

CLASSROOM CONTACT PROGRAMME (Academic Session: 2024 - 2025)

JEE(Advanced)

Test Pattern

JEE(Main+Advanced): ENTHUSIAST COURSE ALL STAR BATCH (SCORE-II)

PAPER (OPTIONAL) Time: 3 Hours Maximum Marks: 180

IMPORTANT NOTE: Students having 8 digits Form No. must fill two zero before their Form No. in OMR. For example, if your Form No. is 12345678, then you have to fill 0012345678.

READ THE INSTRUCTIONS CAREFULLY

GENERAL:

- This sealed booklet is your Question Paper. Do not break the seal till you are told 1. to do so.
- 2. Use the Optical Response Sheet (ORS) provided separately for answering the questions.
- 3. Blank spaces are provided within this booklet for rough work.
- Write your name, form number and sign in the space provided on the back cover of this 4. booklet.
- After breaking the seal of the booklet, verify that the booklet contains 28 pages and that 5. all the 18 questions in each subject and along with the options are legible. If not, contact the invigilator for replacement of the booklet.
- 6. You are allowed to take away the Question Paper at the end of the examination.

OPTICAL RESPONSE SHEET:

- 7. The ORS will be collected by the invigilator at the end of the examination.
- 8. Do not tamper with or mutilate the ORS. Do not use the ORS for rough work.
- Write your name, form number and sign with pen in the space provided for this purpose 9. on the ORS. Do not write any of these details anywhere else on the ORS. Darken the appropriate bubble under each digit of your form number.

DARKENING THE BUBBLES ON THE ORS:

- Use a **BLACK BALL POINT PEN** to darken the bubbles on the ORS. 10.
- Darken the bubble COMPLETELY. 11.
- 12. The correct way of darkening a bubble is as:
- 13. The ORS is machine-gradable. Ensure that the bubbles are darkened in the correct way.
- 14. Darken the bubbles ONLY IF you are sure of the answer. There is NO WAY to erase or "un-darken" a darkened bubble.
- Take $g = 10 \text{ m/s}^2$ unless otherwise stated. 15.

QUESTION PAPER FORMAT:

The question paper has three parts: Physics, Chemistry and Mathematics.

Please see the last page of this booklet for rest of the instructions

COME	HEFFIH	CONSTANTS	

Atomic No. : H = 1, B = 5, C = 6, N = 7, O = 8, F = 9, Al = 13, P = 15, S = 16,

Cl = 17, Br = 35, Xe = 54, Ce = 58

Atomic masses: H = 1, Li = 7, B = 11, C = 12, N = 14, O = 16, F = 19, Na = 23, Mg = 24,

Al = 27, P = 31, S = 32, Cl = 35.5, Ca = 40, Fe = 56, Br = 80, I = 127,

Xe = 131, Ba=137, Ce = 140

• Boltzmann constant $k = 1.38 \times 10^{-23} J K^{-1}$

• Coulomb's law constant $\frac{1}{4\pi\varepsilon_0} = 9 \times 10^9$

• Universal gravitational constant $G = 6.67259 \times 10^{-11} \text{ N-m}^2 \text{ kg}^{-2}$

Speed of light in vacuum $c = 3 \times 10^8 \text{ ms}^{-1}$

• Stefan–Boltzmann constant $\sigma = 5.67 \times 10^{-8} \text{ Wm}^{-2}\text{-K}^{-4}$

• Wien's displacement law constant $b = 2.89 \times 10^{-3} \text{ m-K}$

 $\bullet \qquad \quad Permeability \ of \ vacuum \qquad \qquad \mu_0 = 4\pi \times 10^{-7} \ NA^{-2}$

• Permittivity of vacuum $\in_0 = \frac{1}{\mu_0 c^2}$

• Planck constant $h = 6.63 \times 10^{-34} \text{ J-s}$

Space for Rough Work

E-2/28 1001CJA106216240179



HAVE CONTROL → HAVE PATIENCE → HAVE CONFIDENCE ⇒ 100% SUCCESS

BEWARE OF NEGATIVE MARKING

PART-1: PHYSICS

SECTION-I (i): (Maximum Marks: 12)

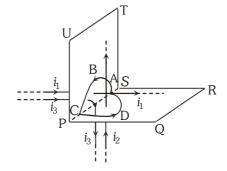
- This section contains FOUR (04) questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme :

Full Marks : +3 If ONLY the correct option is chosen.

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered)

Negative Marks : -1 In all other cases

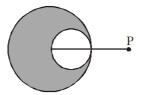
- 1. In Young's double slit experiment, the distance d between the slits S₁ and S₂ is 1.0 mm. What should be the width of each slit so as to obtain 5 maxima of the two slit interference pattern within the central maximum of the single slit diffraction pattern?
 - (A) 0.2 mm
 - (B) 0.4 mm
 - (C) 12 cm
 - (D) 0.1 mm
- 2. Figure shows an amperian path ABCDA. Part ABC is in vertical plane PSTU while part CDA is in horizontal plane PQRS. Direction of circulation along the path is shown by an arrow near point B and at D. $\oint \vec{B} \cdot \vec{dl}$ for this path according to Ampere's law will be :-



- (A) $(i_1 i_2 + i_3)\mu_0$
- (B) $(-i_1 + i_2)\mu_0$
- (C) $i_3\mu_0$
- (D) $(i_1 + i_2)\mu_0$

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3. A spherical cave of radius R/2 was carved out from a uniform sphere of radius R and original mass M. The center of the cave is at R/2 from the center of the large sphere. Point P is at a distance 2R from the center of the large sphere and on the joint line of the two centers. The magnitude of gravitational field strength g at point P is ______.



