{cm} = \frac{4R \sin(\phi/2)}{3\phi} = \frac{2R}{\pi} \left(\because \phi = \frac{\pi}{3} \right)$

For the arc, $y_{cm} = \frac{2R \sin(\phi/2)}{\phi} = \frac{3R}{\pi}$

2. A

Sol. If acceleration of block 2 is a_2 to the right, then

$$5a_2 = a_r + a = 6 + 4$$

$$\boxed{a_2 = 2 \text{ m/s}^2}$$

3. C

Sol. $\alpha = \frac{\tau}{I} = \frac{FL}{\frac{mL^2}{3}} = \frac{3F}{m\ell} \Rightarrow a_{cm} = \frac{\ell}{2} \alpha = \frac{3F}{2m}$

$$\Sigma F_x = ma_{cm}$$

$$N_x + F = \frac{3F}{2} \Rightarrow N_x = \frac{F}{2}$$

$$N_y = Mg$$

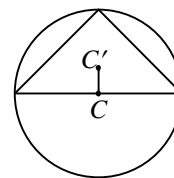
4. C

 Sol. C.M. of triangle is at $\frac{a}{3}$ from centre of circular plate

$$m_{\text{triangle}} = \frac{m_{\text{circle}}}{\pi}$$

$$y_{CM} = \frac{M_y - m_y}{M - m}$$

$$\text{On solving, } \frac{a}{3(\pi - 1)}$$



5. C

 Sol. $-\Delta U = \Delta K_e$

$$-[U_B - U_A] = \frac{1}{2}mv^2$$

Ball will leave when normal at B = 0

$$\therefore mg \sin \beta - N_B = \frac{mv_B^2}{R} \Rightarrow 0 \text{ at B} \Rightarrow mg \sin \beta = \frac{mv_B^2}{R}$$

6. D

 Sol. Block number 1 and $2n$ will suffer one collision each, block number 2 and $2n - 1$ will suffer two collision each similarly block number n and $n + 1$ will suffer n collision each. So total number of collisions will be $2(1 + 2 + \dots + n) = n(n + 1)$

7. A

$$\text{Sol. } r = R \left(\frac{\ell_1}{\ell_2} - 1 \right) = 132.4 \left(\frac{70}{60} - 1 \right) \approx 22.1 \Omega$$

8. B

 Sol. 100Ω , 25Ω and 20Ω are in parallel.

 Their, net resistance is 10Ω

$$\therefore R_{\text{net}} = 4 \Omega + 10 \Omega + 6 \Omega = 20 \Omega$$

$$V = i R_{\text{net}} = 80 \text{ V}$$

9. A

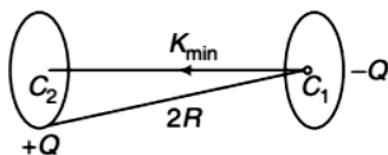
 Sol. Current decreases $\frac{20}{30}$ times or $\frac{2}{3}$ times. Therefore, net resistance should become $\frac{2}{3}$ times.

$$\therefore R + 50 = \frac{3}{2}(2950 + 50)$$

 Solving we get, $R = 4450 \Omega$

10. A

Sol.



$$k_{C_1} + U_{C_1} = k_{C_2} + U_{C_2}$$

$$k_{\text{min}} + qV_{C_1} = 0 + qV_{C_2} \quad \dots(i)$$

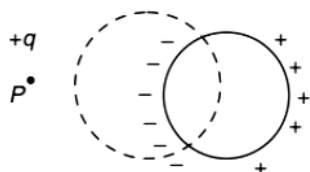
$$V_{C_1} = \frac{1}{4\pi\epsilon_0} \left(\frac{Q}{2R} - \frac{Q}{R} \right)$$

$$V_{C_2} = \frac{1}{4\pi\epsilon_0} \left(\frac{Q}{2} - \frac{Q}{2R} \right)$$

Substituting these values in Eq. (i), we can find K_{\min} .

11. C

Sol.



The induced charges on conducting sphere due to $+q$ charge at P are as shown in figure.

Now, net charge inside the closed dotted surface is negative. Hence, according to Gauss's theorem net flux is negative.

12. A

Sol. $p^2V = \text{constant}$

$$\therefore \left(\frac{nRT}{V} \right)^2 V = \text{constant}$$

$$\therefore T^2 \propto V$$

$$\text{or } T \propto \sqrt{V}$$

V is made three times. So, T will become $\sqrt{3}$ times.

