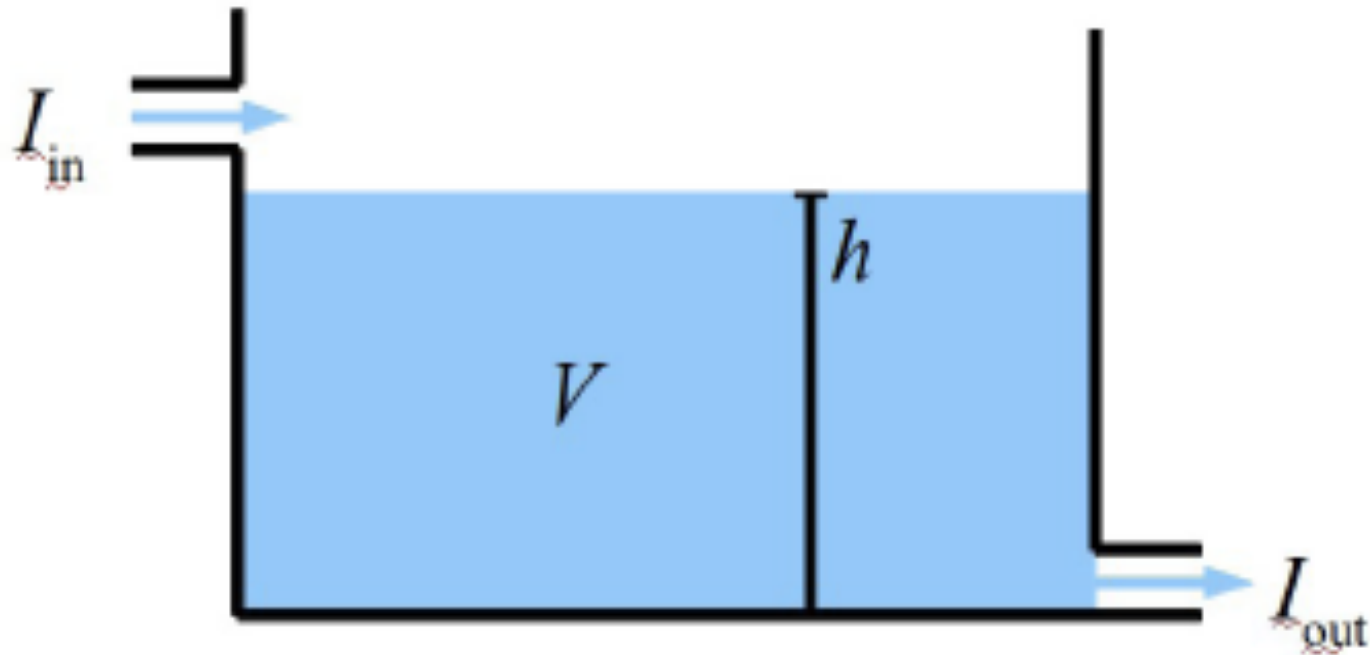
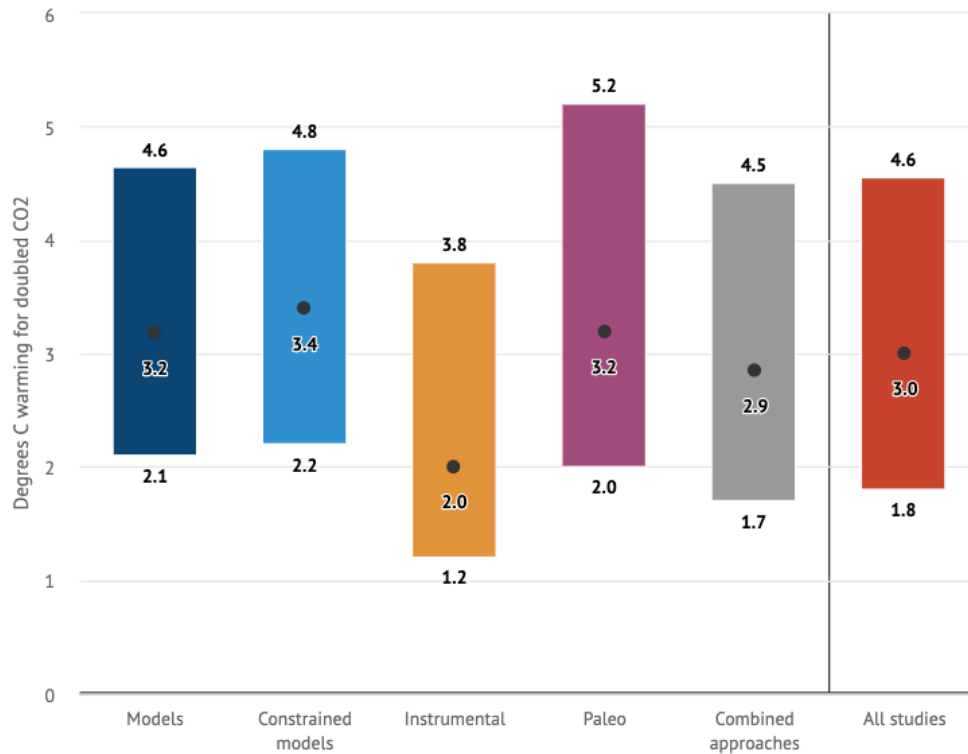