(A)
$$g = \frac{GM}{4R^2}$$

(B)
$$g = \frac{5GM}{8R^2}$$

(C)
$$g = \frac{3GM}{16R^2}$$

(D)
$$g = \frac{7GM}{36R^2}$$

- 4. In a circuit for finding the resistance of a galvanometer by half deflection method, a 6 V battery and a high resistance of 11 k Ω are used. The figure of merit of the galvanometer is 60μ A/division. In the absence of shunt resistance, the galvanometer produces a deflection of $\theta = 9$ divisions when current flows in the circuit. The value of the shunt resistance that can cause the deflection of $\theta/2$, is closest to:-
 - (A) 55 Ω
 - (B) 110Ω
 - (C) 220 Ω
 - (D) 550 Ω

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SECTION-I (ii): (Maximum Marks: 24)

• This section contains **SIX (06)** questions.

• Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).

• For each question, choose the option(s) corresponding to (all) the correct answer(s)

• Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 If only (all) the correct option(s) is (are) chosen.

Partial Marks : +3 If all the four options are correct but ONLY three options are chosen.

Partial Marks : +2 If three or more options are correct but ONLY two options are chosen and

both of which are correct.

Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a

correct option.

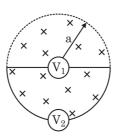
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered).

Negative Marks : -2 In all other cases.

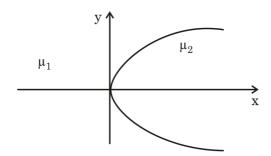
- For Example: If first, third and fourth are the ONLY three correct options for a question with second option being an incorrect option; selecting only all the three correct options will result in +4 marks. Selecting only two of the three correct options (e.g. the first and fourth options), without selecting any incorrect option (second option in this case), will result in +2 marks. Selecting only one of the three correct options (either first or third or fourth option), without selecting any incorrect option (second option in this case), will result in +1 marks. Selecting any incorrect option(s) (second option in this case), with or without selection of any correct option(s) will result in −2 marks.
- 5. Three nonconducting infinite planar sheets are parallel to the y-z plane. Each sheet has a uniform surface charge density. The first sheet, with a negative surface charge density $-\sigma$, passes through the x-axis at x = 1 m. The second sheet has an unknown surface charge density and passes through the x-axis at x = 2m. The third sheet has a negative surface charge density -3σ and passes through the x-axis at x = 4 m. The net electric field due to the sheets is zero at x = 1.5 m.
 - (A) The surface charge density on the second sheet is $+2\sigma$.
 - (B) The electric field at x = -2 m is $\frac{\sigma}{\epsilon_0}$
 - (C) The electric field at x = 3 m is $\frac{\sigma}{\epsilon_0}$
 - (D) The electric field at x = 6m is $\frac{-\sigma}{\epsilon_0}$

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6. A time varying magnetic field exists in a cylindrical region of radius a. A semi circular conductor of negligible resistance with a small voltmeter V_2 of resistance 2R is placed coaxially with cylindrical region as shown in diagram. A small voltmeter V_1 having resistance R is connected across the two ends of semicircular conductor as shown in diagram. Magnetic field is varying at a rate of $\frac{dB}{dt}$. Choose correct option(s).



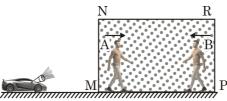
- (A) Current passing through voltmeter V_1 is $\frac{\pi a^2}{6R} \cdot \frac{dB}{dt}$
- (B) Reading of voltmeter V_1 is zero because it is connected to a conductor which along diameter of cylinderical region.
- (C) Reading of voltmeter is V_1 is $\frac{\pi a^2}{6}$. $\frac{dB}{dt}$
- (D) Reading of voltmeter V_2 is $\frac{\pi a^2}{3}$. $\frac{dB}{dt}$
- 7. A light ray coming from medium of refractive index μ_1 along the line y=8 is incident on the interface of a medium of refractive index μ_2 whose curve is given by $y^2=16x$. Then just after first refraction:



- (A) If $\mu_1 = 1$ and $\mu_2 = \sqrt{2}$ then angle of deviation is $\frac{\pi}{12}$.
- (B) If $\mu_1 = 1$ and $\mu_2 = \sqrt{2}$ then angle of deviation is $\frac{5\pi}{12}$.
- (C) If $\mu_1 = \sqrt{2}$ and $\mu_2 = 1$ then angle of deviation is $\frac{\pi}{4}$.
- (D) If $\mu_1 = \sqrt{2}$ and $\mu_2 = 1$ then angle of deviation is $\frac{\pi}{2}$.

