

Term description

Term description

—

Term description

Term description



Komponenta výukového serveru TI – NP-úplné problémy 2

Component of Learning Server for
Theoretical Computer Science –
NP-complete problems 2

Phat Tran Dai

Bakalářská práce

Vedoucí práce: Borivoj Gulas

Ostrava, 2025

Zadání bakalářské práce

Student:

Phat Dai Tran

Studijní program:

B0613A140014 Informatika

Téma:

Komponenta výukového serveru TI - NP-úplné problémy 2
Component of Learning Server for Theoretical Computer Science - NP-complete problems 2

Jazyk vypracování:

čeština

Zásady pro vypracování:

V rámci diplomových a bakalářských prací vzniká výukový server pro předměty teoretické informatiky. Jedná se o sadu dynamických webových stránek umožňujících studentům pochopení různých typů úloh a problémů tím, že si mohou zadat na stránce libovolné zadání a zobrazí se jim řešení včetně postupu. Cílem této práce je vytvořit komponentu (tedy sadu webových stránek) pro výuku vybraných NP-úplných problémů a převodů mezi nimi.

1. Nastudujte si problematiku tříd složitosti problémů a s tím souvisejícím převodem mezi problémy.
2. Vytvořte dynamické webové stránky umožňující uživateli následující:
 - a) Nechat si zobrazit postupně po krocích postup algoritmu s polynomiální časovou složitostí převádějícího zadanou instanci jednoho problému na instanci jiného problému (budou implementovány alespoň 3 různé převody mezi problémy).
 - b) Zadat libovolnou instanci každého z problémů vyskytujících se v těchto převodech.
 - c) Zobrazit odpověď na otázku daného problému pro zadanou instanci, v případě kladné odpovědi i se zdůvodněním.
3. Není cílem mít co nejefektivněji implementován samotný převod, ale mít jej implementován tak, aby uživateli byla myšlenka tohoto převodu co nejsrozumitelněji ukázána.
4. Vytvořte i ukázkové vstupní instance pro implementované problémy tak, aby uživatel mohl vše vyzkoušet i bez zadávání vlastních vstupů (alespoň 5 instancí pro každý problém).

Studenti řešící toto zadání s rozdílným číslem v názvu mohou (ale nemusí) spolupracovat tak, že výsledek může mít společné uživatelské rozhraní apod. Ale každý bude implementovat jiné 3 převody mezi problémy.

Seznam doporučené odborné literatury:

- [1] Sipser, M.: Introduction to the Theory of Computation, PWS Publishing Company, 1997.
- [2] Papadimitriou, C.: Computational Complexity, Addison Wesley, 1993.
- [3] Sawa, Z.: Prezentace přednášek předmětu Teoretická informatika, dostupné online <https://www.cs.vsb.cz/sawa/ti/index.html>

Formální náležitosti a rozsah bakalářské práce stanoví pokyny pro vypracování zveřejněné na webových stránkách fakulty.

Vedoucí bakalářské práce: **Ing. Martin Kot, Ph.D.**

Datum zadání:

Datum odevzdání:

Garant studijního programu: doc. Mgr. Miloš Kudělka, Ph.D.

V IS EDISON zadáno:

F

E

A

R

D

Abstrakt

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At.

Klíčová slova: Lorem, ipsum, dolor, sit, amet,, consectetur, adipiscing, elit,, sed, do, eiusmod, tempor, incididunt, ut, labore, et, dolore, magnam, aliquam, quaerat.

Abstract

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

Keywords: Lorem, ipsum, dolor, sit, amet,, consectetur, adipiscing, elit,, sed, do, eiusmod, tempor, incididunt, ut, labore, et, dolore, magnam, aliquam, quaerat.

Poděkování

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequale doleamus animo, cum corpore dolemus, fieri.

Seznam použitých zkratek a symbolů

WTF	– What the fuck
DPC	– Do x^2 pice
KDPC	– Kurva do pice → aaaah

Obsah

Úvod	12
1 Heading Level 1	14
1.1 Heading Level 2	14
2 OFDM - Orthogonal Frequency Division Multiplexing	16
2.1 Introduction	16
2.2 Subheading Level 2	17
2.3 Prokázání netranzitivity	17
2.4 Subheading Level 2	17
2.4.1 Subheading Level 3	17
3 Heading Level 1	19
3.1 Subheading Level 2	19
3.2 Subheading Level 2	20
3.3 Subheading Level 2	21
3.4 Subheading Level 2	22
4 Heading Level 1	23
4.1 Heading Level 2	23
4.1.1 Heading Level 2	23
4.2 Heading Level 3	23
5 Heading 5	24
6 Závěr	26
7 Literatura	28
A Qsort implementation	31
B Shit table	32
C OpenGL Shader Compilation	33
D C# code	34