# 1. Feedback basics



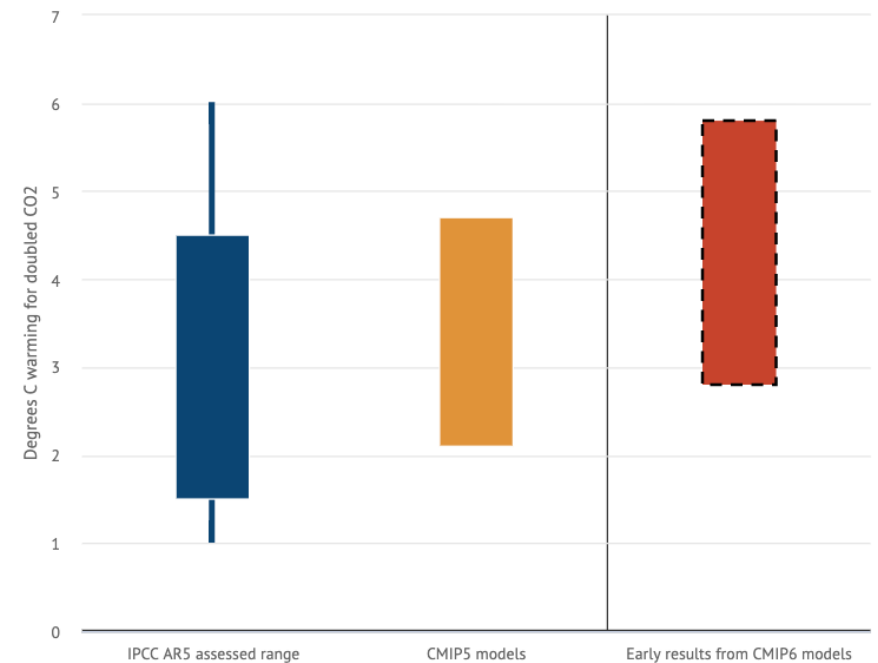
# New GCM versions are running hotter

model estimates of the equilibrium climate sensitivity are increasing



Hausfather, 2018, Carbonbriefs

Equilibrium climate sensitivity estimates

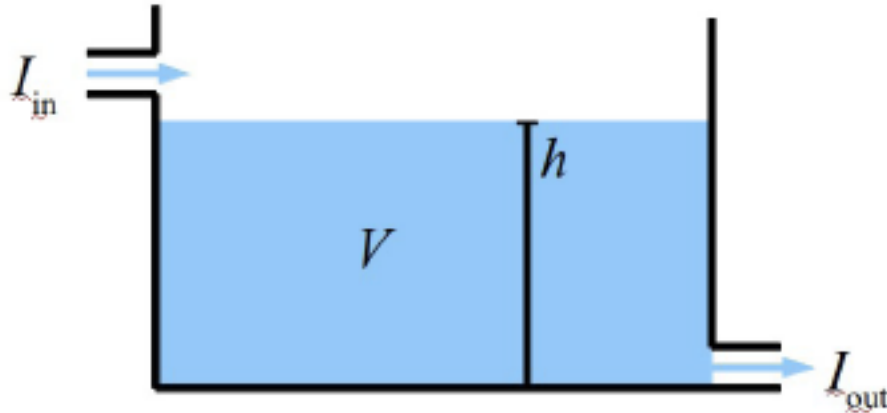


Belcher et al., UK Met office, March 2019



# Feedback math

Strong negative feedback = big outflow pipe = big  $k$

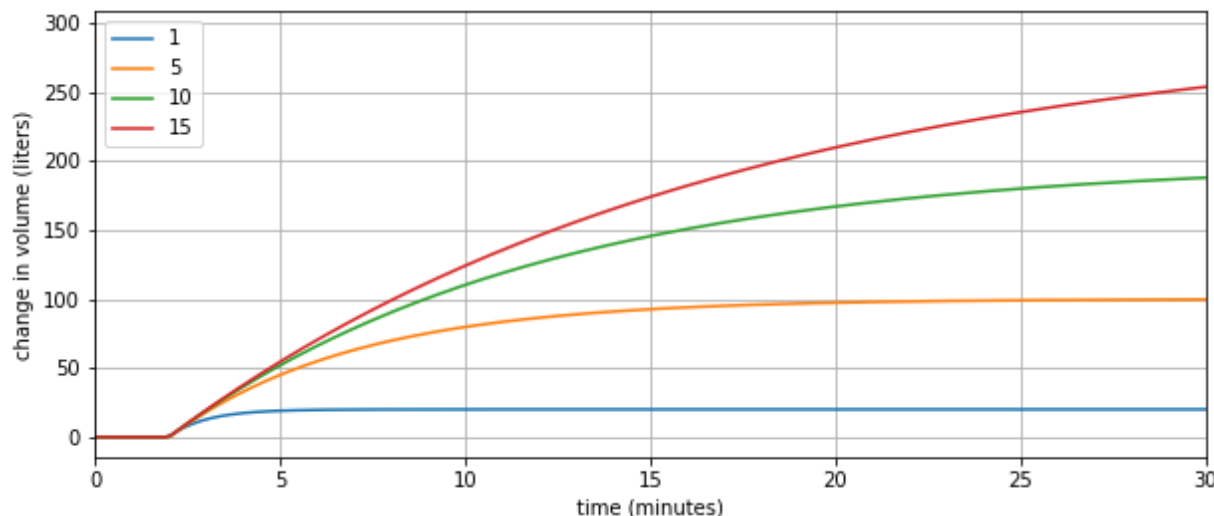