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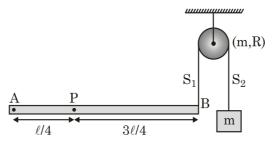
8. A car is moving with a velocity $\frac{3v}{10}$ towards a medium MNRP as shown, where 'v' is the speed of sound in air. Two men A and B are moving towards each other in the medium with the velocities $\frac{v}{6}$ and $\frac{v}{9}$ respectively. The speed of sound in medium is 7v and medium is kept at rest. The car is emitting a sound of frequency f. Then choose the correct option(s).



- (A) The wavelength received by the man A is $\frac{49v}{10f}$.
- (B) The wavelength received by the man A is different form the wavelength received by man B.
- (C) The ratio of frequency observed by the man A to that observed by the man B is $\frac{123}{128}$
- (D) The frequency observed by the man B is $\left(\frac{640}{441}\right) f$.

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9. A uniform rod of mass m and length ℓ is hinged at point P such that the rod can rotate in a vertical plane. One end B of the rod is connected through the massless string which passes over the pulley of mass m and radius R and the other end of the string is connected with the block of mass m as shown in the figure. (There is no slipping between the string and the pulley) Initially rod is horizontal. At t = 0, the system is released, then which of the following is/are correct.



- (A) Acceleration of the block is $\frac{36}{95}$ g
- (B) Acceleration of the centre of mass of the rod is $\frac{12}{95}$ g
- (C) Tension in the string S_1 is $\frac{41}{95}$ mg
- (D) Tension in the string S_2 is $\frac{39}{95}$ mg
- 10. A small metal plate of area 2 cm² is placed at a distance of 2 m from a monochromatic light source of $\lambda = 1000$ Å and power rating of 100 W and light energy conversion efficiency of 10%, emitting light uniformly in all directions. Light falls normally on the plate (work function, $\phi = 10\text{eV}$). Assuming one out of 10^6 photons is able to eject a photoelectron, identify correct statements
 - (A) KE max of photoelectron emitted is 2.4 eV
 - (B) Saturation current is 3.2×10^{-12} A
 - (C) Saturation current is 4.5×10^{-12} A
 - (D) KE max of photoelectron emitted is 3.2 eV

Note: No questions have been asked in the section II of this paper. Please leave section II blank on the OMR answer sheet.

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SECTION-III: (Maximum Marks: 24)

• This section contains **EIGHT (08)** questions.

• The answer to each question is a **SINGLE DIGIT INTEGER** ranging from 0 to 9, both inclusive.

• For each question, enter the correct integer value of the answer in the place designated to enter the answer.

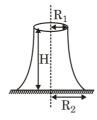
• For each question, marks will be awarded in <u>one of the following categories</u>:

Full Marks : +3 If only the correct answer is given.

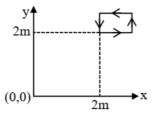
Zero Marks : 0 If no answer is given.

Negative Marks : -1 In all other cases

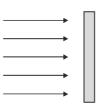
1. A solid object having uniform density (ρ) and varying cross-sectional area (which is circular) is placed on smooth horizontal surface as shown. If the stress throughout its height remains same and having value equal to c, the value of $R_2 = R_1 e^{\frac{\rho g H}{nc}}$. The value of n is :-



2. The magnetic field existing in a region is given by $\vec{B} = 0.2 (1 + 2x) \hat{k} T$. A square loop of edge 50 cm carrying 0.5 A current is placed in x-y plane with its edges parallel to the x-y axes, as shown in figure. The magnitude of the net magnetic force experienced by the loop is α mN. Find the value of $\alpha/10$, where α is a least integer.

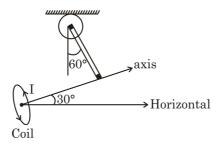


3. The shaded area in the figure is the side view of a disk shaped magnetic field region of radius R and thickness d. A parallel electron beam being accelerated by a voltage V is normally incident onto the region. If the spatial distribution of the magnetic field in the region such that the beam is focused to a point along the disk central axis at a distance L (>> R) from the disk is $B = \frac{y^{\eta}}{d^{\alpha}L^{\beta}}\sqrt{\frac{\lambda mV}{e}}$, find the value of $\frac{20\alpha}{\lambda + \beta + \eta}$. Given m and e are the electron's mass and charge and y is the distance of incident electron from axis of disc.



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4. A magnetized needle of length 10 cm is freely suspended by its south pole from a hook as shown in figure. Mass of needle is 2 milligram. In equilibrium, the needle makes an angle of 60° from vertical. The magnetic pole strength is concentrated at the ends of the needle. The magnetic pole strength of needle (in A-m) is β . Find the value of 10β . (Given: number of turns in coil = 1,000, radius of coil = 10 cm, current in coil = $\frac{100}{\pi}$ A and end of needle is lying on the axis of coil at a distance of 2 m from the centre of coil.)



