

Bachelor's thesis

# **APPLICATION OF MACHINE LEARNING TO PREDICT STAR FORMATION RATES IN SDSS DATA**

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April 23, 2025



## Assignment of bachelor's thesis

**Title:** Experiment with Machine Learning on Hierarchical Multi-Modal Astronomical Data  
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**Branch / specialization:** Artificial Intelligence 2021  
**Department:** Department of Applied Mathematics  
**Validity:** until the end of summer semester 2025/2026

### Instructions

Current astronomy is flooded by Petabyte-scaled data detected in all frequencies of the electromagnetic spectrum. In order to find new physically interesting objects and phenomena, advanced machine learning of such data becomes a natural part of data analysis. One of the most important astronomical surveys is the Sloan Digital Sky Survey (SDSS) containing several millions of sky images in five spectral filters and a similar amount of spectra observed by the same telescope. It gives a unique opportunity to study advanced machine learning methods applied to multi-dimensional and dimensionally multi-modal data. A combination of SDSS multi-color images and spectra exposed at different times results in a multi-dimensional semi-sparse datacube of about a hundred terabytes in size. For this purpose there was recently developed a parallel processing and storage framework Hierarchical Semi-Sparse Cubes (HiSS -Cube). HiSS-Cube also handles the uncertainty estimates and pre-computes the data in several scales, allowing fast interactive zooming of a given part of the sky and quick machine learning experiments on coarse data in order to identify the interesting parts of latent space before focusing on them in a higher resolution.

A unique HiSS-Cube design allows interesting experiments with multi-modal and hierarchically structured multi-scale data.

The main tasks are:



- 1) Install the HiSS-Cube system and download the data required for its run (SDSS images and spectra of some selected parts of the sky)
- 2) Identify interesting science cases where the machine learning methods trained on a combination of multi-modal data (i.e. images and spectra treated together) are expected to give better accuracy against the combination of results of methods trained on each type of modality separately.
- 3) Perform experiments with different ML methods (e.g. classification, regression, clustering, tSNE, CNN) on several data samples and analyze results. Compare the performance on combined multi-modal data with single-modal experiments.
- 4) Use HiSS-Cube to get all pre-computed resolutions (i.e. images and spectra of different sizes with various degrees of smearing) of the same sky region.
- 5) Perform simple experiments (e.g. star-galaxy-classification) on different scales of the same data and compare execution time concerning the precision.
- 6) (optional) Try to get access to the large cluster and perform the experiments on the whole SDSS archive

The recommended literature will be delivered by the supervisor of the thesis.

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Citation of this thesis: Rustamov Farukh. *Application of Machine Learning to Predict Star Formation Rates in SDSS Data*. Bachelor's thesis. Czech Technical University in Prague, Faculty of Information Technology, 2025.

*I would like to express my sincere gratitude to my supervisor, **RNDr. Petr Škoda, CSc.**, for his valuable guidance, insightful feedback, and continuous support throughout the development of this thesis.*

*I would also like to thank **Ing. Ondřej Podstavek** for his expert advice and assistance with machine learning methods, which significantly contributed to the quality and depth of the experimental work.*

*The authors acknowledge the support of the OP VVV funded project CZ.02.1.01/0.0/0.0/16\_019/0000765 “Research Center for Informatics”.*

*The access to the computational infrastructure of the OP VVV funded project CZ.02.1.01/0.0/0.0/16\_019/0000765 “Research Center for Informatics” is also gratefully acknowledged. Most of the experiments and data processing were carried out using the RCI cluster.*

## **Declaration**

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In Prague on April 23, 2025

## Abstract

In this thesis, we investigate the application of machine learning methods to predict the star formation rate (SFR) in astronomical objects based on photometric and spectroscopic data from the Sloan Digital Sky Survey (SDSS).

**Keywords** machine learning, SDSS, star formation rate, spectroscopy, photometry

# Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
1.1	General Description and Relevance of the Study . . . . .	1
1.2	SDSS Data Description . . . . .	1
1.3	Prediction of Star Formation Rate (SFR) . . . . .	2
1.4	Research Challenges . . . . .	2
1.5	Objectives and Tasks . . . . .	3
1.6	Terminology and Illustrations . . . . .	3
1.6.1	Spectra and Spectral Analysis . . . . .	3
1.6.1.1	Definition of a Spectrum . . . . .	3
1.6.1.2	Why Spectral Analysis Is Needed . . . . .	3
1.6.2	The SDSS $u, g, r, i, z$ Filters . . . . .	3
1.6.3	Star Formation Rate (SFR) . . . . .	4
1.6.3.1	What Is SFR . . . . .	4
1.6.3.2	How SFR Is Determined . . . . .	4
1.6.3.3	Why SFR Matters . . . . .	4
1.7	Conclusion of the Introduction . . . . .	4
<b>2</b>	<b>Data Exploration</b>	<b>6</b>
2.1	Dataset Overview and Initial Filtering . . . . .	6
2.2	SFR Estimation Quality: FLAG Keyword . . . . .	7
2.3	Image and Spectrum Data Availability . . . . .	7
2.4	Analysis of NaN Block Lengths and Positions . . . . .	8
2.5	Detection and Removal of Multi-Object Cutouts . . . . .	10
2.6	Summary of Final Dataset . . . . .	10
2.6.1	Exploratory Embedding Analysis with t-SNE, UMAP, and PCA . . . . .	11
<b>3</b>	<b>Machine Learning Methodology</b>	<b>15</b>
3.1	Comparative Analysis: The Scene Dataset Example . . . . .	15
3.2	Star–Galaxy–Quasar classification . . . . .	17
3.3	Overview of Learning Algorithms . . . . .	17
3.4	Experimental Setup . . . . .	17
3.4.1	Data Splitting Strategy . . . . .	18
3.4.2	Preprocessing . . . . .	18
3.4.3	Hyperparameter Tuning . . . . .	18
3.5	Evaluation Metrics . . . . .	18

3.6	Multimodal Fusion Strategies . . . . .	19
3.6.1	Early Fusion . . . . .	19
3.6.2	Late Fusion . . . . .	19
3.7	Decision Tree Regression . . . . .	19
3.8	Convolutional Neural Network: VGGNet12 . . . . .	22
3.8.1	Architecture and Training Protocol . . . . .	22
3.8.2	Training Curves: Photographs . . . . .	23
3.8.3	Hyperparameter Sweep: Photographs . . . . .	23
3.8.4	Training Curves: Spectra . . . . .	24
3.8.5	Hyperparameter Sweep: Spectra . . . . .	25
3.8.6	Training Curves: Early Fusion . . . . .	25
3.8.7	Hyperparameter Sweep: Early Fusion . . . . .	26
3.8.8	Overall Metrics and Runtime . . . . .	27
3.9	Gradient Boosting Machine: LightGBM . . . . .	27
3.9.1	Architecture and Training Protocol . . . . .	28
3.9.2	Training Curves: Photographs . . . . .	28
3.9.3	Hyperparameter Sweep: Photographs . . . . .	29
3.9.4	Training Curves: Spectra . . . . .	29
3.9.5	Hyperparameter Sweep: Spectra . . . . .	30
3.9.6	Training Curves: Early Fusion . . . . .	31
3.9.7	Hyperparameter Sweep: Early Fusion . . . . .	31
3.9.8	Overall Metrics and Runtime . . . . .	32
3.10	Impact of Photo and Spectra Quality on Model Performance . . . . .	33
3.11	Summary and Outlook . . . . .	36

## List of Figures

1.1	An example of an object. Top 5 pixel photos, bottom a spectrum.	2
1.2	Example of atomic spectral lines for different elements.[6]	4
1.3	Transmission curves of the SDSS $u, g, r, i, z$ filters.	5
2.1	Distribution of <b>AVG</b> (log SFR) in the filtered sample [10].	7
2.2	Percentage of spectra by fraction of missing (NaN) flux values at Zoom level 0 for <b>FLAG</b> =0 [10]	8
2.3	Distribution of consecutive NaN run lengths at each resolution for <b>FLAG</b> =0 [10]	9
2.4	Typical wavelength regions where NaN gaps commonly occur (Zoom level 0) [10]	9
2.5	Example of a cutout containing multiple detected sources, excluded from the final sample [10]	10
2.6	Embeddings of photo and spectral data at four zoom levels (Z0–Z3) using t-SNE, UMAP, and PCA, colored by <b>AVG</b> [17].	12
3.1	CLASS1 (left) and CLASS2 (right) label distributions for the Scene dataset [19].	16
3.2	MFCC plot of the audio and street-scene photo taken during the recording [19].	16
3.3	Class distribution for star–galaxy–quasar labels: galaxies outnumber quasars by a factor of 10, and stars comprise fewer than 30 objects [10].	17
3.4	DT on photographs: $R^2$ , MAE, RMSE, and NMAD vs. max. tree depth. Best $d = 4$ (all except NMAD).	20
3.5	DT on spectra: $R^2$ , MAE, RMSE, and NMAD vs. max. tree depth. Best $d = 2$ .	20
3.6	DT early fusion: $R^2$ , MAE, RMSE, and NMAD vs. tree depth. Best $d = 3$ by $R^2$ .	21
3.7	DT: metric comparison across modalities (photo, spectra, early, late).	21
3.8	DT: wall-clock runtime across modalities.	22
3.9	VGGNet12 photo: training (blue) vs. validation (orange) loss per epoch; red dashed line marks lowest val. loss.	23
3.10	VGGNet12 photo: $R^2$ , MAE, RMSE, NMAD vs. learning rate.	23

3.11	VGGNet12 spectra: training vs. validation loss per epoch; red dashed line = best epoch.	24
3.12	VGGNet12 spectra: $R^2$ , MAE, RMSE, NMAD vs. learning rate.	25
3.13	VGGNet12 early fusion: training vs. validation loss; red dashed line = best epoch.	25
3.14	VGGNet12 early fusion: $R^2$ , MAE, RMSE, NMAD vs. learning rate.	26
3.15	VGGNet12: metric comparison across modalities.	27
3.16	VGGNet12: wall-clock runtime across modalities.	27
3.17	LightGBM photo: training vs. validation RMSE per iteration; red dashed line = best iteration.	28
3.18	LightGBM photo: $R^2$ , MAE, RMSE, NMAD vs. learning rate & max_depth.	29
3.19	LightGBM spectra: training vs. validation RMSE; red dashed line = best iteration.	29
3.20	LightGBM spectra: $R^2$ , MAE, RMSE, NMAD vs. learning rate & max_depth.	30
3.21	LightGBM early fusion: training vs. validation RMSE; red dashed line = best iteration.	31
3.22	LightGBM early fusion: $R^2$ , MAE, RMSE, NMAD vs. learning rate & max_depth.	31
3.23	LightGBM: metric comparison across modalities.	32
3.24	LightGBM: wall-clock runtime across modalities.	32
3.25	Decision Tree performance vs. photo quality (q0–q3) [36].	33
3.26	VGGNet12 performance vs. photo quality (q0–q3) [37].	34
3.27	LightGBM performance vs. photo quality (q0–q3) [38].	34
3.28	Decision Tree performance vs. spectra quality (q0–q3) [36].	35
3.29	VGGNet12 performance vs. spectra quality (q0–q3) [37].	35
3.30	LightGBM performance vs. spectra quality (q0–q3) [38].	36

## List of Tables

2.1	Record counts at successive filtering stages.	6
2.2	NaN block statistics for FLAG=0 at each zoom level.	8

## List of code listings

## List of abbreviations

SDSS	Sloan Digital Sky Survey
SFR	Star Formation Rate
CNN	Convolutional Neural Network
MFCC	Mel-Frequency Cepstral Coefficients
MAE	Mean Absolute Error
RMSE	Root Mean Square Error
NMAD	Normalized Median Absolute Deviation
DT	Decision Tree
VGG	Visual Geometry Group
ML	Machine Learning
HDF5	Hierarchical Data Format version 5
RCI	Research Computing Infrastructure
MLP	Multilayer Perceptron

# Chapter 1

## Introduction

### 1.1 General Description and Relevance of the Study

In recent years, multimodal machine learning has become a rapidly advancing area of research with applications ranging from autonomous driving and medical diagnostics to astronomical data analysis. The integration of different data types—such as images, text, audio, and structured signals—enables models to capture richer representations and make more accurate predictions in complex domains.