$$\frac{dV}{dt} = I_{in} - I_{out} = I_{in} - kV$$

$$\frac{d\Delta V}{dt} = \Delta I_{in} - \frac{\Delta V}{\lambda}$$

$$\Delta V_{final} = \lambda \Delta I_{in}$$

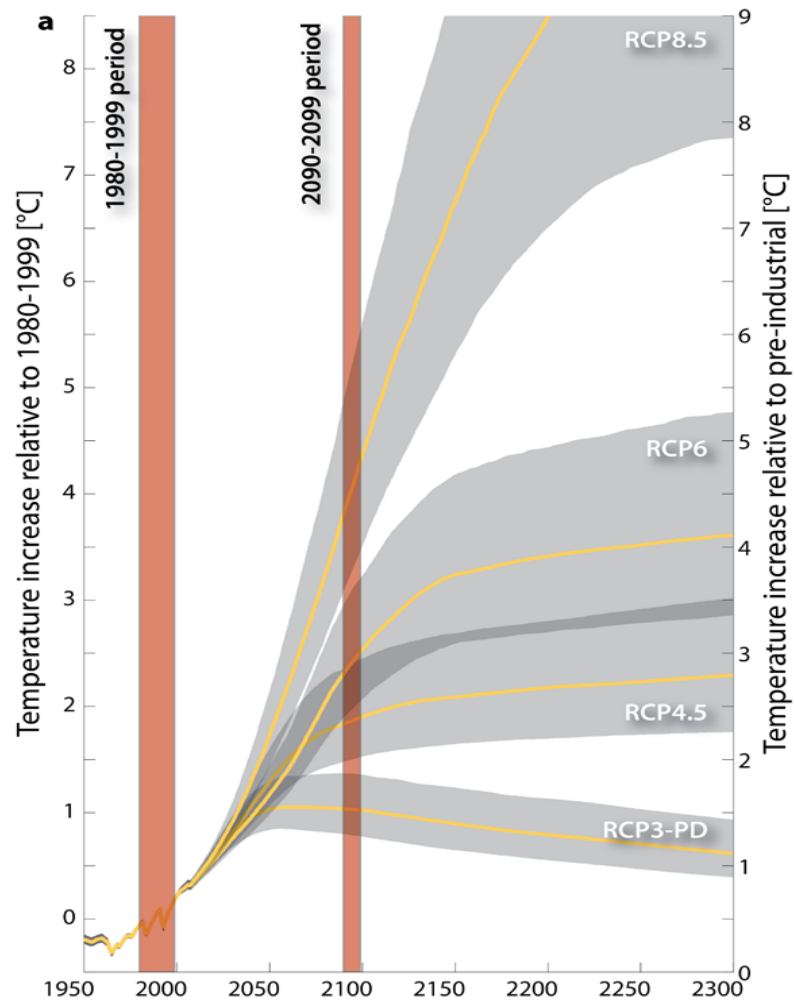
$$\Delta V(t) = \lambda \Delta I_{in} (1 - e^{-t/\lambda})$$



As  $\lambda=1/k$  gets larger  
Pipe gets smaller  
Time constant increases  
Equilibrium volume goes up

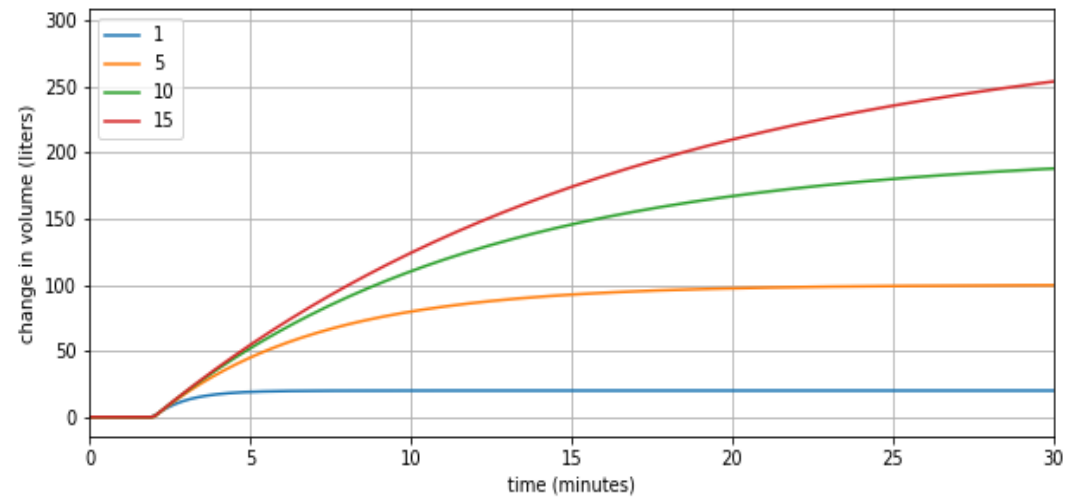
# Note the similarity with CMIP 5 fully coupled atmos/ocean GCMs

