

# Competishun

52/6, Opposite Metro Mas Hospital, Shipra Path, Mansarovar

**Date:** 14/10/2024

**Time:** 3 hours

**Max. Marks:** 300

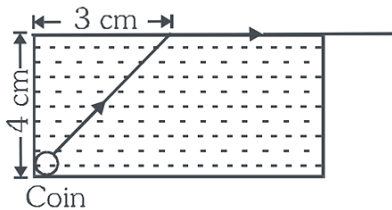
## Comprehensive Cumulative Test CT-1 (2025)

### Physics

#### Single Choice Question

- Q1** A particle is projected up the incline such that its component of velocity along the incline is 10 m/s. Time of flight is 2 second and maximum perpendicular distance during the motion from the incline is 5m. Then velocity of projection will be :-  
 a) 10m/s                      b)  $10\sqrt{2}$  m/s                      c)  $5\sqrt{5}$  m/s                      d) none of these

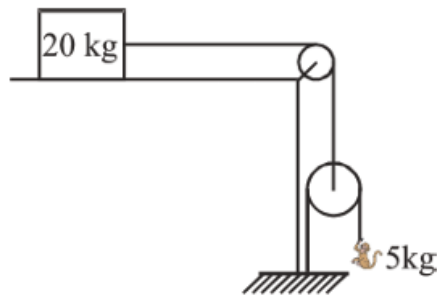
- Q2** A small coin is resting on the bottom of a beaker filled with a liquid. A ray of light from the coin travels up to the surface of the liquid and moves along its surface (see figure).



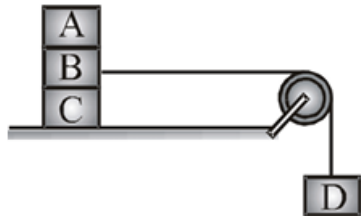
How fast is the light travelling in the liquid ?

- a)  $1.2 \times 10^8$  m/s                      b)  $1.8 \times 10^8$  m/s                      c)  $2.4 \times 10^8$  m/s                      d)  $3.0 \times 10^8$  m/s
- Q3** An object is placed in front of a convex mirror at a distance of 50cm. A plane mirror is introduced covering the lower half of the convex mirror. If the distance between the object and the plane mirror is 30 cm, it is found that there is no parallax between the images formed by the two mirrors. What is the radius of curvature of the convex mirror?  
 a) 12.5 cm                      b) 25 cm                      c) 75 cm                      d) 100 cm

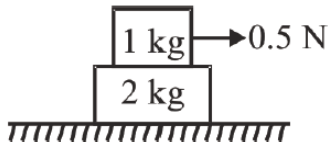
- Q4** What will be the acceleration of 20kg blocks. If the monkey climbs up the rope with acceleration of  $2\text{ m/s}^2$ . If all surfaces are smooth string and pulley are light.:-



- a)  $2\text{ m/s}^2$       b)  $3\text{ m/s}^2$       c)  $4\text{ m/s}^2$       d) 0
- Q5** These blocks A,B and C of equal mass  $m$  are placed one over the other on a smooth horizontal ground as shown in figure. Coefficient of friction between any two blocks of A,B and C is  $1/2$ . The maximum value of mass of block D so that the blocks A, B and C move without slipping over each other is :-



- a)  $6m$       b)  $5m$       c)  $3m$       d)  $4m$
- Q6** A force of  $0.5\text{ N}$  is applied on the upper block as shown in figure. The coefficient of static friction between the two blocks is  $0.1$  and that between the lower block and the surface is zero. The work done by the lower block on the upper block for a displacement of  $3\text{ m}$  of the upper block is :-

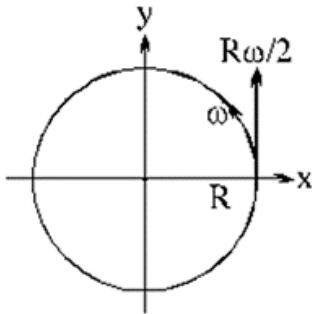


- a) 1 J      b) -1 J      c) 2 J      d) -2 J
- Q7** A block of mass  $m$  is at rest with respect to a lift when placed on inclined plane of inclination  $\theta$  inside the lift. If lift move upward at constant velocity  $v$  then work done by friction force on block in  $t$  time is :-
- a) Zero      b)  $mgt^2 v \cos^2 \theta$       c)  $mgtv \sin^2 \theta$       d)  $\frac{1}{2} mgtv \sin 2\theta$

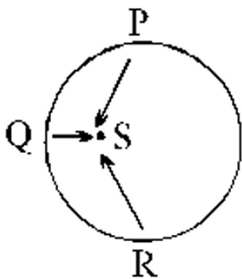
- Q8**  $F = 2x^2 - 3x - 2$ . Choose correct option :-

- a)  $x = -1/2$  is position of stable equilibrium  
 b)  $x = 2$  is position of stable equilibrium  
 c)  $x = -1/2$  is position of unstable equilibrium  
 d)  $x = 2$  is position of neutral equilibrium

- Q9** A body moves in a circle of radius  $R$  having centre at origin, with an angular velocity  $\omega$  in the x-y plane as shown in the figure. Another body moves parallel to y-axis with constant velocity  $(R\omega/2)$ . At time  $t = 0$ , both particles are at  $(R,0)$ . The value of time  $t$ , when first body has velocity only along positive x-axis w.r.t. the second body is



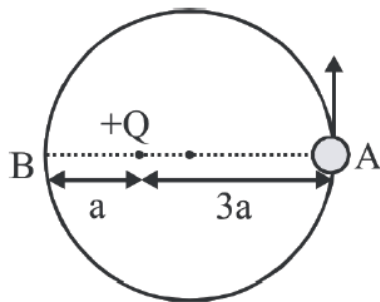
- a)  $\pi / 6\omega$       b)  $5\pi / 3\omega$       c)  $5\pi / 6\omega$       d) None of these
- Q10** An object moves counter-clockwise along the circular path shown below. As it moves along the path its acceleration vector continuously points towards point S. The object



