

Competishun

52/6, Opposite Metro Mas Hospital, Shipra Path, Mansarovar

Date: 01/07/2024

Time: 3 hours

Max. Marks: 300

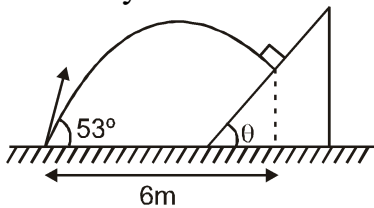
PRATHAM-1_(24-25)-MCT-2

Physics

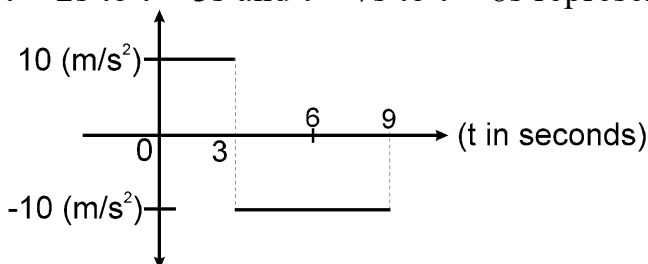
Single Choice Question

- Q1** The maximum height attained by a projectile is increased by 5%, keeping the angle of projection constant, what is the percentage increase in horizontal range?
- a) 5% b) 10% c) 20% d) 40%

- Q2** A particle is projected with a speed 10 m/s as shown in figure. The particle strikes normally on the inclined plane. Then angle θ is : ($g = 10 \text{ m/s}^2$)

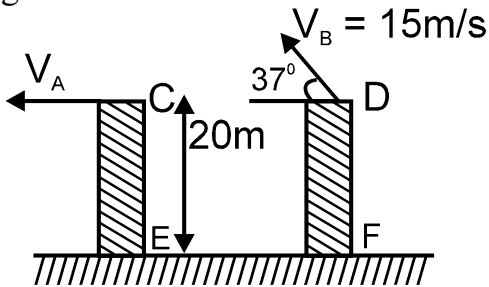


- a) $\tan^{-1} 1$ b) $\tan^{-1} 3$ c) $\tan^{-1} 2$ d) $\tan^{-1} \frac{4}{3}$
- Q3** A block is kept on a smooth inclined plane of angle of inclination θ that moves with a constant horizontal acceleration so that the block does not slide relative to the inclined plane. If the inclined plane stops, the normal contact force offered by the plane on the block changes by the factor
- a) $\cos\theta$ b) $\sec^2\theta$ c) $\sin^2\theta$ d) $\sin\theta$
- Q4** A particle starts moving along a straight line at $t = 0$. Its acceleration-time graph is shown. Correct relation between magnitudes of displacements between time durations $t = 2\text{s}$ to $t = 3\text{s}$ and $t = 7\text{s}$ to $t = 8\text{s}$ represented by S_{23} and S_{78} respectively is :

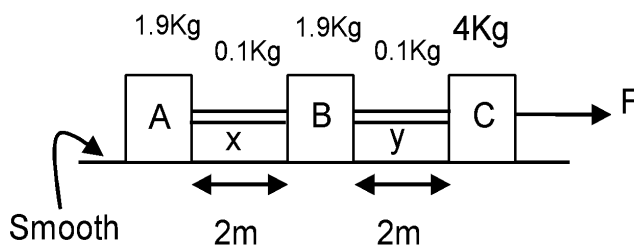


- a) $S_{23} > S_{78}$ b) $S_{78} > S_{23}$ c) $S_{23} = S_{78}$ d) insufficient information to decide

- Q5** The engine of a futuristic nuclear powered car for which power and speed can have fantastic values (say 600 kph) can produce a maximum acceleration of 5 m/s^2 and its brakes can produce a maximum retardation of 10 m/s^2 . The minimum time in which a person can reach his workplace, located 1.5 km away from his home using this car
- a) 5 sec b) 10 sec c) 15 sec. d) 30 sec
- Q6** CE and DF are two walls of equal height (20 meter) from which two particles A and B of same mass are projected as shown in the figure. A is projected horizontally towards left while B is projected at an angle 37° (with horizontal towards left) with velocity 15 m/sec. If A always sees B to be moving perpendicular to EF, then the range of A on ground is :