## CMIP5 models



AR5 chapter 11

## Our bathtub



# Feedback math

Write Climate Energy Budget as:

$$d\Delta E / dt = \Delta F + \Delta R \text{ with } \Delta R = f \Delta T$$

$$d\Delta E / dt = \Delta F + f \Delta T$$

1. An external change  $\Delta F$  to the climate forcing
2. Climate system responds with a change  $\Delta R$  to the surface radiative flux

To a good approximation the total feedback is the sum of individual feedback factors, each representing a climate process:

$$\frac{d\Delta E}{dt} = \Delta F + (f_{PL} + f_{WV} + f_{LR} + \dots)\Delta T = \Delta F + \left(\sum f_n\right)\Delta T$$

Compare with the Climate Sensitivity

$$\frac{\Delta E}{dt} = \Delta F - \frac{\Delta T}{\lambda}$$

Therefore, the feedback factor is related to the climate sensitivity:

$$f = -1/\lambda$$

# Feedback math

Can write feedback factor as

$$f = \sum_n f_n = \Delta R / \Delta T \quad \Delta R = f \Delta T$$

In climate modelling, we attempt to estimate each feedback factor  $f_n$  for a given feedback mechanism ' $n$ ' according to:

$$f_n = \frac{\Delta R_n}{\Delta T} = \left( \frac{\Delta R_n}{\Delta climate_n} \right) \left( \frac{\Delta climate_n}{\Delta T} \right)$$

where  $n$ =Planck, clouds, sea-ice, water vapor, etc.

$\Delta R_n$  is called the “radiative response” due to feedback  $n$

In the case of sea-ice, it is negative (more negative upward radiation) when sea ice fraction increases, and positive (less reflection) when sea ice fraction decreases.

# Individual feedback factors

Water Vapour FdBk:  $f_{wv} = \left( \frac{\Delta R}{\Delta H_2O} \right) \left( \frac{\Delta H_2O}{\Delta T} \right)$  (Positive/Amplifying)

(Positive +) (Positive +)

Albedo Feedback:  $f_{ice} = \left( \frac{\Delta R}{\Delta ice} \right) \left( \frac{\Delta ice}{\Delta T} \right)$  (Positive/Amplifying)

(Negative -) (Negative -)

Lapse Rate FdBk:  $f_{LR} = \left( \frac{\Delta R}{\Delta \Gamma} \right) \left( \frac{\Delta \Gamma}{\Delta T} \right)$  (Negative/Stabilizing)

(Negative -) (Positive +)

Cloud Feedback:  $f_{clouds} = \left( \frac{\Delta R}{\Delta clouds} \right) \left( \frac{\Delta clouds}{\Delta T} \right)$  ( $\pm$  depends on the altitude of the cloud)