Seznam obrázků

1. Some random data visualisation	18
---	----

Seznam tabulek

1. A looong table	19
2. A simple table	20

Seznam algoritmů

1. Binary Search	31
2. Variable Assignment	32

Seznam výpisů

1. Computer program in C language	16
2. Simple SQL query	16
3. C++ method for GLSL shader compilation	33
4. Computer program in C# language	34

Úvod

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facere et urbane Stoicos irridere, statua est in quo a nobis philosophia defensa et.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facere et urbane Stoicos irridere, statua est in quo a nobis philosophia defensa et collaudata est, cum id, quod maxime placeat, facere possimus, omnis voluptas assumenda est, omnis dolor repellendus. Temporibus autem quibusdam et aut officiis debitis aut rerum necessitatibus saepe eveniet, ut et voluptates repudiandae sint et molestiae non recusandae. Itaque earum rerum defuturum, quas natura non depravata desiderat. Et quem ad me accedis, saluto: 'chaere,' inquam, 'Tite!' lictores, turma omnis chorusque: 'chaere, Tite!' hinc hostis mi Albucius, hinc inimicus. Sed iure Mucius. Ego autem mirari satis non queo unde hoc sit tam.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facere et urbane Stoicos irridere, statua est in quo a nobis philosophia defensa et collaudata est, cum id, quod maxime placeat, facere possimus, omnis voluptas assumenda est, omnis dolor repellendus. Temporibus autem quibusdam et aut officiis debitis aut rerum necessitatibus saepe eveniet, ut et voluptates repudiandae sint et molestiae non recusandae. Itaque earum rerum defuturum, quas natura non depravata desiderat. Et quem ad me accedis, saluto: 'chaere,' inquam, 'Tite!' lictores, turma omnis chorusque: 'chaere, Tite!' hinc hostis mi Albucius, hinc inimicus. Sed iure Mucius. Ego autem mirari satis non queo unde hoc sit tam

insolens domesticarum rerum fastidium. Non est omnino hic docendi locus; sed ita prorsus existimo, neque eum Torquatum, qui hoc primus cognomen invenerit, aut torquem illum hosti detraxisse, ut aliquam ex eo est consecutus? – Laudem et caritatem, quae sunt vitae sine metu degendae praesidia firmissima. – Filium morte multavit. – Si sine causa, nollem me ab eo delectari, quod ista Platonis, Aristoteli, Theophrasti orationis ornamenta neglexerit. Nam illud quidem physici, credere aliquid esse minimum, quod profecto numquam putavisset, si a Polyaeo, familiari suo, geometrica discere maluisset quam illum etiam ipsum dedocere. Sol Democrito magnus videtur, quippe homini erudito in geometriaque perfecto, huic pedalis fortasse; tantum enim esse omnino in nostris poetis aut inertissimae segnitiae est aut fastidii delicatissimi. Mihi quidem videtur, inermis ac nudus est. Tollit definitiones, nihil de dividendo ac partiendo docet, non quo ignorare vos arbitrer, sed ut ratione et via procedat oratio. Quaerimus igitur, quid sit extremum et ultimum bonorum, quod omnium philosophorum sententia tale debet esse.

Kapitola 1

Heading Level 1

QQ *hello* ja fi diofjosdfodsjsodslsdlkjflskdjklffffffffffffffffffffffff kldkjksdfjlsdfljjjj.j..jll jsem k a v o.

$$f(x) = y$$
$$\begin{pmatrix} 1 & 2 & \dots & 10 \\ 2 & 2 & \dots & 10 \\ \vdots & \vdots & \ddots & \vdots \\ 10 & 10 & \dots & 10 \end{pmatrix}$$

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aeque doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

1.1 Heading Level 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat.

$$\Omega = \{(2, 1), (2, 1), (5, 1), (5, 1), \\ (2, 4), (2, 4), (5, 4), (5, 4), \\ (2, 4), (2, 4), (5, 4), (5, 4), \\ (2, 4), (2, 4), (5, 4), (5, 4)\}$$

Velikost pravděpodobnostního prostoru je $|\Omega| = 16$. Z rozepsané Ω vidíme, že počet případů, kdy kostka B vyhraje nad A je vyšší (10) než počet, kdy prohraje (6). Pravděpodobnost vypočteme jako:

$$P(B > A) = \frac{2 + 4 \cdot 2}{|\Omega|} = \frac{10}{16} = \underline{\underline{0.625}}$$

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aeque doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facete et urbane Stoicos irridente, statua est in quo a nobis philosophia defensa et collaudata est, cum id, quod maxime placeat, facere possimus, omnis voluptas assumenda est, omnis dolor repellendus. Temporibus autem quibusdam et aut officiis debitis aut rerum necessitatibus saepe eveniet, ut et voluptates repudiandae sint et molestiae non recusandae.