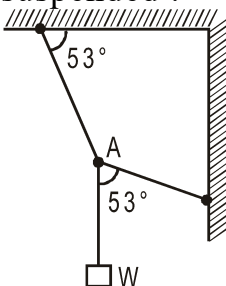


- a) 24 m b) 30 m c) 26 m d) 28 m
- Q7** Three blocks A, B & C are connected by two strings x & y as shown in figure



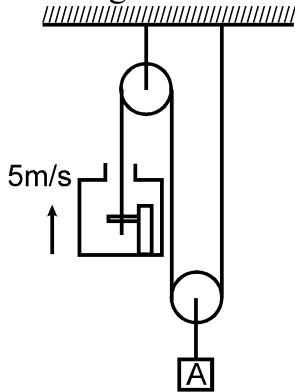
The system is pulled in right direction by force F. If breaking strength of strings x & y are 100N & 220N respectively then maximum value of F for which none of strings will break is

- a) 400N b) 440N c) 300N d) 330N
- Q8** For the equilibrium condition shown, the cords are strong enough to withstand a maximum tension 100 N. What is the largest value of W (in newton) that can be suspended :



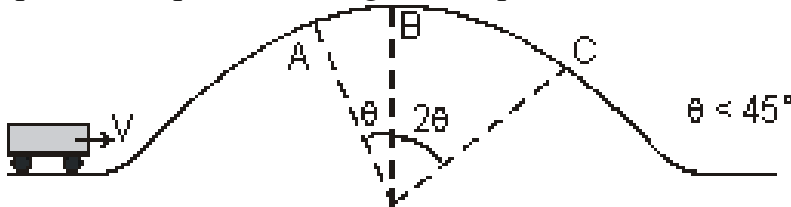
- a) 100 N b) 35 N c) 80 N d) 55 N

- Q9** A motor is fixed inside a box which is moving upwards with velocity 5 m/s. String is winding at the rate 3 m/s. Then the velocity of block A will be:



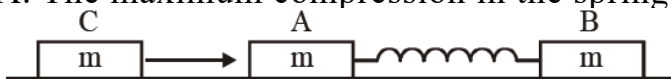
- a) 2.5 m/s downwards b) 5 m/s downwards c) 1 m/s downwards
d) 2 m/s downwards

- Q10** A self propelled vehicle (assume it as a point mass) runs on a track with constant speed V . It passes through three positions A, B and C on the circular part of the track.



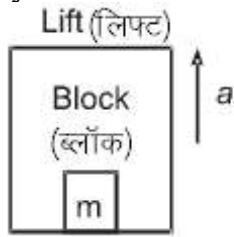
Suppose N_A , N_B and N_C are the normal forces exerted by the track on the vehicle when it is passing through points A, B and C respectively then

- a) $N_A = N_B = N_C$ b) $N_B > N_A > N_C$ c) $N_C > N_A > N_B$ d) $N_B > N_C > N_A$
- Q11** Two identical blocks A and B each of mass m resting on the smooth horizontal floor are connected by a light spring of natural length L and spring constant K . A third block C of mass m moving with a speed v along the line joining A and B collides with A. The maximum compression in the spring is

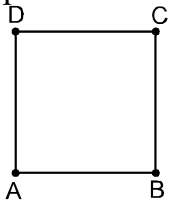


- a) $v\sqrt{\frac{M}{2K}}$ b) $\sqrt{\frac{mv}{2K}}$ c) $\sqrt{\frac{mv}{K}}$ d) $\sqrt{\frac{m}{2K}}$
- Q12** In an Atwood machine the sum of two masses is constant. The string & pulley are ideal. If the string can sustain tension equal to $15/32$ of the weight of sum of two masses then the least acceleration of two masses will be:
- a) $g/4$ b) $g/2$ c) $g/5$ d) None of these
- Q13** A bird is flying towards east with a velocity 40 km/hr and a train is moving with a velocity 40 km/hr towards east. A man in train drops a food packet. The path of food packet as seen by bird till it falls on ground is (ignore air resistance)
- a) parabola b) circle c) hyperbola d) straight line

- Q14** A body of mass m is placed inside a lift as shown in figure. If lift starts accelerating with acceleration a in upward direction starting from rest at $t = 0$, then the work done by normal reaction during time duration $t = 0$ to $t = t$ as seen from frame of the lift is –