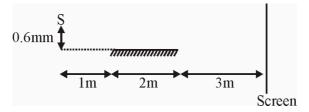
5. The given system is in equilibrium. The velocity of wave in strings A & B is respectively x and y (in m/s). Given the answer $\frac{x+y}{15}$.

$$\mu_A = 4 \times 10^{-3} \ kg/m$$

$$\mu_B = 16 \times 10^{-3} \ kg/m$$

$$2kg$$

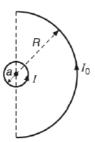
6. In a particular set up, interference is observed on an screen as shown. Wavelength of light emitted by source is 4000 Å. Out of two coherent sources, one is obtained by reflection with a plane mirror of length 2m. The number of points on the screen where intensity is minimum, is:



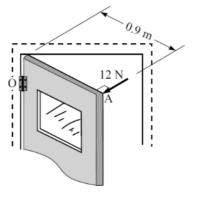
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7. A small current carrying loop having current I is placed in the plane of paper as shown. Another semicircular loop having current I_0 is placed concentrically in the same plane as that of small loop, the radius of semi-circular loop is R(R>>a). Find the force applied by the smaller ring on bigger ring in newton.

Given R = 1m, I =
$$I_0 = \frac{40}{\sqrt{\mu_0}}$$
 A, a = 0.1 m



8. The figure shows a 0.9 m wide uniform door hinged at the edge being subjected to a force of magnitude 12 N as shown. About the given axis, the moment of inertia of the door is 1.2 kg m². Neglecting gravity, what is the force (in N) exerted by the hinge as soon as the force is applied?



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PART-2: CHEMISTRY

SECTION-I (i): (Maximum Marks: 12)

• This section contains **FOUR (04)** questions.

- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme :

Full Marks : +3 If ONLY the correct option is chosen.

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered)

Negative Marks : -1 In all other cases

1. Concentration of H_2SO_4 and Na_2SO_4 in a solution is 1 M and 1.8×10^{-2} M, respectively. Molar solubility of $PbSO_4$ in the same solution is :

[Given: Solubility product of PbSO₄(K_{sp}) = 1.6 ×10⁻⁸. For H₂SO₄, Ka₁ is very large and Ka₂ = 1.2 × 10⁻⁴]

(A)
$$\frac{8}{9} \times 10^{-6} \,\text{M}$$

(B)
$$\sqrt{1.6} \times 10^{-4} \,\text{M}$$

(C)
$$1.33 \times 10^{-4} \,\mathrm{M}$$

(D)
$$1.6 \times 10^{-6} \,\mathrm{M}$$

2. An element "X" (atomicity = 2) forms oxide X_MO_N & X_PO_R (in significant amount) with oxygen during burning of fossil fuel at high temperature in an automobile engine. The oxide X_PO_R is a lung irritant & usually causes respiratory problems in children.

Which of the following is correct regarding $X_MO_N \& X_PO_R$?

- (A) Both X_MO_N & X_PO_R are diamagnetic.
- (B) Both X_MO_N & X_PO_R have tendency to dimerize.
- (C) Mixture of X_MO_N & X_PO_R when cooled yields blue color liquid.
- (D) Both X_MO_N & X_PO_R follow octet rule.

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- 3. The complex compound that shows paramagnetic and is a low spin complex among the following.
 - (A) $K_3[Co(NO_2)_6]$
 - (B) $(NH_4)_2[PtCl_6]$
 - (C) $K_2[Co(CN)_6]$
 - (D) $K_2[NiF_6]$
- 4. Isopentane $\xrightarrow[hV]{\text{Br}_2}$ monobromo products.

Select correct statement about mono bromo product.

- (A) Total monobromo products are 6 in which molecules of major products are optically active.
- (B) Total monobromo products are 6 in which major product is optically inactive.
- (C) Total monobromo products are 4 in which molecules of major products are optically active.
- (D) Total monobromo products are 4 in which major product is optically inactive.

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SECTION-I (ii): (Maximum Marks: 24)

- This section contains SIX (06) questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s)
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 If only (all) the correct option(s) is (are) chosen.

Partial Marks : +3 If all the four options are correct but ONLY three options are chosen.

Partial Marks : +2 If three or more options are correct but ONLY two options are chosen and

both of which are correct.

Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a

correct option.

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered).

Negative Marks : -2 In all other cases.

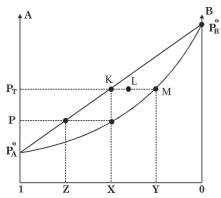
● For Example: If first, third and fourth are the ONLY three correct options for a question with second option being an incorrect option; selecting only all the three correct options will result in +4 marks. Selecting only two of the three correct options (e.g. the first and fourth options), without selecting any incorrect option (second option in this case), will result in +2 marks. Selecting only one of the three correct options (either first or third or fourth option), without selecting any incorrect option (second option in this case), will result in +1 marks. Selecting any incorrect option(s) (second option in this case), with or without selection of any correct option(s) will result in −2 marks.

