

# Competishun

52/6, Opposite Metro Mas Hospital, Shipra Path, Mansarovar

Date: 16/12/2024

Time: 3 hours

Max. Marks: 300

UTS-1\_MT-10 (24-25)

## Physics

### Single Choice Question

**Q1** The impedance of a series RL circuit is same as the series RC circuit when connected to the same AC source separately keeping the same resistance. The frequency of the source is

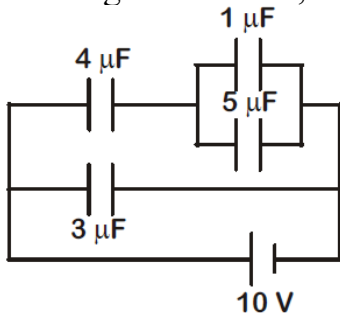
a)  $\frac{1}{\sqrt{LC}}$

b)  $\frac{1}{2\pi\sqrt{LC}}$

c)  $\frac{R}{L}$

d)  $\frac{1}{RC}$

**Q2** In the given circuit, the charge on  $4\ \mu\text{F}$  capacitor will be



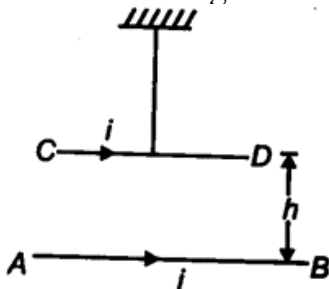
a)  $5.4\ \mu\text{C}$

b)  $9.6\ \mu\text{C}$

c)  $13.4\ \mu\text{C}$

d)  $24\ \mu\text{C}$

**Q3** In the arrangement shown, AB is a fixed current carrying long wire. Wire CD is held stationary with the help of an ideal string in gravity. If tension in the string is two times the weight of wire CD, mass per unit length of wire CD is



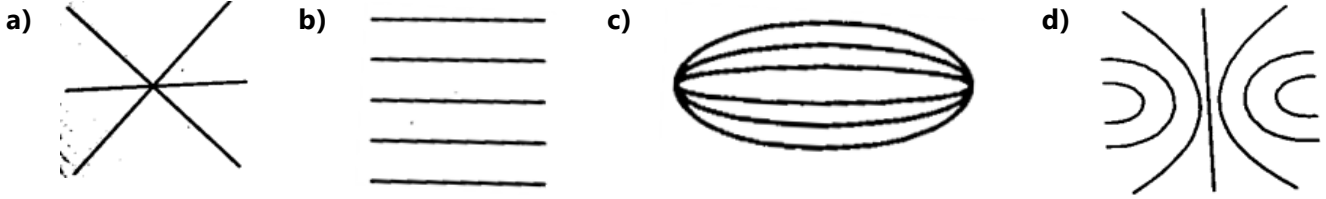
a)  $\frac{\mu_0 i^2}{2\pi hg}$

b)  $\frac{\mu_0 i^2}{4\pi hg}$

c)  $\frac{\mu_0 i^2}{\pi hg}$

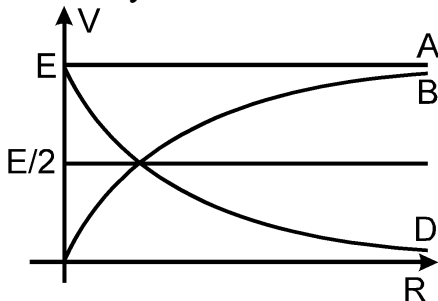
d)  $\frac{\mu_0 i^2}{2hg}$

**Q4** Which of the following represents the equipotential lines/surfaces of a dipole?

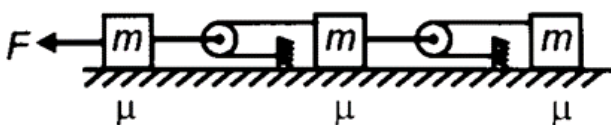


- Q5** Two particles are moving towards each other along a line joining them, so that their centre of mass does not move. After elastic collision between them,
- a) their centre of mass will move
  - b) their velocities will not change
  - c) their speeds will not change
  - d) their velocities will not change only if they have equal mass

**Q6** A cell of emf  $E$  having an internal resistance ' $r$ ' is connected to a variable external resistance  $R$ . The potential difference ' $v$ ' across the resistance  $R$  varies with  $R$  as shown by the curve:



- a) A
  - b) B
  - c) C
  - d) D
- Q7** Let  $K_1$  be the maximum kinetic energy of photoelectrons emitted by a light of wavelength  $\lambda_1$  and  $K_2$  corresponding to  $\lambda_2$ . If  $\lambda_1 = 2\lambda_2$  then.
- a)  $K_1 < \frac{K_2}{2}$
  - b)  $K_1 > 2K_2$
  - c)  $2K_1 = K_2$
  - d)  $K_1 = 2K_2$
- Q8** Two beams of light having intensities  $4I$  and  $9I$  interfere to produce an interference pattern on a screen. The phase difference between the beams is  $\frac{\pi}{2}$  at point A and  $\pi$  at point B. Then the difference between the resultant intensities at points A and B on the screen is
- a)  $12 I$
  - b)  $6 I$
  - c)  $9 I$
  - d)  $8 I$
- Q9** On a table, three blocks (including the first block) are placed as shown in the figure. Mass of each block is  $m$  and coefficient of friction for each block is  $\mu$ . A force  $F$  is applied on the first block so as to move the system. The minimum value of  $F$  should be