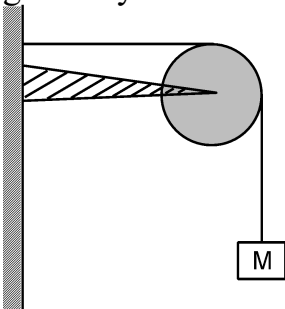


- a) $\frac{1}{2} ma (g + a) t^2$ b) Zero c) $\frac{1}{2} m (g + a) t^2$ d) $\frac{1}{2} mgat^2$
- Q15** Four particles A, B, C and D are initially at the four corners of a square as shown. They move with constant speed u . A is always moving towards B, B is moving towards C, C is moving towards D and D is moving towards A. Then the distance between the particles A and B.



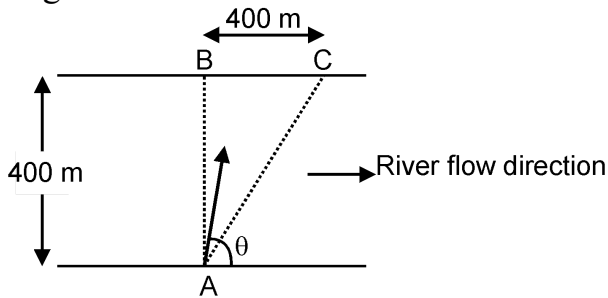
- a) is decreasing with constant rate
 b) is decreasing initially at faster rate and the rate is continuous decreasing
 c) is decreasing initially at faster rate and the rate is continuously increasing
 d) is decreasing but nothing can be concluded about the rate of decrease
- Q16** The position vector of particle at any time t is $\vec{r} = 3t\hat{i} + 3t^2\hat{j}$. The velocity vector makes an angle θ with positive x-axis. The rate of change of θ at time $t = 3$ sec will be (in rad/sec) :
- a) $\frac{2}{37}$ b) $\frac{2}{33}$ c) $\frac{2\sqrt{2}}{37}$ d) $\frac{5}{37}$

- Q17** A string of negligible mass goes over a clamped pulley of mass m supports a block of mass M as shown in figure. The magnitude of force on the pulley by the clamp is given by



- a) $\sqrt{2}Mg$ b) $\sqrt{2} mg$ c) $(\sqrt{(M + m)^2 + m^2}) g$
 d) $(\sqrt{(M + m)^2 + M^2}) g$

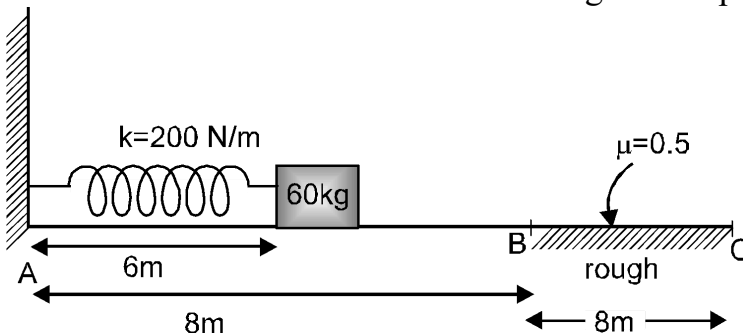
- Q18** A river is flowing with a speed of 1 km h^{-1} . A swimmer wants to go to point C starting from A. He swims with a speed of 5 km h^{-1} at an angle θ w.r.t. the river flow, at what angle with the river bank should the swimmer swim ?



