

$$\frac{2210622}{2}$$

$$f = A \cdot \bar{B} + B \cdot C$$

A	B	C	$A \bar{B}$	$B C$	f
0	0	0	0	0	0
0	0	1	0	0	0
0	1	0	0	0	0
0	1	1	0	1	1
1	0	0	1	0	1
1	0	1	1	0	1
1	1	0	0	0	0
1	1	1	0	1	1

for $f = 0$, class 0: $(0,0,0)$, $(0,0,1)$, $(0,1,0)$,
 $(1,1,0)$

class 1: $f = 1$: $(0,1,1)$, $(1,0,0)$, $(1,0,1)$, $(1,1,1)$

for this to be linearly separable,

$w_1 A + w_2 B + w_3 C + b > 0$; for all points where $f = 1$

$w_1 A + w_2 B + w_3 C + b < 0$; $f = 0$

$$\begin{array}{l} \text{for } f = 0 \\ (0,0,0) \rightarrow b < 0 \\ (0,0,1) \rightarrow w_3 + b < 0 \\ (0,1,0) \rightarrow w_2 + b < 0 \\ (1,1,0) \rightarrow w_1 + w_2 + b < 0 \end{array}$$

$$\begin{array}{l} \text{for } f = 1 \\ (0,1,1) \rightarrow w_2 + w_3 + b > 0 \\ (1,0,0) \rightarrow w_1 + b > 0 \\ (1,0,1) \rightarrow w_1 + w_3 + b > 0 \\ (1,1,1) \rightarrow w_1 + w_2 + w_3 + b > 0 \end{array}$$

Contradiction:

$$(1, 0, 0) \rightarrow w_1 + b > 0 \Rightarrow w_1 > -b$$

$$(0, 1, 1) \rightarrow w_2 + w_3 + b > 0 \Rightarrow w_2 + w_3 > -b$$

again,

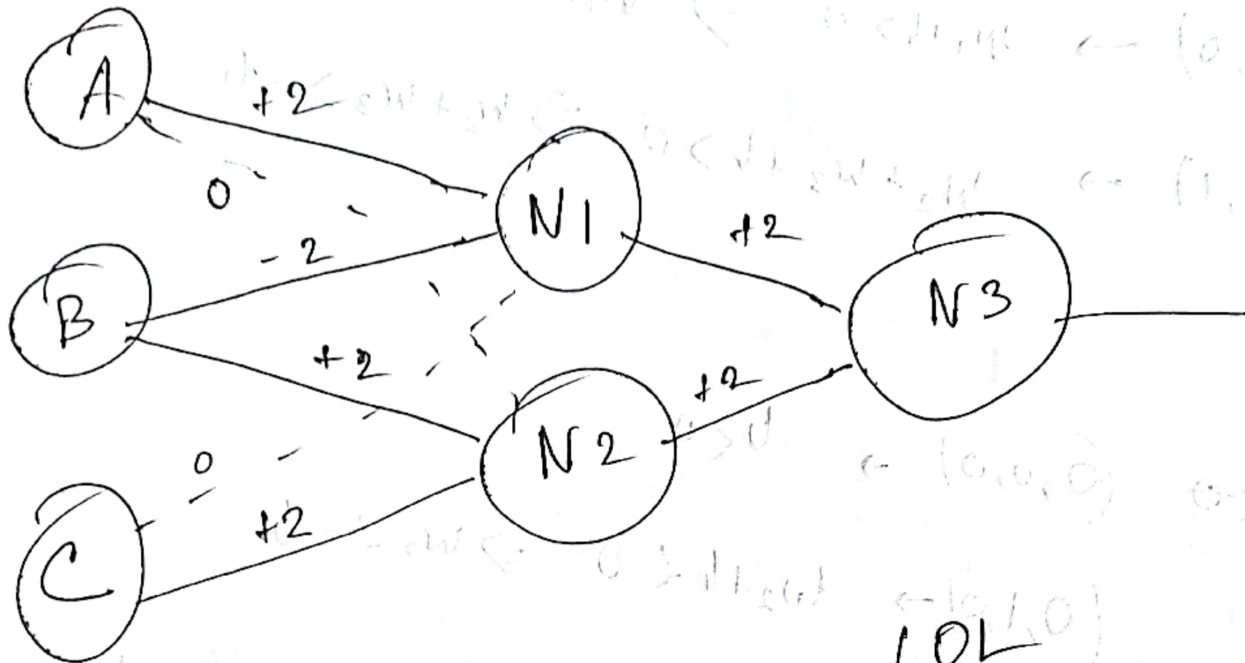
$$b < 0 \quad (0, 0, 0) \rightarrow b < 0$$

$$(0, 1, 0) \rightarrow w_2 + b < 0 \Rightarrow w_2 < -b$$

So, there are contradictions, thus, the function is not linearly separable.

not solvable by using a single perceptron.

Solution:



IL

↓
1/0

N2: let function be $f(2B+2C-\frac{2}{b})$

N1: $f(2A-2B-0.5)$

if $f(u) > 0$, $f(u) = 1$

$f(u) \leq 0$, $f(u) = 0$

N3: $f(2N1+2N2-0.5)$

$f(u) = 1$; $f(u) > 0$

$f(u) = 0$; $f(u) \leq 0$

A	B	C	N1	N2	N3
0	0	0	-0.5; 0	-2; 0 -1.5; 0	-0.5; 0
0	0	1	-0.5; 0	0; 0	-0.5; 0
0	1	0	-2.5; 0	0; 0	-0.5; 0
0	1	1	-2.5; 0	2; 1	1.5; 1
1	0	0	1.5; 1	-2; 0 0; 0	1.5; 1
1	0	1	1.5; 1	0; 0	1.5; 1
1	1	0	-0.5; 0	0; 0	-0.5; 0
1	1	1	-0.5; 0	2; 1	1.5; 1

$$N3 = f(A\bar{B} + BC)$$

$$2 - 2 - 0.5$$

So, the following network solves it,

not a single neuron as ~~it~~

it is not linearly

separable separable.