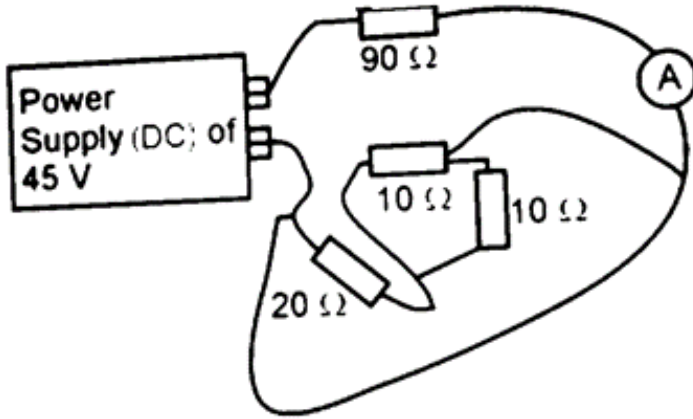


- a)  $8 \mu mg$
- b)  $9 \mu mg$
- c)  $7 \mu mg$
- d)  $5 \mu mg$

**Q10** A simple pendulum of length  $\ell$  is hanging from ceiling of an elevator moving up with a constant velocity  $v$ . The time period of simple pendulum is

- a)  $T = 2\pi\sqrt{\frac{\ell}{g}}$       b)  $T = 2\pi\sqrt{\frac{\ell}{g+v}}$       c)  $T = 2\pi\sqrt{\frac{v\ell}{g}}$       d)  $T = 2\pi\sqrt{\frac{\ell}{v}}$

**Q11** What will the ideal ammeter read for the circuit shown here?



- a) 0.5 A      b)  $\frac{45}{130}$  A      c)  $\frac{45}{94}$  A      d)  $\frac{9}{23}$  A

**Q12** Instantaneous displacement current of 1.0 A in the space between the parallel plates of  $1\mu\text{F}$  capacitor can be established by changing potential difference of:

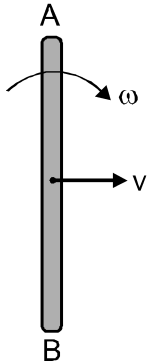
- a)  $10^{-6}$  V/s      b)  $10^6$  V/s      c)  $10^{-8}$  V/s      d)  $10^8$  V/s

**Q13** The energy spectrum of a black body exhibits maximum around a wavelength  $\lambda_0$ . The temperature of the black body is now changed such that the energy is maximum

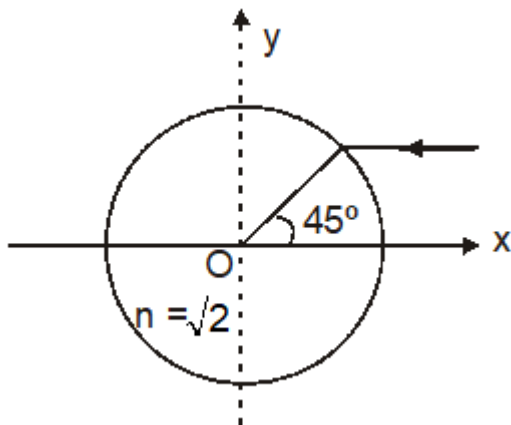
around a wavelength  $\frac{3\lambda_0}{4}$ . The power radiated by the black body will now increase by a factor of

- a)  $\frac{256}{81}$       b)  $\frac{64}{27}$       c)  $\frac{16}{9}$       d)  $\frac{4}{3}$

- Q14** A metal rod of length  $\ell$ , moving with an angular velocity  $\omega$  and velocity of its centre is  $v$ . Find potential difference between points A and B at the instant shown in figure. A uniform magnetic field of strength  $B$  exist perpendicular to plane of paper :



- a)  $Bv\ell$       b)  $Bv\ell + \frac{1}{2}B\omega\ell^2$       c)  $B\omega\ell - \frac{1}{2}B\omega\ell^2$       d)  $Bv\ell + B\omega\left(\frac{\ell}{2}\right)^2$
- Q15** A pressure-pump has a horizontal tube of cross-sectional area  $10 \text{ cm}^2$  for the outflow of water at a speed of  $20 \text{ m/s}$ . The force exerted on the vertical wall just in front of the tube which stops water horizontally flowing out of the tube, is: [given : density of water =  $1000 \text{ kg/m}^3$ ]
- a)  $300 \text{ N}$       b)  $500 \text{ N}$       c)  $250 \text{ N}$       d)  $400 \text{ N}$
- Q16** Pressure gradient in the horizontal direction in a static fluid is represented by ( $z$ -direction is vertically upwards, and  $x$ -axis is along horizontal,  $d$  is density of fluid) :
- a)  $\frac{\partial p}{\partial z} = -dg$       b)  $\frac{\partial p}{\partial x} = dg$       c)  $\frac{\partial p}{\partial x} = 0$       d)  $\frac{\partial p}{\partial z} = 0$
- Q17** A vernier calliper has 20 divisions on the vernier scale, which coincide with 19 on the main scale. The least count of the instrument is  $0.1 \text{ mm}$ . The main scale divisions are of-
- a)  $0.5 \text{ mm}$       b)  $1 \text{ mm}$       c)  $2 \text{ mm}$       d)  $1/4 \text{ mm}$
- Q18** A light ray parallel to  $x$ -axis is incident on a transparent sphere of refractive index  $\sqrt{2}$  as shown in figure. Then unit vector in the direction of emergent ray is-