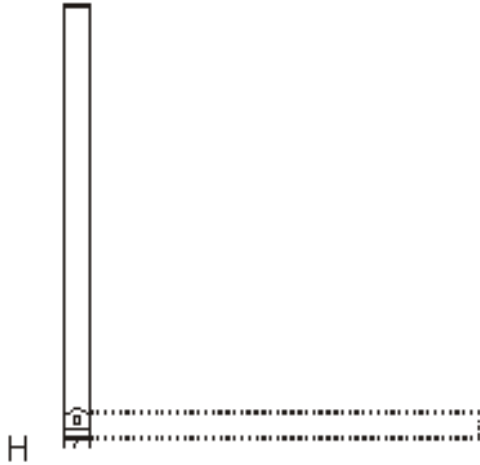
- a) 30° b) 37° c) 53° d) 60°
- Q19** A standing man observes rain falling with speed 20 m/s at an angle 30° with vertical, with what velocity man should run so that rain appears to fall vertically :
- a) 10 m/s b) $10\sqrt{3} \text{ m/s}$ c) 5 m/s d) 20 m/s
- Q20** A simple pendulum is oscillating in a vertical plane. If resultant acceleration of bob of mass m at a point A is in horizontal direction, find the tangential force at this point in terms of tension T and mg .
- a) mg b) $\frac{mg}{T} \sqrt{T^2 - (mg)^2}$ c) $\frac{mg}{T} \sqrt{(mg)^2 + T^2}$ d) $\frac{T}{mg} \sqrt{(mg)^2 + T^2}$

Numerical

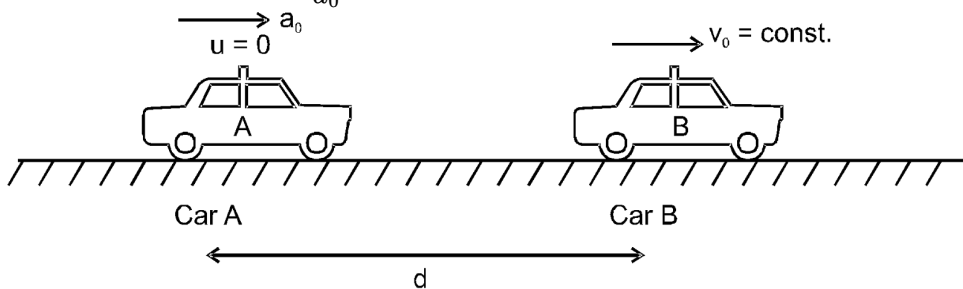
- Q21** A block of mass 60 kg is released from rest when compression in the spring is 2 m (natural length of spring is 8 m). Surface AB is smooth while surface BC is rough. Block travels x distance before coming to complete rest. Value of x is : [$g = 10 \text{ m/s}^2$]



- Q22** A thin rod of length 1 m is kept vertical and is hinged from the lower end 'H'. Its linear mass density varies with the distance (x) from the end 'H' as $\lambda = (12x) \text{ kg/m}$, where x is distance along rod from point H. The potential energy (in Joules) of the rod is 5N. Find N (at H the potential energy is zero) ($g = 10 \text{ m/s}^2$)

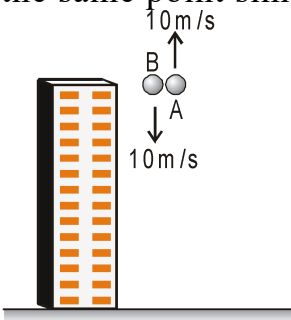


- Q23** The car B is moving with constant velocity V_0 on a long straight road. Another car A starts moving with constant acceleration a_0 to catch the car B. Initial separation between the cars is 'd'. The minimum time for which the car A should accelerate to catch the car B is $\frac{x \times V_0}{a_0}$. Find the value of x:



- Q24** A particle which is initially at rest has time-dependent acceleration given as $a = 3t^2$. Velocity (in m/s) of the particle at $t = 2 \text{ sec.}$ is :

- Q25** Both A & B are thrown simultaneously as shown from a very high tower. Find distance between the two balls after 1 seconds. (Assume that the balls are thrown from the same point simultaneously)



- Q26** Some persons hired a boat for 3 hours. The river flows at a speed of 2.5 km/hr and the speed of the boat is 7.5 km/hr relative to the water. How far (in km) can they get from the port rowing along the river flow if they want to be back in 3 hrs. Fill the value of α if distance is $(4 + \alpha) \text{ km}$