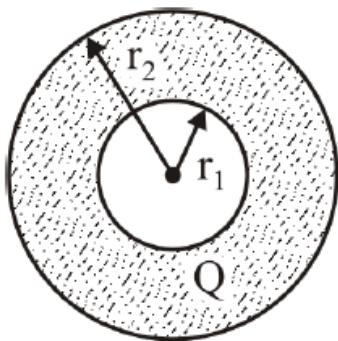
- a) speeds up at P,Q and R      b) slows down at P,Q and R  
c) speeds up at P and slows down at R      d) slows down at P and speeds up at R
- Q11** Which one of the following statement does not hold good when two balls of masses  $m_1$  and  $m_2$  undergo elastic collision?
- a) If  $m_1 = m_2$  and collision is oblique then after collision they move perpendicular to each other  
b) When  $m_1 \gg m_2$  and  $m_2$  at rest, after collision the ball of mass  $m_2$  moves with double the velocity of  $m_1$ .  
c) When  $m_1 = m_2$  and  $m_2$  at rest, there will be maximum transfer of kinetic energy.  
d) When collision is oblique and  $m_2$  at rest with  $m_1 = m_2$ , after collision the balls move in opposite directions.
- Q12** A ball P of mass  $m$  moving with velocity  $u$  collides head on with another identical ball Q at rest. If the coefficient of restitution is  $e$ , then the ratio of velocities of P and Q after the collision is :-

- a)  $\frac{1+e}{1-e}$       b)  $\frac{1-e}{1+e}$       c)  $\frac{1+e}{2}$       d)  $\frac{1-e}{2}$

- Q13** The diagram shows a small bead of mass  $m$  carrying charge  $q$ . The bead can freely move on the smooth fixed ring placed on a smooth horizontal plane. In the same plane a charge  $+Q$  has also been fixed as shown. The potential at the point A due to  $+Q$  is  $V$ . The minimum velocity with which the bead should be projected from the point A so that it can complete a circle should be ( $K = 1/4\pi\epsilon_0$ )



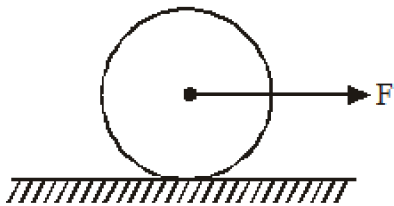
- a)  $\sqrt{\frac{4KQq}{ma}}$       b)  $\sqrt{\frac{6KQq}{ma}}$       c)  $\sqrt{\frac{4KQq}{3ma}}$       d)  $\sqrt{\frac{KQq}{ma}}$
- Q14** A charge  $Q$  is distributed uniformly within the material of a hollow sphere of inner and outer radii  $r_1$  and  $r_2$  (See figure). The electric field at distance  $x$  from centre for  $r_1 < x < r_2$  will be :-



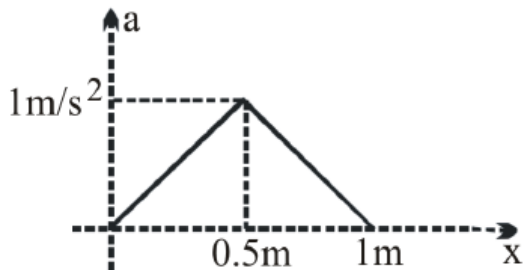
- a)  $\frac{Q(x^3 - r_1^3)}{4\pi\epsilon_0 x^2 r_2^3}$       b)  $\frac{Q(x^3 - r_1^3)}{4\pi\epsilon_0 x^2 (r_2^3 - r_1^3)}$       c)  $\frac{Qx}{4\pi\epsilon_0 (r_2^3 - r_1^3)}$       d)  $\frac{Q(x^3 - r_1^3)}{4\pi\epsilon_0 r_1^2 (r_2^2 - r_1^2)}$
- Q15** An asteroid of mass  $m$  is approaching earth initially at a distance of  $10 R_e$  from surface of earth and speed  $V_i$ . It hits the earth with a speed  $V_f$  ( $R_e$  and  $M_e$  are radius and mass of earth), then-
- a)  $V_f^2 = V_i^2 + \frac{2Gm}{MeR} \left(1 - \frac{1}{10}\right)$       b)  $V_f^2 = V_i^2 + \frac{2GMe}{Re} \left(1 + \frac{1}{10}\right)$       c)  $V_f^2 = V_i^2 + \frac{2GMe}{Re} \left(1 - \frac{1}{10}\right)$
- d)  $V_f^2 = V_i^2 + \frac{2GM}{Re} \left(1 - \frac{1}{10}\right)$
- Q16** Two bodies of masses  $m_1$  and  $m_2$  are initially at rest at infinite distance apart. They are then allowed to move towards each other under mutual gravitational attraction. Their relative velocity of approach at a separation distance  $r$  between them is:-

- a)  $\left[2G \frac{(m_1 - m_2)}{r}\right]^{1/2}$       b)  $\left[\frac{2G}{r} (m_1 + m_2)\right]^{1/2}$       c)  $\left[\frac{r}{2G(m_1 m_2)}\right]^{1/2}$       d)  $\left[\frac{2G}{r} m_1 m_2\right]^{1/2}$

- Q17** A circular platform is mounted on a frictionless vertical axle passing through centre. Its radius  $R = 2\text{m}$  and moment of inertia about the axis is  $200 \text{ kg-m}^2$ . It is initially at rest. A  $50 \text{ kg}$  man stands on the edge of platform and begins to walk along the edge at speed of  $1 \text{ m/sec}$  relative to the ground. Time taken by the man to complete one revolution is:-
- a)  $2\pi \text{ sec}$                       b)  $\frac{\pi}{2} \text{ sec}$                       c)  $\pi \text{ sec}$                       d)  $\frac{3\pi}{2} \text{ sec}$
- Q18** When the kinetic energy of a body executing S.H.M. is  $1/3$  of the potential energy. The displacement of the body is  $x$  percent of the amplitude, where  $x$  is :-
- a) 33                      b) 87                      c) 67                      d) 50
- Q19** A solid sphere of mass  $m$  is lying at rest on a rough horizontal surface. The coefficient of friction between the ground and sphere is  $\mu$ . The maximum value of  $F$ , So that the sphere will not slip, is equal to :