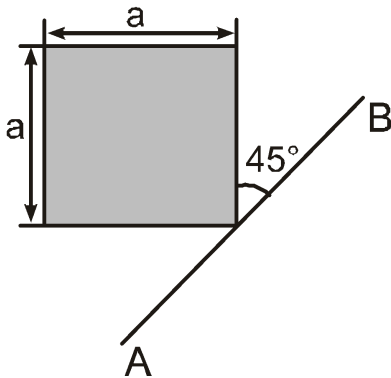


- a)  $-\hat{j}$       b)  $-\frac{1}{\sqrt{2}}\hat{i} - \frac{1}{\sqrt{2}}\hat{j}$       c)  $-\frac{1}{2}\hat{i} - \frac{\sqrt{3}}{2}\hat{j}$       d)  $-\frac{\sqrt{3}}{2}\hat{i} - \frac{1}{2}\hat{j}$

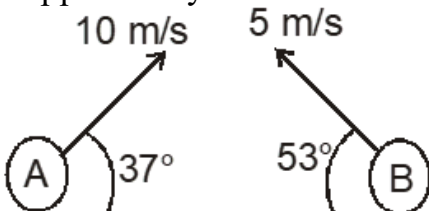
- Q19** A satellite is in a circular orbit around the earth has kinetic energy  $E_k$ . Minimum amount of energy that is added so that it escapes the earth's gravitational field is:
- a)  $E_k$                       b)  $E_k/2$                       c)  $E_k/4$                       d)  $2 E_k$
- Q20** A ideal gas is expanded to double its volume by two different process. One is isobaric and the other is isothermal. Let  $W_1$  and  $W_2$  be the respective work done, then :
- a)  $W_2 = W_1 \ln(2)$                       b)  $W_2 = \frac{W_1}{\ln(2)}$                       c)  $W_2 = \frac{W_1}{2}$                       d)  $W_1 = \frac{W_2}{2}$

### Numerical

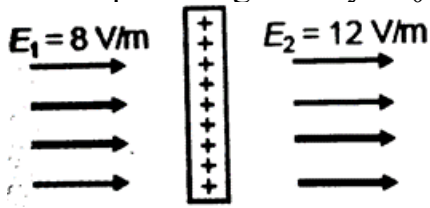
- Q21** In Bohr's atomic model, the electron is assumed to revolve in a circular orbit of radius  $0.5 \text{ \AA}$ . If the speed of electron is  $2.2 \times 10^6 \text{ m/s}$ , then the current associated with the electron will be \_\_\_\_\_  $\times 10^{-2} \text{ mA}$ . [Take  $\pi$  as  $\frac{22}{7}$ ]
- Q22** In the resonance tube experiment, first resonant length is  $\ell_1$  and the second resonant length is  $\ell_2$ , then the third resonant length is  $n \ell_2 - m \ell_1$ , find  $(m + n)$ .
- Q23** Find the moment of inertia (in  $\text{kg.m}^2$ ) of a thin uniform square sheet of mass  $M = 3\text{kg}$  and side  $a = 2\text{m}$  about the axis AB which is in the plane of sheet :



- Q24** Two stones are in the same horizontal line and are  $50\sqrt{5} \text{ m}$  away. They are projected with a velocity of  $10 \text{ m/s}$  and  $5 \text{ m/s}$ . respectively and with an angle of  $37^\circ$  and  $53^\circ$  with horizontal respectively. Find the minimum distance between them in meters. Suppose they don't strike the ground during the motion. (take  $g = 10\text{m/s}^2$ )



- Q25** The net electric field on two sides of an infinite sheet is shown in the figure. Assuming that sheet is placed in a uniform electric field. The surface charge density on the plate is given by  $n\epsilon_0$ . Value of  $n$  is \_\_\_\_\_.