In astrophysics, large-scale surveys like the Sloan Digital Sky Survey (SDSS) [1] provide both photometric and spectroscopic data for millions of celestial objects. These complementary modalities offer unique views: images capture structural and morphological features, while spectra encode detailed physical and chemical properties.

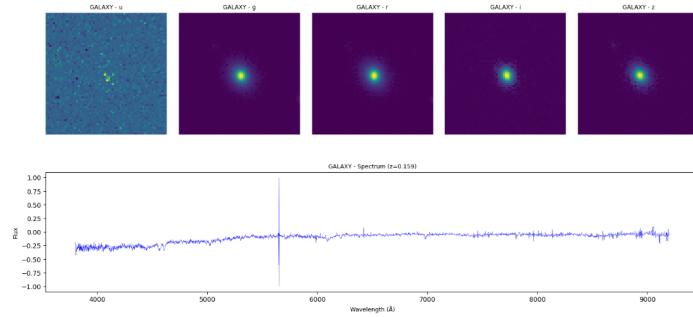
This thesis investigates the application of multimodal machine learning techniques to predict the \*\*star formation rate (SFR)\*\* [2] in galaxies using data from SDSS. The motivation lies in the need to efficiently process massive astronomical datasets and build models that leverage the strengths of both image-based and spectroscopic inputs.

### 1.2 SDSS Data Description

The SDSS dataset provides a unique opportunity to study the properties of astronomical objects using comprehensive observations. Each object in the sample is characterized by the following components:

- **Five-Band Photometry.** For each object, five images are available corresponding to different spectral bands (denoted as  $u$ ,  $g$ ,  $r$ ,  $i$ , and  $z$ ) [3]. Each image captures a specific portion of the spectrum, enabling a detailed analysis of the structural and physical properties of the objects.

- **Spectroscopic Data.** In addition to the photometric images, each object is provided with a spectrum that offers information on its chemical composition, temperature, and dynamics.



■ **Figure 1.1** An example of an object. Top 5 pixel photos, bottom a spectrum.

### 1.3 Prediction of Star Formation Rate (SFR)

One of the primary objectives of this research is to predict the star formation rate (SFR) using the available SDSS data. In our dataset, the SFR is represented by the column AVR (mean value of the SFR distribution) [4]. By applying machine learning techniques, we aim to evaluate the feasibility of accurately predicting SFR using various types of input data.

The planned experiments include:

- Predicting SFR using only photometric images.
- Predicting SFR using only spectroscopic data.
- Employing a multimodal approach that combines both images and spectra.

### 1.4 Research Challenges

Working with the SDSS data presents several challenges:

- 1. Data Filtering.** The original dataset contains over 4 million objects, and we need to determine which of these are suitable for machine learning.
- 2. Quality of Images and Spectra.** Multiple quality levels allow optimization of the pipeline, but determining the optimal resolution is non-trivial.
- 3. Multiple Objects in One Image.** Overlapping signals can degrade machine learning performance, so automatic object detection and isolation methods are needed.

## 1.5 Objectives and Tasks

The primary objective of this thesis is to develop an optimal methodology for predicting SFR using SDSS data. To achieve this, the following tasks will be addressed:

1. Perform a detailed analysis of the raw data, assess its quality, and apply filtering.
2. Develop algorithms for the automatic detection and isolation of objects within images.
3. Investigate the impact of different quality levels of images and spectra on prediction accuracy.
4. Compare the effectiveness of models using single modalities with multi-modal approaches.
5. Conduct a comparative study using the Scene dataset and try to adapt findings to SDSS.

## 1.6 Terminology and Illustrations

### 1.6.1 Spectra and Spectral Analysis

#### 1.6.1.1 Definition of a Spectrum

A spectrum in astronomy represents the dependence of an object's emitted intensity on wavelength. Specialized spectrographs attached to telescopes record these spectra [5].

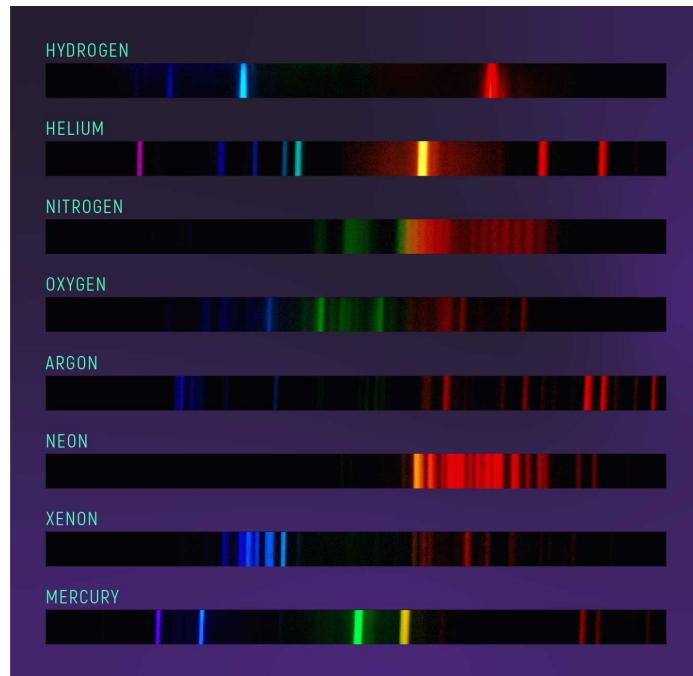
#### 1.6.1.2 Why Spectral Analysis Is Needed

- **Chemical Composition:** Spectral lines reveal elemental makeup.
- **Velocity Measurements:** Line shifts indicate motion.
- **Physical Conditions:** Emission/absorption lines indicate temperature, density.

All of these diagnostics are discussed in Chapter 1 (“Why Record Spectra of Astronomical Objects?”) of Tennyson’s second edition [5, p. 1–6].

### 1.6.2 The SDSS $u$ , $g$ , $r$ , $i$ , $z$ Filters

SDSS uses five broadband filters with approximate effective wavelengths of  $u = 354\text{ nm}$ ,  $g = 477\text{ nm}$ ,  $r = 623\text{ nm}$ ,  $i = 762\text{ nm}$  and  $z = 913\text{ nm}$  [3]



**Figure 1.2** Example of atomic spectral lines for different elements.[6]

### 1.6.3 Star Formation Rate (SFR)

#### 1.6.3.1 What Is SFR

SFR quantifies the rate of star formation in solar masses per year ( $M_{\odot} \text{ yr}^{-1}$ ).

#### 1.6.3.2 How SFR Is Determined

Emission line luminosity, especially  $\text{H}\alpha$ , is used:

$$\text{SFR}(M_{\odot} \text{ yr}^{-1}) \approx 7.9 \times 10^{-42} L(\text{H}\alpha) (\text{erg s}^{-1}).$$

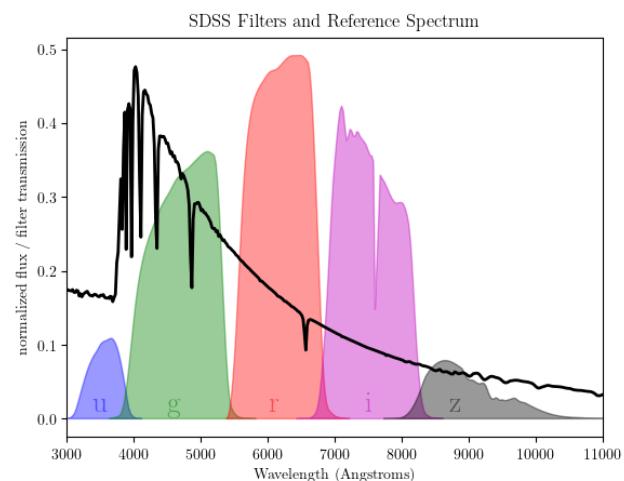
[7]

#### 1.6.3.3 Why SFR Matters

The star formation rate governs the chemical enrichment and overall evolutionary pathway of galaxies, as well as their energy output through radiation, stellar winds, and supernova feedback (8).

## 1.7 Conclusion of the Introduction

In summary, this thesis explores the prediction of SFR in astronomical objects using SDSS data, leveraging both images and spectra. Multimodal preliminary studies motivate the methodology detailed in subsequent chapters.



■ **Figure 1.3** Transmission curves of the SDSS  $u$ ,  $g$ ,  $r$ ,  $i$ ,  $z$  filters.

..... Chapter 2

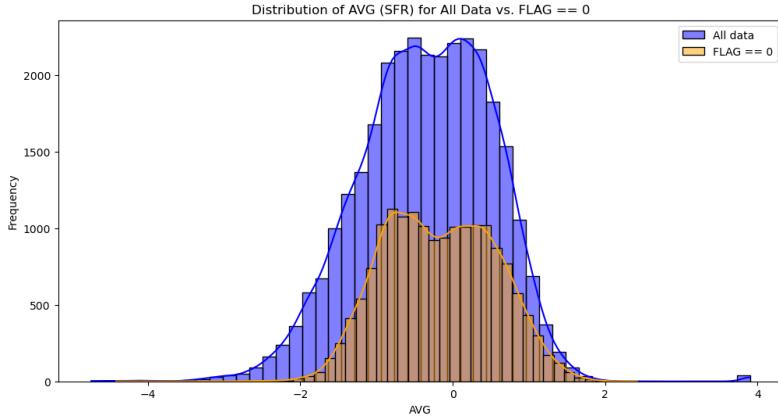
## Data Exploration

### 2.1 Dataset Overview and Initial Filtering

We source our sample from the SDSS Data Release 7 star formation rate (SFR) catalog, which initially contains 4,851,200 objects. To ensure that every galaxy has both imaging and spectroscopic data, we retain only those entries with available multi-band cutouts and 1D spectra, reducing the sample to 151,190 records. Next, we remove entries where the logarithmic SFR indicator `AVG` is undefined (`NaN`), leaving 34,613 objects. Finally, we exclude the placeholder value `AVG = -99`, resulting in 30,752 records. Of these, 16,841 have `FLAG=0` (high-quality SFR estimates) [9] and 13,911 have `FLAG≠0`. Table 2.1 summarizes these counts [10].

■ **Table 2.1** Record counts at successive filtering stages.

Filtering step	# of Objects
Initial SDSS SFR catalog	4,851,200
With image & spectrum available	151,190
Removing <code>NaN</code> in <code>AVG</code>	34,613
Excluding <code>AVG = -99</code>	30,752
( <code>FLAG=0</code> )	16,841
( <code>FLAG≠0</code> )	13,911



■ **Figure 2.1** Distribution of AVG (log SFR) in the filtered sample [10].

