

**FIITJEE**  
**ALL INDIA TEST SERIES**  
**JEE (Advanced)-2025**  
**FULL TEST – III**  
**PAPER –1**  
**TEST DATE: 18-02-2025**

**ANSWERS, HINTS & SOLUTIONS**

**Physics**

**PART – I**

**SECTION – A**

1. B

Sol. The magnetic induction of the solenoid is directed along its axis. Therefore, the Lorentz force acting on the electron at any instant of time will lie in the plane perpendicular to the solenoid axis. Since the electron velocity at the initial moment is directed at right angles to the solenoid axis, the electron trajectory will lie in the plane perpendicular to the solenoid axis. The Lorentz force can be found from the formula  $F = evB$ .

The trajectory of the electron in the solenoid is an arc of the circle whose radius can be determined from the relation  $evB = mv^2/r$ , whence

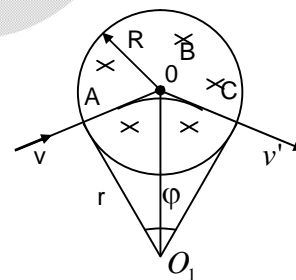
$$r = \frac{mv}{eB}$$

The trajectory of the electron is shown in figure, where  $O_1$  is the centre of the arc  $AC$  described by the electron,  $v'$  is the velocity at which the electron leaves the solenoid. The segments  $OA$  and  $OC$  are tangents to the electron trajectory at points  $A$  and  $C$ . The angle between  $v$  and  $v'$  is obviously  $\phi = \angle AO_1C$  since  $\angle OAO_1 = \angle OCO_1$ .

In order to find  $\phi$ , let us consider the right triangle  $OAO_1$ ; side  $OA = R$  and side  $AO_1 = r$ . Therefore,  $\tan(\phi/2) = R/r = eBR/(mv)$ .

Therefore, 
$$\phi = 2 \tan^{-1} \left( \frac{eBR}{mv} \right)$$

Obviously, the magnitude of the velocity remains unchanged over the entire trajectory since the Lorentz force is perpendicular to the velocity at any instant. Therefore, the transit time of electron in the solenoid can be determined from the relation

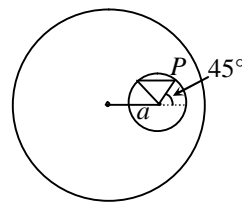


2. A

Sol.  $F = eE = \frac{e\rho a}{3\epsilon_0}$

$$r\sqrt{2} = \frac{1}{2} \frac{F}{m} t^2$$

$$t = \sqrt{\frac{6\sqrt{2}r\epsilon_0 m}{e\rho a}}$$



3. D

Sol.  $\mu(x) = a - bx$

where values of a and b are 2 and 1 respectively in SI unit.

4. C

5. A, B, C, D

Sol. At the time of maximum elongation angular speed of B and C are equal, let speed of B is  $2v$  and C is  $v$ , By conserving angular momentum of the system about the centre

$$mv_0 2R = m2v(2R) + mv(R)$$

$$v = \frac{2v_0}{5}, \quad v_B = \frac{4v_0}{5}, \quad v_C = \frac{2v_0}{5}$$

Conserving energy of the system  $\frac{1}{2}mv_0^2 = \frac{1}{2}kx_{\max}^2 + \frac{1}{2}m\left(\frac{4v_0}{5}\right)^2 + \frac{1}{2}m\left(\frac{2v_0}{5}\right)^2$

$$\therefore x_{\max} = \sqrt{\frac{m}{5k}}v_0$$

6. A, B, C

Sol. Use Relative Motion w.r.t. Box.

7. A, B, C

Sol.  $\vec{F} = (v_1\hat{i} + v_2\hat{k}) \times (A\hat{k}) = Av(-\hat{j})$

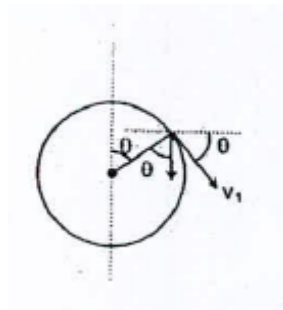
$$\frac{mv^2}{R} = Av$$

$$R = \frac{mv}{A}$$

$$\omega = \frac{A}{m}$$

$$\vec{v} = v_1 \cos\theta \hat{i} - v_1 \sin\theta \hat{j} + v_2 \hat{k}$$

$$\vec{v} = v_1 \cos\left(\frac{A}{m}t\right) \hat{i} - v_1 \sin\left(\frac{A}{m}t\right) \hat{j} + v_2 \hat{k}$$



