

Problem 1

steps in solving single layer perceptron

$$d = 0.4 \rightarrow \text{Given.}$$

$y \rightarrow$ actual o/p

$y_{out} \rightarrow$ predicted o/p

given table

x_1	x_2	bias	y	y_{out}	error	w_1 0.2	w_2 0.3	w_0 -0.5
0	0	1	0	0	0	0.2	0.3	-0.5
0	1	1	1	0	1	0.2	0.7	-0.1
1	0	1	1	1	0	0.2	0.7	-0.1
1	1	1	1	1	0	0.2	0.7	-0.1

S₁: Understand the problem

S₂: Initialize the NNw parameter (Neural network)

→ i) epochs (ii) learning rate η

ii) bias i/p iv) T/p weights / bias weights

↓
also called as threshold.

S₃: Start the training process.

For each iteration (epochs) perform the foll;

i) Compute the summation.

$$f(x) = x_1 * w_1 + x_2 * w_2 + \text{bias} * w_0$$

ii) Apply activation function \rightarrow unit/ sigmoid fn.

$$y_{\text{out}} = \begin{cases} 1 & f(x) > 0 \\ 0 & f(x) \leq 0 \end{cases}$$

iii) Update the input & bias weights

$$\text{error} = y - y_{\text{out}}$$

$$w_1 = w_1 + (1) * \text{error} * x_1$$

$$w_2 = w_2 + (1) * \text{error} * x_2$$

$$w_0 = w_0 + (1) * \text{error} * \text{bias}$$

$$1) f(x) = (0 * 0.2) + (0 * 0.3) + (1 * -0.5) =$$

$$f(x) = 0 - 0.5 = -0.5$$

$$y_{\text{out}} = 0$$

error $\Rightarrow y - y_{\text{out}} \Rightarrow 0 - 0 = 0$. \rightarrow no updation for weight required.

$$2) f(x) = (0 * 0.2) + (1 * 0.3) + (1 * -0.5)$$

$$= 0.3 - 0.5 = -0.2$$

$$y_{\text{out}} = 0$$

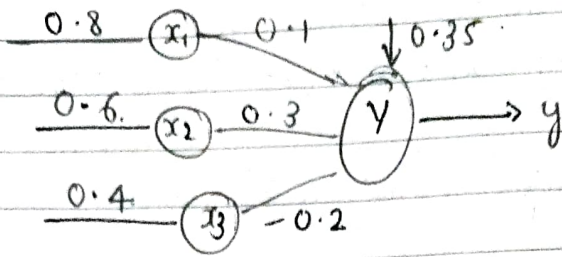
error $\Rightarrow y - y_{\text{out}} = 1 - 0 = 1$. \rightarrow so update weights

$$w_1 = 0.2 + 0.4 * 1 = 0.6$$

$$= 0.2 //$$

$$w_2 = 0.3 + 0.4 * 1 = 0.7$$

$$w_0 = -0.5 + 0.4 * 1 = -0.1$$

Ex - for sigmoid.Problem 2

$$y = x_1 w_1 + x_2 w_2 + x_3 w_3 + b \cdot w_b$$

$$= (0.8 \times 0.1) + (0.6 \times 0.3) + (0.4 \times -0.2) + 0.35$$

$$= 0.18 + 0.35$$

$$= 0.53$$

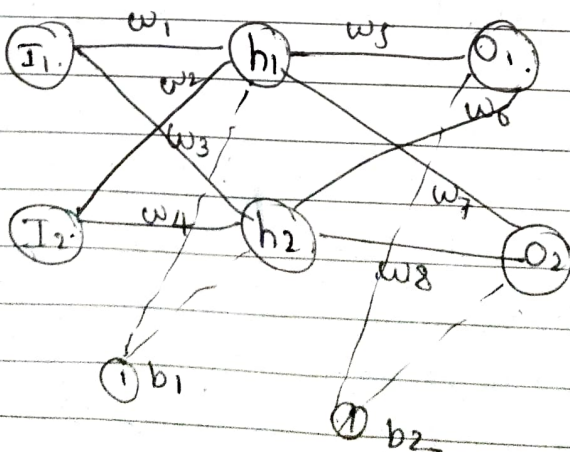
Applying sigmoid function

$$f(x) = \frac{1}{1 + e^{-x}} = \frac{1}{1 + e^{-0.53}}$$

$$= 0.63$$

$$\approx 1$$

Backpropagation derivation & working with ex



$$b_2 w = 0.6$$

$$b_1 w = 0.35 \text{ (weight for bias)}$$

$$w_1 = 0.15$$

$$w_2 = 0.20$$

$$w_3 = 0.25$$

$$w_4 = 0.30$$

$$w_5 = 0.40$$

$$w_6 = 0.45$$

$$w_7 = 0.50$$

$$w_8 = 0.55 \text{ (weight of bias)}$$

$$x_1 = 0.05$$

$$x_2 = 0.10$$

$$\begin{aligned} h_1 &= x_1 * w_1 + x_2 * w_2 + b_1 * w \\ &= (0.05 * 0.15) + (0.10 * 0.20) + (0.35 * 1) \\ &= \underline{\underline{0.3775}} \end{aligned}$$

$$\text{out } h_1 = \frac{1}{1 + e^{-h_1}} = \frac{1}{1 + e^{-0.3775}} = \underline{\underline{0.59326}}$$

$$\begin{aligned} h_2 &= x_1 * w_3 + x_2 * w_4 + b_1 * w \\ &= (0.05 * 0.25) + (0.10 * 0.30) + (1 * 0.35) \\ &= \underline{\underline{0.3925}} \end{aligned}$$

$$\text{out } h_2 = \frac{1}{1 + e^{-h_2}} = \frac{1}{1 + e^{-0.39}} = \underline{\underline{0.5968}}$$

$$\begin{aligned} o_1 &= \text{out } h_1 * w_5 + \text{out } h_2 * w_6 + b_2 * w \\ &= (0.59 * 0.40) + (0.59 * 0.45) + (1 * 0.35) \\ &= \underline{\underline{1.10}} \end{aligned}$$

$$\text{out } o_1 = \frac{1}{1 + e^{-1.10}} = 0.75$$

$$\begin{aligned} o_2 &= (\text{out } h_1 + w_7) + \text{out } h_2 * (w_8 + b_2 * w) \\ &= \underline{\underline{0.7729}} \end{aligned}$$