## 2.2 SFR Estimation Quality: FLAG Keyword

According to the SDSS documentation:

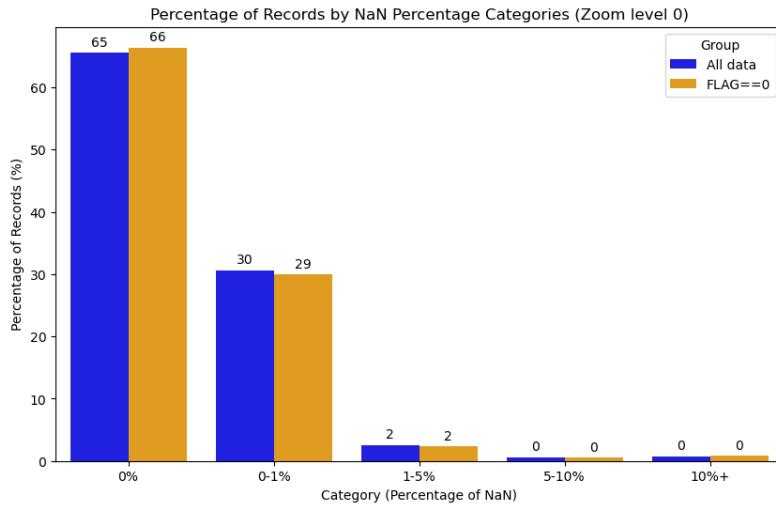
”The FLAG keyword indicates the status of the SFR estimation. If FLAG=0 then all is well [9] and for statistical studies in particular, it is recommendable to focus on these objects as in all other cases the detailed method to estimate SFR or SFR/M\* will be (slightly) different and can introduce subtle biases.”

We proceed exclusively with the FLAG=0 subset (16,841 galaxies).

## 2.3 Image and Spectrum Data Availability

Using the HISS-Cube [11] pipeline applied to SDSS DR7, we obtain four resolutions of imaging and spectroscopic data for each FLAG=0 galaxy [10] :

- Image cutouts: (16,841, 5, 64, 64), (16,841, 5, 32, 32), (16,841, 5, 16, 16), (16,841, 5, 8, 8)
- Spectra: (16,841, 4620), (16,841, 2310), (16,841, 1155), (16,841, 577)

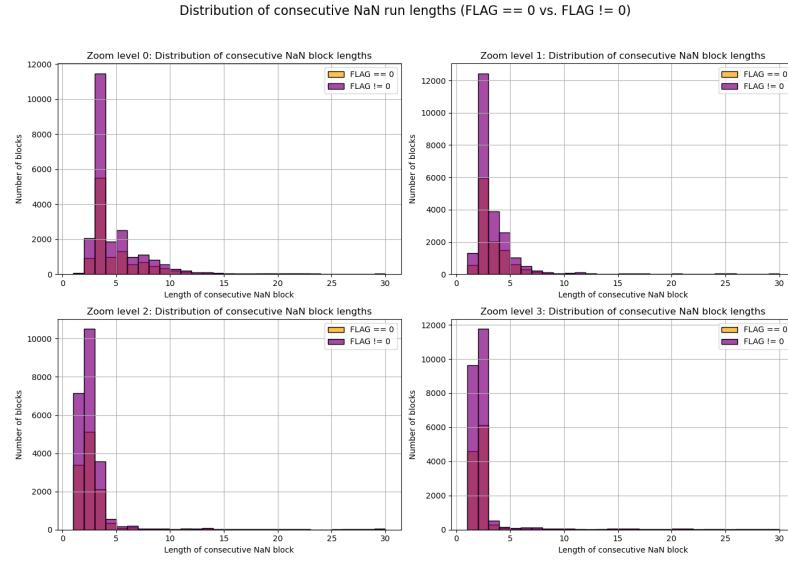


**Figure 2.2** Percentage of spectra by fraction of missing (NaN) flux values at Zoom level 0 for FLAG=0 [10] .

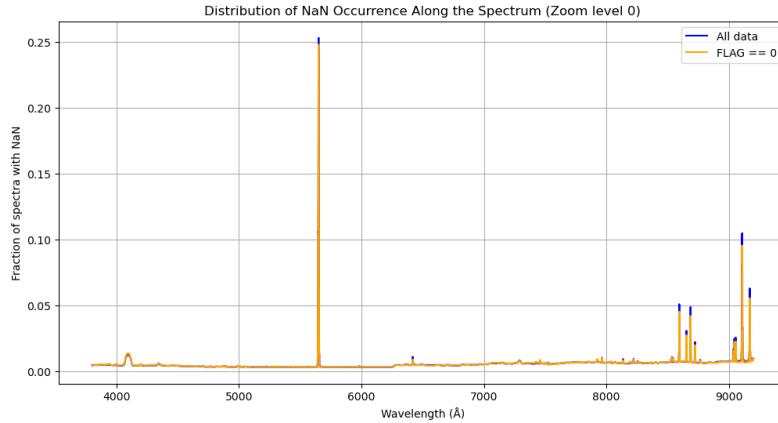
## 2.4 Analysis of NaN Block Lengths and Positions

**Table 2.2** NaN block statistics for FLAG=0 at each zoom level.

Zoom level	# NaN blocks	Mean length	Max length
0	12,207	34.69	4,620
1	12,045	18.11	2,310
2	11,954	9.68	1,155
3	11,875	5.46	577

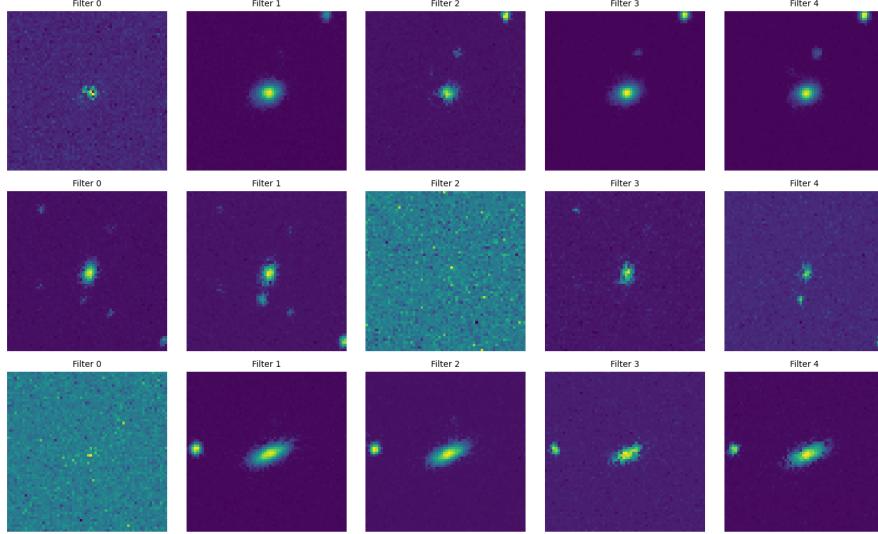


**Figure 2.3** Distribution of consecutive NaN run lengths at each resolution for FLAG=0 [10] .



**Figure 2.4** Typical wavelength regions where NaN gaps commonly occur (Zoom level 0) [10] .

## 2.5 Detection and Removal of Multi-Object Cutouts



**Figure 2.5** Example of a cutout containing multiple detected sources, excluded from the final sample [10].

In order to detect and remove cutouts containing multiple objects, we implement a simple image-processing pipeline inspired by standard thresholding and connected-component labeling techniques. First, pixel values are normalized to the  $[0,1]$  range. We then binarize the central filter image (usually the  $r$ -band) at a fixed global threshold of 0.9—this value was chosen heuristically to separate background sky from source signal, following best practices in image thresholding [12]. Next, we apply the connected-component labeling algorithm (`ndimage.label`) to the binary image to count discrete regions. If more than one connected region is found, the index is flagged as a “multi-object” cutout. Finally, a small subset of these multi-object indices is visualized to confirm the detection. Our implementation is provided in Listing [10] and closely follows the methodology of Sezgin and Sankur’s survey on thresholding techniques [12] as well as the standard workflow described in Gonzalez and Woods’s digital image processing text [13].

## 2.6 Summary of Final Dataset

The cleaned dataset for supervised regression consists of:

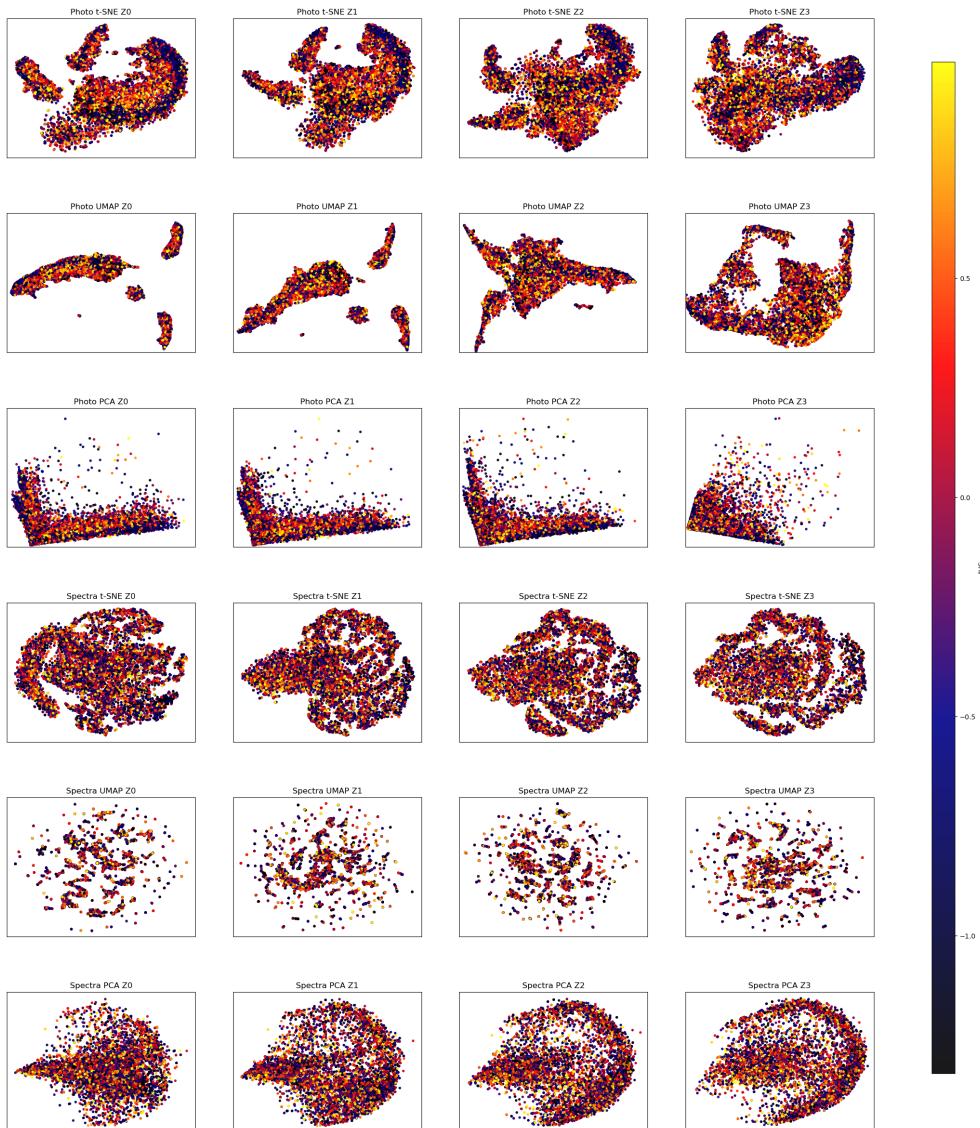
- Multi-band image cutouts at four resolutions
- One-dimensional spectra at four samplings
- Robust SFR labels (AVG, FLAG=0)

- Total of 11,179 galaxies

### 2.6.1 Exploratory Embedding Analysis with t-SNE, UMAP, and PCA

To gain intuition about the structure of our image and spectral datasets in relation to the target variable `AVG`, we applied three popular dimensionality-reduction methods:

- **t-SNE** [14]
- **UMAP** [15]
- **PCA** [16]



**Figure 2.6** Embeddings of photo and spectral data at four zoom levels (Z0–Z3) using t-SNE, UMAP, and PCA, colored by AVG [17].