- a)  $\frac{7}{5} \mu mg$                       b)  $\frac{4}{7} \mu mg$                       c)  $\frac{5}{7} \mu mg$                       d)  $\frac{7}{2} \mu mg$
- Q20** A body initially at rest, starts moving along x-axis in such a way so that its acceleration vs displacement plot is as shown in figure. The maximum velocity of particle is :-

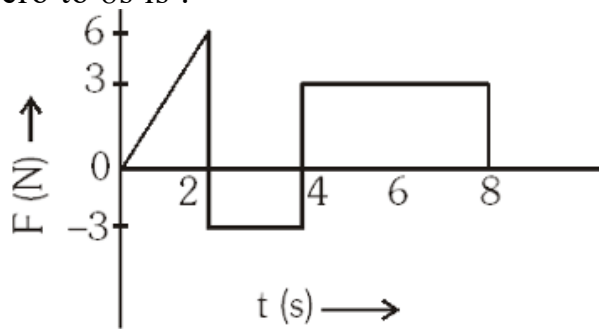


- a)  $1 \text{ m/s}$                       b)  $6 \text{ m/s}$                       c)  $2 \text{ m/s}$                       d) None

### Numerical

- Q21** A compound microscope has an eyepiece of focal length  $10 \text{ cm}$  and an objective of focal length  $4\text{cm}$ . Calculate the magnification, if an object is kept at a distance of  $5 \text{ cm}$  from the objective so that final image is formed at the least distance of distinct vision ( $20 \text{ cm}$ ) :-

- Q22** The force 'F' acting on a particle of mass 'm' is indicated by the force-time graph shown below. The change in momentum of the particle over the time interval from zero to 8s is :-

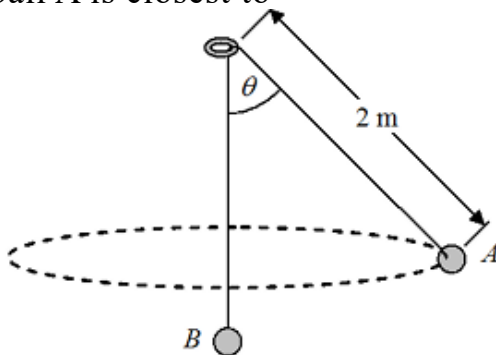


- Q23** The potential energy of a 1 kg particle free to move along the x-axis is given by :-

$$U(x) = \left( \frac{x^4}{4} - \frac{x^2}{2} \right) \text{ J}$$

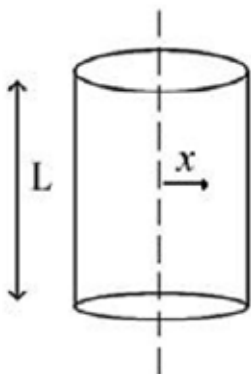
The total mechanical energy of the particle is 2 J. Then the maximum speed (in m/s) is  $\frac{N}{\sqrt{2}}$ . Then N is :-

- Q24** Two very small balls A and B of masses 4.0 kg and 5.0 kg are affixed to the ends of a light inextensible cord that passes through a frictionless ring of negligible radius compared to the length of the cord. The ring is fixed at some height above the ground. Ball A is pulled aside and given a horizontal velocity so that it starts moving on a circular path parallel to the ground, keeping ball B in equilibrium as shown. Speed of the ball A is closest to

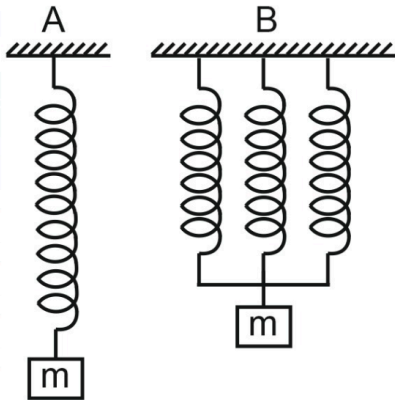


- Q25** A long cylindrical volume contains a uniformly distributed charge of density  $\rho \text{ Cm}^{-3}$ .

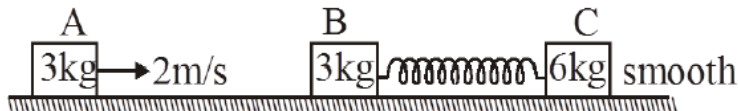
The electric field inside the cylindrical volume at a distance  $x = \frac{2\epsilon_0}{\rho} \text{ m}$  from its axis is \_\_\_\_\_  $\text{Vm}^{-1}$



- Q26** The mass of planet is  $1/9$  of the mass of the earth and its radius is half that of the earth. If a body weight  $9\text{ N}$  on the earth. Its weight on the planet would be :- (in N)
- Q27** The moment of inertia of a square lamina about the perpendicular axis through its centre of mass is  $20\text{ kg-m}^2$ . Then, its moment of inertia about an axis touching its side and in the plane of the lamina will be :-
- Q28** The rotational kinetic energy of two bodies of moments of inertia  $9\text{ kg-m}^2$  and  $1\text{ kg-m}^2$  are same. The ratio of their angular momentum is :-
- Q29** The springs in fig. A and B are identical but length in A is three times each of that in B. The ratio of period  $T_A/T_B$  is :-



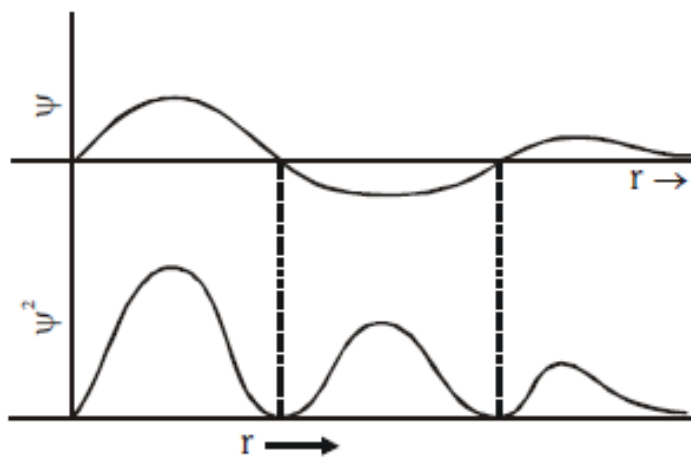
- Q30** For shown situation, if collision between block A and B is perfectly elastic, then find the maximum energy stored in spring in joules.