13. A

Sol. $W_{\text{net}} = 2p_0V_0$

$$Q_{+ve} = Q_{ABC} = W_{ABC} + \Delta U_{ABC}$$

$$= \text{area under the graph} + nC_v\Delta T$$

$$= (3p_0V_0) + n\left(\frac{3}{2}R\right)(T_C - T_A)$$

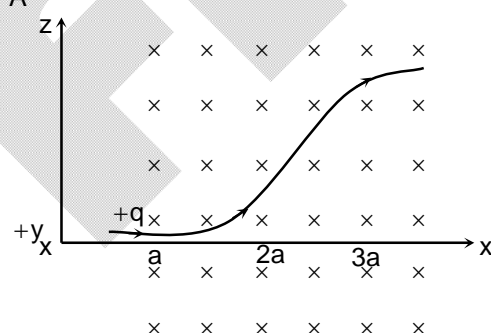
$$= (3p_0V_0) + \frac{3}{2}(p_CV_C - p_AV_A)$$

$$= 10.5 p_0V_0$$

$$\eta = \frac{W_{\text{net}}}{Q_{+ve}} = \frac{4}{21}$$

14. A

Sol.



15. C

Sol. Conceptual

16. A

$$\text{Sol. } \tan \phi = \frac{X_C}{R} \quad \frac{1}{\omega C} = R$$

$$\tan \frac{\pi}{4} = \frac{X_C}{R} \quad \frac{1}{\omega R} = C$$

$$X_C = R$$

i leads emf \therefore circuit is LC

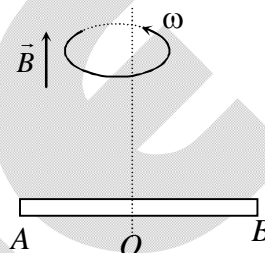
17. D

Sol. Potential difference between

$$O \text{ and } A \text{ is } V_A - V_O = \frac{1}{2} B l^2 \omega$$

$$O \text{ and } B \text{ is } V_B - V_O = \frac{1}{2} B l^2 \omega$$

$$\text{So } V_A - V_B = 0$$



18. B

$$\text{Sol. } \lambda = \frac{h}{\sqrt{2mE}} \Rightarrow \lambda \propto \frac{1}{\sqrt{E}}$$

$$\Rightarrow \frac{\lambda_1}{\lambda_2} = \sqrt{\frac{E_2}{E_1}} \Rightarrow \frac{10^{-10}}{0.5 \times 10^{-10}} = \sqrt{\frac{E_2}{E_1}}$$

$$\Rightarrow E_2 = 4E_1$$

$$\text{Hence added energy} = E_2 - E_1 = 3E_1$$

19. A

Sol. Using Moseley's law, we get

$$\frac{\lambda_2}{\lambda_1} = \frac{(Z_1 - a)^2}{(Z_2 - a)^2}$$

$$\lambda_2 = \frac{200 \times (74 - 1)^2}{(78 - 1)^2} = 179.76 \text{ \AA}$$

20. C

$$\text{Sol. } {}^x\lambda = \frac{\ln 2}{t_{1/2}}$$

$${}^y\lambda = \frac{\ln 2}{t_{1/2}}$$

$$\frac{{}^x A}{{}^y A} = \frac{{}^x \lambda {}^x N_0 e^{-x\lambda t}}{{}^y \lambda {}^y N_0 e^{-y\lambda t}}$$

$$e^{\ln 2} = 2$$

SECTION – B

21. 2

Sol. D_1 is reverse biased therefore it will act like an open circuit.

$$i = \frac{12}{6} = 2.00 \text{ A}$$

22. 3

Sol. Psueodo force and friction will make a force couple. Normal reaction and Mg will make a force couple.

When block is about to topple normal reaction will shift to edge.

23. 2

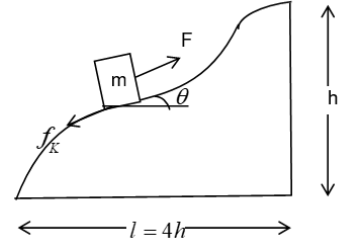
Sol. $\Delta W_f = -\int \mu mg \cos \theta ds$

$$= -\mu mg \int_0^l dx$$

$$= -\mu mgl = 0.5mg4h = -2mgh$$

$$\Delta W_g = -mgh$$

$$\therefore \Delta W_{fr} / \Delta W_g = 2$$



24. 5

Sol. $mg = kx$ (for m to leave the ground)

$$m_0 g x = \frac{1}{2} k x^2 \quad \text{or} \quad m_0 = \frac{m}{2} = 5 \text{ kg}$$