- Q27** A particle is projected from horizontal surface of earth at speed u making an angle $\theta = \cos^{-1} \left(\sqrt{\frac{5}{72}} \right)$ with the horizontal. If equation of trajectory for the particle is $y = kx - 2x^2$ (where k is a constant) then what is the speed (in m/s) of projection. (Assume that particle was projected from origin and motion of particle is in xy plane, where x -axis is along the horizontal direction and $+y$ -axis is vertically upward) [Take $g = 10 \text{ m/s}^2$]
- Q28** A particle projected from ground at some angle with verticle has displacement (w.r.t. point of projection) $\vec{S}_1 = 6\hat{i} + 8\hat{j}$ and $(8\hat{i} + 6\hat{j})$ at some moment t_1 and t_2 respectively. If the range of the projectile is $\frac{37x}{7}$ m then calculate x
- Q29** A body of mass 1 kg rests on a horizontal floor with which it has a coefficient of static friction $\frac{1}{\sqrt{3}}$. It is desired to make the body move by applying the minimum possible force F N. The value of F will be _____. (Round off to the Nearest Integer) [Take $g = 10 \text{ ms}^{-2}$]
- Q30** A particle of mass 2kg starts to move at position $x = 0$ and time $t = 0$ under the action of force $F = (10 + 4x)$ N along the x -axis on a frictionless horizontal track. Find the power delivered by the force in watts at the instant the particle has moved by the distance 5m.

Chemistry

Single Choice Question

- Q31** The nucleus of an atom is located at $x = y = z = 0$. If the probability of finding an electron in $d_{x^2-y^2}$ orbital in a tiny volume around $x=a$, $y=0$, $z=0$ is 1×10^{-5} , what is the probability of finding the electron in the same size volume around $x=0$, $y=a$, $z=0$?
- a) 1×10^{-5} b) $1 \times 10^{-5} \times a$ c) $-1 \times 10^{-5} \times a$ d) zero
- Q32** B has a smaller first ionization enthalpy than Be. Consider the following statements.
 (I) It is easier to remove 2p electron than 2s electron
 (II) 2p electron of B is more shielded from the nucleus by the inner core of electrons than the 2s electrons of Be
 (III) 2s electron has more penetration power than 2p electron
 (IV) Atomic radius of B is more than Be (atomic number B = 5, Be = 4)
 The correct statements are
- a) (I), (II) and (IV) b) (I), (III) and (IV) c) (I), (II) and (III)
 d) (II), (III) and (IV)
- Q33** Calculate the minimum and maximum number of electrons which may have magnetic quantum number, $m = +1$ and spin quantum number, $s = -\frac{1}{2}$ in chromium (Cr):
- a) 0, 1 b) 1, 2 c) 4, 6 d) 2, 3
- Q34** Consider the following statements :
1. If all the reactants are not taken in their stoichiometric ratio, then at least one reactant will be left behind.
 2. 2 moles of $H_2(g)$ and 3 moles of $O_2(g)$ produce 2 moles of water.
 3. equal wt. of carbon and oxygen are taken to produce CO_2 then O_2 is limiting reagent.
- The above statements 1, 2, 3 respectively are (T = True, F = False)
- a) T T T b) F T F c) F F F d) T F T
- Q35** Which of the following equations is a balanced one
- a) $5BiO_3^- + 22H^+ + Mn^{2+} \longrightarrow 5Bi^{3+} + 7H_2O + MnO_4^-$
 b) $5BiO_3^- + 14H^+ + 2Mn^{2+} \longrightarrow 5Bi^{3+} + 7H_2O + 2MnO_4^-$
 c) $2BiO_3^- + 4H^+ + Mn^{2+} \longrightarrow 2Bi^{3+} + 2H_2O + MnO_4^-$
 d) $6BiO_3^- + 12H^+ + 3Mn^{2+} \longrightarrow 6Bi^{3+} + 6H_2O + 3MnO_4^-$
- Q36** The strength of 10^{-2} M Na_2CO_3 solution in terms of molality will be (density of solution = 1.10 g mL^{-1}). (Molecular weight of $Na_2CO_3 = 106 \text{ g mol}^{-1}$)
- a) 9.00×10^{-3} b) 1.5×10^{-2} c) 5.1×10^{-3} d) 11.2×10^{-3}