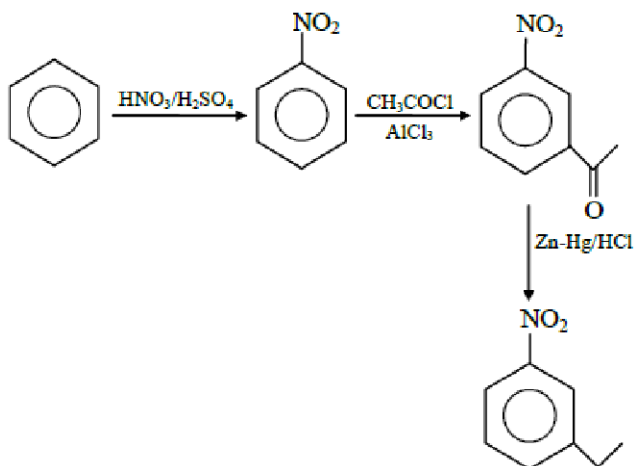


## Chemistry

### Single Choice Question

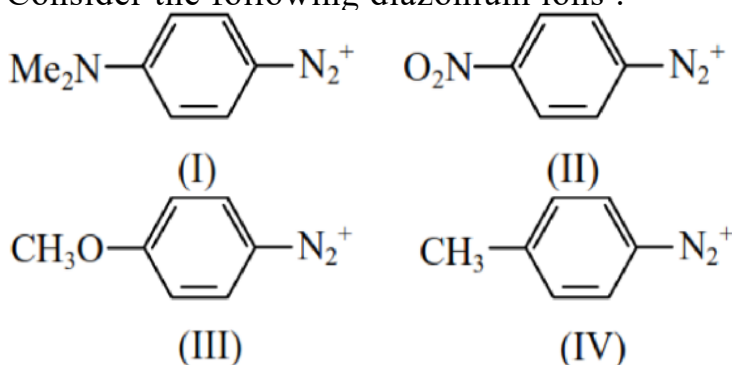
- Q26** If isotopic distribution of  $C^{12}$  and  $C^{14}$  is 98.0% and 2.0%, respectively, then the number of  $C^{14}$  atoms in 12 g of carbon is  
 a)  $1.032 \times 10^{22}$       b)  $1.20 \times 10^{22}$       c)  $5.88 \times 10^{23}$       d)  $6.02 \times 10^{23}$
- Q27** The correct order for the wavelength of absorption in the visible region is :  
 a)  $[Ni(NO_2)_6]^{4-} < [Ni(NH_3)_6]^{2+} < [Ni(H_2O)_6]^{2+}$   
 b)  $Ni(NO_2)_6]^{4-} < [Ni(H_2O)_6]^{2+} < [Ni(NH_3)_6]^{2+}$   
 c)  $[Ni(H_2O)_6]^{2+} < [Ni(NH_3)_6]^{2+} < [Ni(NO_2)_6]^{4-}$   
 d)  $[Ni(NH_3)_6]^{2+} < [Ni(H_2O)_6]^{2+} < [Ni(NO_2)_6]^{4-}$

**Q28**



Which step is wrong in above synthesis ?

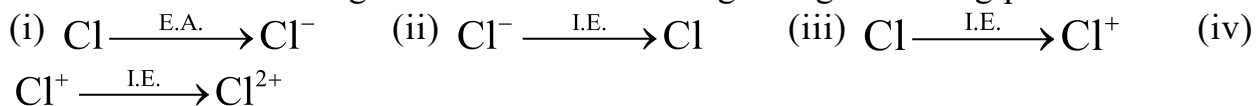
- a) (i)      b) (ii)      c) (iii)      d) None
- Q29** Consider the following diazonium ions :



The order of reactivity towards diazo-coupling with phenol in the presence of dil. NaOH is –

- a)  $I < IV < II < III$       b)  $I < III < IV < II$       c)  $III < I < II < IV$       d)  $III < I < IV < II$

**Q30** Which of the following statement is correct regarding following process?



- a) | I.E. of process (ii) |=| E.A. of process (i) |  
 b) | I.E. of process (iii) |=| I.E. of process (ii) |  
 c) | I.E. of process (iv) |=| E.A. of process (i) |  
 d) | I.E. of process (iv) |=| I.E. of process (iii) |

**Q31** In chromyl chloride, the number of d-electrons present on chromium is same as in (Given atomic no. of Ti : 22, V : 23, Cr : 24, Mn : 25, Fe : 26)

- a) Ti (III)                      b) Fe (III)                      c) V (IV)                      d) Mn (VII)

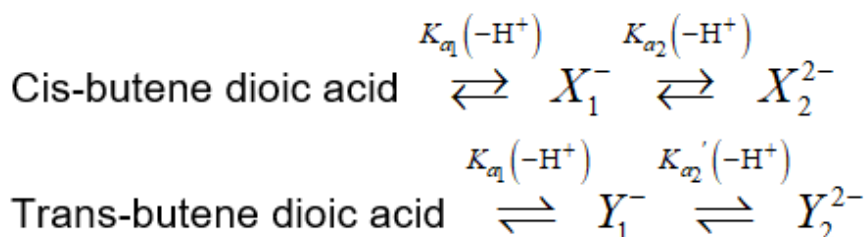
**Q32** If equivalent conductance of 1M benzoic acid is  $12.8 \text{ ohm}^{-1} \text{ cm}^2 \text{ eq}^{-1}$  and if the conductance of benzoate ion and  $\text{H}^+$  ion are  $42$  and  $288.42 \text{ ohm}^{-1} \text{ cm}^2 \text{ eq}^{-1}$  respectively. its degree of dissociation is

- a) 39%                      b) 3.9%                      c) 0.35%                      d) 0.039%

**Q33** What is  $[\text{H}^+]$  of a solution that is 0.01 M in HCN and 0.02 M in NaCN ( $K_a$  for HCN =  $6.2 \times 10^{-10}$ )

- a)  $3.1 \times 10^{10}$                       b)  $6.2 \times 10^5$                       c)  $6.2 \times 10^{-10}$                       d)  $3.1 \times 10^{-10}$

**Q34**



The incorrect statement regarding above information is:

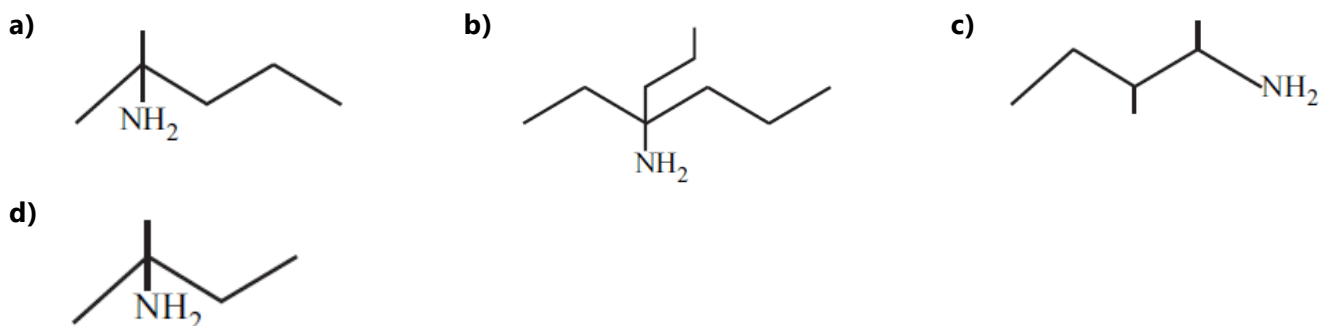
- a)  $X_2^{2-}$  species is more basic than  $Y_2^{2-}$  species  
 b)  $X_1^-$  species is more basic than  $Y_1^-$  species                      c)  $K_{a1}$  is greater than  $K_{a1}'$   
 d)  $K_{a2}'$  is greater than  $K_{a2}'$