The Pearson correlations between embedding axes and AVG are:

<b>Method / Modality</b>	$\rho_x$	$\rho_y$	<b>Method / Modality</b>	$\rho_x$	$\rho_y$
t-SNE Photo Z0	-0.03	-0.04	t-SNE Spectra Z0	-0.10	+0.06
t-SNE Photo Z1	-0.03	-0.06	t-SNE Spectra Z1	-0.15	+0.02
t-SNE Photo Z2	0.00	-0.09	t-SNE Spectra Z2	-0.16	+0.00
t-SNE Photo Z3	-0.06	-0.03	t-SNE Spectra Z3	-0.15	-0.02
UMAP Photo Z0	+0.03	+0.00	UMAP Spectra Z0	+0.02	-0.02
UMAP Photo Z1	+0.03	+0.03	UMAP Spectra Z1	-0.03	+0.00
UMAP Photo Z2	-0.05	-0.01	UMAP Spectra Z2	-0.02	-0.01
UMAP Photo Z3	+0.08	-0.02	UMAP Spectra Z3	-0.02	+0.02
PCA Photo Z0	-0.03	+0.01	PCA Spectra Z0	-0.11	+0.05
PCA Photo Z1	-0.05	-0.01	PCA Spectra Z1	-0.14	+0.03
PCA Photo Z2	-0.07	-0.04	PCA Spectra Z2	-0.14	+0.01
PCA Photo Z3	-0.07	+0.03	PCA Spectra Z3	-0.14	-0.01

The silhouette scores and cluster-average AVG (for  $k = 3$ ) are:

<b>Method / Modality</b>	<b>Silhouette</b>	<b>Cluster averages of AVG</b>
t-SNE Photo Z0	0.43	[-0.174, -0.169, -0.183]
t-SNE Photo Z1	0.43	[-0.189, -0.174, -0.161]
t-SNE Photo Z2	0.42	[-0.167, -0.121, -0.238]
t-SNE Photo Z3	0.44	[-0.240, -0.108, -0.171]
t-SNE Spectra Z0	0.40	[-0.091, -0.160, -0.290]
t-SNE Spectra Z1	0.41	[-0.268, -0.174, -0.070]
t-SNE Spectra Z2	0.39	[-0.221, -0.244, -0.065]
t-SNE Spectra Z3	0.37	[-0.119, -0.283, -0.124]
UMAP Photo Z0	0.49	[-0.184, -0.156, -0.218]
UMAP Photo Z1	0.51	[-0.221, -0.149, -0.158]
UMAP Photo Z2	0.43	[-0.131, -0.267, -0.162]
UMAP Photo Z3	0.42	[-0.117, -0.232, -0.183]
UMAP Spectra Z0	0.37	[-0.162, -0.153, -0.210]
UMAP Spectra Z1	0.35	[-0.190, -0.150, -0.182]
UMAP Spectra Z2	0.38	[-0.183, -0.164, -0.179]
UMAP Spectra Z3	0.34	[-0.176, -0.194, -0.156]
PCA Photo Z0	0.54	[-0.150, -0.201, -0.212]
PCA Photo Z1	0.56	[-0.137, -0.245, -0.221]
PCA Photo Z2	0.58	[-0.120, -0.295, -0.291]
PCA Photo Z3	0.62	[-0.134, -0.303, -0.207]
PCA Spectra Z0	0.39	[-0.194, -0.246, -0.056]
PCA Spectra Z1	0.49	[-0.286, -0.159, -0.079]
PCA Spectra Z2	0.49	[-0.276, -0.075, -0.163]
PCA Spectra Z3	0.46	[-0.264, -0.168, -0.070]

The embedding analysis reveals:

- **t-SNE** and **UMAP** uncover local, nonlinear structure but show weak linear correlation with **AVG**, indicating complex manifold relationships [14, 15].
- **PCA** yields stronger linear gradients in the first component—especially for spectra—suggesting that principal components capture a significant fraction of SFR variance in a linear subspace [16].
- Higher-resolution photos produce higher silhouette scores (up to 0.62 for PCA Photo Z3), indicating clearer cluster separation by SFR labels.

In summary, t-SNE and UMAP highlight nonlinear patterns, while PCA emphasizes linear trends. Combining insights from all three methods guides our feature-engineering and model-selection strategies.

## ..... Chapter 3

# Machine Learning Methodology

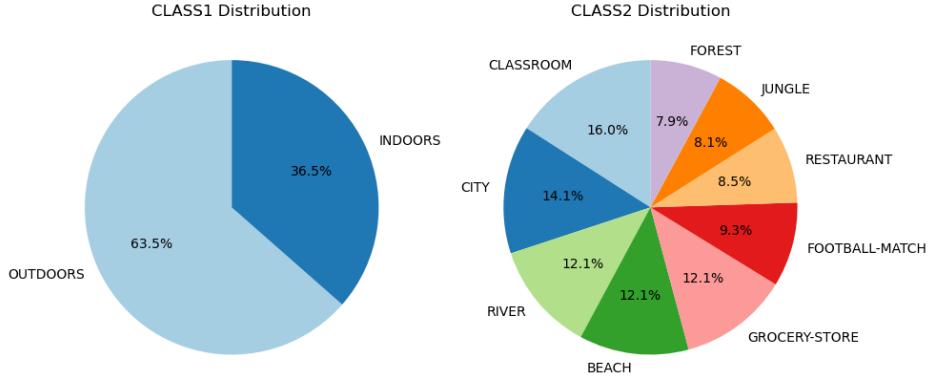
## 3.1 Comparative Analysis: The Scene Dataset Example

To preliminarily evaluate the benefits of multimodal learning, we conducted experiments on the publicly available *Scene dataset* [18]. This dataset contains two modalities:

- **Images:** Still frames extracted from videos, each depicting one of eight different environmental scenes.
- **Audio features:** Each image is paired with Mel-Frequency Cepstral Coefficients (MFCCs), representing the corresponding sound context.

The classification task consists of two hierarchical objectives:

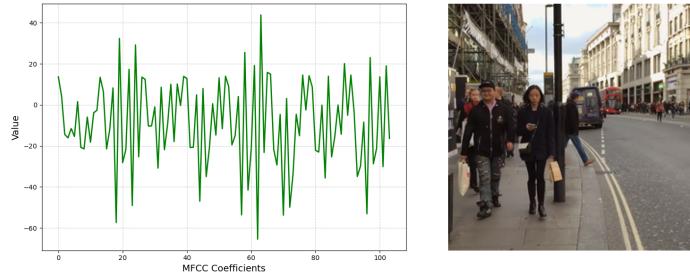
- **CLASS1:** Binary classification of the scene as **indoors** or **outdoors**.
- **CLASS2:** Fine-grained classification into one of the eight specific scene types: *classroom, city, river, beach, grocery store, football match, restaurant, forest, jungle*.



■ **Figure 3.1** CLASS1 (left) and CLASS2 (right) label distributions for the Scene dataset [19].

During experiments, we observed that prediction accuracy for image-only and multimodal models exceeded 99% for both CLASS1 and CLASS2. Although this suggests strong signal content in the data, it also poses a limitation: the task is too easy to effectively assess the comparative advantage of multimodal learning. In such high-performance regimes, additional modalities do not yield noticeable improvements, making it unsuitable for drawing robust conclusions about fusion strategies.

Therefore, while this dataset helped validate our pipeline, it does not serve as a suitable benchmark for comparing modality contributions. The main focus of this thesis remains on the more challenging SFR prediction task using SDSS data, where both image and spectral inputs contain complementary and non-trivial signals.



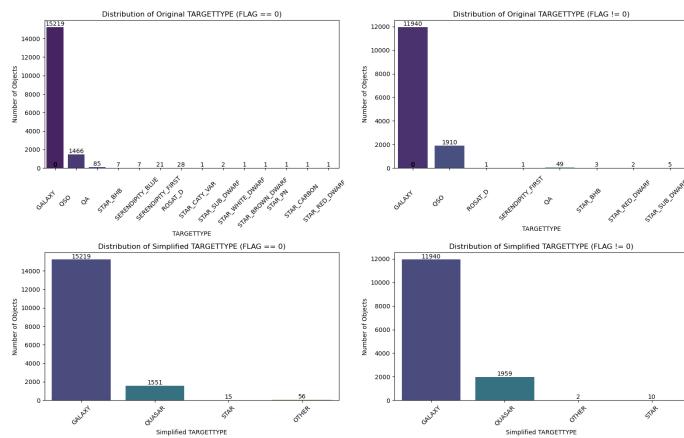
■ **Figure 3.2** MFCC plot of the audio and street-scene photo taken during the recording [19].

Preliminary machine learning results on this dataset indicate that the multimodal approach significantly improves accuracy:

- **Decision Trees:** Audio-only 0.81/0.66, Combined 0.97/0.92.
- **Neural Networks:** Audio 0.94, Images 0.99, Combined 0.99.

### 3.2 Star–Galaxy–Quasar classification

Unfortunately, attempting a star–galaxy–quasar classification on this dataset proves problematic due to a severe class imbalance. The sample contains roughly ten times more galaxies than quasars, while stars number fewer than 30 instances, making any supervised classifier highly biased toward the majority class. This imbalance stems from the fact that the dataset was originally curated for SFR prediction, not object-type classification.



**Figure 3.3** Class distribution for star–galaxy–quasar labels: galaxies outnumber quasars by a factor of 10, and stars comprise fewer than 30 objects [10].

### 3.3 Overview of Learning Algorithms

To predict the logarithmic star-formation rate (**AVG** in  $[-4, 4]$ ) we employ three baseline models:

- **Decision Tree Regression (DT).** A non-parametric tree model that recursively partitions feature space by axis-aligned splits, offering interpretability and a natural baseline [20].
  - **Convolutional Neural Network (VGGNet12).** A 12-layer CNN architecture that excels at large-scale image feature extraction [21].
  - **Gradient Boosting Machine (LightGBM).** An efficient implementation of gradient-boosted decision trees optimized for speed and memory [22].

### 3.4 Experimental Setup

### 3.4.1 Data Splitting Strategy

We shuffle and split the cleaned sample into training, validation, and test subsets in a 60/20/20 ratio using stratified sampling on AVG. We then perform 5-fold cross-validation on the training set to estimate generalization error and tune hyperparameters [23, 24].

### 3.4.2 Preprocessing

- *Images*: pixel values are linearly scaled to  $[0, 1]$  by dividing by 255 [25], then flattened for decision-tree/LightGBM models or fed as 2D arrays into VGGNet12 [26].
- *Spectra*: Any object with NaN flux values removed, yielding 11,179 gap-free spectra[27].
- *Early Fusion*: Concatenate image and spectral vectors into one feature vector [28].
- *Late Fusion*: Average photo-only and spec-only model predictions[28].

### 3.4.3 Hyperparameter Tuning

**DT**: grid search over `max_depth`  $\in \{1, \dots, 6\}$  with 5-fold CV, selecting the depth maximizing mean test  $R^2$  [20].

**VGGNet12**: sweep over learning rate (`lr`) and fixed dropout=0.5, early stopping patience=30 [29, 30].

**LightGBM**: grid over `learning_rate` and `max_depth`, early stopping round=10 [31].

## 3.5 Evaluation Metrics

We evaluate all models using:

- *Coefficient of Determination ( $R^2$ )*. Variance explained [20].

$$R^2 = 1 - \frac{\sum_{i=1}^N (y_i - \hat{y}_i)^2}{\sum_{i=1}^N (y_i - \bar{y})^2}.$$

- *Mean Absolute Error (MAE)*. Average absolute deviation [20].

$$\text{MAE} = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i|.$$

- *Root Mean Square Error (RMSE)*. Quadratic penalty on large errors [20].

$$\text{RMSE} = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2}.$$

- *Normalized Median Absolute Deviation (NMAD)*.  $1.4826 \times \text{median}(|\epsilon - \text{median}(\epsilon)|)$  [32].

$$\text{NMAD} = 1.4826 \times \text{median}(|\epsilon_i - \text{median}(\epsilon)|), \quad \epsilon_i = y_i - \hat{y}_i.$$

## 3.6 Multimodal Fusion Strategies

### 3.6.1 Early Fusion

Concatenate CNN feature vector (size  $N_{\text{img}}$ ) with spectral vector (size  $N_{\text{spec}}$ ) into one regressor input [33].