8. A

Sol.  $\vec{dF} = i \left( \vec{d\ell} \times \vec{B} \right)$

$$\vec{\tau} = i \vec{A} \times \vec{B}$$

9. A

Sol. By using  $(\mu-1)t = n\lambda$ , we can find value of  $n$ , that is order of the fringe produced at P, if that particular strip has been placed over any of the slit. If two strips are used in conjunction (over each other), path difference due to each is added to get net path difference created. If two strips are used over different slits, their path differences are subtracted to get net path difference.

$$\text{Now, } n_1 = \frac{(\mu_1 - 1)t_1}{\lambda} = 5$$

$$n_2 = 4.5$$

$$\text{and } n_3 = 0.5$$

For (A), order of the fringe is 4.5 i.e. 5<sup>th</sup> dark

For (B), net order is  $5 - 0.5 = 4.5$

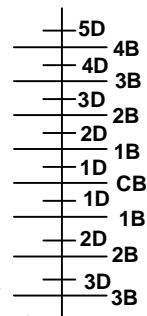
i.e. fifth dark

For (C) net order is  $5 - (0.5 + 4.5) = 0$

i.e. it is central bright again at P.

For (D) net order is  $(5+0.5) - (4.5) = 1$

i.e. first bright



10. A

Sol.  $q_B = -q \left(1 - \frac{1}{K}\right)$

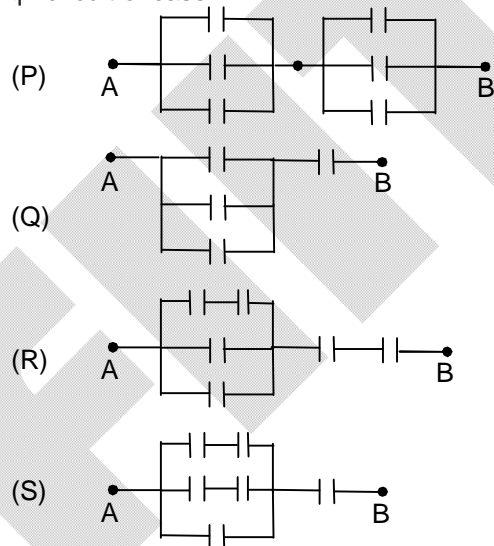
$$q_A = +q$$

$$q_C = +q \left(1 - \frac{1}{K}\right)$$

$$q_D = -q$$

11. B

Sol. Eq. circuit of case P



### SECTION – B

12. 96

Sol. From the velocity component of object w.r.t. mirror is

$$(V_{OM})_{||} = -\frac{v^2}{u^2}(V_{OM})_{||} \Rightarrow (V_{OM})_{||} = -\left(\frac{60}{-20}\right)^2 (10) = -90 \text{ m/s}$$

$$\frac{dm}{dt} = - \left[ \frac{u(V_{IM})_{\parallel} - v(V_{IM})_{\parallel}}{u^2} \right] = \left[ \frac{(-20) \times 10^2 (-90) - (60) \times 10^{-2} (10)}{(-20 \times 10^{-2})^2} \right] \text{ per sec.}$$

$$\frac{dm}{dt} = -3 \times 10^2 \text{ per sec} \quad \Rightarrow (V_{IM})_{\perp} = h_0 \frac{dm}{dt} + m(V_{OM})_{\perp}$$

$$(V_{IM})_{\perp} = 2 \times 10^{-2} \times (-3 \times 10^2) + (3)(-15) = -6 - 45 = -51 \text{ m/s}$$

$$(\vec{V}_{VM})_{\perp} = (V_{IM})_{\parallel} \hat{i} + (V_{IM})_{\perp} \hat{j}$$

$$\vec{V}_{IG} = \vec{V}_{IM} + \vec{V}_{MG} (-90\hat{i} - 51\hat{j}) + (-6\hat{i} + 10\hat{j})$$

