

Komponenta výukového serveru TI - P--úplné problémy 2

Component of Learning Server for Theoretical Computer Science - NP-complete problems 2

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Diplomová práce

Vedoucí práce: Borivoj Gulas

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OFDM - Orthogonal Frequency Division Multiplexing

1.1 Introduction

In Kapitola 1.1, we see how to turn Sections into Chapters. And in kapitole 1.1, it is done manually.

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do. [1]. Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do. [2].

$$\sum_{i=1}^{n} i = 1 + 2 + 3 + \dots + n$$

Code snippet in C programming language:

```
1 #include <stdio.h>
2
3 int main() {
4  printf("hello, world!\n");
5  return 0;
6 }
```

Obrázek 1: Computer program in C language

More simple langauge, for example SQL:

```
sql
 1 SELECT
 2
    c.customer id,
3
   c.fname,
4
     c.lname,
5
    c.email
 6 FROM customer c
7 WHERE EXISTS (
     SELECT *
8
9
     FROM purchase p
10
     WHERE p.customer_id = c.customer_id
11 )
```

Obrázek 2: lksdfljdl

1.2 Subheading Level 2

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$$\begin{bmatrix} 1 & * & * \\ * & 1 & * \\ * & * & 1 \end{bmatrix}$$

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1.3 Prokázání netranzitivity

První úkolem je ukázat, že vztahy mezi kostkami nejsou tranzitivní, to znamená, že vztahy mezi kostkami jsou tzv. cyklické¹ Tvrdíme totiž, že platí B > A, C > B a současně A > C. To znamená, že žádná kostka není "nejlepší" ve všech případech.

Pro každou dvojici kostek vypočítáme pravděpodobnost vítězství jedné kostky nad druhou, konkrétně P(B > A), P(C > B) a P(A > C), a ověříme, že všechny tyto pravděpodobnosti jsou větší než $\frac{1}{2}$.

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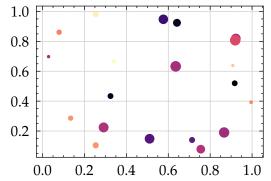
¹Wikipedia, *Intransitivity*: https://en.wikipedia.org/wiki/Intransitivity

1.4 Subheading Level 2

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1.4.1 Subheading Level 3

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Obrázek 3: Some random data visualisation

Heading Level

$$f(x) = y$$

$$\begin{pmatrix} 1 & 2 & \dots & 10 \\ 2 & 2 & \dots & 10 \\ \vdots & \vdots & \ddots & \vdots \\ 10 & 10 & \dots & 10 \end{pmatrix}$$

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2.1 Heading Level 2

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$$\Omega = \left\{ (2,1), (2,1), (5,1), (5,1), \\ (2,4), (2,4), (5,4), (5,4), \\ (2,4), (2,4), (5,4), (5,4), \\ (2,4), (2,4), (5,4), (5,4) \right\}$$

Velikost pravděpodobnostního prostoru je $|\Omega|=16$. Z rozepsané Ω vidíme, že počet případů, kdy kostka B vyhraje nad A je vyšší (10) než počet, kdy prohraje (6). Pravděpodobnost vypočteme jako:

$$P(B > A) = \frac{2 + 4 \cdot 2}{|\Omega|} = \frac{10}{16} = \underline{0.625}$$

Heading Level 1

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3.1 Subheading Level 2

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Fancy-Algorithm 1 do something 2 do something else 3 while still something to do do 4 | do even more 5 | if not done yet then 6 | wait a bit 7 | resume working 8 | else 9 | go home 10 | end 11 end

Algorithm 1: My cool algorithm

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4 Heading Level 1

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5 Heading Level 1

necessitatibus saepe eveniet, ut et voluptates repudiandae sint et molestiae non recusandae. Itaque earum rerum defuturum, quas natura non depravata desiderat. Et quem ad me accedis, saluto: 'chaere,' inquam, 'Tite!' lictores, turma omnis chorusque: 'chaere, Tite!' hinc hostis mi Albucius, hinc inimicus. Sed iure Mucius. Ego autem mirari satis non queo unde hoc sit tam insolens domesticarum rerum fastidium. Non est omnino hic docendi locus; sed ita prorsus existimo, neque eum Torquatum, qui hoc primus cognomen invenerit, aut torquem illum hosti detraxisse, ut aliquam ex eo est consecutus? – Laudem et caritatem, quae sunt vitae.

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6.2 Heading Level 3

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Term: hello [1, p. 358] Secon term: Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magnam aliquam quaerat voluptatem. Ut enim aeque doleamus animo, cum corpore dolemus, fieri. Halting: it is something [4, p. 23]

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