5. Select correct statement(s):

- (A) Orbital angular momentum depends on two quantum number is ℓ and $m\ell$.
- (B) Total energy does not very in 1s orbital of H-atom with distance from nucleus.
- (C) Whenever a radiation intacts with matter it displays wave nature while when it propagates it exhibit particle nature.
- (D) Boundary surface diagram of p atomic orbitals is dumbell but $|\psi^2|$ is not same at different points on boundary surface.

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6.



X = Mole fraction of liquid A in liquid solution.

Y = Mole fraction of vapour A in vapour mixture.

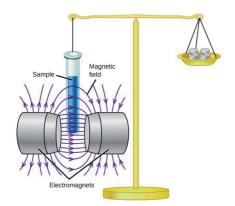
Length of line segments KL and LM are in the ratio of 2 : 3.

[Given : $P_T = 480 \text{ mm Hg}$, $P_A^{\circ} = 300 \text{ mm of Hg}$, $P_B^{\circ} = 600 \text{ mm of Hg}$]

- (A) X is 0.4
- (B) Y is 0.25
- (C) P is 428.57 mmHg.
- (D) Moles of A in vapour phase at 480 mmHg is 0.4, if total moles of A and B are 1 and 3 respectively.
- 7. The possible type of ions that can be produced by oxides of Vanadium on treatment with acidic or alkaline solutions is/are.
 - $(A) VO^{+}$
 - (B) VO²⁺
 - (C) VO_2^+
 - (D) VO_4^{3-}

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8.



The above apparatus shows a sample kept in presence of an electromagnet against some amount of weight on the right side.

Assume weight of all samples used in different experiment is same then which of the following sample(s) will require significantly more weight to be kept on right side to balance as compared to the weight required to balance the sample of $H_2O(\ell)$. (The sample can be in either solid or liquid or gas)

- (A) $C_6H_6(\ell)$
- (B) $K_4[Fe(CN)_6](s)$
- (C) $K_3[Fe(CN)_6](s)$
- (D) $ClO_2(g)$
- 9. Sucralose is artificial sweetner, the preparation of sucralose involves a multi-step chemical reaction where sucrose is selectively chlorinated by substituting three specific hydroxyl groups by 3 atoms of Cl.

Select the correct statement(s) about sucralose.

- (A) It is 600 times sweeter than cane sugar.
- (B) It has 9 chiral carbons.
- (C) By weight 40% Cl is present in sucralose.
- (D) Sucrose and sucralose both do not give positive test with Tollen's reagent.

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10. An organic acid A $(C_{11}H_{12}O_2)$ can easily be oxidized by H^{\bigoplus} , KMnO₄ to a dibasic acid which reacts with ethyleneglycol to produce a polymer dacron. Upon ozonolysis, A gives an aliphatic ketone as one of the product.

A gives product B with following reagents.

$$C_{11}H_{12}O_{2} \xrightarrow{\begin{subarray}{c} (i) \ H_{2} \ , Pd-C \\ (ii) \ NH_{3} \ , \Delta \\ \hline (iii) \ Br_{2} \ , NaOH, \Delta \\ (iv) \ CHCl_{3} \ , KOH, \Delta \\ (v) \ H_{2} \ , Pd-C \\ \hline \end{subarray}} (B)$$

Correct statement(s) about A is/are:

- (A) It gives positive bromine water test.
- (B) It gives effervescence with NaHCO₃.
- (C) It give violet coloured complex with neutral FeCl₃.
- (D) It gives positive test with 2,4-Dinitrophenyl hydrazine (2,4-DNP)

Note: No questions have been asked in the section II of this paper. Please leave section II blank on the OMR answer sheet.

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SECTION-III: (Maximum Marks: 24)

• This section contains **EIGHT (08)** questions.

• The answer to each question is a **SINGLE DIGIT INTEGER** ranging from 0 to 9, both inclusive.

• For each question, enter the correct integer value of the answer in the place designated to enter the answer.

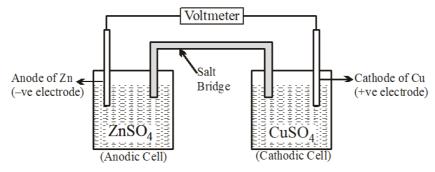
• For each question, marks will be awarded in <u>one of the following categories</u>:

Full Marks : +3 If only the correct answer is given.

Zero Marks : 0 If no answer is given.

Negative Marks : -1 In all other cases

The most popular electrochemical cell, Daniel cell was originally developed by the English chemist John F.
 Daniel. The general assembly of the cell is as given below:



An undergraduate student made up a Daniel cell using 100 cm³ each of 0.100 M CuSO₄ and 0.100 M ZnSO₄ solution respectively. The two compartments are connected by suitable salt bridge.

[Given:
$$E_{Cu^{2+}/Cu}^0 = 0.34 \, V$$
, $E_{Zn^{2+}/Zn}^0 = -0.76 \, V$, $\frac{2.303 RT}{E} = 0.06$, $\log 2 = 0.3$]

A lab mate of the student asked her for some solid CuCl₂. While she was lifting the bottle from a shelf, the lid of the bottle slipped and some amount of CuCl₂ fell in the CuSO₄ compartment without changing the volume. She measured the emf of the cell again and found that it had increased by 9 mV. She used this data to calculate the amount of CuCl₂ that had split in the compartment. Calculate the mass of CuCl₂ that had split into the Daniel cell?