13. 2

Sol.  $\Delta U_1 = mC_v \Delta T$

$$= 1 \times \frac{3}{2} R \Delta T$$

$$= \frac{3R\Delta T}{2}$$

$$\Delta U_2 = \frac{1}{2} k (x_2^2 - x_1^2)$$

$$PA = kx$$

$$x = \frac{PA}{k}$$

$$x^2 = \frac{P(Ax)}{k} = \frac{RT}{k}$$

$$\Delta U_2 = \frac{R}{2} (T_2 - T_1)$$

$$= \frac{R\Delta T}{2}$$

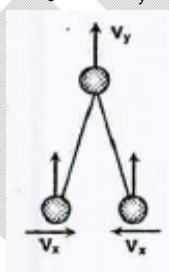
$$\Delta U = \Delta U_1 + \Delta U_2 = 2R\Delta T$$

$$C = 2R$$

14. 1

Sol. From collision

$$mv_0 = 3mv_y$$



$$v_y = \frac{v_0}{3}$$

From COE

$$\frac{1}{2} mv_0^2 - 3 \frac{1}{2} mv_y^2 + 2 \frac{1}{2} mv_x^2$$

$$\frac{1}{2} mv_x^2 \left( 1 - 2 \frac{v_0^2}{9} \right) = mv_x$$

$$v_x = \frac{v_0}{\sqrt{3}}$$

From frame of ball B,

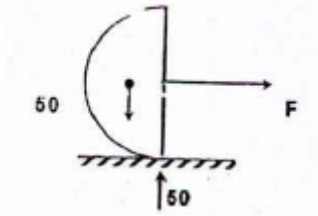
$$3T = \frac{mv_x^2}{\ell}$$

$$\therefore T = \frac{mv_x^2}{3\ell} = \frac{(3)(v_2^2)}{3 \times 3 \times 1} = 1$$

15. 5

$$\text{Sol. } F = \left(\frac{10}{2}\right)(10)^2 \times \frac{3 \times 0.8}{8}$$

$$= 5 \times 100 \times 0.3 = 150 \text{ N}$$



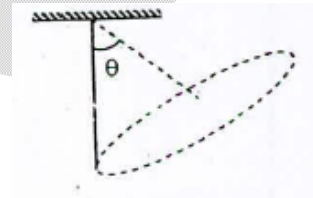
16. 3

$$\text{Sol. } \omega = \sqrt{\frac{g_{\text{eff}}}{\ell \cos \theta}}$$

$$v = \omega r = \omega \ell \sin \theta$$

$$= \sin \theta \sqrt{\frac{\ell g_{\text{eff}}}{\cos \theta}}$$

$$\sin \theta = \frac{qE}{mg_{\text{eff}}}, \cos \theta = \frac{g}{g_{\text{eff}}} \Rightarrow v = \frac{qE}{m} \sqrt{\frac{\ell}{g}}$$



17. 1

$$\text{Sol. } AP = r = (x^2 + d^2)^{1/2}$$

Electric field at A due to wire 1

$$E = \frac{\lambda}{2\pi\epsilon_0 r}$$

Force on each elemental length  $dF = E \cdot dq$

$$dF = \left(\frac{\lambda}{2\pi\epsilon_0 r}\right)(\lambda dx) = \frac{\lambda^2 dx}{2\pi\epsilon_0 (x^2 + d^2)^{1/2}}$$

Net force on the elemental length

$$dF_{\text{net}} = 2dF \cos \theta$$

$$= \frac{\lambda^2 dx \cdot \cos \theta}{\pi\epsilon_0 (x^2 + d^2)^{1/2}} = \frac{\lambda^2 dx \cdot d}{\pi\epsilon_0 (d^2 + x^2)}$$

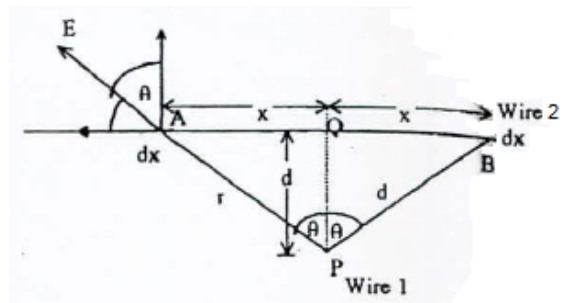
Hence total force required to hold the wire

$$2 = \int dF_{\text{net}}$$

$$F_{\text{net}} = \frac{\lambda^2 d}{\pi\epsilon_0} \int_{-\infty}^{\infty} \frac{dx}{(d^2 + x^2)} = \frac{\lambda^2}{2\epsilon_0} = \frac{(3 \times 10^{-6})^2}{2 \times 8.86 \times 10^{-12}} = 0.51 \text{ Newton.}$$