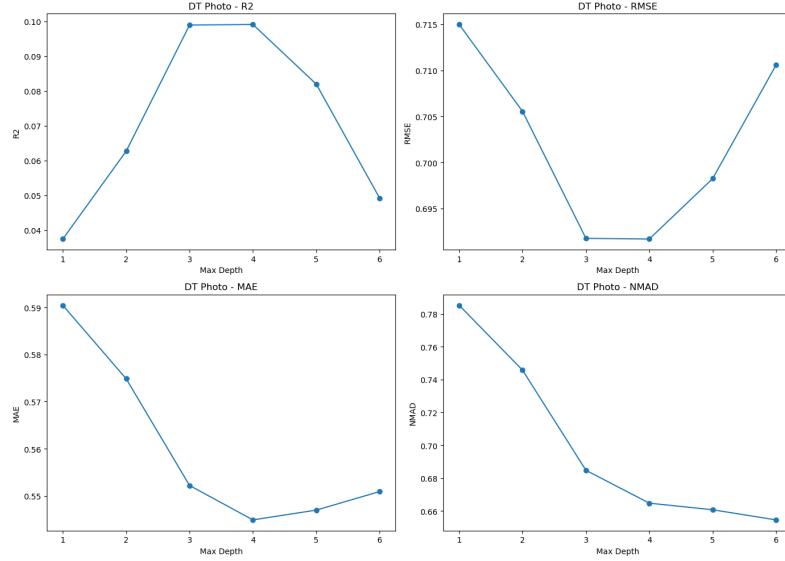
### 3.6.2 Late Fusion

Average independent predictions:

$$\hat{y}_{\text{late}} = \frac{1}{2}(\hat{y}_{\text{photo}} + \hat{y}_{\text{spec}}).$$

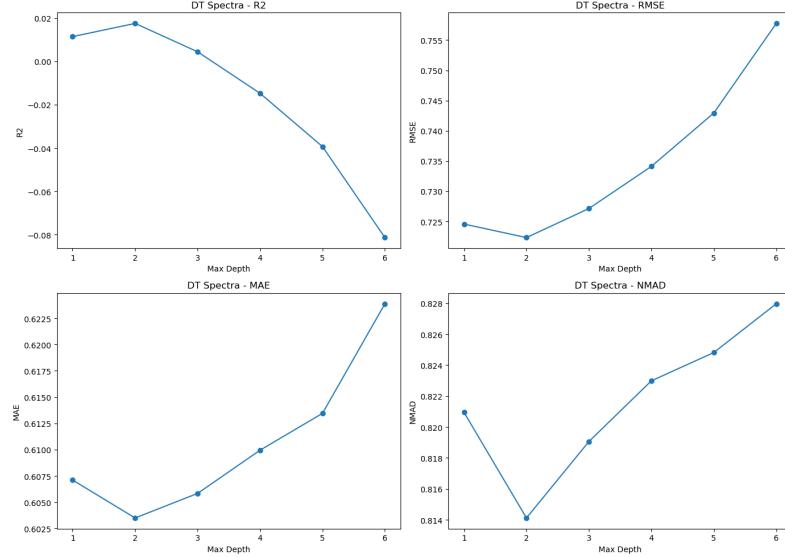
## 3.7 Decision Tree Regression

We fit DT regressors of depth 1–6 to photo, spectra, and early-fused data, then average photo and spectra for late fusion.



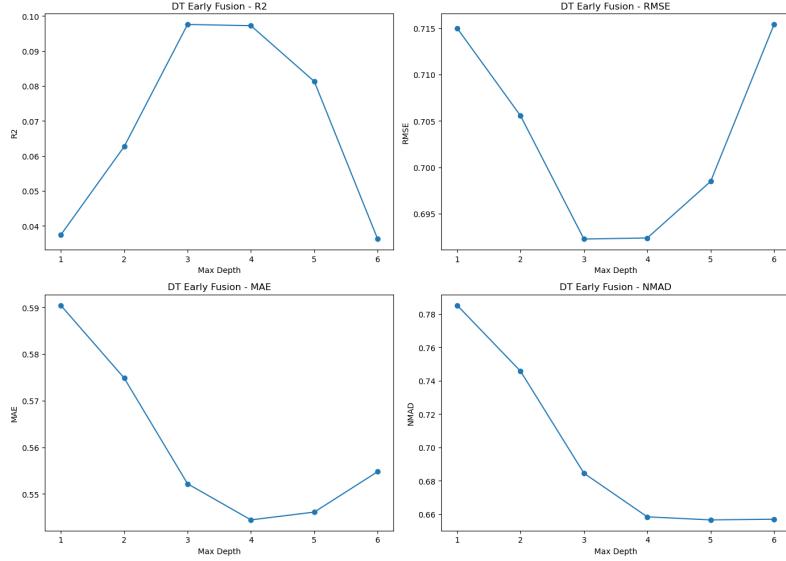
■ **Figure 3.4** DT on photographs:  $R^2$ , MAE, RMSE, and NMAD vs. max. tree depth. Best  $d = 4$  (all except NMAD).

**Figure 1:** Photo-only DT performance.



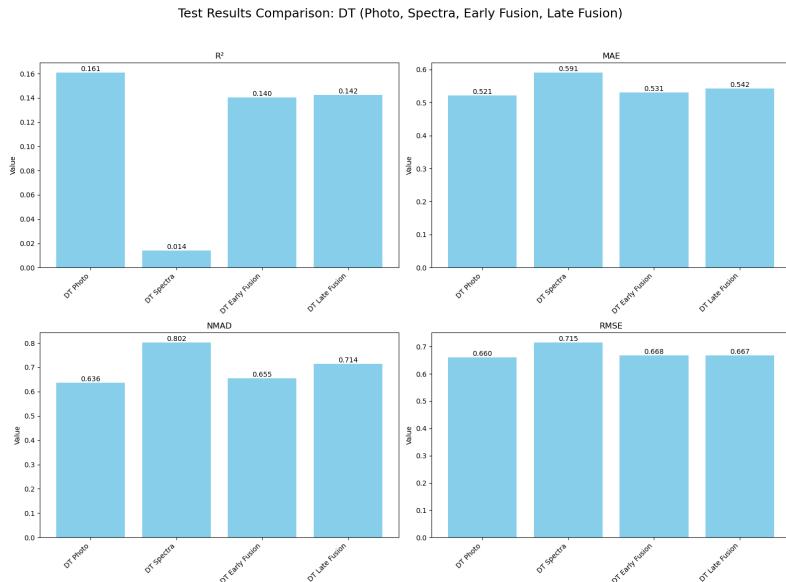
■ **Figure 3.5** DT on spectra:  $R^2$ , MAE, RMSE, and NMAD vs. max. tree depth. Best  $d = 2$ .

**Figure 2:** Spectra-only DT performance.

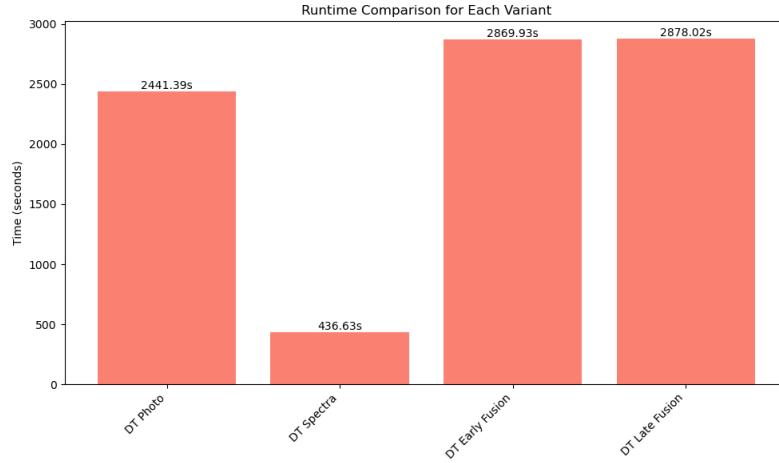


■ **Figure 3.6** DT early fusion:  $R^2$ , MAE, RMSE, and NMAD vs. tree depth. Best  $d = 3$  by  $R^2$ .

**Figure 3:** Early fusion DT performance.



■ **Figure 3.7** DT: metric comparison across modalities (photo, spectra, early, late).



**Figure 3.8** DT: wall-clock runtime across modalities.

## 3.8 Convolutional Neural Network: VGGNet12

The VGGNet12 model stacks  $3 \times 3$  convolutions, max-pooling, then three FC layers with dropout, fine-tuned from ImageNet [21].

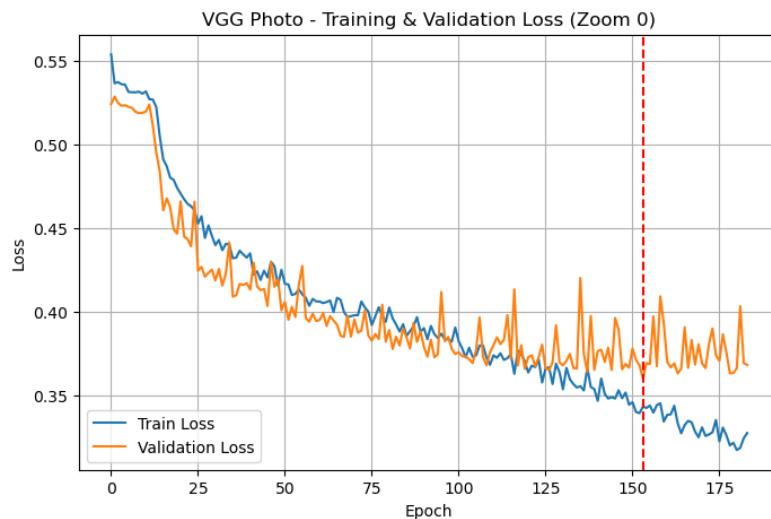
### 3.8.1 Architecture and Training Protocol

We optimize custom MSE loss,

$$\mathcal{L}_{\text{MSE}} = \frac{1}{N} \sum_{i=1}^N (\hat{y}_i - y_i)^2,$$

using Adam, early stopping (patience=30), and focus hyperparameter tuning on learning rate [34, 30, 29].

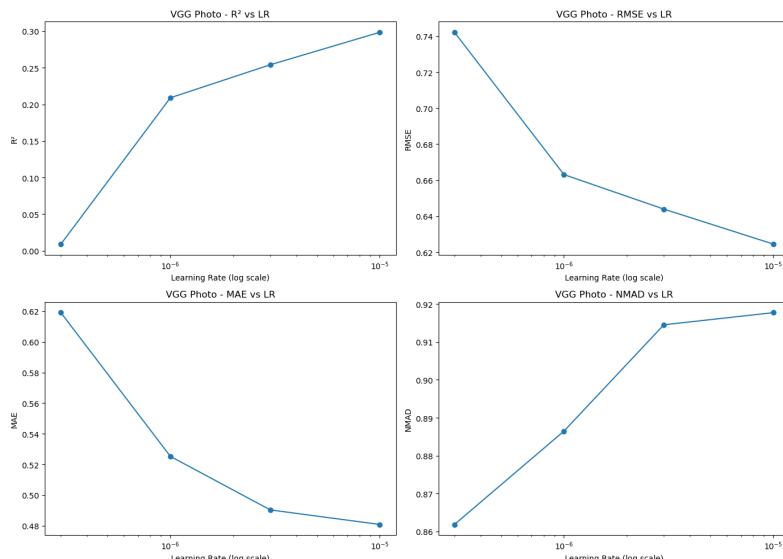
### 3.8.2 Training Curves: Photographs



■ **Figure 3.9** VGGNet12 photo: training (blue) vs. validation (orange) loss per epoch; red dashed line marks lowest val. loss.