Itaque earum rerum defuturum, quas natura non depravata desiderat. Et quem ad me accedis, saluto: 'chaere,' inquam, 'Tite!' lictores, turma omnis chorusque: 'chaere, Tite!' hinc hostis mi Albucius, hinc inimicus. Sed iure Mucius. Ego autem mirari satis non queo unde hoc sit tam insolens domesticarum rerum fastidium. Non est omnino hic docendi locus; sed ita prorsus existimo, neque eum Torquatum, qui hoc primus cognomen invenerit, aut torquem illum hosti detraxisse, ut aliquam ex eo est consecutus? – Laudem et caritatem, quae sunt vitae.

Kapitola 2

OFDM - Orthogonal Frequency Division Multiplexing

2.1 Introduction

In refKapitola 2.1, we see how to turn Sections into Chapters. And in refkapitole 2.1, it is done manually.

$$\leq \pm$$

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do. [1]. Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do. [2].

$$\sum_{i=1}^n i = 1 + 2 + 3 + \dots + n$$

Code snippet in C programming language:

```
1  #include <stdio.h>
2
3  int main() {
4      printf("hello, world!\n");
5      return 0;
6  }
```

Výpis 1: Computer program in C language

More simple language, for example SQL:

```
1  SELECT
2      c.customer_id,
3      c.fname,
4      c.lname,
5      c.email
6  FROM customer c
7  WHERE EXISTS (
8      SELECT *
9      FROM purchase p
10     WHERE p.customer_id = c.customer_id
11 )
```

Výpis 2: Simple SQL query

2.2 Subheading Level 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua quaerat. [3]

$$\begin{bmatrix} 1 & * & * \\ * & 1 & * \\ * & * & 1 \end{bmatrix}$$

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua quaerat voluptatem. Ut enim aequae doleamus animo, cum corpore dolemus, fieri.

2.3 Prokázání netranzitivity

První úkolem je ukázat, že vztahy mezi kostkami nejsou tranzitivní, to znamená, že vztahy mezi kostkami jsou tzv. cyklické¹. Tvrdíme totiž, že platí $B > A$, $C > B$ a současně $A > C$. To znamená, že žádná kostka není „nejlepší“ ve všech případech.

Pro každou dvojici kostek vypočítáme pravděpodobnost vítězství jedné kostky nad druhou, konkrétně $P(B > A)$, $P(C > B)$ a $P(A > C)$, a ověříme, že všechny tyto pravděpodobnosti jsou větší než $\frac{1}{2}$.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua quaerat voluptatem. Ut enim aequae doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

2.4 Subheading Level 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua quaerat.

```

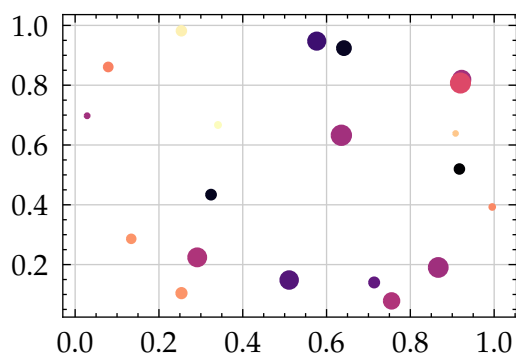
1  #show "ArtosFlow": name => box[
2    #box(image(
3      "logo.svg",
4      height: 0.7em,
5    ))
6    #name
7  ]
8
9  This report is embedded in the
10 ArtosFlow project. ArtosFlow is a
11 project of the Artos Institute.
```

2.4.1 Subheading Level 3

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua quaerat voluptatem. Ut enim aequae doleamus animo,

¹Wikipedia, *Intransitivity*: <https://en.wikipedia.org/wiki/Intransitivity>

cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut.



Obrázek 1: Some random data visualisation

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequale doleamus animo, cum corpore dolemus, fieri.

Kapitola 3

Heading Level 1

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat.

3.1 Subheading Level 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequae doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut.