As  $F_{\text{net}}$  is independent of separation between the wire. Hence required work done

$$W = 0.51 \times 2 = 1 \text{ Joule.}$$



**Chemistry****PART – II****SECTION – A**

18. C

Sol.  $T \propto V^3 \Rightarrow PV^{-2} \text{ constant} \Rightarrow C = \frac{5R}{2} + \frac{R}{3} = \frac{17R}{6}$

19. B

Sol.  $w = -1 \times 3 \text{ L} \cdot \text{atm} = -300 \text{ J}$

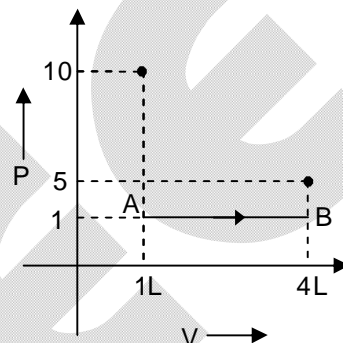
$$\frac{10 \times 1}{300} = \frac{5 \times 4}{T} \Rightarrow T = 600 \text{ K}$$

$$q = 50 \times 300 = 15000 \text{ J}$$

$$\Rightarrow \Delta U = q + w = 14700 \text{ J}$$

$$\Delta H = \Delta U + (PV)$$

$$= 14700 + (20 - 10) \times 100 = 15700 \text{ J}$$



20. A

21. D

22. A, B, C

Sol. (A)  $-\frac{d[A]}{dt} = \frac{d[B]}{dt} + \frac{d[C]}{dt}$

(B)  $K[A] = K_1[A] + K_2[A]$

Where K is overall rate constant.

$$K = K_1 + K_2$$

$$\text{or } \frac{dK}{dT} = \frac{dK_1}{dT} + \frac{dK_2}{dT}$$

$$Ae^{\frac{E_a}{RT}} \left[ \frac{E_a}{RT^2} \right] = A_1 e^{\frac{E_{a1}}{RT}} \left[ \frac{E_{a1}}{RT^2} \right] + A_2 e^{\frac{E_{a2}}{RT}} \left[ \frac{E_{a2}}{RT^2} \right]$$

$$\text{or } K.E_a = K_1 E_{a1} + K_2 E_{a2}$$

$$\text{or } E_a = \frac{K_1 E_{a1} + K_2 E_{a2}}{K} = \frac{x_1 y_1 + x_2 y_2}{x_1 + y_2}$$

(C)  $t_{1/2} = \frac{\ln 2}{K} = \frac{\ln 2}{x_1 + x_2}$

(D)  $\ln \frac{K'}{K} = \frac{E_a}{R} \left[ \frac{1}{T_1} - \frac{1}{T_2} \right]$

23. A, C, D

Sol. Addition of an electron to a negatively charged atom requires energy therefore endothermic process