Best params (photo): { lr: 1e-05, dropout: 0.5 }

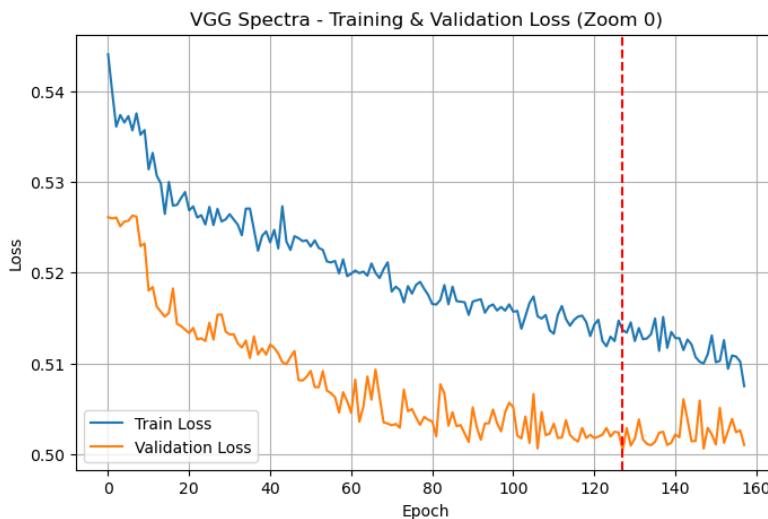
### 3.8.3 Hyperparameter Sweep: Photographs



■ **Figure 3.10** VGGNet12 photo:  $R^2$ , MAE, RMSE, NMAD vs. learning rate.

**Best params (photo): { lr: 1e-05, dropout: 0.5 }**

### 3.8.4 Training Curves: Spectra

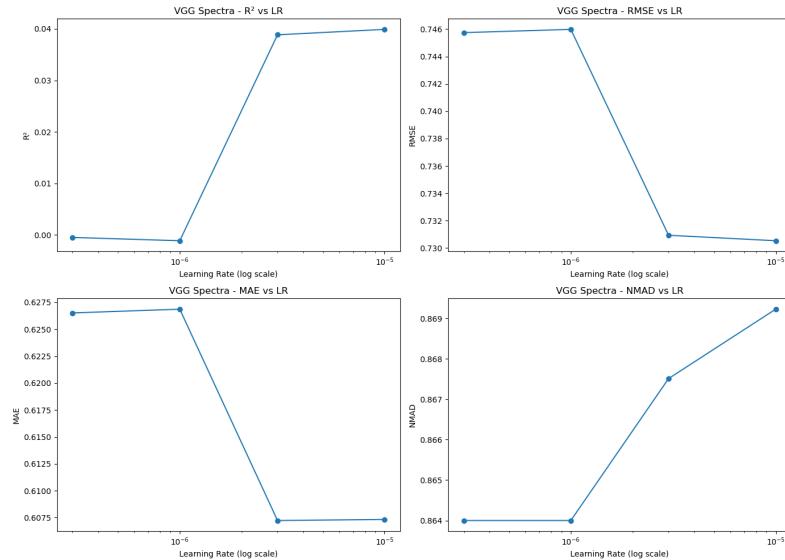


■ **Figure 3.11** VGGNet12 spectra: training vs. validation loss per epoch; red dashed line = best epoch.

**Best params (spectra): { lr: 3e-06, dropout: 0.5 }**

On this graph, it is particularly noticeable that there are epochs where the validation loss dips below the training loss. This behavior is expected in networks using dropout: during training dropout with  $p = 0.5$  randomly deactivates neurons, adding noise and raising training loss, whereas no dropout is applied during validation, so the validation loss can occasionally be lower than the training loss [35].

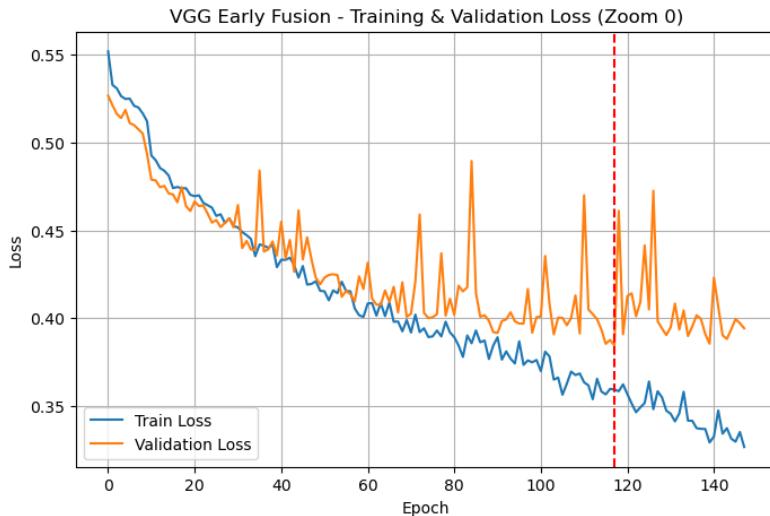
### 3.8.5 Hyperparameter Sweep: Spectra



■ **Figure 3.12** VGGNet12 spectra:  $R^2$ , MAE, RMSE, NMAD vs. learning rate.

Best params (spectra): { lr: 3e-06, dropout: 0.5 }

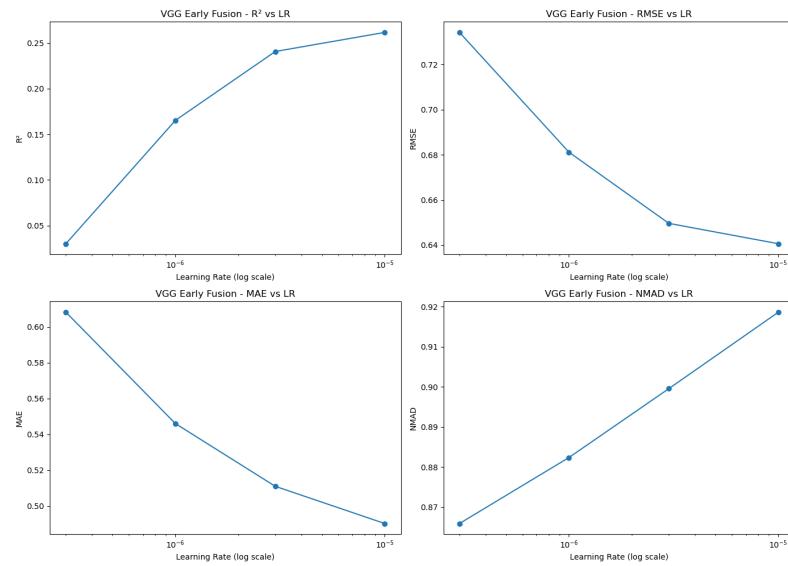
### 3.8.6 Training Curves: Early Fusion



■ **Figure 3.13** VGGNet12 early fusion: training vs. validation loss; red dashed line = best epoch.

Best params (early fusion): { lr: 1e-05, dropout: 0.5 }

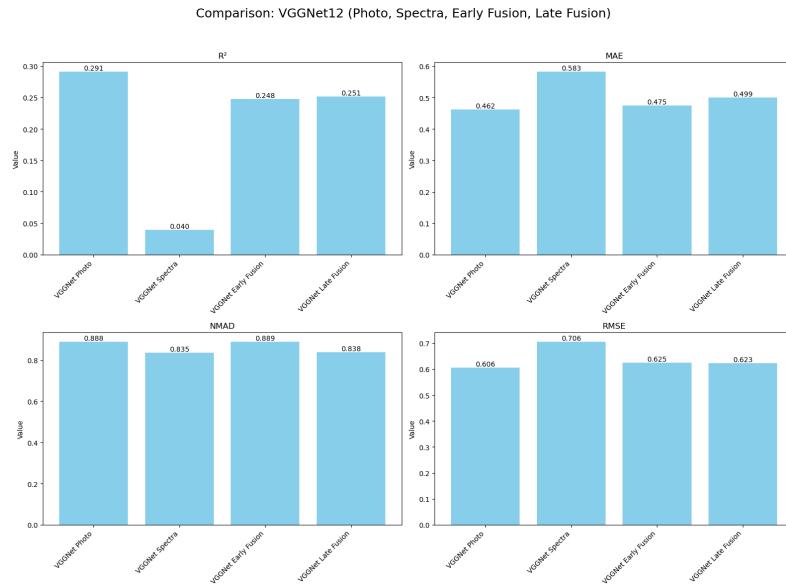
### 3.8.7 Hyperparameter Sweep: Early Fusion



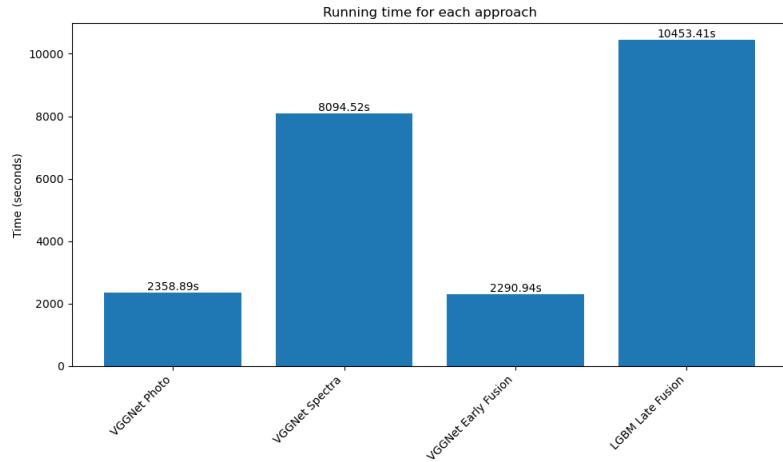
■ **Figure 3.14** VGGNet12 early fusion:  $R^2$ , MAE, RMSE, NMAD vs. learning rate.

Best params (early fusion): { lr: 1e-05, dropout: 0.5 }

### 3.8.8 Overall Metrics and Runtime



■ **Figure 3.15** VGGNet12: metric comparison across modalities.



■ **Figure 3.16** VGGNet12: wall-clock runtime across modalities.

## 3.9 Gradient Boosting Machine: LightGBM

LightGBM grows trees leaf-wise with histogram-based splitting and optimizes RMSE with early stopping (10 rounds) [22, 31].

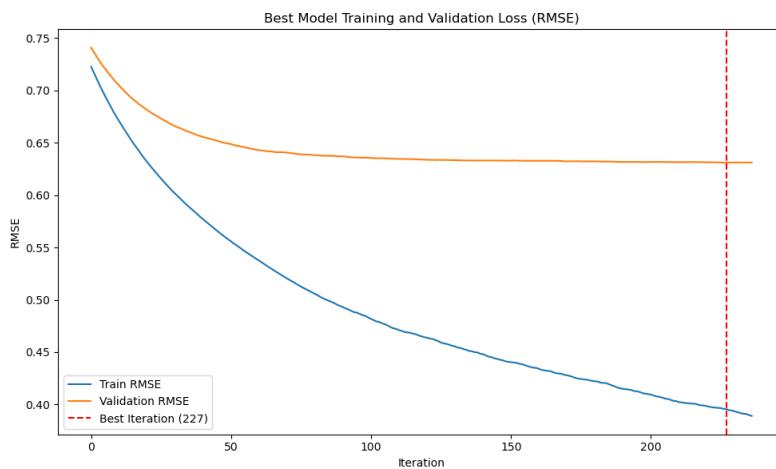
### 3.9.1 Architecture and Training Protocol

We minimize RMSE:

$$\text{RMSE} = \sqrt{\frac{1}{N} \sum_{i=1}^N (\hat{y}_i - y_i)^2},$$

and tune `learning_rate` and `max_depth`; early stopping prevents overfitting [Probst2019].