Index	Value
1	10
2	11
3	12
4	13
1	10
2	11
3	12
4	13
1	10
2	11
3	12
4	13
1	10
2	11
3	12
4	13
1	10
2	11
3	12

Index	Value
4	13
1	10
2	11
3	12
4	13
1	10
2	11
3	12
4	13
1	10
2	11
3	12
4	13
1	10
2	11
3	12
4	13
1	10
2	11
3	12
4	13

Tabulka 1: A looong table

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat.

3.2 Subheading Level 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aeque doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facete et urbane Stoicos irridente, statua est in quo a nobis philosophia defensa et collaudata est, cum id, quod maxime placeat, facere possimus, omnis voluptas assumenda est, omnis dolor repellendus. Temporibus autem quibusdam et.

Shape	Area
Circle	πr^2

Shape	Area
Square	a^2
Rectangle	ab

Tabulka 2: A simple table

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequaeque doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facere et urbane Stoicos irridere, statua est in quo a nobis philosophia defensa et collaudata est, cum id, quod maxime placeat, facere possimus, omnis voluptas assumenda est, omnis dolor repellendus. Temporibus autem quibusdam et.

We define:

$$\phi := \frac{1 + \sqrt{5}}{2} \quad (1)$$

With Rovnice 1, we get:

$$F_n = \left\lfloor \frac{1}{\sqrt{5}} \phi^n \right\rfloor$$

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequaeque doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facere et urbane Stoicos irridere, statua est in quo a nobis philosophia defensa et collaudata est, cum id, quod maxime placeat, facere possimus, omnis voluptas assumenda est, omnis dolor repellendus. Temporibus autem quibusdam et.

$$E = \sqrt{m_0^2 + p^2} \\ \approx 125 \text{ GeV}$$

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat.

$$E = mc^2 \quad (2.1)$$

$$= \sqrt{p^2 c^2 + m^2 c^4} \quad (2.2)$$

3.3 Subheading Level 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequaeque doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut.

3.4 Subheading Level 2

The dot product of two vectors \vec{a} and \vec{b} can be calculated as shown in Rovnice 3.

$$\begin{aligned}\langle a, b \rangle &= \vec{a} \cdot \vec{b} \\ &= a_1 b_1 + a_2 b_2 + \dots a_n b_n \\ &= \sum_{i=1}^n a_i b_i.\end{aligned}\tag{3.1}$$

The sum notation in Rovnice 3.1 is a useful way to express the dot product of two vectors.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facete et urbane Stoicos irridente, statua est in quo a nobis philosophia defensa et collaudata est, cum id, quod maxime placeat, facere possimus, omnis voluptas assumenda est, omnis dolor repellendus. Temporibus autem quibusdam et.

Kapitola 4

Heading Level 1

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

4.1 Heading Level 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

4.1.1 Heading Level 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

4.2 Heading Level 3

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri. [1, p. 358]

 Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequi doleamus animo, cum corpore dolemus, fieri. [4, p. 23]

Kapitola 5

Heading 5

Jelikož základ nehomogenní funkce je roven jedné, počet výskytů (násobnost) tohoto základu v multimnožině kořenu charakteristické rovnice je roven jedné a největší exponent n -ka nehomogenní funkce je taktéž roven jedné, je tvar obecného partikulárního řešení rekurentní rovnice p_n roven:

$$p_n^{(p)} = n^1(\beta_1 n^1 + \beta_0)1^n = n(\beta_1 n + \beta_0) = \beta_1 n^2 + \beta_0 n$$
$$p_n^{(p)} = \varphi n^2 + \gamma n \quad (\gamma = \beta_0, \varphi = \beta_1).$$

Neznámé γ a φ nalezneme substitucí členů p_n v původní rekurentní rovnici:

$$p_n = 3p_{n-1} - 2p_{n-2} - 10n.$$

partikulárním řešením $p_n^{(p)}$ a vyřešíme soustavu dvou rovnic (dvě kvůli dvěma neznámým), kde si za n zvolíme jakékoliv čísla z \mathbb{N}_0 .