25. 4

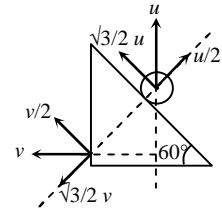
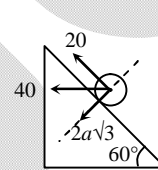
Sol. Conservation of momentum along horizontal

$$m40 = 6 \times v \quad \dots(i)$$

Newton's law of restitution

$$\frac{u}{2} + \frac{\sqrt{3}}{2} v = 20\sqrt{3} \quad \dots(ii)$$

Linear momentum of ball will remain conserved along inclined



Before Collision

$$\frac{\sqrt{3}}{2} u = 20$$

$$u = \frac{40}{\sqrt{3}} \quad \dots(iii)$$

From (i), (ii) and (iii)

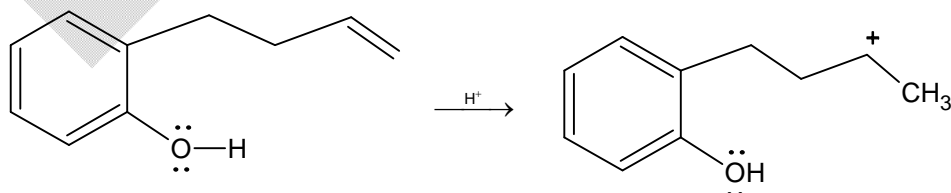
$$m = 4 \text{ kg}$$

Chemistry

PART – B

SECTION – A

26. C
Sol. Intensity of incident radiations depends on no. of photons in the incident light and simultaneously no. of photoelectrons increases and photoelectric current increases
27. A
Sol. In all the three options groups are arranged at ortho position. So after that the value of dipole moment will depend on the electro negativity difference.
28. C
Sol. For helium is a very light gas for which attraction is ignored and do not have vanderwall constant 'a' in the equation of compressibility factor and for helium $Z > 1$.
29. A
Sol. $\text{Na}_2\text{CO}_3 \longrightarrow \text{NaHCO}_3 \quad x$
 $\text{NaHCO}_3 \longrightarrow \text{H}_2\text{CO}_3 \quad x$
 $\text{NaHCO}_3 \longrightarrow \text{H}_2\text{CO}_3 \quad y$
 With phenolphthalein as indication $10 \text{ mL} \times 1\text{N} \times 2$
 2 mill g. equation = x
 with methyl orange as indicator
 $10\text{mL} \times 0.2\text{N} \times 4 \text{ milli gram equation} = x + y$
 $y = 2 \text{ mili gram eq.}$
 $\text{Normality} = \frac{2\text{milligram eq.}}{20\text{mL}} = 0.1\text{N}$
 $N = n_f \times \text{molarity } M = 0.05 \text{ M}$
30. D
Sol. For first order reaction, $t = \frac{2.303}{k} \log \frac{a}{a-x} \quad t_{99.9} = \frac{2.303}{k} \log \frac{100}{100-99.9} = \frac{2.303}{k} \times 3$
 $t_{50} = \frac{2.303}{k} \log \frac{2.303}{k} \log 2 = \frac{2.303}{k} \times 0.301 \quad t_{99.9/t50} = 10 \text{ approx.}$
31. C
Sol. The cations will be liberated in the sequence of decreasing reduction potentials. Cations having E° value < -0.83 (reduction potential of water) will not be liberated from aqueous solutions
32. C
Sol. Iodine is a bulky group due to ortho effect mesomeric effect stops at ortho position & hence a and b will be longer than C bond
33. B
Sol.



More stable carbocation forms at this position

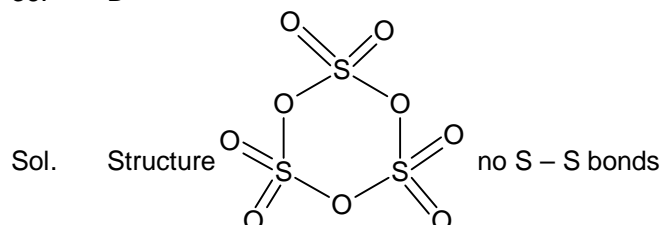
34. B

Sol. Benzilic acid involves transformation of α -diketones to α -hydroxyl acid by means of OH^-

35. C

Sol. CO_2 , in CO_2 carbon is already in its maximum oxidation state and cannot be oxidised further. While N, Cl, S are not in their maximum oxidation state.