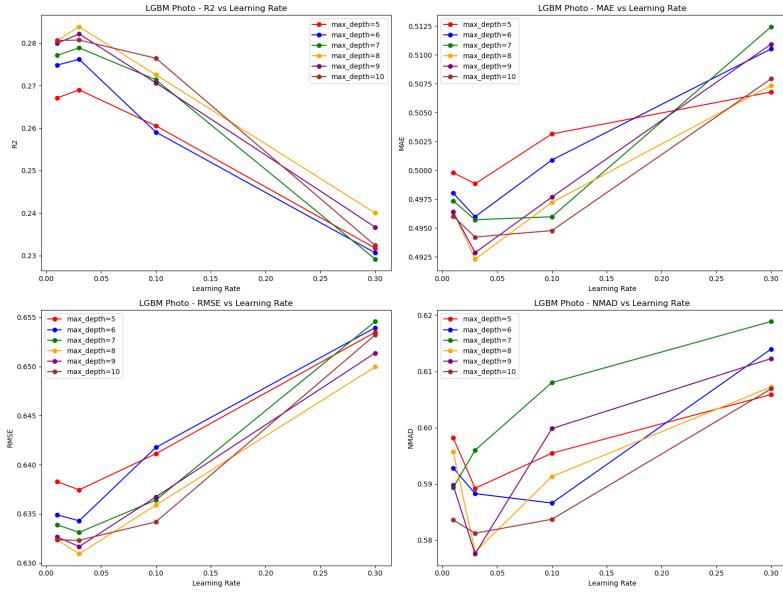
### 3.9.2 Training Curves: Photographs



■ **Figure 3.17** LightGBM photo: training vs. validation RMSE per iteration; red dashed line = best iteration.

**Best params (photo): { `learning_rate`: 0.1, `max_depth`: 8 }**

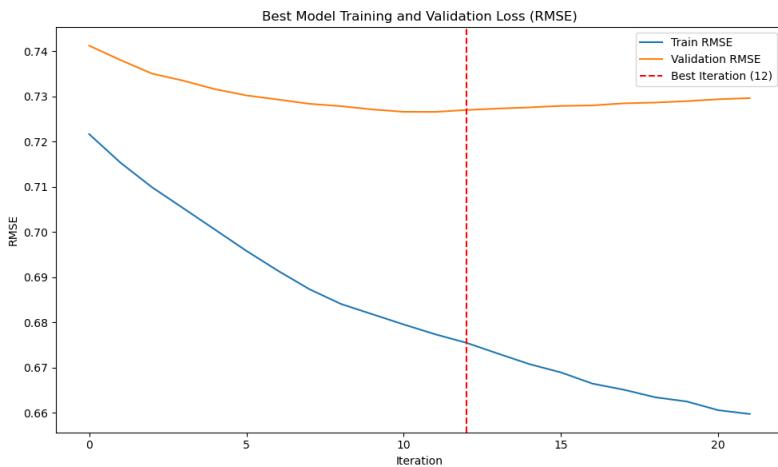
### 3.9.3 Hyperparameter Sweep: Photographs



**Figure 3.18** LightGBM photo:  $R^2$ , MAE, RMSE, NMAD vs. learning rate & max\_depth.

Best params (photo): { learning\_rate: 0.1, max\_depth: 8 }

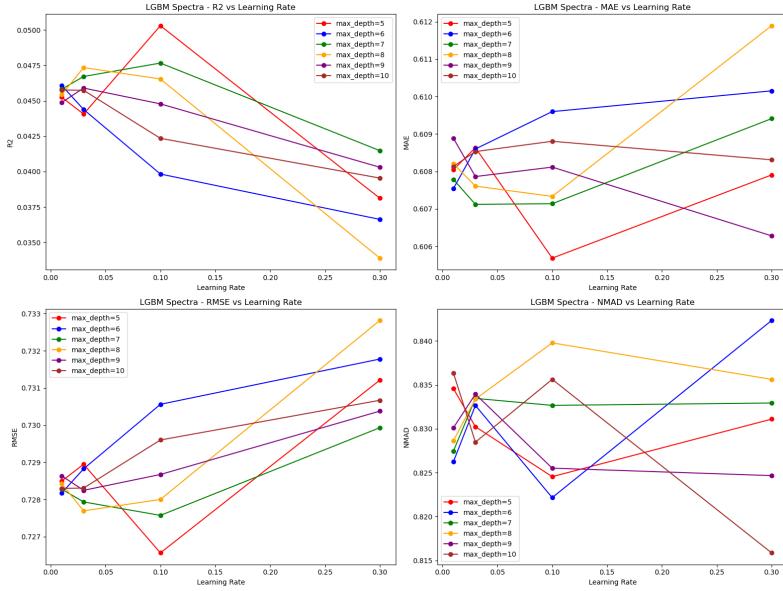
### 3.9.4 Training Curves: Spectra



**Figure 3.19** LightGBM spectra: training vs. validation RMSE; red dashed line = best iteration.

**Best params (spectra): { learning\_rate: 0.03, max\_depth: 7 }**

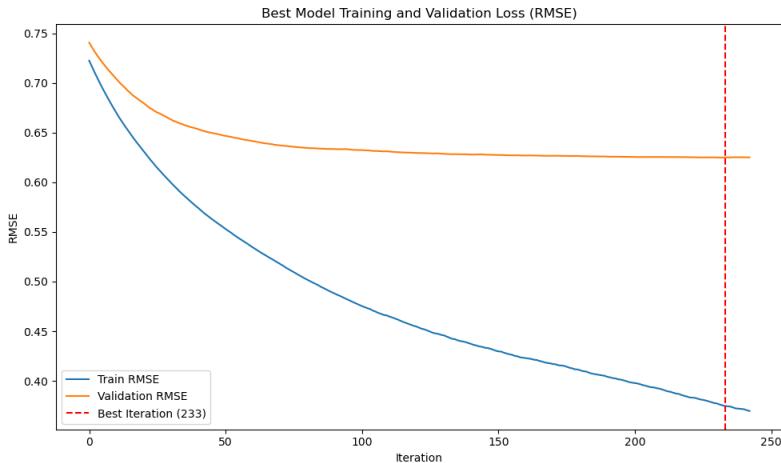
### 3.9.5 Hyperparameter Sweep: Spectra



■ **Figure 3.20** LightGBM spectra:  $R^2$ , MAE, RMSE, NMAD vs. learning rate & max\_depth.

**Best params (spectra): { learning\_rate: 0.03, max\_depth: 7 }**

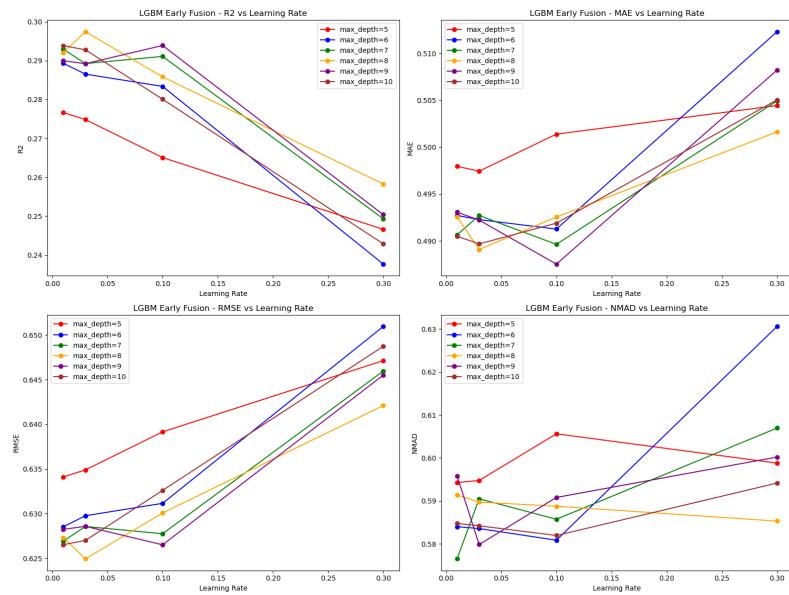
### 3.9.6 Training Curves: Early Fusion



**Figure 3.21** LightGBM early fusion: training vs. validation RMSE; red dashed line = best iteration.

Best params (early fusion): { learning\_rate: 0.1, max\_depth: 9 }

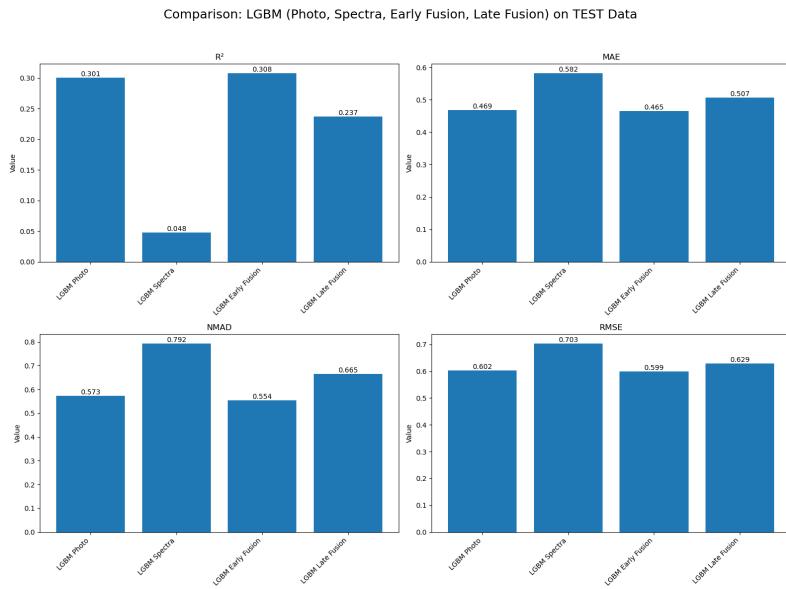
### 3.9.7 Hyperparameter Sweep: Early Fusion



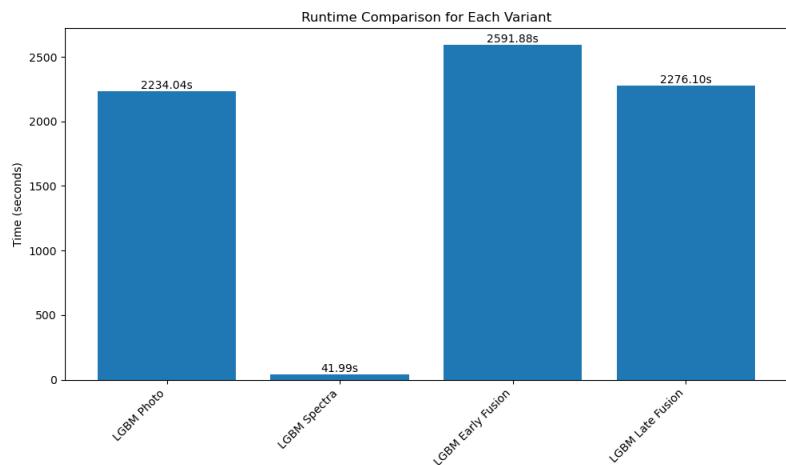
**Figure 3.22** LightGBM early fusion:  $R^2$ , MAE, RMSE, NMAD vs. learning rate & max\_depth.

**Best params (early fusion): { learning\_rate: 0.1, max\_depth: 9 }**

### 3.9.8 Overall Metrics and Runtime



■ **Figure 3.23** LightGBM: metric comparison across modalities.