## Chemistry

### Single Choice Question

**Q31** The wave function  $\psi$  vs radial distance ( $r$ ) and square of wave function  $(\psi)^2$  vs radial distance ( $r$ ) graph of certain orbital is given. Identify the orbital.



a) 3 s

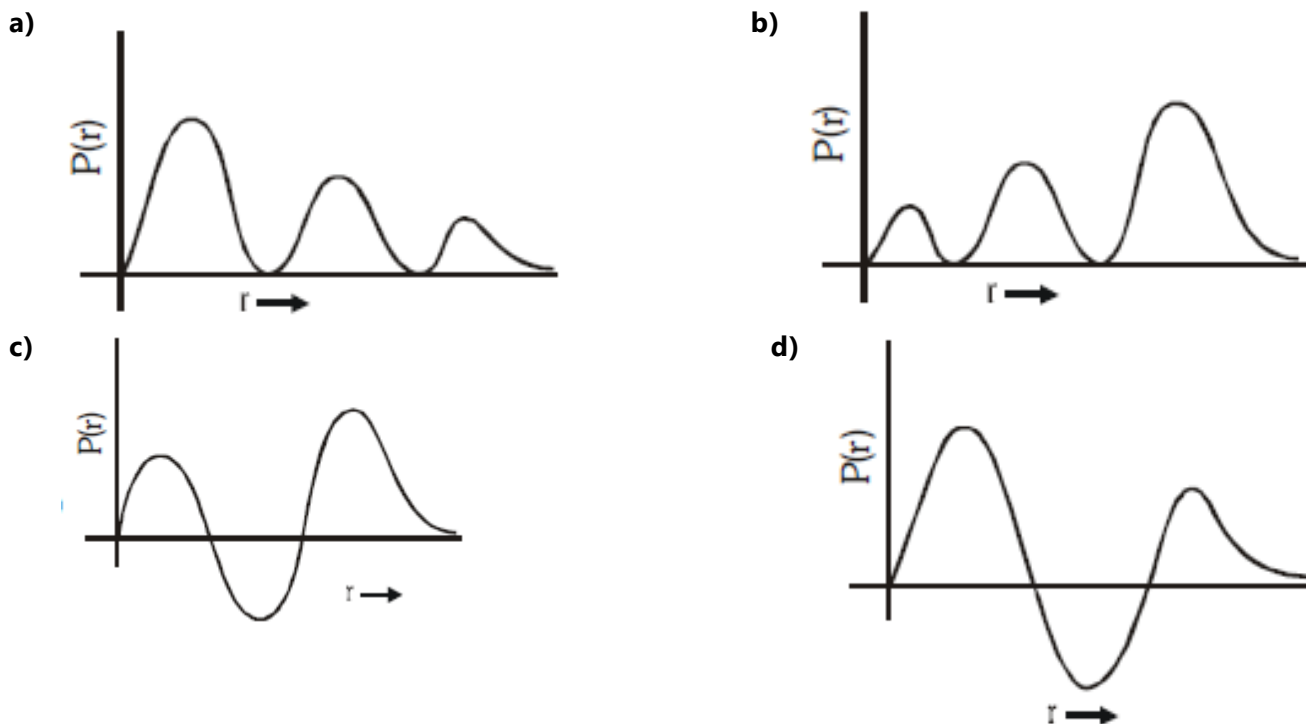
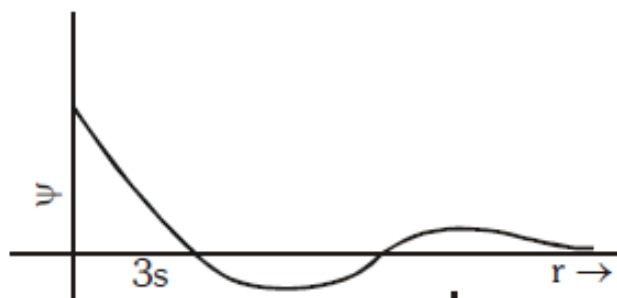
b) 4 d

c) 3p

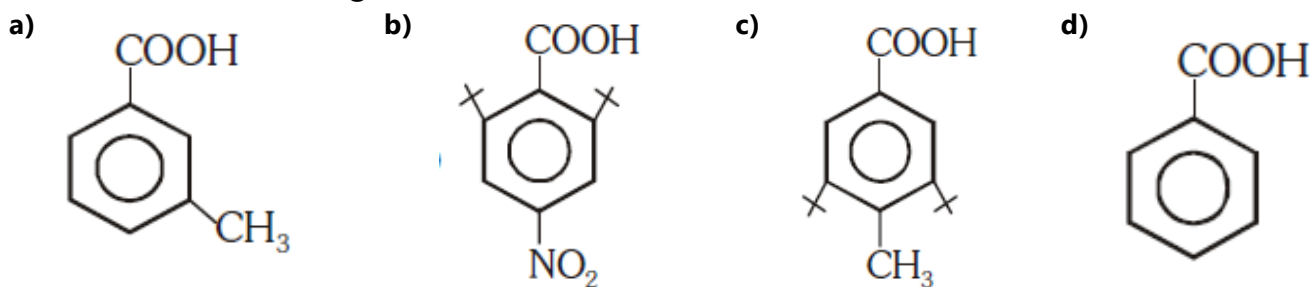
d) 4 p



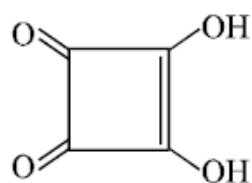
- Q32** The wave function ( $\psi$ ) versus radial distance ( $r$ ) curve for certain orbital is given. Predict the shape of  $\psi^2 \cdot 4\pi r^2$  (radial probability distribution function) versus  $r$  graph.