**Q35** The electron gain enthalpy (in kJ/mol) of fluorine, chlorine, bromine and iodine, respectively, are :



- a) -296, -325, -333 and -349                      b) -333, -325, -349 and -296  
 c) -349, -333, -325 and -296                      d) -333, -349, -325 and -296



**Q36** A primary amine on treatment with  $\text{NaNO}_2/\text{HCl}$  gives alcohol which on dehydration followed by ozonolysis gives two compounds. One of them gives +ve iodoform test but negative tollen's test while other gives +ve tollen's test but negative iodoform test. If alcohol does not produce any colour in victor maeyer test then structure of amine will be :

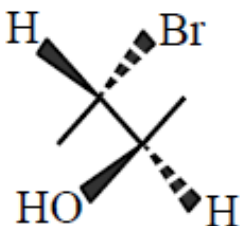


**Q37** Match the compounds of column-I with the reagent of column-II, which can distinguish between the compounds of column-I.

	Column-I		Column-II
(P)	$\text{CH}_3-\text{C}\equiv\text{C}-\text{H}$ (I), $\text{CH}_3-\text{CH}=\text{O}$ (II)	(1)	Tollen's reagent
(Q)	 (I),  (II)	(2)	Lucas reagent
(R)	$\text{CH}_3-\text{CH}(\text{OH})-\text{CH}_3$ (I), $\text{CH}_3-\text{C}(=\text{O})-\text{CH}_3$ (II)	(3)	Neutral $\text{FeCl}_3$

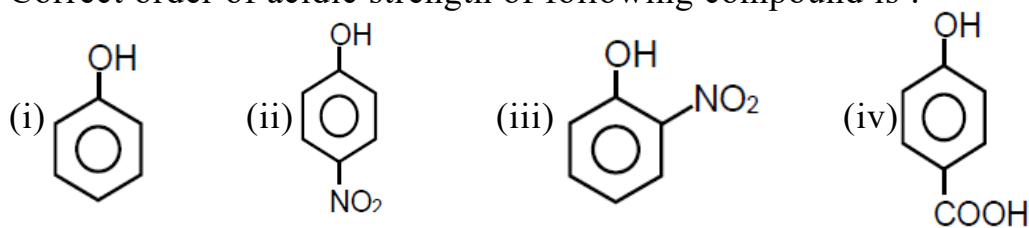
a) P-3; Q-2; R-1   b) P-1; Q-2; R-3   c) P-2; Q-1; R-3   d) P-1; Q-3; R-2

**Q38** The correct IUPAC name of the compound is



a) (2R, 3R)-3-Bromo-2-butanol   b) (2R, 3S)-3-Bromo-2-hydroxybutane  
c) (2R, 3S)-3-Bromo-2-butanol   d) (2S, 3R)-2-Bromo-3-butanol

**Q39** Correct order of acidic strength of following compound is :

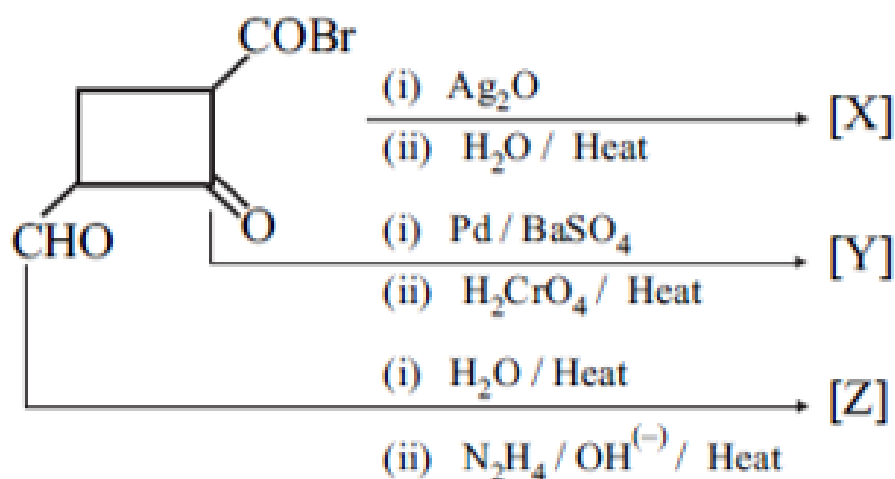


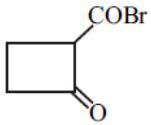
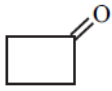
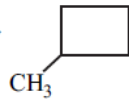
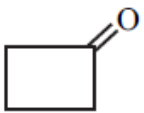

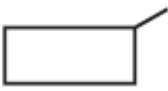
- a)  $iv > ii > iii > i$     b)  $iii > ii > iv > i$     c)  $iv > iii > ii > i$     d)  $ii > iii > iv > i$

**Q40** A doctor by mistake administers a  $Ba(NO_3)_2$  solution to a patient for radiography investigations. Which of the following should be given as the best to prevent the absorption of soluble barium?