36. D



37. B

Sol. $[\text{Co}(\text{NH}_3)_2\text{Cl}_4]^-$ = cis and trans isomerism
 $\text{AuCl}_2\text{Br}_2^-$ square planar cis and trans isomersim
 $[\text{Co}(\text{NO}_2)] [\text{NH}_3]^{2+}$ = No isomerism

38. C

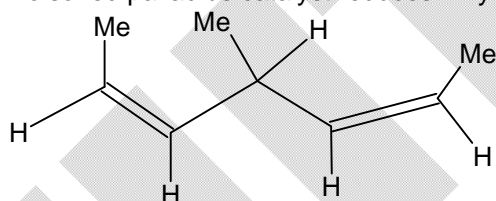
Sol. VBT is based on measurement of magnetic moment measurement. Based on that structure is being predicted.

39. B

Sol. Fehlings solution can separate reducing and non-reducing sugars.
 Glucose – Reducing sugar
 Sucrose – non-reducing sugar.

40. B

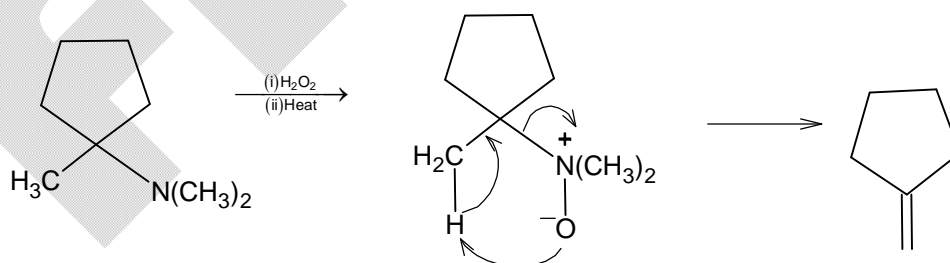
Sol. Poisoned palladium catalyst reduces Alkyne to cis-Alkene.



Optically inactive product

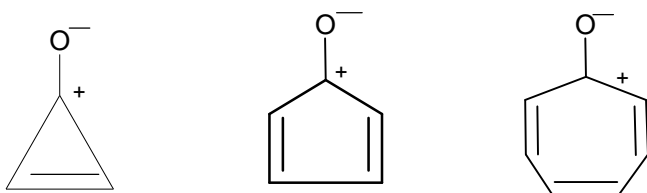
41. D

Sol.



Less stable alkene is the major product

42. B
Sol.



Aromatic

Anti-aromatic

Aromatic

Anti-aromatic is the least stable

43. A

Sol. Partial pressure of $O_2 = \frac{2}{7} \times 2660 \text{ mm}$

Thus 1 L of O_2 is present at 0°C and 760 mm

So no. of O_2 molecules = $\frac{0.02 \times 10^{23}}{22.4}$

$PV = nRT$

No. of moles of $O_2 = \frac{1 \text{ atm} \times 1 \text{ L}}{0.0821^{-1} \text{ atm}} \times 273 \text{ K} = \frac{1}{22.4}$

44. C

Sol. They have different bond connectivity. Hence constitutional isomers.

45. C

Sol. Zone refining is based on the principal that impurities are more soluble in molten state than solid state.

Hence molten zone contains more impurities than the original metal.

SECTION – B

46. 25

Sol. $AB_2 \rightleftharpoons AB(g) + B(g)$

500

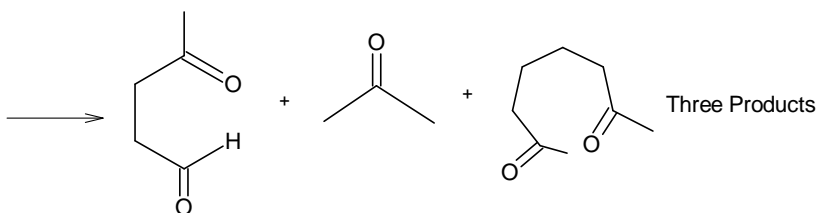
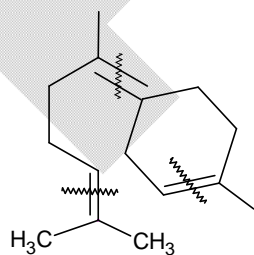
500 – x x x

Require = 600 torr = 500 – x + x + x, x = 100 torr

$K_p = \frac{P_{AB} \cdot P_B}{P_{AB_2}} = \frac{100 \times 100}{400} = 25 \text{ torr}$