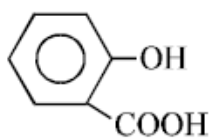
- Q33** Which of the following is most acidic :



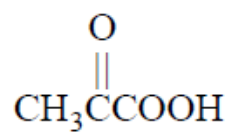
- Q34** Consider the following compound



I



II

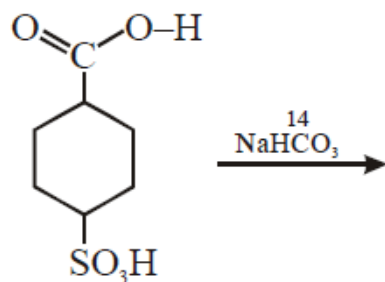


III

Which of the above compounds reacts with  $\text{NaHCO}_3$  giving  $\text{CO}_2$

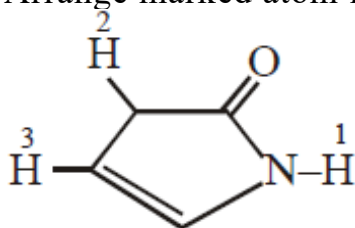
- a) I, II and III      b) I and III      c) II and III      d) I and II

**Q35** In given reaction Gas liberated is/are



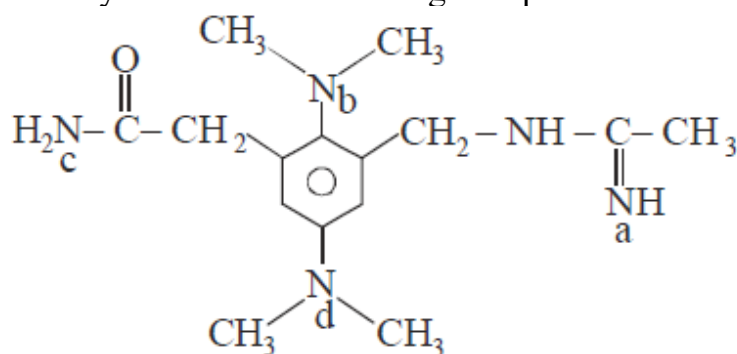
- a)  $\text{CO}_2$  &  $\text{SO}_3$       b)  $\text{SO}_3$  &  $^{14}\text{CO}_2$       c)  $^{14}\text{CO}_2$  only      d)  $\text{SO}_2$  only

**Q36** Arrange marked atom in decreasing order of acidic strength



- a)  $1 > 2 > 3$       b)  $3 > 2 > 1$       c)  $2 > 1 > 3$       d)  $2 > 3 > 1$

**Q37** Basicity order of N following compound is :



- a)  $b > d > a > c$       b)  $a > b > d > c$       c)  $a > b > c > d$       d)  $a > c > b > d$

**Q38** 10 ml of  $\frac{M}{200} \text{H}_2\text{SO}_4$  is mixed with 40 ml of  $\frac{M}{200} \text{H}_2\text{SO}_4$ . The pH of the resulting solution is

- a) 1      b) 2      c) 2.3      d) none of these

**Q39**  $\text{Na}_3\text{PO}_4$  which should be added in 10 L of  $1.0 \times 10^{-5} \text{M} - \text{BaCl}_2$  solution without any precipitation of  $\text{Ba}_3(\text{PO}_4)_2$  is  $[\text{Ksp}^2 \text{ of } \text{Ba}_3(\text{PO}_4)_2] = 4 \times 10^{-23}$

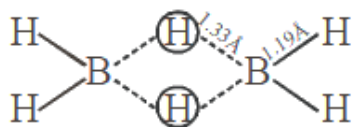
- a)  $2 \times 10^{-4} \text{ gm}$       b) 0.328 gm      c) 0.164 gm      d) 0.82 gm

**Q40** The electronic configuration of elements X and Z are  $1s^2 2s^2 2p^6 3s^2 3p^5$  and  $1s^2 2s^2 2p^5$  respectively What is the position of element X with respect to position of Z in the periodic table -

- a) Just below element Z      b) Just above Z      c) Left to the Z      d) right to the Z

- Q41** Decreasing ionization potential for K, Ca & Ba is  
a)  $\text{Ba} > \text{K} > \text{Ca}$     b)  $\text{Ca} > \text{Ba} > \text{K}$     c)  $\text{K} > \text{Ba} > \text{Ca}$     d)  $\text{K} > \text{Ca} > \text{Ba}$
- Q42** The types of bonds present in  $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$  are  
a) electrovalent and covalent    b) electrovalent, coordinate covalent & H-bond  
c) covalent, coordinate covalent & H-bonds  
d) electrovalent, covalent, coordinate covalent & H-bond
- Q43** If ethylene molecule lies in X -Y plane then nodal planes of the  $\pi$ -bond will lie in  
a) XZ plane    b) YZ plane    c) In a plane that bisects C-C axis    d) XY plane
- Q44** Bond angle and bond polarity are important parameters associated for bonding in molecule.  
Which of the following bond angle order is incorrect.  
a)  $\text{NH}_3 > \text{PH}_3$     b)  $\text{BF}_3 < \text{BH}_3$     c)  $\text{O}(\text{CH}_3)_2 < \text{O}(\text{C}_2\text{H}_5)_2$     d)  $\text{CO}_3^{2-} < \text{CO}_2$
- Q45** Bond angle and bond polarity are important parameters associated for bonding in molecule.  
Which of the following molecule is polar and non-planar  
a)  $\text{CH}_2\text{Cl}_2$     b)  $\text{PCl}_5$     c)  $\text{SO}_2$     d)  $\text{XeF}_4$
- Q46** The pair of species having identical shapes for molecules of both species is  
a)  $\text{XeF}_2, \text{CO}_2$     b)  $\text{BF}_3, \text{PCl}_3$     c)  $\text{PF}_5, \text{IF}_5$     d)  $\text{CF}_4, \text{SF}_4$
- Q47** Which is the incorrect match for the energy distance function for following interaction -  
a) Debye force :  $r^{-6}$     b) Ion-induced dipole interaction :  $r^{-2}$   
c) London force :  $r^{-6}$     d) Keesom force:  $r^{-3}$
- Q48** C-H bond distance is the longest in:  
a)  $\text{C}_2\text{H}_2$     b)  $\text{C}_2\text{H}_4$     c)  $\text{C}_2\text{H}_6$     d)  $\text{C}_2\text{H}_2\text{Br}_2$
- Q49** In which of the following molecule C-C bond length will be highest ?  
a)  $\text{CF}_3 - \text{CF}_3$     b)  $\text{F}_2\text{CH} - \text{CHF}_2$     c)  $\text{FCH}_2 - \text{CH}_2\text{F}$     d)  $\text{CH}_3 - \text{CF}_3$