If the answer is 'x' gm then the value of $\frac{x}{0.45}$ is _____. (Molecular mass of CuCl₂ = 135 g)

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2. A vertical cylinder closed from both ends is equipped with an easily moving piston dividing the volume into two parts, each containing one mole of air. In equilibrium at 320 K, the volume of the upper part is 4.0 times greater than that of the lower part. At what temperature (in kelvin) will the ratio of volume of upper part to lower part will be 3?

If the answer is T, then the value of $\left(\frac{T}{50}\right)$ is.

3. An athlete in a gymnasium room lifts a 50 kg mass through a vertical distance of 2.0 m; $g = 9.8 \text{ ms}^{-2}$. The mass is allowed to fall through 2.0 m distance while coupled to an electrical generator. The electrical generator produces an equal amount of electrical work. This electrical work is used to produce aluminum by Hall's process involving the change,

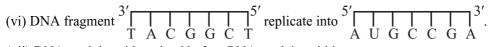
$$Al_2O_3$$
 (molten) + $3C(s) \rightarrow 2Al(1) + 3CO(g)$; $\Delta G^{\circ} = 588$ kJ/mol.

How many times (in Hundred) must the athlete lift the 50 kg mass and drop to couple the generator to produce sufficient Gibbs free energy to produce 27g Al?

- 4. Three moles of copper(II) sulphide is treated with excess dilute HNO₃ to yield a precipitate "X" and gas "Y".
 "X" is then separately treated with excess dilute HNO₃ again along with heating to yield gas "Y" again. The total moles of gas "Y" produced will be.
- Total number of degenerate orbitals in 2nd excited state of Be³⁺ will be _____.
 (Assume absence of external electric and magnetic filed)

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- **6.** How many total statements are correct about DNA.
 - (i) DNA has specific sequence of nucleotides.
 - (ii) DNA synthesis takes place from 5' end to 3' end.
 - (iii) DNA double helix model is the secondary structure of DNA
 - (iv) β -D ribose sugar is present in nucleotide of DNA.
 - (v) Phosphodiester linkage is present in DNA.



- (vii) DNA nucleic acid evolved before RNA nucleic acid in nature.
- (viii) deoxy Adenosine, deoxy guanosine, deoxy thymidine and deoxy cytidine nucleoside are present in nucleotides of DNA.
- (ix) Many genes are present in DNA which have information of specific protein in form of specific sequence of nucleotides.
- 7. Hydrolysis of tetrapeptide gives two asparagine, and two glycine amino acids. Calculate the value of X.

If
$$X = 0.3 Z$$

Where Z is % of nitrogen by weight in tetrapeptide.

8. $\begin{array}{c} CH_2OH \\ Alcohol \\ 2^{\circ} \text{ or } 3^{\circ} \end{array} \times X \xrightarrow{(i) O_3} W_1 + W_2 \\ \hline OH/\Delta \\ Ph - C = CH - C - Ph \\ CH_3 & O \end{array}$

How many total 2° and 3° alcohol with molecular formula $C_{15}H_{16}O$ can perform the above reactions.

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PART-3: MATHEMATICS

SECTION-I (i): (Maximum Marks: 12)

• This section contains **FOUR (04)** questions.

- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme :

Full Marks : +3 If ONLY the correct option is chosen.

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered)

Negative Marks : -1 In all other cases

1. If $\int \frac{\left(\frac{1}{x} + \frac{1}{x^2}\right)(x-1) dx}{\left(\frac{1}{x^4} + \frac{1}{x^2}\right)\sqrt{(x^4 - x^3 + x^2)(x^4 + x^3 + x^2)}} = \sec^{-1}(f(x)) + c, \ f(1) = 2 \text{ then local minimum value of}$

f(x) is

(Where 'c' is the constant of integration)

(A) 2

(B) 5

(C) 6

- (D) 8
- 2. Consider three sets $E_1 = \{1, 3, 4\}$, $F_1 = \{1, 4, 5\}$ and $G_1 = \{3, 4, 5, 6\}$. Two elements are chosen at random, without replacement, from the set E_1 , and let S_1 denote the set of these chosen elements.

Let $E_2 = E_1 - S_1$ and $F_2 = F_1 \cup S_1$. Now two elements are chosen at random, without replacement, from the set F_2 and let S_2 denote the set of these chosen elements.

Let $G_2 = G_1 \cup S_2$. Finally, two elements are chosen at random, without replacement, from the set G_2 and let S_3 denote the set of these chosen elements.