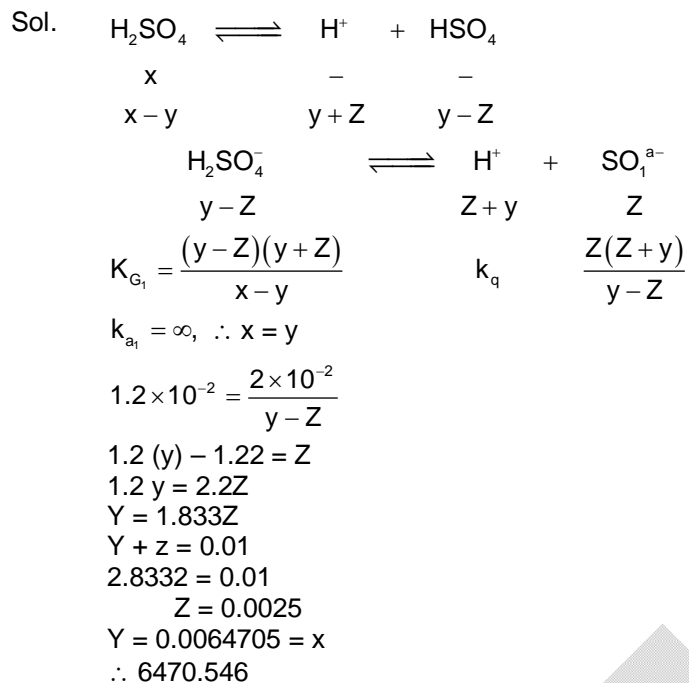
47. 3

Sol.

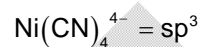
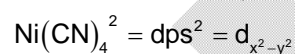
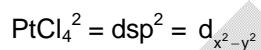
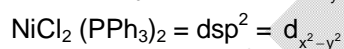
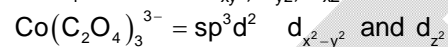
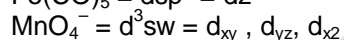
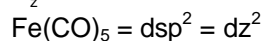


Three Products

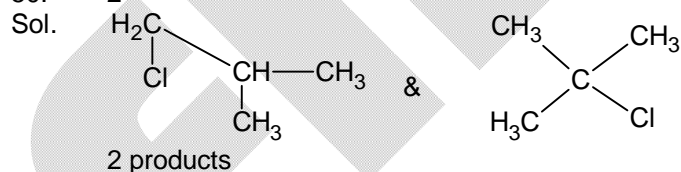
48. 6470



49. 2

Sol. d_{z^2} orbital has no mola plane.

50. 2



Mathematics

PART – C

SECTION – A

51. D

$$\text{Sol. } \sin^{-1} \frac{|2 \times 3 + (-1) \times 6 + 2 \times (-2)|}{\sqrt{2^2 + (-1)^2 + 2^2} \cdot \sqrt{3^2 + 6^2 + (-2)^2}}$$

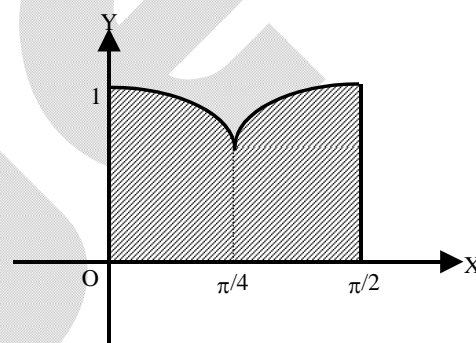
52. C

$$\begin{aligned} \text{Sol. } \frac{dy}{dx} &= \cos^{-1} x^4 x^2 \\ &= -\cos^{-1} x^2 \\ &= \frac{2\pi}{3} \times \frac{1}{2^{1/4}} - \frac{\pi}{4} \end{aligned}$$

53. A

$$\begin{aligned} \text{Sol. } f(x) &= \cos x \text{ for } 0 \leq x \leq \pi/4 \\ &= \sin x \text{ for } \pi/4 < x \leq \pi/2 \end{aligned}$$

$$\begin{aligned} \text{Required} &= 2 \int_0^{\pi/4} \cos x dx = 2 \sin x \Big|_0^{\pi/4} \\ &= \sqrt{2} \text{ sq. units.} \end{aligned}$$



54. D

$$\begin{aligned} \text{Sol. } (1 - x^4) (1 + {}^9C_1 x + {}^9C_2 x^2 + {}^9C_3 x^3 + \dots + {}^9C_9 x^9) \\ \text{Coefficient of } x^7 = {}^9C_7 - {}^9C_3 = -48 \end{aligned}$$