$$p_n \leftarrow p_n^{(p)}:$$

$$\begin{aligned} p_n^{(p)} &= 3p_{n-1}^{(p)} - 2p_{n-2}^{(p)} - 10n \\ \varphi n^2 + \gamma n &= 3(\varphi(n-1)^2 + \gamma(n-1)) \\ &\quad - 2(\varphi(n-2)^2 + \gamma(n-2)) - 10n \\ \varphi n^2 + \gamma n &= 3(\varphi(n^2 - 2n + 1) + \gamma n - \gamma) \\ &\quad - 2(\varphi(n^2 - 4n + 4) + \gamma n - 2\gamma) - 10n \\ \varphi n^2 + \gamma n &= 3(\varphi n^2 - 2\varphi n + \varphi + \gamma n - \gamma) \\ &\quad - 2(\varphi n^2 - 4\varphi n + 4\varphi + \gamma n - 2\gamma) - 10n \\ \varphi n^2 + \gamma n &= 3\varphi n^2 - 6\varphi n + 3\varphi + 3\gamma n - 3\gamma \\ &\quad - 2\varphi n^2 + 8\varphi n - 8\varphi - 2\gamma n + 4\gamma - 10n \\ \varphi n^2 + \gamma n &= \varphi n^2 + 2\varphi n - 5\varphi + \gamma n + \gamma - 10n \\ 0 &= 2\varphi n - 5\varphi + \gamma - 10n \end{aligned}$$

Nyní si za n zvolíme například nulu a jedničku.

$$n = 0: \quad 0 = 2\varphi \cdot 0 - 5\varphi + \gamma - 10 \cdot 0$$

$$n = 1: \quad 0 = 2\varphi \cdot 1 - 5\varphi + \gamma - 10 \cdot 1$$

$$\begin{cases} 0 = -5\varphi + \gamma \\ 0 = 2\varphi - 5\varphi + \gamma - 10 \end{cases}$$

$$\begin{cases} 0 = \gamma - 5\varphi \\ 10 = \gamma - 3\varphi \end{cases}$$

$$\left(\begin{array}{cc|c} 1 & -5 & 0 \\ 1 & -3 & 10 \end{array}\right) \xrightarrow[R_2 \leftarrow R_2 - R_1]{\sim} \left(\begin{array}{cc|c} 1 & -5 & 0 \\ 0 & 2 & 10 \end{array}\right) \xrightarrow[R_2 \leftarrow \frac{1}{2}R_2]{\sim} \left(\begin{array}{cc|c} 1 & -5 & 0 \\ 0 & 1 & 5 \end{array}\right)$$

$$\varphi = 5$$

$$\gamma - 5 \cdot \varphi = 0 \Leftrightarrow \gamma = 25$$

Tudíž řešení partikulární rovnice $p_n^{(p)}$ je:

$$p_n^{(p)} = \varphi n^2 + \gamma n$$

$$\underline{p_n^{(p)} = 5n^2 + 25n.}$$

Závěr

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequae doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequae doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facete et urbane Stoicos irridente, statua est in quo a nobis philosophia defensa et.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequae doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facete et urbane Stoicos irridente, statua est in quo a nobis philosophia defensa et collaudata est, cum id, quod maxime placeat, facere possimus, omnis voluptas assumenda est, omnis dolor repellendus. Temporibus autem quibusdam et aut officiis debitis aut rerum necessitatibus saepe eveniet, ut et voluptates repudiandae sint et molestiae non recusandae. Itaque earum rerum defuturum, quas natura non depravata desiderat. Et quem ad me accedis, saluto: 'chaere,' inquam, 'Tite!' lictores, turma omnis chorusque: 'chaere, Tite!' hinc hostis mi Albucius, hinc inimicus. Sed iure Mucius. Ego autem mirari satis non queo unde hoc sit tam.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aequae doleamus animo, cum corpore dolemus, fieri tamen permagna accessio potest, si aliquod aeternum et infinitum impendere malum nobis opinemur. Quod idem licet transferre in voluptatem, ut postea variari voluptas distinguere possit, augeri amplificarique non possit. At etiam Athenis, ut e patre audiebam facete et urbane Stoicos irridente, statua est in quo a nobis philosophia defensa et collaudata est, cum id, quod maxime placeat, facere possimus, omnis voluptas assumenda est, omnis dolor repellendus. Temporibus autem quibusdam et aut officiis debitis aut rerum necessitatibus saepe eveniet, ut et voluptates repudiandae sint et molestiae non recusandae. Itaque earum rerum defuturum, quas natura non depravata desiderat. Et quem ad me accedis, saluto: 'chaere,' inquam, 'Tite!' lictores, turma omnis chorusque: 'chaere, Tite!' hinc hostis mi Albucius, hinc inimicus. Sed iure Mucius. Ego autem mirari satis non queo unde hoc sit tam insolens domesticarum rerum fastidium. Non est omnino hic docendi locus; sed ita prorsus existimo, neque eum Torquatum, qui hoc primus cognomen invenerit, aut torquem illum hosti