**Tip:** Think of fraction like a derivative and treat it independently

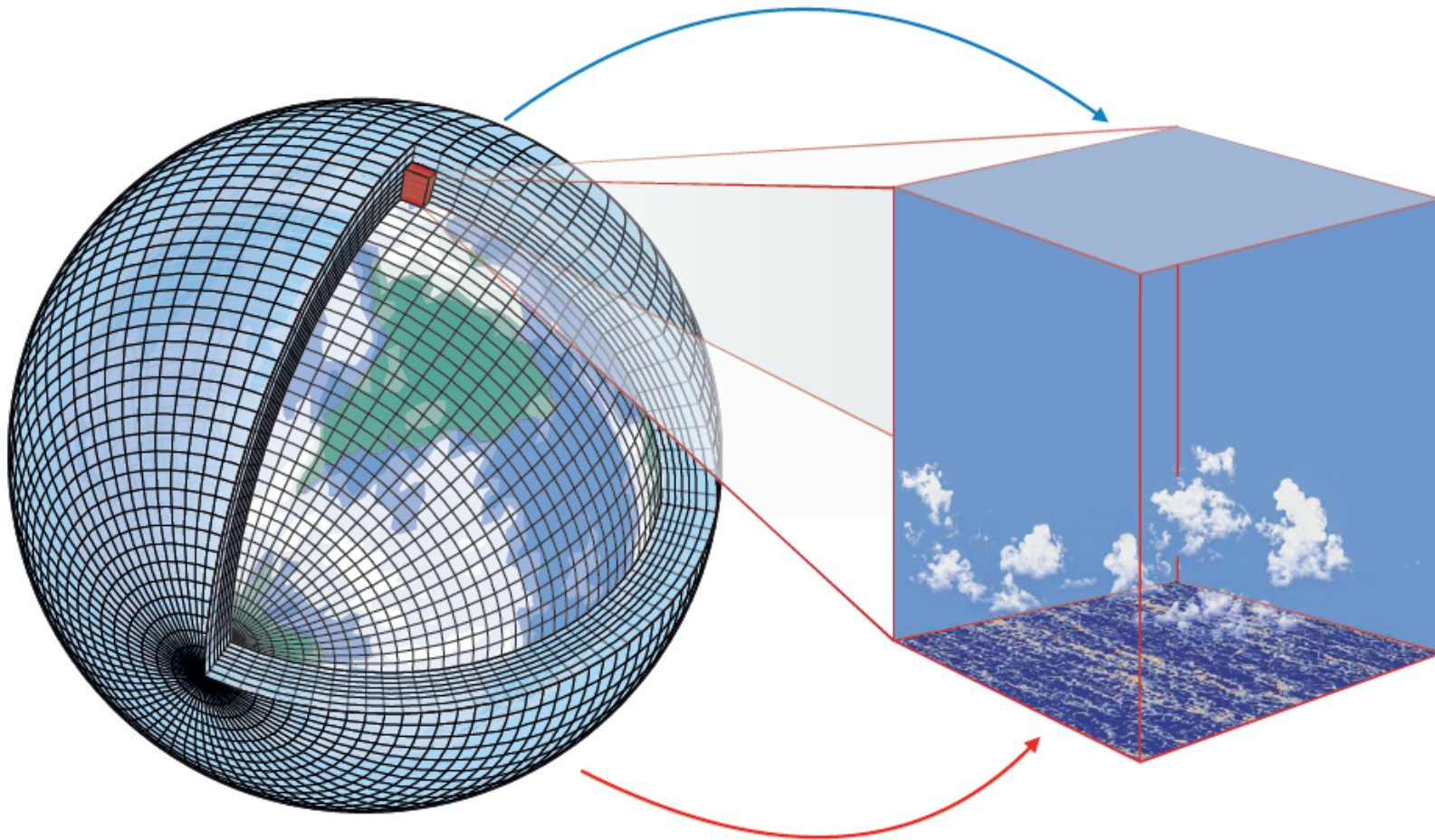


# 1. Summary

$$f_{ice} = \left( \frac{\Delta R}{\Delta ice} \right) \left( \frac{\Delta ice}{\Delta T} \right)$$

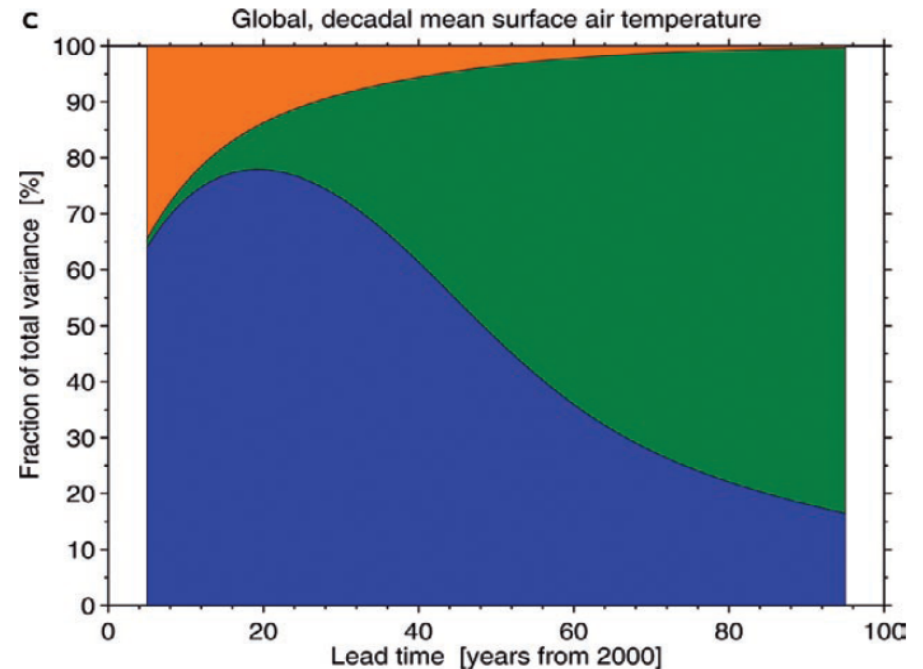
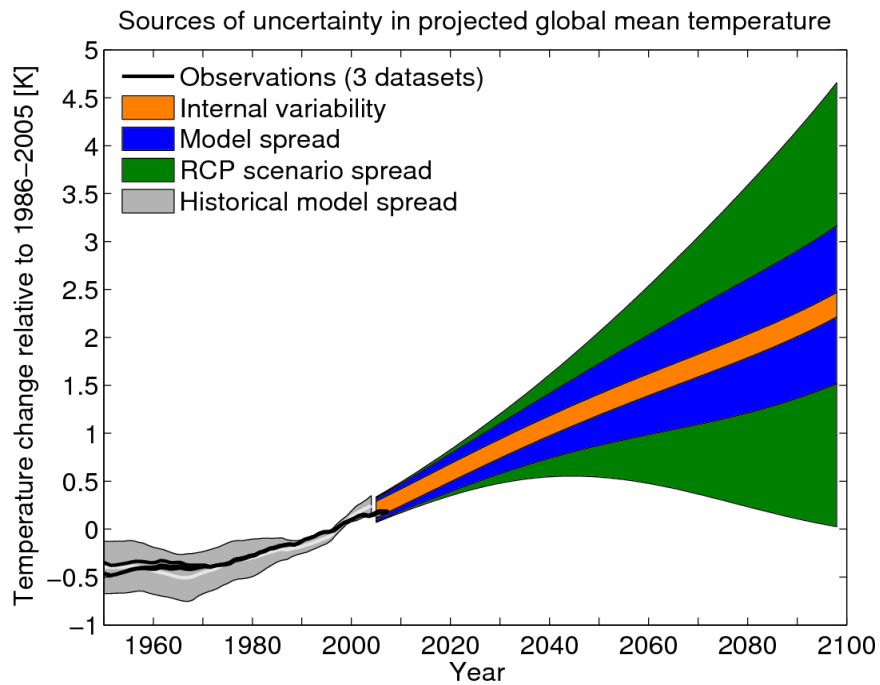
- Finding the paired derivatives in terms like  $f_{ice}$  is a better use of computer time than running “black box” projections for a range of forcings
- The first term is called the “radiative kernel” and can be calculated offline using the model’s radiation code, or a single kernel can be shared between models
- The second term requires the full GCM, it is the derivative that accounts for all the feedbacks