55. C

$$\begin{aligned} \text{Sol. } \text{The chord of contact of tangents from } (\alpha, \beta) \text{ is} \\ \alpha x + \beta y = 1 \quad \dots (1) \end{aligned}$$

$$\text{Also, } (\alpha, \beta) \text{ lies on } 2x + y = 4, \text{ so that } 2\alpha + \beta = 4$$

$$\Rightarrow \frac{\alpha}{2} + \frac{\beta}{4} = 1$$

$$\text{Hence, (1) passes through } \left(\frac{1}{2}, \frac{1}{4} \right).$$

56. C

$$\begin{aligned} \text{Sol. } \text{Equation of line is } (2x + 3y + 4) + \lambda (6x - 3y + 12) = 0 \quad \dots (1) \\ (1) \text{ is normal to circle, therefore (1) passes through } (2, 0) \end{aligned}$$

$$\Rightarrow \lambda = \frac{-1}{3} \text{ and required equation is } y = 0.$$

57. A

$$\begin{aligned} \text{Sol. } \Rightarrow 2y \frac{dy}{dx} x = -y^2 - \sin 2x \quad \Rightarrow y^2 + 2yx \frac{dy}{dx} = -\sin 2x \end{aligned}$$

$$\Rightarrow \frac{d}{dx}(xy^2) = \frac{d}{dx}(\cos^2 x) \quad \Rightarrow xy^2 = \cos^2 x + c$$

58. D

Sol.
$$\begin{vmatrix} (a^x + a^{-x})^2 & (a^x - a^{-x})^2 & 1 \\ (b^y + b^{-y})^2 & (b^y - b^{-y})^2 & 1 \\ (c^z + c^{-z})^2 & (c^z - c^{-z})^2 & 1 \end{vmatrix}$$

Operating $C_1 \rightarrow C_1 - C_2$

$$\begin{vmatrix} 4a^x a^{-x} & (a^x - a^{-x})^2 & 1 \\ 4b^y b^{-y} & (b^y - b^{-y})^2 & 1 \\ 4c^z c^{-z} & (c^z - c^{-z})^2 & 1 \end{vmatrix} = 4 \begin{vmatrix} 1 & (a^x - a^{-x})^2 & 1 \\ 1 & (b^y - b^{-y})^2 & 1 \\ 1 & (c^z - c^{-z})^2 & 1 \end{vmatrix} = 0.$$

59. C

Sol. $0 < \frac{3}{x^2 + 1} \leq 3, \frac{3}{x^2 + 1} = 2 \Rightarrow x = \frac{1}{\sqrt{2}}$ and $\frac{3}{x^2 + 1} = 1 \Rightarrow x = \sqrt{2}$

$$I = \int_0^{1/\sqrt{2}} 2dx + \int_{1/\sqrt{2}}^{\sqrt{2}} 1 \cdot dx + \int_{\sqrt{2}}^{\infty} 0 dx = \sqrt{2} + \sqrt{2} - \frac{1}{\sqrt{2}} = 2\sqrt{2} - \frac{1}{\sqrt{2}} = \frac{3}{\sqrt{2}}.$$

60. C

Sol.
$$\int \frac{\ln x}{(1 + \ln x)^2} dx$$

Let $\ln x = t \Rightarrow dx = e^t dt$

$$\int \frac{te^t}{(1+t)^2} dt = \int \frac{e^t(t+1-1)}{(1+t)^2} dt$$

$$= \int \frac{e^t(t+1-1)}{(1+t)^2} dt$$

$$= \int e^t \left\{ \frac{1}{t+1} - \frac{1}{(1+t)^2} \right\} dt$$

$$= \frac{e^t}{t+1} + c \quad \text{since } \int e^x(f(x) + f'(x))dx = e^x f(x) + c$$

$$= \frac{e^{\ln x}}{1 + \ln x} + c = \frac{x}{1 + \ln x} + c.$$

61. A

Sol. $f(x) = \log_{1/2} \log_4 \log_3 [(x-4)^2] \Rightarrow \log_4 (\log_3 [x-4]^2) > 0 \Rightarrow \log_3 [(x-4)^2] > 1$
 $\Rightarrow [(x-4)^2] \geq 4 \Rightarrow (x-4)^2 - 4 \geq 0 \Rightarrow (x-2)(x-6) \geq 0$
 $\Rightarrow x \in (-\infty, 2] \cup [6, \infty).$