Let $E_3 = E_2 \cup S_3$. Given that $E_1 = E_3$, let p be the conditional probability of the event $S_1 = \{1, 3\}$. Then the value of p is

- (A) $\frac{4}{5}$
- (B) $\frac{3}{5}$
- (C) $\frac{1}{5}$
- (D) $\frac{2}{5}$

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3. Let θ_1 , θ_2 , ..., θ_{100} be positive valued angles (in radian) such that $\sum_{i=1}^{100} \theta_i = 2\pi$. Define the complex numbers $z_1 = e^{i\theta_1}$ and $z_k|z_{k-1}| = 2^{k-1}z_{k-1}e^{i\theta_k}$ for k = 2, 3, ..., 100, where $i = \sqrt{-1}$. Consider the statements P and Q given below:

$$P: |z_2-z_1| + |z_3-z_2| + ... + |z_{100}-z_{99}| + |z_1-z_{100}| \geq 2^{101} - 2$$

$$Q: \left| 2^{98}z_2 - 2^{99}z_1 \right| + \left| 2^{97}z_3 - 2^{98}z_2 \right| + \ldots \left| z_{100} - 2z_{99} \right| + \left| 2^{99}z_1 - z_{100} \right| \geqslant 2^{100}\pi$$

- (A) P is TRUE and Q is FALSE
- (B) Q is TRUE and P is FALSE
- (C) both P and Q are TRUE
- (D) both P and Q are FALSE
- 4. Let a, b and c are real numbers such that the system of linear equations

$$x + y + z = a$$

$$x + 5y - z = b$$

$$x - y + 2z = c + 2$$
 is consistent.

- Let |M| represent the determinant of the matrix $M = \begin{bmatrix} a & -2 & b \\ 2 & 1 & c \\ 1 & 0 & 3 \end{bmatrix}$. Let 'P' be the plane containing all those
- (a, b, c) for which above system of linear equations is consistent and 'D' be the square of distance of the point (1, 1, 1) from the plane 'P'. Then the value of |M| + 14D is
- (A) 32
- (B) 16
- (C) 20
- (D) 12

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SECTION-I (ii): (Maximum Marks: 24)

• This section contains **SIX (06)** questions.

- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s)

• Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 If only (all) the correct option(s) is (are) chosen.

Partial Marks : +3 If all the four options are correct but ONLY three options are chosen.

Partial Marks : +2 If three or more options are correct but ONLY two options are chosen and

both of which are correct.

Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a

correct option.

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered).

Negative Marks : -2 In all other cases.

- For Example: If first, third and fourth are the ONLY three correct options for a question with second option being an incorrect option; selecting only all the three correct options will result in +4 marks. Selecting only two of the three correct options (e.g. the first and fourth options), without selecting any incorrect option (second option in this case), will result in +2 marks. Selecting only one of the three correct options (either first or third or fourth option), without selecting any incorrect option (second option in this case), will result in +1 marks. Selecting any incorrect option(s) (second option in this case), with or without selection of any correct option(s) will result in −2 marks.
- 5. Let $f: (0, \frac{\pi}{2}) \to R$ satisfies differential equation $xf'(x) + (x \tan x + 1) f(x) = \sec x \& f(\frac{\pi}{4}) = 0$, then choose correct option(s)

(A)
$$f\left(\frac{\pi}{3}\right) = \frac{3\left(\sqrt{3}-1\right)}{2\pi}$$

- (B) f(x) = 1 has a solution
- (C) Area bounded by g(x) = xf(x), x-axis from $x = \frac{\pi}{4}$ to $x = \frac{\pi}{2}$ is $(\sqrt{2} 1)$ square units
- (D) g(x) = xf(x) is a bounded function

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- 6. Consider two circles $S_1 : x^2 + y^2 8x = 0$ and $S_2 : x^2 + y^2 + 2x = 0$
 - (A) Number of common tangents of S_1 and S_2 is 3
 - (B) Radical axis of S_1 and S_2 is x = 3
 - (C) Equation of circumcircle of the triangle formed by point of intersection of direct common tangents and the points where common tangents touches S_2 is $x^2 + y^2 + \frac{11}{3}x + \frac{8}{3} = 0$
 - (D) Equation of circumcircle of the triangle formed by point of intersection of direct common tangents and the points where common tangents touches S_1 is $x^2 + y^2 + \frac{8}{3}x + \frac{11}{3} = 0$
- 7. Let $f: R \to (0, 1)$ be a continuous function. Then which of the following function(s) must has(have) the value zero at some point in the interval (0, 1)?
 - (A) $x^{10} f(2x)$
 - (B) $x^2 \int_{0}^{x} f(t) dt$
 - (C) $\left(\int_{0}^{\frac{\pi}{2}-x} f(3t) \sin t \, dt\right) x$
 - (D) $\sqrt{x^3} \int_{0}^{x} \sqrt[3]{f(t)} dt$
- 8. Let $g(x) = \begin{cases} 2(x+1) &, & -\infty < x \leqslant -1 \\ \sqrt{1-x^2} &, & -1 < x < 1 \\ |||x|-1|-1| &, & 1 \leqslant x < \infty \end{cases}$, then choose the correct option(s):
 - (A) g(x) is non-differentiable at exactly three points
 - (B) g(x) is continuous in $(-\infty, 1]$
 - (C) g(x) is differentiable in $(-\infty, -1)$
 - (D) g(x) has discontinuity at x = 1 but continuous at x = -1