detraxisse, ut aliquam ex eo est consecutus? – Laudem et caritatem, quae sunt vitae sine metu degendae praesidia firmissima. – Filium morte multavit. – Si sine causa, nollem me ab eo delectari, quod ista Platonis, Aristoteli, Theophrasti orationis ornamenta neglexerit. Nam illud quidem physici, credere aliquid esse minimum, quod profecto numquam putavisset, si a Polyaeo, familiari suo, geometrica discere maluisset quam illum etiam ipsum dedocere. Sol Democrito magnus videtur, quippe homini erudito in geometriaque perfecto, huic pedalis fortasse; tantum enim esse omnino in nostris poetis aut inertissimae segnitiae est aut fastidii delicatissimi. Mihi quidem videtur, inermis ac nudus est. Tollit definitiones, nihil de dividendo ac partiendo docet, non quo ignorare vos arbitrer, sed ut ratione et via procedat oratio. Quaerimus igitur, quid sit extremum et ultimum bonorum, quod omnium philosophorum sententia tale debet esse.

Literatura

- [1] MUNROE, Randall. *Types of Editors* [online]. 12. března 2014. Dostupné z: <https://xkcd.com/1341/>
- [2] GÜNTHER-HAUG, Barbara. *Den Boden unter den Füßen verlieren*. B.m.: MVG, 2020.
- [3] STEYERL, Hito. *Drill*. 20. června 2019
- [4] MEHTA, Jiten a Eric KINNEAR. *Boost Performance and Security with Modern Networking* [online]. 26. června 2020 [cit. 2020-09-17]. Dostupné z: <https://developer.apple.com/videos/play/wwdc2020/10111/>
- [5] PREKAS, George, Marios KOGIAS a Edouard BUGNION. ZyGOS: Achieving Low Tail Latency for Microsecond-Scale Networked Tasks. In: *Proceedings of the 26th Symposium on Operating Systems Principles* [online]. B.m.: Association for Computing Machinery, 2017, s. 325–341. Dostupné z: doi:10.1145/3132747.3132780
- [6] OMAROVA, Saule a Graham STEELE. There's a Lot We Still Don't Know About Libra. *The New York Times* [online]. 2019. Dostupné z: <https://www.nytimes.com/2019/11/04/opinion/facebook-libra-cryptocurrency.html>
- [7] DONNE, John. *The "Anniversaries" and the "Epicedes and Obsequies"*. B.m.: Indiana University Press, 1995. The Variorum Edition of the Poetry of John Donne.
- [8] BROWN, George C., ed. A Swedish Traveller in Early Wisconsin: The Observations of Fredrika Bremer. *Wisconsin Magazine of History*. 2. vyd. 1978, 61–62.
- [9] In: J. K. ROWLING *Harry Potter and the Order of the Phoenix*. cca. 2003, s. 135–139.
- [10] MÄDJE, Laurenz. *Tokenization of + and - with scientific notation* [online]. 18. července 2020. Dostupné z: <https://github.com/typst/typstc/issues/3>
- [11] *Terminator 2: Judgment Day*. Carolco Pictures; Pacific Western Productions; Lightstorm Entertainment; Le Studio Canal+ S.A. 1. července 1991.
- [12] *Conspiracy Theories and Interior Design*. In: Universal Television; Sony Pictures Television; Krasnoff Foster Productions; Harmonious Claptrap; Russo Brothers Film. 18. listopad 2010.
- [13] *The wire*. Blown Deadline Productions. 2002.
- [14] DOAN, T. D., D. B. TRAN THOAI a Hartmut HAUG. Kinetics and luminescence of the excitations of a nonequilibrium polariton condensate. *Physical Review B* [online]. 2020, 102(16), 165126–165139. Dostupné z: doi:10.1103/PhysRevB.102.165126
- [15] JERRENTROP, Andreas, Tobias MUELLER, Ulrich GLOWALLA, Meike HERDER, Nadine HENRICHS, Andreas NEUBAUER a Juergen R. SCHAEFER. Teaching medicine