62. A

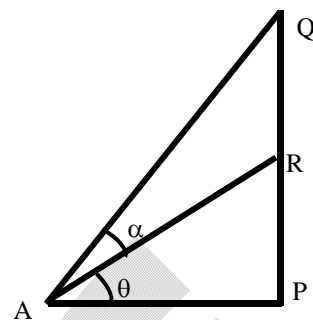
Sol. $\tan(\theta + \alpha) = \frac{PQ}{AP} = \frac{1}{n}$

$$\tan \theta = \frac{PR}{AP} = \frac{(1/2)PQ}{AP} = \frac{1}{2n}$$

$$\alpha = (\theta + \alpha) - \theta$$

$$\Rightarrow \tan \alpha = \frac{\tan(\theta + \alpha) - \tan \theta}{1 + \tan(\theta + \alpha)\tan \theta}$$

$$= \frac{\frac{1}{n} - \frac{1}{2n}}{1 + \frac{1}{n} \cdot \frac{1}{2n}} = \frac{n}{2n^2 + 1}$$



63. C

Sol. Normal to hyperbola will be
 $ax \cos \theta + by \cot \theta = a^2 + b^2$
 If this is same as $lx + my + n = 0$, comparing the coefficients,

$$\frac{a \cos \theta}{l} = \frac{b \cot \theta}{m} = \frac{a^2 + b^2}{-n}$$

$$\sec \theta = -\frac{an}{l(a^2 + b^2)}, \quad \tan \theta = \frac{-bn}{m(a^2 + b^2)}$$

$$\sec^2 \theta - \tan^2 \theta = 1$$

$$\Rightarrow \frac{a^2}{l^2} - \frac{b^2}{m^2} = \frac{(a^2 + b^2)^2}{n^2}$$

64. A

Sol. Any point on the parabola is $(x, x^2 + 7x + 2)$
 Its distance from the line $y = 3x - 3$ is given by

$$P = \frac{|3x - (x^2 + 7x + 2) - 3|}{\sqrt{9 + 1}} = \frac{|x^2 + 4x + 5|}{\sqrt{10}} = \frac{x^2 + 4x + 5}{\sqrt{10}} \quad (\text{as } x^2 + 4x + 5 > 0 \text{ for all } x \in \mathbb{R})$$

$$\frac{dP}{dx} = 0 \Rightarrow x = -2$$

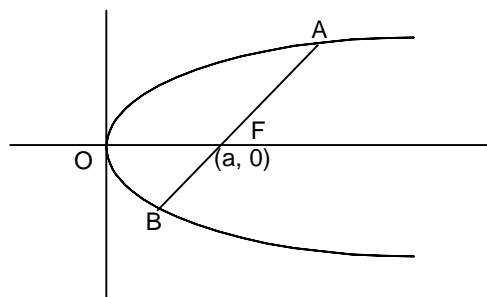
The required point $\equiv (-2, -8)$.

65. A

Sol. $FA = 4, FB = 5$

We know that $\frac{1}{a} = \frac{1}{AF} + \frac{1}{FB}$

$$\Rightarrow a = \frac{20}{9} \Rightarrow 4a = \frac{80}{9}$$



66. D

Sol. $\frac{n}{4n^4 + 1} = \frac{1}{4} \left[\frac{1}{2n^2 - 2n + 1} - \frac{1}{2n^2 + 2n + 1} \right]$

Hence $\sum_{n=1}^k \frac{n}{4n^4 + 1} = \frac{1}{4} \left[1 - \frac{1}{2k^2 + 2k + 1} \right] = \frac{1}{4}$ as $k \rightarrow \infty$

67. C

Sol. $S - S_n < \frac{1}{300}$

$$\Rightarrow \frac{1}{1 - \frac{1}{3}} - \frac{1 - \frac{1}{3^n}}{1 - \frac{1}{3}} < \frac{1}{300} \Rightarrow \frac{3}{2} \left[1 - 1 + \frac{1}{3^n} \right] < \frac{1}{300}$$

$$\Rightarrow \frac{1}{3^n} < \frac{1}{300} \times \frac{2}{3} \Rightarrow \frac{1}{3^n} < \frac{1}{450} \Rightarrow 3^n > 450$$

\therefore least value of $n = 6$

68. B

Sol. Let $f(x) = x^3 - 3x + a$

$$f'(x) = 3x^2 - 3.$$

For three distinct real roots (i) $f'(x) = 0$ should have two distinct real roots α and β and (ii) $f(\alpha)f(\beta) < 0$

Here $\alpha = 1, \beta = -1$.