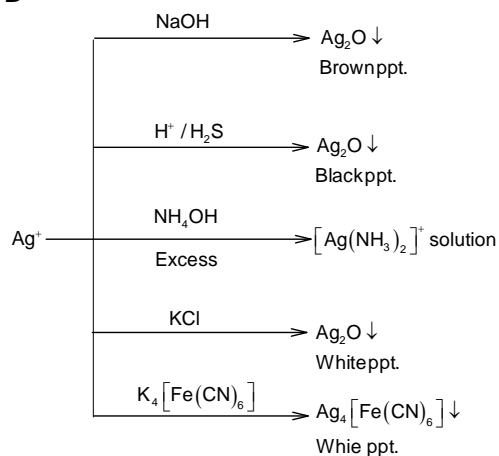
24. A, B, C, D

Sol. All the above structure possess chiral carbon after reduction

25. A

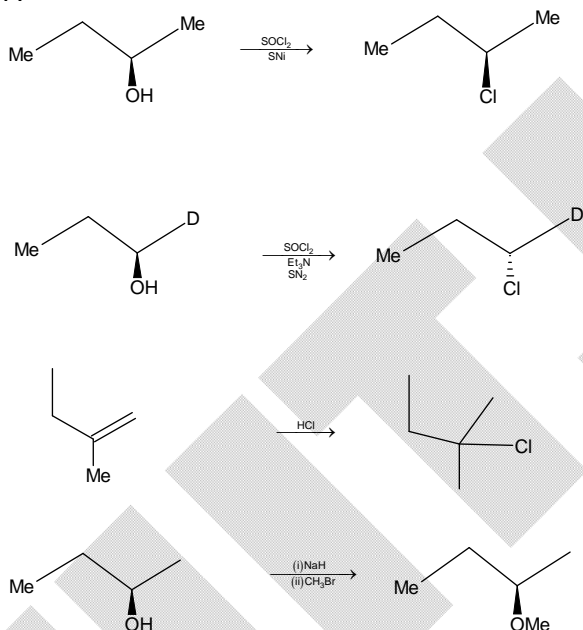
26. B

Sol.



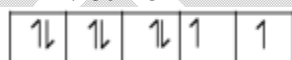
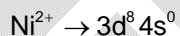
27. A

Sol.



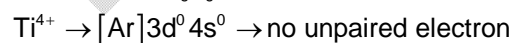
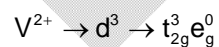
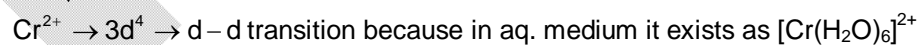
28. C

Sol.



$$n \rightarrow 2$$

$$\mu = \sqrt{n(n+2)}$$



### SECTION – B

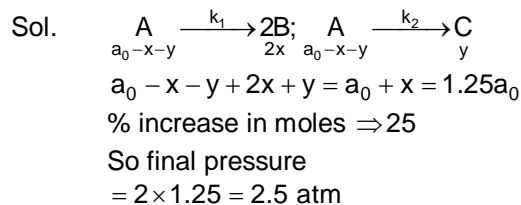
29. 2

Sol.  $N_1 V_1 = N_2 V_2$

$$\therefore \frac{1.575 \times 2}{(90 + 18x) \times 0.250} \times 16.68 = \frac{25}{15}$$

$$\therefore x = 2.$$

30. 2



31. 5

Sol.  $E_n = -\frac{13.6}{n^2} \text{ eV}; E_2 = -\frac{13.6}{2^2}; \quad E_4 = -\frac{13.6}{4^2} \text{ eV / atom}$

$$\Delta E = E_4 - E_2 = 2.55 \text{ eV}$$

Absorbed energy = work function of metal + K.E.

$$\text{K.E.} = 0.05 \text{ eV}$$

32. 3

Sol.  $\text{Hg(l)} \rightleftharpoons \text{Hg(g)},$   
 $\Delta_r S^\circ = 174.4 - 77.4 = 97 \text{ J/K-mol}$   
 $\therefore \Delta G^\circ = \Delta H^\circ - T \Delta S^\circ = 0$   
 $T = \frac{\Delta H^\circ}{\Delta S^\circ}$   
 $= \frac{60.8 \times 1000}{97} = 626.8 \text{ K}$

33. 2

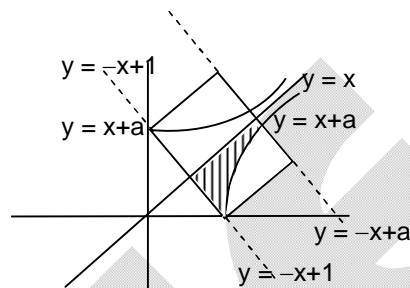
Sol. Atomic mass of N  
 In given sample  
 $= \frac{3}{4} \times 14 + \frac{1}{4} \times 15$   
 $= \frac{57}{4}$   
 Atomic mass of H in given sample  
 $= \frac{4}{5} + \frac{1}{6} \times 2 = \frac{6}{5}$   
 Molar mass of  $\text{NH}_3 = 17.85$   
 Mole of  $\text{NH}_3 = 0.1 \times 10^{-3}$   
 $= 0.0001$   
 Molecules of  $\text{NH}_3$   
 $= 6 \times 10^{19} = 60 \times 10^{18}$   
 Atoms of N  $= 60 \times 10^{18}$   
 Atoms of H  $= 180 \times 10^{18}$   
 Total neutrons  
 $= \frac{3}{4} \times 60 \times 10^{19} \times 7 + \frac{1}{4} \times 60 \times 10^8 \times 8 + \frac{1}{5} \times 1 \times 80 \times 10^{18}$