## 2. Estimating feedback



Schneider et al., 2018

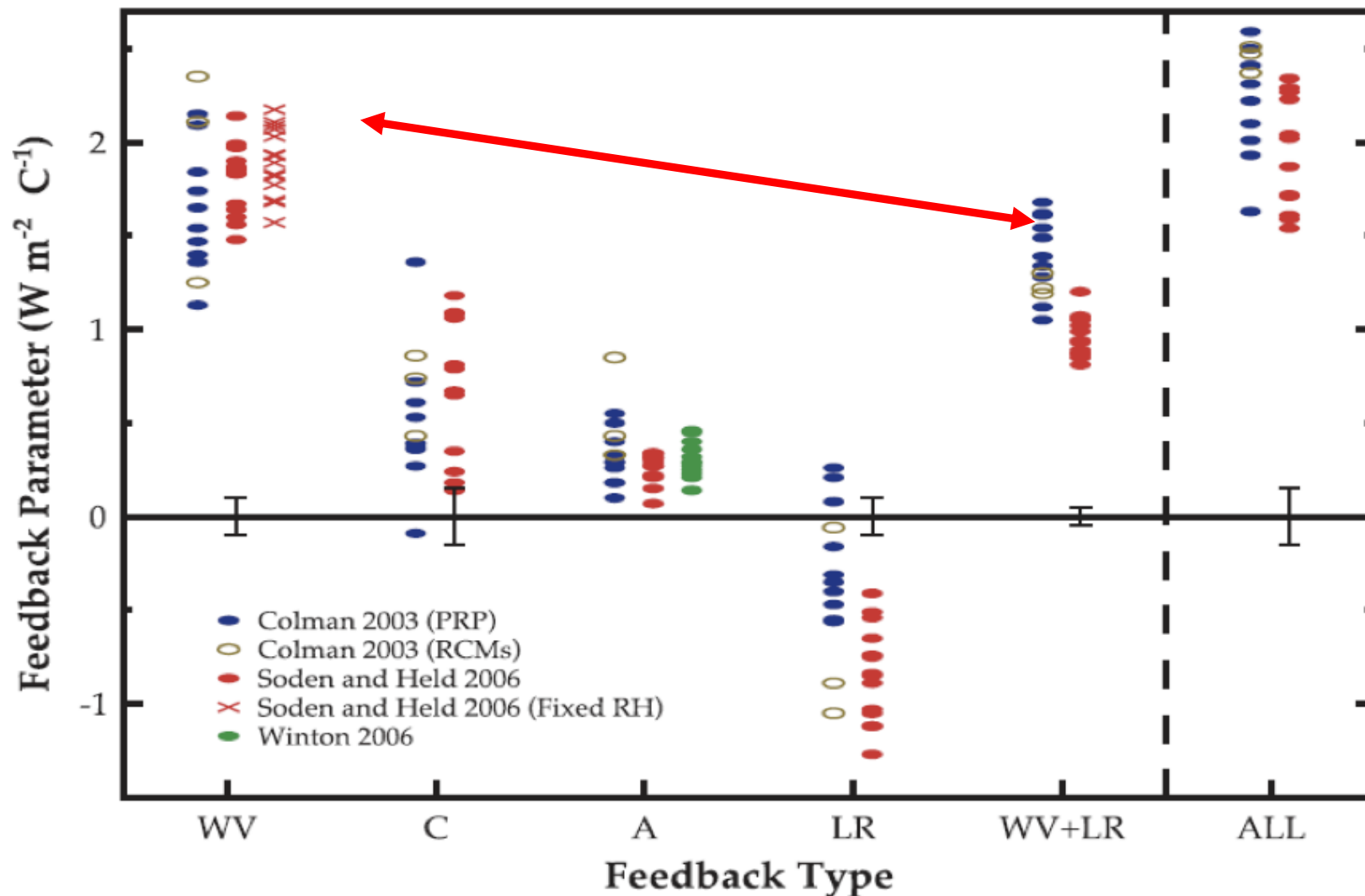
# Caveat: policy dominates physics



IPCC AR5 Figure 11.8

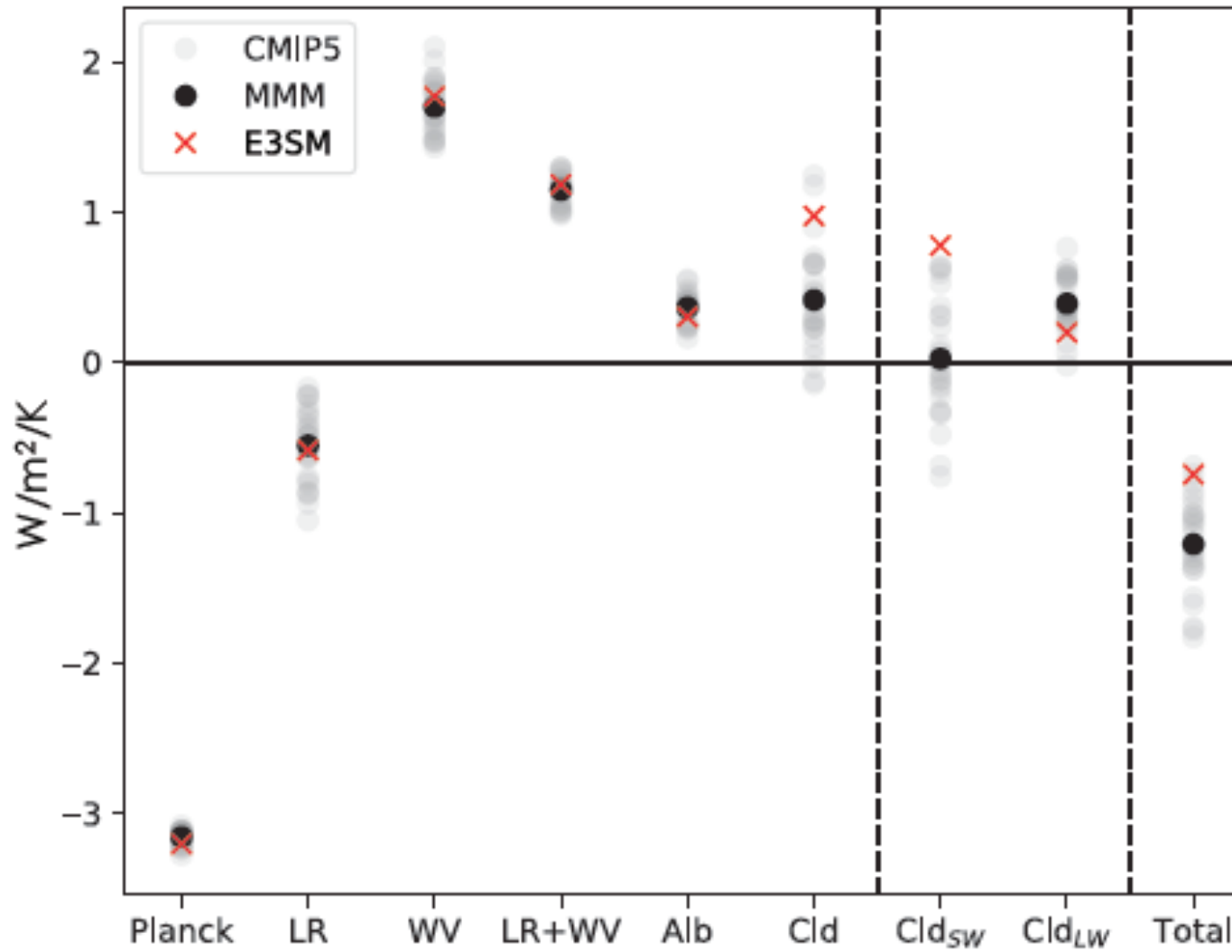
# Feedbacks from models ca 2005

(for comparison remember  $f_{\text{planck}} = -4 \text{ W m}^{-2} \text{ K}^{-1}$ )