- with the help of "Dr. House". *PLoS ONE* [online]. 2018, **13**(3). Dostupné z: [doi:10.1371/journal.pone.0193972](https://doi.org/10.1371/journal.pone.0193972)
- [16] *Informational plaque about Jacoby's 1967 photos*. B.m.: Stiftung Reinbeckhallen. 2020
- [17] *L'oiseau rare, de l'hirondelle au kakapo* [online]. 18. prosinec 2020 [cit. 2020-11-04]. Dostupné z: <https://www.museedesconfluences.fr/fr/evenements/l%E2%80%99oiseau-rare-de-l%E2%80%99hirondelle-au-kakapo>
- [18] DUVAL, Fred. *Renaissance, Les Déracinés*. 1. vyd. Přel. EMEM a Fred BLANCHARD. B.m.: Dargaud, 2018.
- [19] MOORE, Edward F. *Gedanken-experiments on sequential machines*. B.m.: NBS. duben 1956. *Annals of Mathematics Studies*
- [20] SILVER, Nate. Trump's claim to have won Georgia is highly dubious. No network has called it. He's only ahead by 2.5 points there, and the outstanding votes are mostly mail votes in very blue counties, likely very Democratic. Biden may even be a slight favorite there. In: [online]. 4. listopad 2020. Dostupné z: <https://twitter.com/NateSilver538/status/1323889051037028353>
- [21] PEDBOST, Marven F., Trilleen POMALGU, Chris LINTOTT, Nora EISNER a Belinda NICHOLSON. *Defining the Really Habitable Zone* [online]. 2020. Dostupné z: <https://arxiv.org/abs/2003.13722>
- [22] ISHKUR. *Ishkur's Guide to Electronic Music* [online]. [cit. 2020-11-12]. Dostupné z: <http://www.techno.org/electronic-music-guide/>
- [23] MATTERMOST. Mattermost Privacy Policy. *Policies* [online]. [cit. 2020-11-29]. Dostupné z: <https://mattermost.com/privacy-policy/>
- [24] WORTH, Jon. *Jon Worth Euroblog* [online]. Dostupné z: <https://jonworth.eu/>
- [25] PROKOPOV, Nikita. It is fast or it is wrong. *tonsky.me* [online]. 29. prosinec 2018. Dostupné z: <https://tonsky.me/blog/slow-wrong/>
- [26] UNITED NATIONS DEVELOPMENT PROGRAMME. *Human Development Report 2019* [online]. 2019. Dostupné z: <http://hdr.undp.org/sites/default/files/hdr2019.pdf>
- [27] BARROWS, Miellyn Fitzwater. Audio Descriptions. In: [online]. 7. únor 2017. Dostupné z: <https://www.20k.org/episodes/audio>
- [28] *authoritative* [online]. nedatováno [cit. 2020-11-29]. Dostupné z: <https://dictionary.cambridge.org/dictionary/english/authoritative>
- [29] *Logician* [online]. nedatováno [cit. 2019-12-02]. Dostupné z: <http://image-net.org/api/text/wordnet.structure.hyponym?wnid=n10269785>
- [30] INTERNET ENGINEERING TASK FORCE. *Secret Key Transaction Authentication for DNS* [online]. 2000. Dostupné z: <https://tools.ietf.org/html/rfc2845>
- [31] *Roe v. Wade*. 1973
- [32] *Freedom of Information Act*. 1967
- [33] JOHN. Celebrating over five million users, a quarter million daily actives, and over five years of dedicated user support. *Overleaf Blog* [online]. 8. listopad 2019. Do-

stupné z: <https://de.overleaf.com/blog/celebrating-over-five-million-users-and-a-quarter-million-daily-actives>

- [34] PEPE, Alberto. *How many scholarly articles are written in LaTeX?* [online]. 21. únor 2017. Dostupné z: [doi:10.22541/au.148771883.35456290](https://doi.org/10.22541/au.148771883.35456290)

A Qsort implementation

Implementation is in Haskell.

```

1 quicksort [] = []
2 quicksort (p:xs) = (quicksort lesser) ++ [p] ++ (quicksort greater)
3   where
4     lesser = filter (< p) xs
5     greater = filter (>= p) xs

```

Yes. Very cool.

Algorithm 1: Binary Search

```

1: procedure BINARY-SEARCH( $A, n, v$ )
2:   ▷ Initialize the search range
3:    $l \leftarrow 1$ 
4:    $r \leftarrow n$ 
5:
6:   while  $l \leq r$  do
7:      $mid \leftarrow \text{floor}(\frac{l+r}{2})$ 
8:     if  $A[mid] < v$  then
9:        $l \leftarrow m + 1$ 
10:    else if  $A[mid] > v$  then
11:       $r \leftarrow m - 1$ 
12:    else
13:      return  $m$ 
14:    end
15:  end
16:  return null
17: end