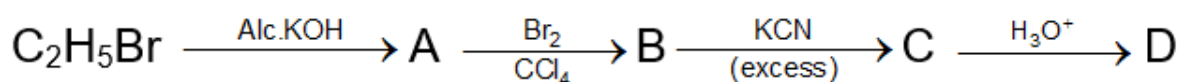
- a) NaCl    b)  $Na_2SO_4$     c)  $Na_2CO_3$     d)  $NH_4Cl$

**Q41**



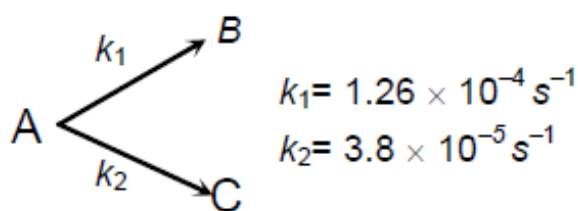
- a)  $X \Rightarrow$    $Y \Rightarrow$    $Z \Rightarrow$  
- b) X & Y are  & Z is 
- c) X, Y & Z all are     d)  $X = Z \neq Y$

**Q42** The acid D obtained through the following sequence of reactions is



- a) Succinic acid    b) Malonic acid    c) Maleic acid    d) Oxalic acid

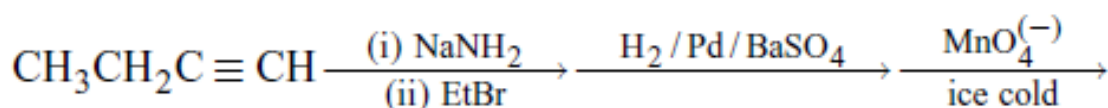
- Q43** A Substance undergoes first order decomposition. The decomposition follows two parallel first order reactions as



The percentage distribution of B and C are

- a) 75% B and 25% C      b) 80% B and 20% C      c) 60% B and 40% C  
d) 76.83% B and 23.17% C

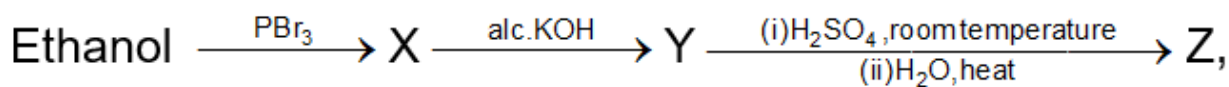
**Q44**



Final product of this reaction

- a) is optically active      b) contain three chiral 'C' atoms      c) is optically inactive  
d) is a racemic mixture

- Q45** Consider the following reaction,



the product Z, is

- a)  $\text{CH}_2=\text{CH}_2$       b)  $\text{CH}_3\text{CH}_2\text{OCH}_2\text{CH}_3$       c)  $\text{CH}_3\text{CH}_2\text{OSO}_3\text{H}$       d)  $\text{CH}_3\text{CH}_2\text{OH}$

### Numerical

- Q46**  $\text{C}_6\text{H}_6$  freezes at  $5.5^\circ\text{C}$ . The temperature at which a solution 10 g of  $\text{C}_4\text{H}_{10}$  in 200 g of  $\text{C}_6\text{H}_6$  freeze is \_\_\_\_\_  $^\circ\text{C}$ . (The molal freezing point depression constant of  $\text{C}_6\text{H}_6$  is  $5.12^\circ\text{C/m}$ .) (Rounded off to the nearest integer)
- Q47** Assuming ideal behaviour, the magnitude of  $\log K$  for the following reaction at  $25^\circ\text{C}$  is  $x \times 10^{-1}$ . The value of x is \_\_\_\_\_. (Integer answer)  
 $3\text{HC}\equiv\text{CH}_g \rightleftharpoons \text{C}_6\text{H}_{6(l)}$   
 [Given:  $\Delta_f G^\circ(\text{HC}\equiv\text{CH}) = -2.04 \times 10^5 \text{ J mol}^{-1}$ ;  $\Delta_f G^\circ(\text{C}_6\text{H}_6) = -1.24 \times 10^5 \text{ J mol}^{-1}$ ;  $R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$ ]
- Q48** Number of amphoteric compound among the following is \_\_\_\_\_  
 (i)  $\text{BeO}$       (ii)  $\text{BaO}$       (iii)  $\text{Be}(\text{OH})_2$       (iv)  $\text{Sr}(\text{OH})_2$

- Q49** A proton and a  $\text{Li}^{3+}$  nucleus are accelerated by the same potential. If  $\lambda_{\text{Li}}$  and  $\lambda_{\text{P}}$  denote the de Broglie wavelengths of  $\text{Li}^{3+}$  and proton respectively, then the value of  $\frac{\lambda_{\text{Li}}}{\lambda_{\text{P}}}$  is  $x \times 10^{-1}$ . The value of  $x$  is \_\_\_\_\_.  
(Rounded off to the nearest integer)  
(Mass of  $\text{Li}^{3+} = 8.3$  mass of proton)
- Q50** Gaseous cyclobutene isomerizes to butadiene in a first order process which has a 'k' value of  $3.3 \times 10^{-4} \text{s}^{-1}$  at  $153^\circ\text{C}$ . The time in minutes it takes for the isomerization to proceed 40 % to completion at this temperature is \_\_\_\_\_.  
(Rounded off to the nearest integer)