34. 8



**Mathematics****PART – III****SECTION – A**

35. D

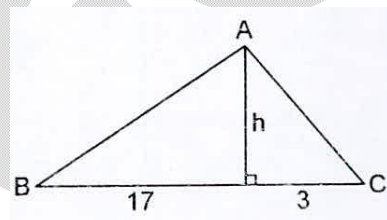
Sol. Required area of shaded region is  $k - \frac{1}{4}$ 

36. B

Sol.  $B + C = \pi - A$   
 $\tan(B + C) = -\tan A$ 

$$\frac{h\left(\frac{1}{17} + \frac{1}{3}\right)}{1 - \frac{h^2}{51}} = -\frac{22}{7} \Rightarrow \left(\frac{20h}{51 - h^2}\right) = -\frac{22}{7}$$

$$\text{Area of triangle ABC } \Delta = -\frac{1}{2} \times 20 \times 11 = 110$$



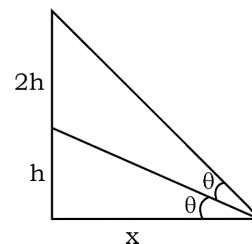
37. B

Sol. Let three digits of N be :  
 Hundred's digit =  $a - d$ , ten's digit =  $a$ , and unit's digit =  $a + d$   
 $(a - d) + a + (a + d) = 15 \Rightarrow a = 5$   
 $N = 100(5 - d) + 50 + (5 + d) \quad \dots(1)$   
 Number obtained by reversing digits of N is  
 $N_1 = 100(5 + d) + 50 + (5 - d) \quad \dots(2)$   
 Now,  $594 = N - N_1 = 10(-2d) + 2d$   
 $\Rightarrow 2d = -6 \Rightarrow d = -3$   
 Thus,  $N = 852$  and  $\frac{1000}{N - 252} = \frac{1000}{600} = \frac{5}{3}$

38. C

Sol. Let  $\frac{h}{x} = a$ . Then  $\tan \theta = a$ ,  $\tan 2\theta = 3a$ .

$$\therefore \frac{2a}{1 - a^2} = 3a \Rightarrow a = \frac{1}{\sqrt{3}}$$



39. A, B, C

Sol.  $\vec{r} = \hat{i} - \hat{j} + \lambda(2\hat{i} + 2\hat{j} - \hat{k})$ ;  $\vec{r} = -2\hat{j} + t(5\hat{i} - 8\hat{j} - \hat{k})$   
 $\therefore A(2\lambda + 1, -2\lambda - 1, -\lambda)$ ;  $B(5t, -8t - 2, -t)$   
 So  $\overline{AB} \cdot (2\hat{i} - 2\hat{j} - \hat{k}) = 0$  and  $\overline{AB} \cdot (5\hat{i} - 8\hat{j} - \hat{k}) = 0$

We get  $t = -\frac{1}{3}, \lambda = -1$

Now shortest distance = AB

$$(\vec{r} - (\hat{i} - \hat{j})) \cdot \vec{n} = 0; \vec{n} = \lambda (\vec{a} \times \vec{b})$$

Where  $\vec{a} = 2\hat{i} - 2\hat{j} - \hat{k}$  and  $\vec{b} = 5\hat{i} - 8\hat{j} - \hat{k}$

40. B, D

Sol. Total number of ways  $= 8 \times {}^{125}C_5 = 62000 = 2^4 \cdot 5^3 \cdot 31$

So, the number of factors of N is  $(1 + 4)(1 + 3)(1 + 1) = 40$

41. A, C

42. B

Sol. (P).  $OA = 1 + 4 \cot \theta$

$$OB = 4 + \tan \theta$$

$$OA + OB = 5 + 4 \cot \theta + \tan \theta \geq 5 + 2\sqrt{4 \cot \theta \tan \theta}$$

$$= 5 + (2 \times 2) = 9$$

(Q). The reflection of  $P(4, -1)$  on  $y = x$  is  $Q(-1, 4)$ .

$$\text{Hence, } PQ = \sqrt{(4+1)^2 + (-1-4)^2} = \sqrt{50} = 5\sqrt{2}.$$

(R).  $AB = 2\sqrt{2}$

$$OC = \sqrt{2}$$

The maximum value of d is

$$OF = \sqrt{2} + 2\sqrt{2} = 3\sqrt{2}$$

(S). The given line is  $x = 4 + \frac{1}{\sqrt{2}} \left( \frac{y+1}{\sqrt{2}} \right)$  or  $y = 2x - 9$

Hence, the intercept made by the x-axis is  $9/2$ .