- Q52** A doubly ionised lithium atom is hydrogen like with atomic number $z = 3$. Find the wavelength (in nano meter) of the radiation required to excite the electron in Li^{2+} from the first to the third Bohr orbit.
[Given : $\frac{1}{R_H} = 912 \text{ \AA}$] (Answer to be round off to nearest integer)
- Q53** Maximum number of moles of barium phosphate formed when 0.9 mole of barium chloride is mixed with 0.4 mole of sodium phosphate is x then what will be the value of $10x$
- Q54** How many benzenoid isomer are possible for cresol
- Q55** Calculate the total number of structural isomers of 3°-amines for the molecular formula $\text{C}_6\text{H}_{15}\text{N}$ are?
- Q56** The reaction $\text{Cl}_2 (\text{g}) + \text{S}_2\text{O}_3^{2-} \longrightarrow \text{SO}_4^{2-} + \text{Cl}^-$ is to be carried out in basic medium. Starting with 1.5 mole of Cl_2 , 0.1 mole $\text{S}_2\text{O}_3^{2-}$ and 3 mole of OH^- . How many moles of OH^- will be left in solution after the reaction is complete. Assume no other reaction occurs.
- Q57** Aluminum carbide (Al_4C_3) liberates methane on treatment with water. The grams of aluminum carbide required to produce 11.2 L of methane under STP conditions is :
[Given : $\text{Al} = 27$]
- Q58** If 240 g of carbon is taken in a container to convert it completely to CO_2 but in industry it has been found that 280 g of CO was also formed along with CO_2 . Find the mole percentage yield of CO_2 . The reactions occurring are :
 $\text{C} + \text{O}_2 \longrightarrow \text{CO}_2$; $\text{C} + \text{O}_2 \longrightarrow \text{CO}$
- Q59** An electron in an atom jumps in such a way that its kinetic energy changes from x to $\frac{x}{4}$. The change in potential energy will be if your answer is p then what will be value of $\frac{2p}{x}$:
- Q60** The number of $4f$ electrons in the ground state electronic configuration of Gd^{2+} is _____.
[Atomic number of Gd = 64]

Mathematics

Single Choice Question

- Q61** If both roots of the equation $x^2 - 6ax + 2 - 2a + 9a^2 = 0$ exceed 3, then
 a) $a < 1$ b) $a > \frac{11}{9}$ c) $a > \frac{3}{2}$ d) $a < \frac{3}{2}$
- Q62** If $\tan\theta$ and $\cot\theta$ are the roots of the equation $x^2 + 2x + 1 = 0$ then the least value of $x^2 + \tan\theta x + \cot\theta$, is
 a) $\frac{3}{4}$ b) $\frac{5}{4}$ c) $\frac{-5}{4}$ d) $\frac{-3}{4}$
- Q63** Let $P = \cos \frac{\pi}{20} \cos \frac{3\pi}{20} \cos \frac{7\pi}{20} \cos \frac{9\pi}{20}$ and $Q = \cos \frac{\pi}{15} \cos \frac{2\pi}{15} \cos \frac{4\pi}{15} \cos \frac{8\pi}{15}$, then which of the following hold good?
 a) $P + Q = 0$ b) $P = -\frac{1}{16}$ c) $Q = \frac{1}{16}$ d) $P - Q = -\frac{1}{8}$
- Q64** Let α, β, γ are roots of the equation $x^3 + qx + q = 0$ then the value of $(\alpha + \beta)^{-1} + (\beta + \gamma)^{-1} + (\gamma + \alpha)^{-1}$ is equal to
 a) 0 b) -1 c) 1 d) 2
- Q65** Consider the quadratic equation $(c - 5)x^2 - 2cx + (c - 4) = 0$, $c \neq 5$. Let S be the set of all integral values of c for which one root of the equation lies in the interval (0, 2) and its other root lies in the interval (2, 3). Then the number of elements in S is
 a) 11 b) 18 c) 12 d) 10
- Q66** The value of K for which the quadratic equation $(1 - 2k)x^2 - 6kx - 1 = 0$ and $kx^2 - x + 1 = 0$ have at least one root in common is/are
 a) $\left\{\frac{1}{2}\right\}$ b) $\left\{\frac{1}{3}, \frac{2}{9}\right\}$ c) $\left\{\frac{2}{9}\right\}$ d) $\left\{\frac{1}{2}, \frac{2}{9}\right\}$
- Q67** If λ be the ratio of the roots of the quadratic equation in x, $3m^2x^2 + m(m - 4)x + 2 = 0$, then the least value of m for which $\lambda + \frac{1}{\lambda} = 1$, is
 a) $4 - 2\sqrt{3}$ b) $4 - 3\sqrt{2}$ c) $2 - \sqrt{3}$ d) $-2 + \sqrt{2}$
- Q68** If α and β are the roots of the quadratic equation, $x^2 + x \sin\theta - 2\sin\theta = 0$, $\theta \in \left(0, \frac{\pi}{2}\right)$, then $\frac{\alpha^{12} + \beta^{12}}{(a^{-12} + \beta^{-12}) \cdot (\alpha - \beta)^{24}}$ is equal to :
 a) $\frac{2^{12}}{(\sin\theta - 8)^6}$ b) $\frac{2^{12}}{(\sin\theta - 4)^{12}}$ c) $\frac{2^6}{(\sin\theta + 8)^{12}}$ d) $\frac{2^{12}}{(\sin\theta + 8)^{12}}$
- Q69** The number of real roots of the equation $5 + |2^x - 1| = 2^x (2^x - 2)$ is :
 a) 4 b) 2 c) 1 d) 3