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- 9. If $z^{11} = 1$, then which of the following is(are) true?
 - (A) There are exactly 5 complex numbers for which $\cos(\arg(z)) < 0$
 - (B) The value of $|1 \alpha_i|^2 + |1 + \alpha_i|^2 = 4$ where α_i is non-real roots of $z^{11} = 1$ and $i = 1, \dots, 10$
 - (C) The range of |1 + z| contains 6 distinct elements
 - (D) For non-real z, arg $\left(\frac{1+z}{1-z}\right)$ contains 10 distinct elements
- 10. Let A and B be two square matrices of order 3 then which of the following statement(s) is(are) correct?
 - (A) ABA^T is symmetric matrix
 - (B) AB BA is skew symmetric matrix
 - (C) If $B = |A|A^{-1}$, $|A| \neq 0$ then $adj.(A^{T}) B$ is a skew symmetric matrix
 - (D) If $B + A^{T} = \mathbf{O}$ and A is skew symmetric matrix then B^{15} is also skew symmetric matrix

Note: No questions have been asked in the section II of this paper. Please leave section II blank on the OMR answer sheet.

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SECTION-III: (Maximum Marks: 24)

• This section contains **EIGHT (08)** questions.

• The answer to each question is a **SINGLE DIGIT INTEGER** ranging from 0 to 9, both inclusive.

• For each question, enter the correct integer value of the answer in the place designated to enter the answer.

• For each question, marks will be awarded in <u>one of the following categories</u>:

Full Marks : +3 If only the correct answer is given.

Zero Marks : 0 If no answer is given.

Negative Marks : -1 In all other cases

- 1. If N denotes the number of positive integral solutions of equation $xy = 2^3 \cdot 3^4 \cdot 5^6 \cdot (x + y)$, then $\frac{N}{91}$ is equal to
- 2. Three distinct numbers are chosen one by one without replacement form the set $\{1,2,3,.....9\}$. If it is known that sum of first two chosen numbers is even, then $\frac{p}{q}$ is the probability that sum of all three numbers is even. Then (q-2p) is equal to (where p & q are coprime numbers)
- 3. Consider the parabola $y^2 = 4x$. Let P and Q be two points (4,-4) and (9,6) on the parabola. Let R be a moving point on the arc of the parabola between P and Q. If 'A' denote the maximum area of ΔRPQ then $\left[\frac{\sqrt{5A}}{2}\right]$ is equal to (where [.] denotes greatest integer function)
- 4. Evaluate

$$\lim_{x \to 0} \lim_{n \to \infty} \frac{\left[(n+x) \left(n + 2x \right) \dots \left(n + 2nx \right) \left(\tan^2 \left(\frac{\pi}{2n} \right) \dots \tan^2 \left(\frac{2\pi}{2n} \right) \dots \tan^2 \left(\frac{3\pi}{2n} \right) \dots \tan^2 \left(\frac{(n-1)\pi}{2n} \right) \right) \right]^{\frac{1}{2n}}}{n - \sqrt{n}}$$

- 5. Let S_1 and S_2 are focii of the hyperbola with length of transverse axis equal to 20. Perpendicular distance of S_1 from normal at P is 20. If the normal at P divides the line segment joining S_1 and S_2 in ratio 5: 1 externally. If the square of length of semi-conjugate axis is λ , then the value of $\frac{\lambda}{5}$ is
- 6. Suppose $\det\begin{bmatrix} \sum\limits_{k=1}^{n}k & \sum\limits_{k=1}^{n}{}^{n}C_{k}k^{2} \\ \sum\limits_{k=1}^{n}{}^{n}C_{k}k & \sum\limits_{k=0}^{n}{}^{n}C_{k}3^{k} \end{bmatrix} + \frac{n(n+1).4^{n}}{2} = 0$, holds for some positive integer n. Then $\frac{9}{251}\sum\limits_{k=1}^{n}\frac{{}^{n}C_{k}}{k+1} \text{ equals}$
- 7. Let \vec{a} , \vec{b} and \vec{c} be vectors in three-dimensional space, where \vec{a} . $\vec{a} = 1$, \vec{b} . $\vec{b} = 2$, \vec{c} . $\vec{c} = 9$, \vec{a} . $\vec{c} = 2$, \vec{b} . $\vec{c} = 1$. If the volume of the parallelopiped, whose adjacent sides are represented by the vectors \vec{a} , \vec{b} and \vec{c} , is $\frac{\sqrt{85}}{3}$, then the value of $\frac{9}{83} |\vec{a} + \vec{b} + \vec{c}|^2$ is
- 8. In a class of 5 students average weight of 4 lightest students is 40 kgs, Average weight of 4 heaviest students is 45 kgs. The difference between maximum and minimum possible average weight overall (in kg) is

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NAME OF THE CANDIDATE	
FORM NO	
I have read all the instructions and shall abide by them.	I have verified the identity, name and Form number of the candidate, and that question paper and ORS codes are the same.
Signature of the Candidate	Signature of the Invigilator

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