## Mathematics

### Single Choice Question

- Q51** The integral  $\int \cos(\log_e x) dx$  is equal to (where C is a constant of integration)
- a)  $x[\cos(\log_e x) - \sin(\log_e x)] + C$       b)  $\frac{x}{2}[\cos(\log_e x) + \sin(\log_e x)] + C$   
 c)  $\frac{x}{2}[\sin(\log_e x) - \cos(\log_e x)] + C$       d)  $x[\cos(\log_e x) + \sin(\log_e x)] + C$
- Q52** If  $a^2 + b = 2$  then maximum value of term independent of x in expression of  $(ax^{1/6} + bx^{-1/3})^9$  ( $a > 0, b > 0$ ) is  $9^k + k + 1$ , then value of k is
- a) 4      b) 2      c) 3      d) 1
- Q53** If a, b, c are distinct odd integers and  $\omega$  is non real cube root of unity and minimum value of  $|a\omega^2 + b + c\omega|$  is k, then value of  $k^2$  is
- a) 12      b) 10      c) 14      d) 8
- Q54** Let two points be A(1, -1) and B(0, 2). If a point P(x', y') be such that the area of  $\Delta PAB = 5$  sq. units and it lies on the line,  $3x + y - 4\lambda = 0$ , then a value of  $\lambda$  is
- a) 4      b) 3      c) 6      d) 8
- Q55** If a, b, c are distinct & rational numbers then
- $$\begin{vmatrix} (a^2 + b^2 + c^2) & ab + bc + ca & ab + bc + ac \\ ab + bc + ca & (a^2 + b^2 + c^2) & (bc + ca + ab) \\ ab + bc + ca & (ab + bc + ca) & (a^2 + b^2 + c^2) \end{vmatrix}$$
- is always :-
- a) Zero   b) Rational & Positive   c) Rational & Negative   d) Irrational and Positive
- Q56** If  $\sum_{i=1}^5 x_i^2 = 40$  &  $\sum_{j=6}^{10} x_j^2 = 20$  and mean of  $x_1, x_2, \dots, x_5$ , is 1 and mean of  $x_6, x_7, \dots, x_{10}$  is 2 then variance of  $x_1, x_2, \dots, x_{10}$  is
- a)  $\frac{13}{4}$       b)  $\frac{15}{4}$       c)  $\frac{17}{4}$       d)  $\frac{19}{4}$
- Q57** Considering only the principal values of the inverse trigonometric functions, the domain of the function  $f(x) = \cos^{-1}\left(\frac{x^2 - 4x + 2}{x^2 + 3}\right)$  is :
- a)  $\left(-\infty, \frac{1}{4}\right]$       b)  $\left[-\frac{1}{4}, \infty\right)$       c)  $\left(-\frac{1}{3}, \infty\right)$       d)  $\left(-\infty, \frac{1}{3}\right]$

- Q58** Let  $S$  be the set of points where the function,  $f(x) = |2 - |x - 3||$ ,  $x \in \mathbb{R}$ , is not differentiable. Then  $\sum_{x \in S} f(f(x))$  is equal to \_\_\_\_\_.
- a) 3                                      b) 4                                      c) 6                                      d) 8
- Q59** Let  $f(x) = e^x - x$  and  $g(x) = x^2 - x$ ,  $\forall x \in \mathbb{R}$ . Then the set of all  $x \in \mathbb{R}$ , where the function  $h(x) = (f \circ g)(x)$  is increasing, is :
- a)  $\left[-1, \frac{-1}{2}\right] \cup \left[\frac{1}{2}, \infty\right)$                                       b)  $[0, \infty)$                                       c)  $\left[0, \frac{1}{2}\right] \cup [1, \infty)$                                       d)  $\left[\frac{-1}{2}, 0\right] \cup [1, \infty)$
- Q60** Let  $S$  be the set of all values of  $\lambda$ , for which the shortest distance between the line  $\frac{x-\lambda}{0} = \frac{y-3}{4} = \frac{z+6}{1}$  and  $\frac{x+\lambda}{3} = \frac{y}{-4} = \frac{z-6}{0}$  is 13. Then  $8 \left| \sum_{\lambda \in S} \lambda \right|$  is equal to -
- a) 304                                      b) 308                                      c) 306                                      d) 302
- Q61** The sum of the absolute maximum and minimum values of the function  $f(x) = |x^2 - 5x + 6| - 3x + 2$  in the interval  $[-1, 3]$  is equal to :
- a) 12                                      b) 15                                      c) 8                                      d) 10
- Q62** Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three unit vectors such that  $|\vec{a} - \vec{b}|^2 + |\vec{a} - \vec{c}|^2 = 8$  Then  $|\vec{a} + 2\vec{b}|^2 + |\vec{a} + 2\vec{c}|^2$  is equal to
- a) 4                                      b) 2                                      c) 8                                      d) 6
- Q63** If the order of the differential equation of the family of circles touching the x-axis at the origin is  $k$ , then  $2k$  is equal to.
- a) 2                                      b) 6                                      c) 3                                      d) 4
- Q64** The area bounded by  $y = xe^{|x|}$  and the lines  $|x| = 1, y = 0$  is
- a) 4 sq unit                                      b) 6 sq units                                      c) 1 sq unit                                      d) 2 sq units
- Q65** Let  $\lambda$  be number of points with integral coordinates lying inside the circle  $x^2 + y^2 = 36$ , then  $\lambda =$
- a) 110                                      b) 109                                      c) 120                                      d) 115
- Q66** Let  $E_1 : \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ ,  $a > b$ . Let  $E_2$  be another ellipse such that it touches the end points of major axis of  $E_1$  and the foci of  $E_2$  are the end points of minor axis of  $E_1$ . If  $E_1$  and  $E_2$  have same eccentricities, then its value is :
- a)  $\frac{-1+\sqrt{5}}{2}$                                       b)  $\frac{-1+\sqrt{8}}{2}$                                       c)  $\frac{-1+\sqrt{3}}{2}$                                       d)  $\frac{-1+\sqrt{6}}{2}$