43. C

Sol. (P). We have  $\frac{1}{\log_3 \pi} + \frac{1}{\log_4 \pi} = \log_\pi 3 + \log_\pi 4 = \log_\pi 12$

But  $\pi^2 < 12 < \pi^3$ , we have  $2 < \log_\pi 12 < 3$ .

(Q).  $3^a = 4; a = \log_3 4$

Similarly,  $b = \log_4 5$  etc.

$$\text{Hence, } abcdef = \log_3 4 \cdot \log_4 5 \cdot \log_5 6 \cdot \log_6 7 \cdot \log_7 8 \cdot \log_8 9 = \log_3 9 = 2$$

(R). We have to find characteristic of  $\log_2 2008$ .

We know that  $\log_2 1024 = 10$  and  $\log_2 2048 = 11$ , therefore  $10 < \log_2 2008 < 11$

Hence, it has characteristic 10.

(S).  $\log_2 (\log_2 (\log_3 x)) = 0 \Rightarrow \log_2 (\log_3 x) = 1 \Rightarrow \log_3 x = 2$

$$\Rightarrow x = 9$$

Similarly, we have  $\log_3 (\log_2 y) = 1$

$$\Rightarrow \log_2 y = 3 \text{ or } y = 8$$

Therefore,  $x - y = 1$ .

44. A

Sol. (P).  $I = \lim_{x \rightarrow 0} \frac{e^{x^2} - 1 + x - e^x + 1}{2 \frac{\sin^2 x}{x^2} \cdot x^2} = \frac{1}{2} \left[ \lim_{x \rightarrow 0} \frac{e^{x^2} - 1}{x^2} + \lim_{x \rightarrow 0} \frac{x - e^x + 1}{x^2} \right] = \frac{1}{2} \left[ 1 - \lim_{x \rightarrow 0} \frac{e^x - x - 1}{x^2} \right]$

(Q).  $I = \lim_{x \rightarrow 0} \left( \frac{3+x}{3-x} \right)^{1/x} = e^{\lim_{x \rightarrow 0} \frac{1}{x} \left( \frac{3+x}{3-x} - 1 \right)} = e^{\lim_{x \rightarrow 0} \frac{2x}{x(3-x)}} = e^{2/3} \Rightarrow 2 + 3 = 5$

(R).  $\lim_{x \rightarrow 0} \frac{(\tan^3 x - x^3) - (\tan x^3 - x^3)}{x^5}$   
 $= \lim_{x \rightarrow 0} \frac{\tan^3 x - x^3}{x^5} - \underbrace{\lim_{x \rightarrow 0} \frac{\tan^3 x - x^3}{x^5}}_{\text{zero (by expansion)}}$   
 $= \lim_{x \rightarrow 0} \frac{(\tan x - x)(\tan^2 x + x \tan x + x^2)}{x^3} = \frac{1}{3} \times 3 = 1$

(S). Rationalising given

$$\lim_{x \rightarrow 0} \frac{(x + 2 \sin x) \left[ \sqrt{(x^2 + 2 \sin x + 1)} + \sqrt{\sin^2 x - x + 1} \right]}{(x^2 + 2 \sin x + 1) - (\sin^2 x - x + 1)}$$

$$= 2 \cdot \lim_{x \rightarrow 0} \frac{x + \sin 2x}{x^2 - \sin^2 x + 2 \sin x + x}$$

$$= 2 \cdot \lim_{x \rightarrow 0} \frac{1 + \frac{\sin 2x}{x}}{x - \frac{\sin^2 x}{x} + 2 + 1} = 2 \left( \frac{1+2}{3} \right) = 2$$

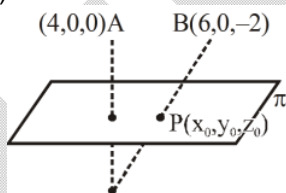
45. C

Sol. Let the plane be  $\alpha x + \beta z + 1 = 0$   
 Pass through  $(1, 0, 1)$ ;  $(3, 2, -1)$

$$\therefore \alpha = -\frac{1}{2}; \beta = -\frac{1}{2}$$

(P).  $\pi : x + z = 2$

(Q).