**Q50** The molecular shape of diborane, is shown



Consider the following statements for diborane :

- (1) Boron is approximately  $sp^3$  hybridised
- (2)  $B-H-B$  angle is  $180^\circ$
- (3) There are two terminal B-H bonds for each boron atom
- (4) There are only 12 bonding electrons available

Of these statements:

- a) 1,3 and 4 are correct
- b) 1,2 and 3 are correct
- c) 2,3 and 4 are correct
- d) 1,2 and 4 are correct

### Numerical

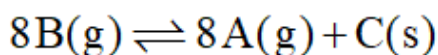
**Q51** Find the total number of following molecule(s) which have all bond lengths are same.  
 $XeF_4$ ,  $SF_4$ ,  $SH_2$ ,  $NO_3^-$ ,  $SiF_4$ ,  $ClF_3$ ,  $PF_2Cl_3$ ,  $XeO_3$ ,  $F_2$

**Q52** Among the following total number of planar molecules is / are  
 $Cl_2O$ ,  $P(CH_3)_3$ ,  $N(CH_3)_3$ ,  $ClO_2$ ,  $CH_3$ ,  $NCl_3$

**Q53** How many compound(s) gives diprotic acid on hydrolysis?  
 $SO_2Cl_2$ ,  $SOCl_2$ ,  $POCl_3$ ,  $XeF_2$ ,  $N_2O_5$ ,  $P_4O_6$ ,  $SF_4$ ,  $BCl_3$

**Q54** The London force is proportional to  $r^{-x}$ , (where  $r$  is inter atomic/molecular distance). What is the value of  $x$ .

**Q55** A vessel contains A(g) and B(g) at 2 atm and 4 atm respectively at TK, the mixture is allowed to attain equilibrium at TK, according to the reaction



At equilibrium,  $\left( \frac{n_A}{n_B} \right)_{eq} = \left( \frac{n_B}{n_A} \right)_{initial}$

Find the value of  $y$  if  $K_c = 2^y$

**Q56** What is the pH of 0.1 M of aq Borax solution ( $K_a$  for  $H_3BO_3 = 2 \times 10^{-10}$ ) ( $\log 2 = 0.30$  [Report your answer nearest integer])

**Q57** Calculate the pH after mixing 1 mole each of  $H_3PO_4$ ,  $NaH_2PO_4$ ,  $Na_2HPO_4$  and  $Na_3PO_4$  For  $H_3PO_4$   $K_{a1} = 10^{-3}$ ,  $K_{a2} = 10^{-7}$ ,  $K_{a3} = 10^{-11}$

- Q58** How many electrons are present in gerade molecular orbital of  $C_2$ .
- Q59** Calculate pH at which  $Mg(OH)_2$  begins to precipitate from a solution containing  $0.1M Mg^{2+}$  ions.  
 $K_{sp}$  of  $Mg(OH)_2 = 10^{-11}$
- Q60** Assuming there no  $2s - 2p$  mixing, the number of paramagnetic species amongst the following :  $H_2, He_2^+, Li_2, Be_2, B_2, C_2, C_2^{2-}, N_2^+, N_2, O_2, O_2^-, S_2$  &  $F_2$  are

## Mathematics

### Single Choice Question

Q61

If the equation  $x^{\log_a x^2} = \frac{x^{k-2}}{a^k}$ ,  $a \neq 0$ , has exactly one solution for  $x$ , then

value(s) of  $k$  are

- a) both integral                      b) irrational                      c) prime                      d) nonreal

Q62

$a, b, c$  are three real number such that  $a^2 + 2c = 7$ ,  $c^2 + 4b = -7$  and  $b^2 + 6a = -14$  then which of the following statement is correct

- a) Roots of the equation  $x^2 + ax + bc = 0$  are real and distinct  
 b) Roots of the equation  $x^2 + ax + bc = 0$  are real and same  
 c) Roots of the equation  $x^2 + ax + bc = 0$  are real and irrational  
 d) Roots of the equation  $x^2 + ax + bc = 0$  are imaginary.

Q63

Let  $P(x) = x^5 + x^2 + 1$  have five roots  $\alpha_1, \alpha_2, \alpha_3, \alpha_4, \alpha_5$  and  $g(x) = x^2 - 2$  then the value of  $g(\alpha_1)g(\alpha_2)g(\alpha_3)g(\alpha_4)g(\alpha_5)$  is :

- a) -21                      b) -19                      c) -23                      d) -25

Q64

If  $\tan 1^\circ = t$ , then value of  $\cos 2^\circ + t \sin 2^\circ$  is

- a) -2                      b) -1                      c)  $\frac{1}{2}$                       d) 1

Q65

Let  $R$  and  $S$  be two non-void relations an a set  $A$ . Which of the following statements is not true

- a)  $R$  and  $S$  are transitive  $\Rightarrow R \cup S$  is transitive  
 b)  $R$  and  $S$  are transitive  $\Rightarrow R \cap S$  is transitive  
 c)  $R$  and  $S$  are symmetric  $\Rightarrow R \cup S$  is symmetric  
 d)  $R$  and  $S$  are reflexive  $\Rightarrow R \cap S$  is reflexive