```

B Shit table

A	B
B	C
C	D

Algorithm 2: Variable Assignment

1: $x \leftarrow y$

C OpenGL Shader Compilation

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua quaerat.

```

1  unsigned int OpenGLShader::Compile(
2      const std::unordered_map<unsigned int, std::string>& sources
3  ) const
4  {
5      EG_PROFILE_FUNCTION();
6
7      EG_CORE_ASSERT(sources.size() >= 0 && sources.size() <= 3,
8          "Can only have three shader sources \
9          (vertex, geometry, fragment)!");
10
11     unsigned int program;
12     EG_OPENGL_CALL(program = glCreateProgram());
13
14     std::vector<unsigned int> shaders(sources.size());
15     for (const auto& [type, source] : sources)
16     {
17         auto shader = CompileSource(type, source);
18         shaders.push_back(shader);
19         EG_OPENGL_CALL(glAttachShader(program, shader));
20     }
21
22     EG_OPENGL_CALL(glLinkProgram(program));
23
24     int status;
25     EG_OPENGL_CALL(glGetProgramiv(program, GL_LINK_STATUS, &status));
26     if (status == GL_FALSE)
27     {
28         int length;
29         EG_OPENGL_CALL(glGetProgramiv(
30             program, GL_INFO_LOG_LENGTH, &length));
31
32         std::vector<char> message(length);
33         EG_OPENGL_CALL(glGetProgramInfoLog(
34             m_RendererID, length, &length, message.data()));
35
36         EG_OPENGL_CALL(glDeleteShader(program));
37         for (auto shader : shaders)
38         {
39             EG_OPENGL_CALL(glDeleteShader(shader));
40         }
41         EG_CORE_ERROR("{} ", message.data());
42         EG_CORE_ASSERT(false, "Shader compilation failed!");
43         return 0;
44     }
45
46     EG_OPENGL_CALL(glValidateProgram(program));
47     for (auto shader : shaders)
48     {
49         EG_OPENGL_CALL(glDeleteShader(shader));
50     }
51
52     return program;
53 }
```

Výpis 3: C++ method for GLSL shader compilation

D C# code

```

1  using System.Diagnostics;
2  using System.Security.Claims;
3  using CoworkingApp.Models;
4  using CoworkingApp.Models.Misc;
5  using CoworkingApp.Models.ViewModels;
6  using CoworkingApp.Services.Repositories;
7  using Microsoft.AspNetCore.Authorization;
8  using Microsoft.AspNetCore.Mvc;
9
10 namespace CoworkingApp.Controllers.ViewControllers;
11
12 public class HomeController
13 {
14     IWorkspaceRepository workspaceRepository,
15     ICoworkingCenterRepository coworkingCenterRepository,
16     IReservationRepository reservationRepository,
17     IUserRepository userRepository
18 }
19 : Controller
20 {
21     [HttpGet]
22     public async Task<IActionResult> Index()
23     {
24         var workspaces = await workspaceRepository.GetWorkspaces(new ()
25         {
26             HasPricing = true,
27             IncludePricings = true,
28             IncludeStatus = true,
29         });
30
31         var coworkingCenters = await coworkingCenterRepository.GetCenters(
32             new CoworkingCenterFilter());
33
34         return View(new HomeIndexViewModel()
35         {
36             Workspaces = workspaces,
37             CoworkingCenters = coworkingCenters
38         });
39     }
40
41     [HttpGet]
42     [Authorize]
43     public async Task<IActionResult> Dashboard(
44         [FromQuery] ReservationSort reservationSort = ReservationSort.None)
45     {
46         var userId = User.GetUserId();
47
48         if (userId == null)
49         {
50             return Unauthorized(new { message = "User not found" });
51         }
52
53         var reservations = await reservationRepository
54             .GetReservations(new ReservationsFilter
55             {
56                 CustomerId = userId,
57                 IsCancelled = false,
58                 IncludeWorkspace = true,
59                 Sort = reservationSort,
60             });
61
62         var user = (await userRepository.GetUsers(new UserFilter
63         {
64             UserId = userId

```

```
65         })).Single();
66
67         return View(new HomeDashboardViewModel
68         {
69             User = user,
70             Reservations = reservations,
71             ReservationSort = reservationSort,
72         });
73     }
74
75     [HttpGet]
76     public async Task<IActionResult> Privacy()
77     {
78         return View();
79     }
80
81     [ResponseCache(
82         Duration = 0,
83         Location = ResponseCacheLocation.None, NoStore = true)]
84     public IActionResult Error()
85     {
86         return View(new ErrorViewModel
87         {
88             RequestId = Activity.Current?.Id ?? HttpContext.TraceIdentifier
89         });
90     }
91 }
```

Výpis 4: Computer program in C# language