Both A and B are on same side of  $\pi$ .  
 Reflection of A in plane is  $A'(2, 0, -2)$   
 Equation of line  $A'B = \vec{r} = 6\hat{i} - 2\hat{k} + \lambda(4\hat{i})$

For P:  $6 + 4\lambda + 0 - 2 = 2 \Rightarrow \lambda = \frac{-1}{2}$

$\therefore P(4, 2, -2)$

$\therefore |4x_0 + y_0 + 2z_0| = 12$

(R). Now  $|PA - PB|_{\min} = 0$   
 $|PA - PB|_{\min}$  will approach

$AB = \sqrt{4 + 0 + 4} = \sqrt{8}$

$\therefore |PA - PB| \in [0, \sqrt{8})$ .

(S). Also, A' will lie on  $\frac{x-2}{1} = \frac{y-\alpha}{0} = \frac{z+\beta}{-1}$ .

$$\Rightarrow \frac{2-2}{1} = \frac{0-\alpha}{0} = -\frac{2+\beta}{-1}$$

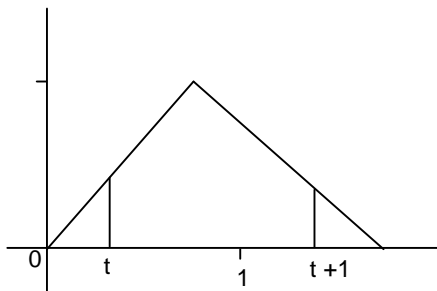
$$\Rightarrow \alpha = 0, \beta = 2$$

$$\therefore \alpha^4 + \beta^4 = 16$$

### SECTION – B

46. 2

Sol. The region M is the large triangle in the diagram below, and the region N is the infinite strip between the lines  $x = t$  and  $x = t+1$  where  $0 < t < 1$



Hence  $M \cap N$  is the pentagon. Its area is given by

$$\frac{1}{2} \left( \sqrt{2}^2 - t^2 - (2 - (t+1))^2 \right) = -t^2 + t + \frac{1}{2}$$

47. 6

Sol.  $t^2 + 3t - 8 = 2 \Rightarrow t = 2, -5$

$$2t^2 - 2t - 5 = -1 \Rightarrow t = 2, -1$$

So, at  $t = 2$

$$\frac{dy}{dx} = \left( \frac{\frac{dy}{dt}}{\frac{dx}{dt}} \right)_{t=2} = \frac{6}{7}$$

48. 4320

Sol.  $a_3$  is coefficient of  $x^3$

$$\frac{10!}{8!} \times 3 \times 4 + \frac{10!}{7!3!} \times 3^3 = 4320$$

49. 1

Sol. Applying  $C_1 \rightarrow C_1 - \sin \theta C_3$  and  $C_2 \rightarrow C_2 + \cos \theta C_3$ , we get

$$f(\theta) = \begin{vmatrix} 1 & 0 & -\sin \theta \\ 0 & 1 & \cos \theta \\ \sin \theta & -\cos \theta & 0 \end{vmatrix}$$

Applying  $R_3 \rightarrow R_3 - \sin \theta R_1 + \cos \theta R_2$ , we get

$$f(\theta) = \begin{vmatrix} 1 & 0 & -\sin \theta \\ 0 & 1 & \cos \theta \\ \sin \theta & 0 & \sin^2 \theta + \cos^2 \theta \end{vmatrix} = 1$$

Thus,  $f\left(\frac{\pi}{6}\right) = 1$

50. 7

Sol.  $a = n$  (111111) is divisible  $7 \times 11 \times 3$ .  
 Hence for  $a$  to be a divisible by 924,  $n = 4$  or  $8$  and  $n + m = 11$ ;  $k = nm$   
 $\therefore (n, m) \equiv (4, 7), (8, 3)$   
 $\therefore \text{required value} = \frac{4 \times 7}{8 \times 3} = 1.67$

51. 3

Sol.