Q66

The sum of the series  $\cot^{-1}\left(2^2 + \frac{1}{2}\right) + \cot^{-1}\left(2^3 + \frac{1}{2^2}\right) + \cot^{-1}\left(2^4 + \frac{1}{2^3}\right) + \dots \infty$

- a)  $\tan^{-1}(2)$                       b)  $\tan^{-1}\left(\frac{1}{2}\right)$                       c)  $-\tan^{-1}\left(\frac{1}{2}\right)$                       d) None of these

- Q67** If  $0 < \theta < 90^\circ$  and  $\theta = \tan^{-1}(2 \tan^2 \theta) - \tan^{-1}\left(\frac{1}{3} \tan \theta\right)$  then -
- a)  $\tan \theta = 1$       b)  $\tan \theta = \frac{1}{2}$       c)  $\tan \theta = 2$       d)  $\tan \theta = \frac{3}{2}$
- Q68** If  $A_1, A_2, A_3, \dots$  are in A.P. then  $\sum_{i=1}^{2n} (-1)^i \left( \frac{A_i + A_{i+1}}{A_i - A_{i+1}} \right)$  is equal to -
- a)  $2n - 1$       b)  $n - 1$       c)  $-2n$       d)  $n + 2$
- Q69** The first three terms of A.G.P. are 3, -1, -1 then next positive term is
- a) 2      b) 3      c)  $\frac{5}{27}$       d)  $\frac{5}{9}$
- Q70** The existence of the unique solution of the system of equations  $2x + y + z = \beta$ ,  $10x - y + \alpha z = 10$  and  $4x + 3y - z = 6$  depends on
- a) Both  $\alpha$  and  $\beta$       b) Neither  $\beta$  nor  $\alpha$       c)  $\beta$  only      d)  $\alpha$  only
- Q71** The co-ordinates of the orthocentre of the triangle formed by the lines  $2x^2 - 2y^2 + 3xy + 3x + y + 1 = 0$  and  $3x + 2y + 1 = 0$  are :-
- a)  $\left(\frac{4}{5}, \frac{3}{5}\right)$       b)  $\left(-\frac{3}{5}, -\frac{1}{5}\right)$       c)  $\left(\frac{1}{5}, -\frac{4}{5}\right)$       d)  $\left(\frac{2}{5}, -\frac{1}{5}\right)$
- Q72** If a circle of radius R passes through the origin O and intersects the coordinate axes at A and B, then the locus of the foot of perpendicular from O on AB is :
- a)  $(x^2 + y^2)^2 = 4R^2 x^2 y^2$       b)  $(x^2 + y^2)(x + y) = R^2 xy$       c)  $(x^2 + y^2)^3 = 4R^2 x^2 y^2$
- d)  $(x^2 + y^2)^2 = 4R^2 x^2 y^2$
- Q73** If the function  $f(x) = \begin{cases} \frac{\sqrt{2 + \cos x} - 1}{(\pi - x)^2}, & x \neq \pi \\ k & x = \pi \end{cases}$  is continuous at  $x = \pi$ , then  $k$  equals :-
- a)  $\frac{1}{4}$       b)  $\frac{1}{2}$       c) 2      d) 0

**Q74** Let  $f(x) = \begin{cases} x^2; & x \in Q \\ 1-x^2 & ; x \notin Q \end{cases}$ , then  $f(x)$  is continuous at

- a)  $x = 0$                       b)  $x = \pm \frac{1}{2}$                       c)  $x = \pm \frac{1}{\sqrt{2}}$                       d)  $x = \frac{1}{\sqrt{2}}$

**Q75** The value of  $\lim_{n \rightarrow \infty} n^2 \left\{ \sqrt{\left(1 - \cos \frac{1}{n}\right)} \sqrt{\left(1 - \cos \frac{1}{n}\right)} \sqrt{\left(1 - \cos \frac{1}{n}\right)} \dots \infty \right\}$  is

- a) 1                                      b) 2                                      c) 0                                      d) 1/2

**Q76** If  $\lim_{x \rightarrow \infty} \left( \frac{3x^2 + x + 1}{x + 1} - ax - b \right) = 2012$ ; then  $a$  &  $b$  are:

- a)  $a = 1, b = 4$     b)  $a = 1, b = -4$     c)  $a = 3, b = 2010$     d)  $a = 3, b = -2014$

**Q77** The perimeter of a triangle is 14 and two of its vertices are  $(-3, 0)$  and  $(3, 0)$ , then the locus of the third vertex is

- a)  $\frac{x^2}{16} + \frac{y^2}{7} = 1$                       b)  $\frac{x^2}{25} + \frac{y^2}{16} = 1$                       c)  $\frac{x^2}{7} + \frac{y^2}{16} = 1$                       d)  $\frac{x^2}{16} + \frac{y^2}{25} = 1$

**Q78** If  $\theta$  be the angle subtended by the circle  $x^2 + y^2 + 2gx + 2fy + c = 0$  at a point  $(x_1, y_1)$  and  $s_1 = x_1^2 + y_1^2 + 2gx_1 + 2fy_1 + c$ , then which is NOT correct?

- a)  $\cot \theta = \frac{2\sqrt{s_1}}{\sqrt{g^2 + f^2 - c}}$                       b)  $\cot \frac{\theta}{2} = \frac{\sqrt{s_1}}{\sqrt{g^2 + f^2 - c}}$                       c)  $\theta = 2 \tan^{-1} = \sqrt{\frac{g^2 + f^2 - c}{s_1}}$   
d)  $\cos \theta = \frac{s_1 + c - g^2 - f^2}{s_1 - c + g^2 + f^2}$

**Q79** If  $\begin{bmatrix} 1 & 2 & \alpha \\ 0 & 1 & 4 \\ 0 & 0 & 1 \end{bmatrix}^n = \begin{bmatrix} 1 & 22 & 2024 \\ 0 & 1 & 44 \\ 0 & 0 & 1 \end{bmatrix}$ , then  $n + \alpha$  is equal to

- a) 144                                      b) 155                                      c) 181                                      d) 191

**Q80** The mean of 5 observations is 4.4 and their variance is 8.24. If three of the observations are 1, 2 and 6. Find the other two observations:

- a) 4, 9                                      b) 8, 4                                      c) 4, 4                                      d) 9, 9



**Numerical**

- Q81** If  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 - 3x + 1 = 0$  and  $a_n = \alpha^n + \beta^n, n \in N$  then value of  $\frac{a_7 + a_5}{a_6} =$
- Q82** If  $2^x = 3^y = 6^{-z}$ , then  $\left(\frac{1}{x} + \frac{1}{y} + \frac{1}{z}\right)$  is equal to
- Q83** Let  $f(x) = -4 \cdot \sqrt{e^{1-x}} + 1 + x + \frac{x^2}{2} + \frac{x^3}{3}$ . If  $g(x)$  is inverse of  $f(x)$ , then the value of  $\frac{1}{g'\left(-\frac{7}{6}\right)}$  is.
- Q84** Let  $\begin{vmatrix} x & 2 & x \\ x^2 & x & 6 \\ x & x & 6 \end{vmatrix} = Ax^4 + Bx^3 + Cx^2 + Dx + E$ . Then the value of  $|5A + 4B + 3C + 2D + E|$  is equal to
- Q85** If two parallel lines  $L_1$  and  $L_2$  with positive slopes are tangent to the circle  $C_1: x^2 + y^2 - 2x - 16y + 64 = 0$ . If  $L_1$  is also tangent to circle  $C_2: x^2 + y^2 - 2x + 2y - 2 = 0$  and the equation of  $L_2$  is  $a\sqrt{a}x - by + c - a\sqrt{a} = 0$  where  $a, b, c \in N$ , then the value of  $\frac{a+b+c}{2} =$
- Q86** If a tangent of slope 2 of ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  is normal to the circle  $x^2 + y^2 + 4x + 1 = 0$ , then the maximum value of  $ab$  is
- Q87** A point P moves in xy-plane in such a way that  $[|x|] + [|y|] = 1$ , where  $[.]$  denotes the greatest integer function. Area of the region representing all possible of the point P is equal to.
- Q88** If  $x \in R$  then absolute difference between the maximum and minimum values of the expression  $\frac{x^2 + 14x + 9}{x^2 + 2x + 3}$  is
- Q89** If  $A = \{2, 4, 5\}$ ,  $B = \{7, 8, 9\}$ , then  $n(A \times B)$  is equal to

**Q90**

The value of  $\lim_{n \rightarrow \infty} \left[ \frac{2n}{2n^2 - 1} \cos \frac{n+1}{2n-1} - \frac{n}{1-2n} \cdot \frac{n(-1)^n}{n^2 + 1} \right]$  is (here  $n \in N$  )

## Answer Key

|             |           |           |          |           |          |           |           |          |          |          |
|-------------|-----------|-----------|----------|-----------|----------|-----------|-----------|----------|----------|----------|
| Que.        | 1         | 2         | 3        | 4         | 5        | 6         | 7         | 8        | 9        | 10       |
| <b>Ans.</b> | <b>B</b>  | <b>B</b>  | <b>B</b> | <b>B</b>  | <b>C</b> | <b>B</b>  | <b>C</b>  | <b>A</b> | <b>B</b> | <b>C</b> |
| Que.        | 11        | 12        | 13       | 14        | 15       | 16        | 17        | 18       | 19       | 20       |
| <b>Ans.</b> | <b>D</b>  | <b>B</b>  | <b>A</b> | <b>B</b>  | <b>C</b> | <b>B</b>  | <b>A</b>  | <b>B</b> | <b>D</b> | <b>A</b> |
| Que.        | 21        | 22        | 23       | 24        | 25       | 26        | 27        | 28       | 29       | 30       |
| <b>Ans.</b> | <b>12</b> | <b>12</b> | <b>3</b> | <b>3</b>  | <b>1</b> | <b>4</b>  | <b>40</b> | <b>3</b> | <b>3</b> | <b>4</b> |
| Que.        | 31        | 32        | 33       | 34        | 35       | 36        | 37        | 38       | 39       | 40       |
| <b>Ans.</b> | <b>D</b>  | <b>B</b>  | <b>B</b> | <b>A</b>  | <b>C</b> | <b>C</b>  | <b>B</b>  | <b>B</b> | <b>B</b> | <b>A</b> |
| Que.        | 41        | 42        | 43       | 44        | 45       | 46        | 47        | 48       | 49       | 50       |
| <b>Ans.</b> | <b>B</b>  | <b>D</b>  | <b>D</b> | <b>B</b>  | <b>A</b> | <b>A</b>  | <b>B</b>  | <b>C</b> | <b>C</b> | <b>A</b> |
| Que.        | 51        | 52        | 53       | 54        | 55       | 56        | 57        | 58       | 59       | 60       |
| <b>Ans.</b> | <b>4</b>  | <b>3</b>  | <b>4</b> | <b>6</b>  | <b>8</b> | <b>10</b> | <b>7</b>  | <b>4</b> | <b>9</b> | <b>6</b> |
| Que.        | 61        | 62        | 63       | 64        | 65       | 66        | 67        | 68       | 69       | 70       |
| <b>Ans.</b> | <b>B</b>  | <b>A</b>  | <b>C</b> | <b>D</b>  | <b>A</b> | <b>B</b>  | <b>A</b>  | <b>C</b> | <b>B</b> | <b>D</b> |
| Que.        | 71        | 72        | 73       | 74        | 75       | 76        | 77        | 78       | 79       | 80       |
| <b>Ans.</b> | <b>B</b>  | <b>C</b>  | <b>A</b> | <b>C</b>  | <b>D</b> | <b>D</b>  | <b>A</b>  | <b>A</b> | <b>B</b> | <b>A</b> |
| Que.        | 81        | 82        | 83       | 84        | 85       | 86        | 87        | 88       | 89       | 90       |
| <b>Ans.</b> | <b>3</b>  | <b>0</b>  | <b>5</b> | <b>11</b> | <b>7</b> | <b>4</b>  | <b>8</b>  | <b>9</b> | <b>9</b> | <b>0</b> |