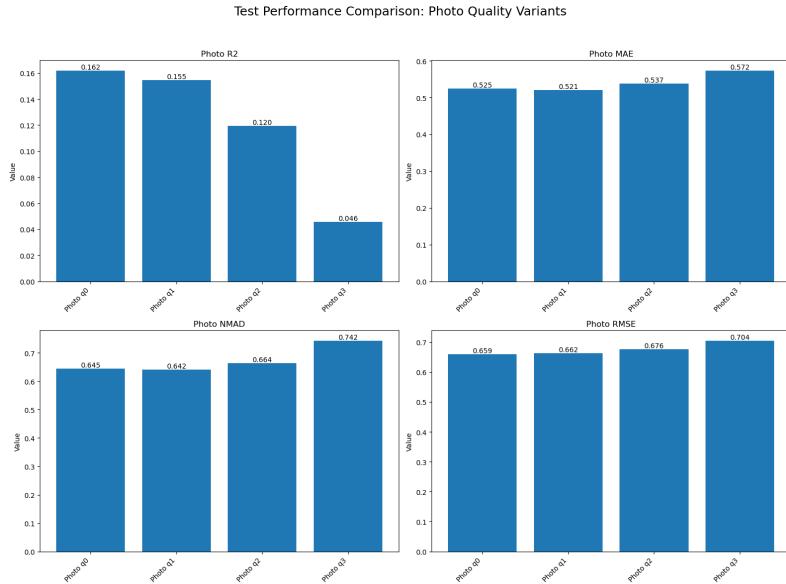


■ **Figure 3.24** LightGBM: wall-clock runtime across modalities.

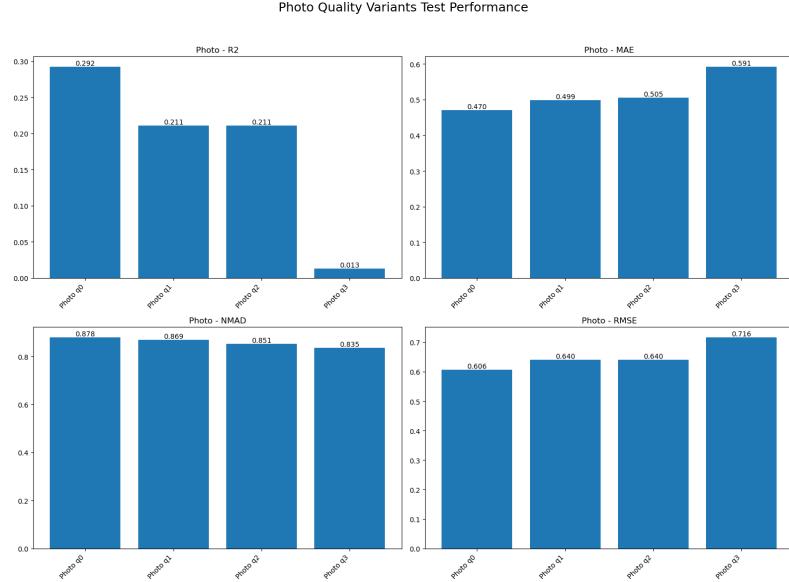
### 3.10 Impact of Photo and Spectra Quality on Model Performance

To understand how input quality affects our models, we trained each algorithm separately on all four photo-quality and four spectra-quality variants using Decision Trees, VGGNet12, and LightGBM. Figures 3.25, 3.26 and 3.27 summarize the photo results, and Figures 3.28, 3.29 and 3.30 the spectra results.

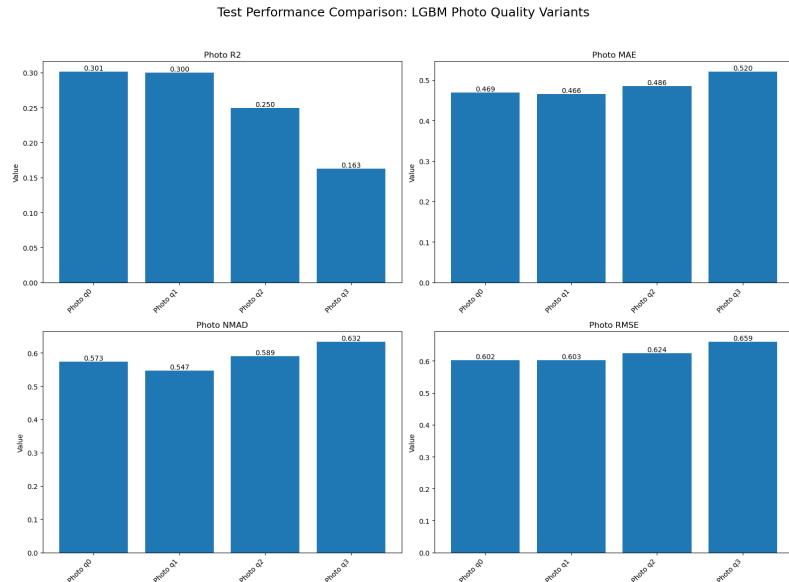
For **photographs**, all metrics improve monotonically with image quality: higher resolution yields higher  $R^2$  and lower MAE, RMSE, and NMAD, at the cost of longer training time.



■ **Figure 3.25** Decision Tree performance vs. photo quality (q0–q3) [36].

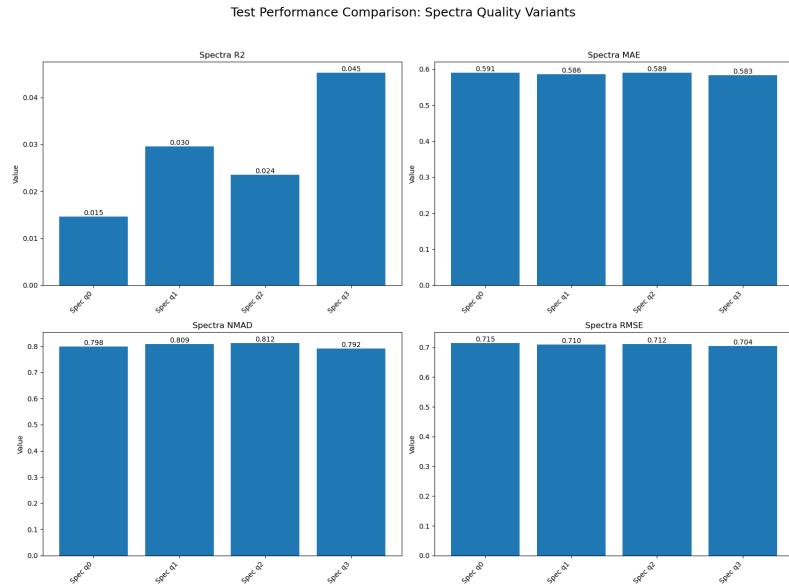


■ **Figure 3.26** VGGNet12 performance vs. photo quality (q0–q3) [37].

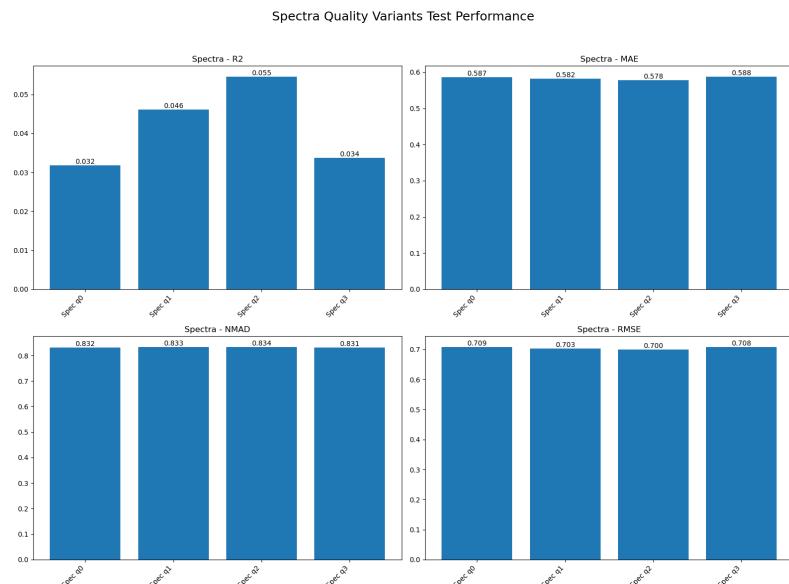


■ **Figure 3.27** LightGBM performance vs. photo quality (q0–q3) [38].

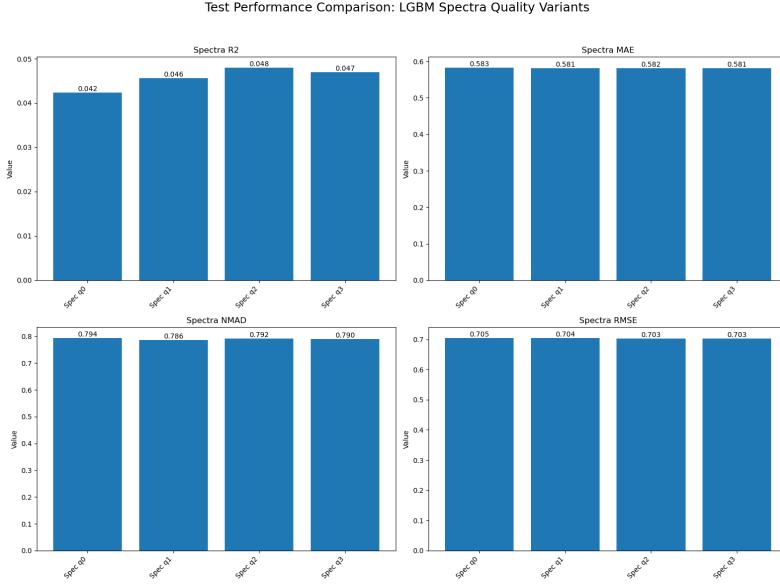
For **spectra**, the trend is inverted: the lowest-resolution spectra produce the best regression accuracy. We attribute this to the smoothing effect of down-sampling, which attenuates high-frequency noise and acts like a built-in Savitzky–Golay filter, improving generalization [39]. Lower-quality variants also run faster.



**Figure 3.28** Decision Tree performance vs. spectra quality (q0–q3) [36].



**Figure 3.29** VGGNet12 performance vs. spectra quality (q0–q3) [37].



**Figure 3.30** LightGBM performance vs. spectra quality (q0–q3) [38].

Based on these insights, we re-ran our final multimodal experiments using the highest photo quality with the lowest spectra quality for each model. On the test set, the early-fusion  $R^2$  changed from

$$(\text{DT} : 0.140, \text{VGG} : 0.248, \text{LGBM} : 0.308) \rightarrow (\text{DT} : 0.155, \text{VGG} : 0.262, \text{LGBM} : 0.308),$$

and late-fusion from

$$(\text{DT} : 0.142, \text{VGG} : 0.251, \text{LGBM} : 0.237) \rightarrow (\text{DT} : 0.160, \text{VGG} : 0.262, \text{LGBM} : 0.237).$$

These small but consistent gains confirm that moderate smoothing of spectral inputs can enhance multimodal performance.

### 3.11 Summary and Outlook

Among all models and fusion strategies evaluated, the early-fusion LightGBM model achieved the best overall performance across metrics (highest  $R^2$ , lowest MAE and RMSE), which is consistent with the literature showing that combining complementary modalities at the feature level often yields superior predictive power [40]. Additionally, VGGNet12 applied to photometric images alone performed remarkably well, underscoring the strength of deep CNN feature extractors for morphological information in galaxy images [41].

These results demonstrate that multimodal approaches—particularly early fusion with efficient tree-based learners—can capture both spectral and visual cues essential for accurate SFR prediction. However, the complexity and diversity of astrophysical data suggest that further research is needed: exploring

larger ensembles of models, advanced fusion techniques (e.g., attention-based or late-stage meta-learners), and integration of additional modalities (e.g., environmental or kinematic data) could drive even better performance.

Overall, this work establishes a solid methodological foundation for predicting galaxy star formation rates using multimodal ML, and points the way toward deeper investigations that leverage state-of-the-art models and richer datasets in future studies.

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