Numerical

- Q81** Let α and β are the roots of quadratic equation $x^2 - x - 1 = 0$, if $a_n = \frac{\alpha^n - \beta^n}{\alpha - \beta}$, $n = 1, 2, 3, \dots$
Then the value of $\frac{a_{2012} - a_{2010}}{a_{2011}}$ is equal to _____.
- Q82** The number of real roots of the equation $e^{4x} - e^{3x} - 4e^{2x} - e^x + 1 = 0$ is equal to _____.
- Q83** The sum of all real values of x for which $\frac{3x^2 - 9x + 17}{x^2 + 3x + 10} = \frac{5x^2 - 7x + 19}{3x^2 + 5x + 12}$ is equal to _____.
- Q84** Number of solutions of equation $\sin x \cdot \sqrt{8\cos^2 x} = 1$ in $[0, 2\pi]$ is _____.
- Q85** If $h(x) = \log_{10} x$, then the value of $\sum_{n=1}^{89} h(\tan n^\circ)$ is _____.
- Q86** If $\sqrt{3}(\cos^2 x) = (\sqrt{3} - 1)\cos x + 1$, the number of solutions of the given equation when $x \in \left[0, \frac{\pi}{2}\right]$ is _____.
- Q87** The number of solutions of the trigonometric equation $\sin 3\theta = 4 \sin \theta \cdot \sin 2\theta \cdot \sin 4\theta$ in $[0, \pi]$, is _____.
- Q88** The number of solution of the equation $\sin x + \sin 2x + \sin 3x = \cos x + \cos 2x + \cos 3x$ in $x \in [0, 2\pi]$, is _____.
- Q89** The exact value of $\operatorname{cosec} 10^\circ + \operatorname{cosec} 50^\circ - \operatorname{cosec} 70^\circ$ is _____.
- Q90** If value of $\frac{4\sin 9^\circ \sin 21^\circ \sin 39^\circ \sin 51^\circ \sin 69^\circ \sin 81^\circ}{\sin 54^\circ}$ is $1/K$, $K \in \mathbb{N}$, then value of K is equal to _____.

Answer Key

Que.	1	2	3	4	5	6	7	8	9	10
Ans.	A	B	C	A	D	A	A	B	C	B
Que.	11	12	13	14	15	16	17	18	19	20
Ans.	A	A	D	B	A	A	D	C	A	B
Que.	21	22	23	24	25	26	27	28	29	30
Ans.	3	8	1	8	20	6	6	2	5	300
Que.	31	32	33	34	35	36	37	38	39	40
Ans.	A	C	D	A	B	A	B	C	A	B
Que.	41	42	43	44	45	46	47	48	49	50
Ans.	D	D	D	C	A	A	A	D	A	C
Que.	51	52	53	54	55	56	57	58	59	60
Ans.	21	11	2	5	7	2	24	50	3	7
Que.	61	62	63	64	65	66	67	68	69	70
Ans.	B	C	A	C	A	C	B	D	C	B
Que.	71	72	73	74	75	76	77	78	79	80
Ans.	D	B	B	C	D	A	C	A	D	C
Que.	81	82	83	84	85	86	87	88	89	90
Ans.	1	2	6	4	0	1	8	6	6	8