- Q67** If  $P$  is a point on the parabola  $y = x^2 + 4$  which is closest to the straight line  $y = 4x - 1$ , then the coordinates of  $P$  are :
- a) (3,13)                      b) (1,5)                      c) (-2,8)                      d) (2,8)
- Q68** 'A' throws a fair coin 3 times whereas 'B' throws the same coin 4 times. The probability that they get equal number of heads is
- a)  $\frac{23}{128}$                       b)  $\frac{35}{128}$                       c)  $\frac{25}{128}$                       d)  $\frac{17}{128}$
- Q69** If  $A$  and  $B$  are two sets such that  $A = \{1, 2, x\}$ ,  $B = \{3, 4, y\}$  and  $\{1, 3\} \times \{2, 4\} \subseteq A \times B$  then the value of  $x + y$  is
- a) 7                      b) 2                      c) 5                      d) 4
- Q70**  $\lim_{x \rightarrow 0} \left[ \min(y^2 - 4y + 11) \frac{\sin x}{x} \right]$  is equal to (where  $[.]$  denotes the greatest integer function) is :-
- a) 2                      b) 4                      c) 6                      d) 8

### Numerical

- Q71** Let  $a, b, c, d$  be four distinct real numbers in A.P. Find the smallest positive value of  $k$  satisfying  $2(a - b) + k(b - c)^2 + (c - a)^3 = 2(a - d) + (b - d)^2 + (c - d)^3$ .
- Q72** A committee of 6 members is to be chosen from among 5 democrates and 3 republicians so that atleast two members of each party serve on the committee. Number of possible ways it can be done, is
- Q73** Let  $S$  be the set which contains all possible values of  $l, m, n, p, q, r$  for which
- $$A = \begin{bmatrix} l^2 - 3 & p & 0 \\ 0 & m^2 - 8 & q \\ r & 0 & n^2 - 15 \end{bmatrix}$$
- be a non-singular idempotent matrix. Find the absolute value of sum of the products of elements of the set  $S$  taken two at a time.
- Q74** If  $a$  and  $b$  are the roots of equation  $x^2 - 7x - 1 = 0$ , then the value of  $\frac{a^{21} + b^{21} + a^{17} + b^{17}}{a^{19} + b^{19}}$  is equal to \_\_\_\_\_.
- Q75** Let  $\text{Max}_{0 \leq x \leq 2} \left\{ \frac{9 - x^2}{5 - x} \right\} = \alpha$  and  $\text{Max}_{0 \leq x \leq 2} \left\{ \frac{9 - x^2}{5 - x} \right\} = \beta$
- If  $\int_{\beta - \frac{8}{3}}^{2\alpha - 1} \text{Max} \left\{ \frac{9 - x^2}{5 - x}, x \right\} dx = \alpha_1 + \alpha_2 \log_e \left( \frac{8}{15} \right)$  then  $\alpha_1 + \alpha_2$  is equal to \_\_\_\_\_





## Answer Key

Que.	1	2	3	4	5	6	7	8	9	10
<b>Ans.</b>	<b>B</b>	<b>D</b>	<b>A</b>	<b>D</b>	<b>C</b>	<b>B</b>	<b>A</b>	<b>A</b>	<b>C</b>	<b>A</b>
Que.	11	12	13	14	15	16	17	18	19	20
<b>Ans.</b>	<b>A</b>	<b>B</b>	<b>A</b>	<b>A</b>	<b>D</b>	<b>C</b>	<b>C</b>	<b>D</b>	<b>A</b>	<b>A</b>
Que.	21	22	23	24	25	26	27	28	29	30
<b>Ans.</b>	<b>112</b>	<b>3</b>	<b>7</b>	<b>20</b>	<b>4</b>	<b>B</b>	<b>A</b>	<b>B</b>	<b>B</b>	<b>A</b>
Que.	31	32	33	34	35	36	37	38	39	40
<b>Ans.</b>	<b>D</b>	<b>B</b>	<b>D</b>	<b>B</b>	<b>D</b>	<b>A</b>	<b>D</b>	<b>C</b>	<b>A</b>	<b>B</b>
Que.	41	42	43	44	45	46	47	48	49	50
<b>Ans.</b>	<b>B</b>	<b>A</b>	<b>D</b>	<b>C</b>	<b>D</b>	<b>1</b>	<b>855</b>	<b>2</b>	<b>2</b>	<b>26</b>
Que.	51	52	53	54	55	56	57	58	59	60
<b>Ans.</b>	<b>B</b>	<b>B</b>	<b>A</b>	<b>B</b>	<b>B</b>	<b>B</b>	<b>B</b>	<b>A</b>	<b>C</b>	<b>C</b>
Que.	61	62	63	64	65	66	67	68	69	70
<b>Ans.</b>	<b>D</b>	<b>B</b>	<b>A</b>	<b>D</b>	<b>B</b>	<b>A</b>	<b>D</b>	<b>B</b>	<b>C</b>	<b>C</b>
Que.	71	72	73	74	75					
<b>Ans.</b>	<b>16</b>	<b>25</b>	<b>29</b>	<b>51</b>	<b>34</b>					