Now $f(\alpha)f(\beta) < 0$

$$\Rightarrow (1 - 3 + a)(-1 + 3 + a) < 0 \Rightarrow (a - 2)(a + 2) < 0$$

$$\Rightarrow -2 < a < 2.$$

69. C

Sol. The line $y = \sqrt{3}x$ can be written as $x = \frac{r}{2}, y = \frac{r\sqrt{3}}{2}$.

If this line cuts the given curve, then

$$\frac{r^4}{16} + \frac{ar^3\sqrt{3}}{8} + \frac{br^2\sqrt{3}}{4} + \frac{cr}{2} + \frac{dr\sqrt{3}}{2} + 6 = 0.$$

Therefore $OA \cdot OB \cdot OC \cdot OD = |r_1| |r_2| |r_3| |r_4| = |r_1 r_2 r_3 r_4| = 96$

70. C

Sol. Plane passing through $(2, 2, 1)$ is $a(x - 2) + b(y - 2) + c(z - 1) = 0$

It passes through $(9, 3, 6)$

$$\Rightarrow 7a + b + 5c = 0 \quad \dots (1)$$

It is \perp to $2x + 6y + 6z - 1 = 0$

$$\Rightarrow 2a + 6b + 6c = 0 \quad \dots (2)$$

$$(1) \text{ and } (2) \Rightarrow \frac{a}{-24} = \frac{b}{-32} = \frac{c}{40}$$

$$\Rightarrow \frac{a}{3} = \frac{b}{4} = \frac{c}{-5}$$

\Rightarrow The required plane is

$$3(x - 2) + 4(y - 2) - 5(z - 1) = 0$$

$$\Rightarrow 3x + 4y - 5z - 9 = 0.$$

SECTION – B

71. 9

$$\text{Sol. S. D} = \frac{\begin{vmatrix} 10 & 2 & 3 \\ 1 & -2 & 2 \\ 3 & -2 & -2 \end{vmatrix}}{\sqrt{8^2 + 8^2 + 4^2}} = \frac{108}{12} = 9$$

72. 0

$$\begin{aligned} \text{Sol. Let } f(x) &= x^3 + 2x^2 + 5x + 2 \cos x \\ \Rightarrow f'(x) &= 3x^2 + 4x + 5 - 2 \sin x \\ &= 3 \left(x + \frac{2}{3} \right)^2 + \frac{11}{3} - 2 \sin x \\ \text{Now } \frac{11}{3} - 2 \sin x &> 0 \quad \forall x \quad (\text{as } -1 \leq \sin x \leq 1) \\ \Rightarrow f'(x) &> 0 \quad \forall x \Rightarrow f(x) \text{ is an increasing function.} \\ \text{Now } f(0) &= 2 \\ \Rightarrow f(x) = 0 &\text{ has no solution in } [0, 2\pi]. \end{aligned}$$

73. 5

$$\begin{aligned} \text{Sol. } T_2 &= {}^nC_1 ab^{n-1} = 135 && \dots(1) \\ T_3 &= {}^nC_2 a^2 b^{n-2} = 30 && \dots(2) \\ T_4 &= {}^nC_3 a^3 b^{n-3} = 10/3 && \dots(3) \\ \text{Dividing (1) by (2)} \\ \frac{{}^nC_1 ab^{n-1}}{{}^nC_2 a^2 b^{n-2}} &= \frac{135}{30} \\ \frac{n}{2} \cdot \frac{b}{a} &= \frac{9}{2} \\ \frac{b}{a} &= \frac{9}{4}(n-1) && \dots (5) \\ \text{Dividing (2) by (3)} \\ \frac{{}^nC_2 a^2 b^{n-2}}{{}^nC_3 a^3 b^{n-3}} &= \frac{30}{10/3} \\ \frac{2}{3} \cdot \frac{b}{a} &= 9 \\ \therefore \frac{b}{a} &= 3(n-2) && \dots(6) \end{aligned}$$

Eliminating a and b from (5) and (6)
 $\Rightarrow n = 5$

74. 4

$$\text{Sol. } k = |z - z_1|^2 + |z - z_2|^2 = |z_1 - z_2|^2 \Rightarrow k = 4$$

75. 8

$$\text{Sol. } \frac{x^2}{4} + \frac{y^2}{3} = 1 \Rightarrow a = 2, b = \sqrt{3} \text{ and } e = \frac{1}{2}$$

$$\text{Sum of distances} = \frac{2a}{e} = \frac{4}{1/2} = 8.$$