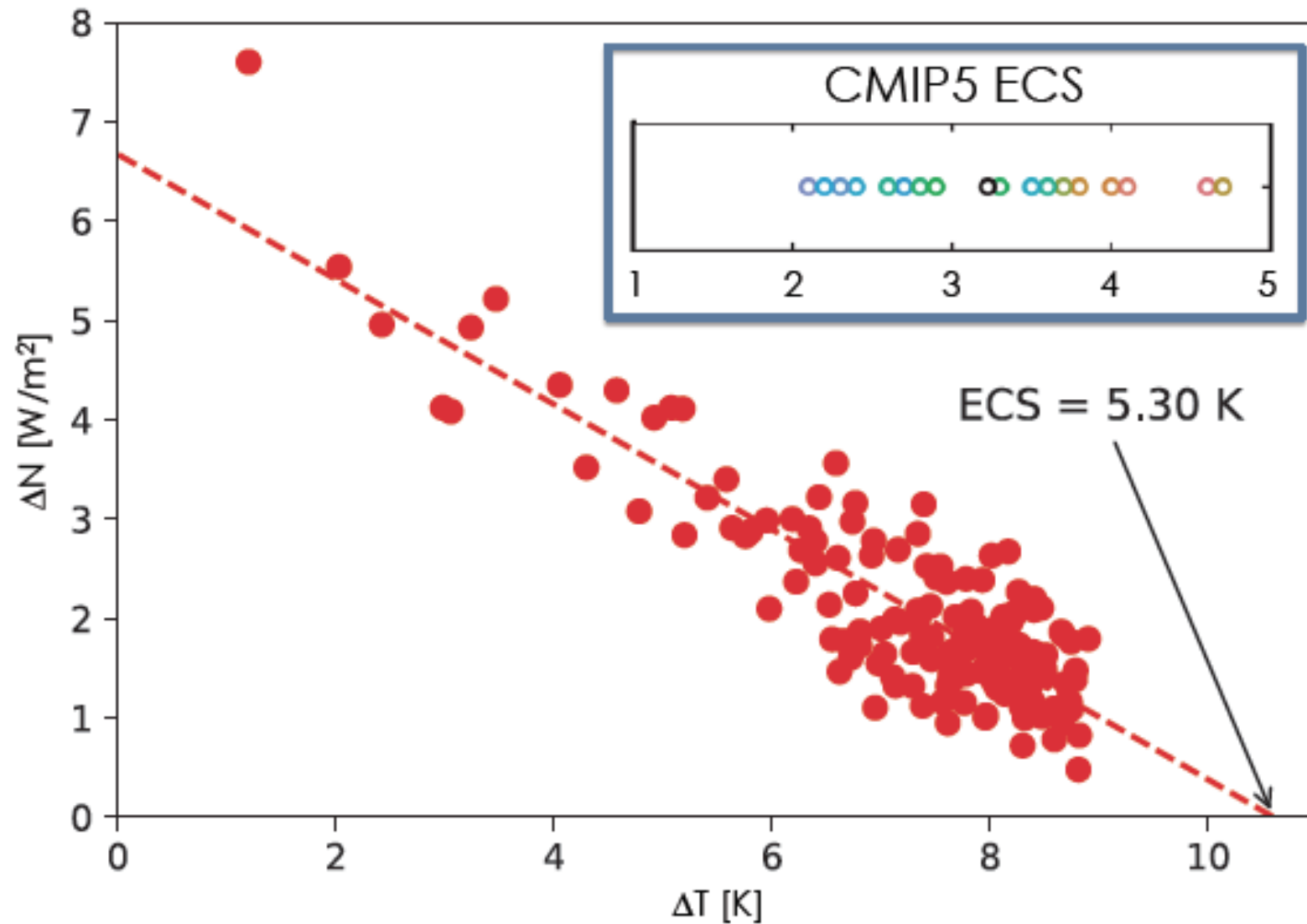
wv=water vapor, c=clouds, a=ice albedo, lr=lapse rate, wv+lr=combined wv and lr

# Feedbacks from models ca 2018



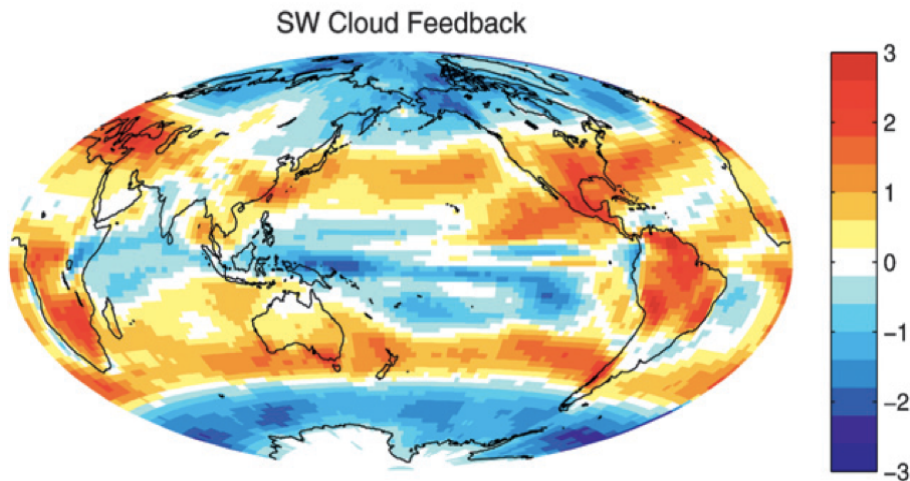
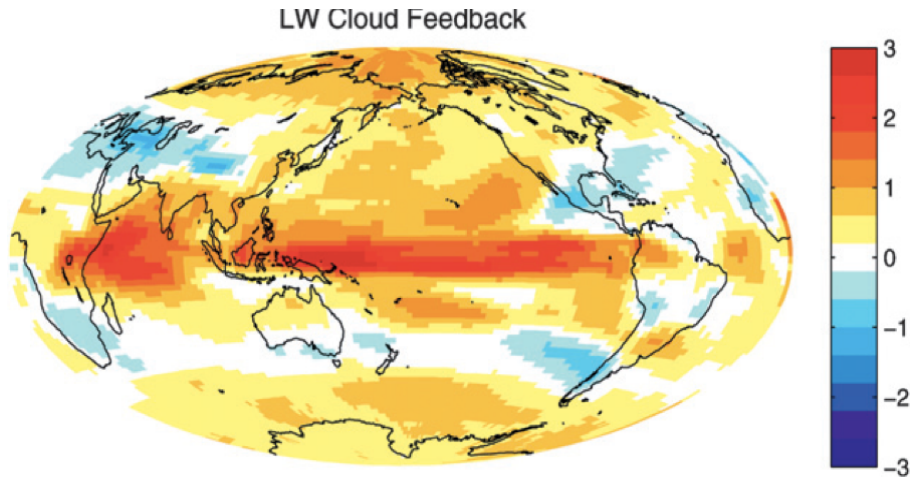
Zelinka et al. 2018

# A Gregory plot for sensitivity



Zelinka et al. 2018

# Spatial feedbacks with radiative kernels



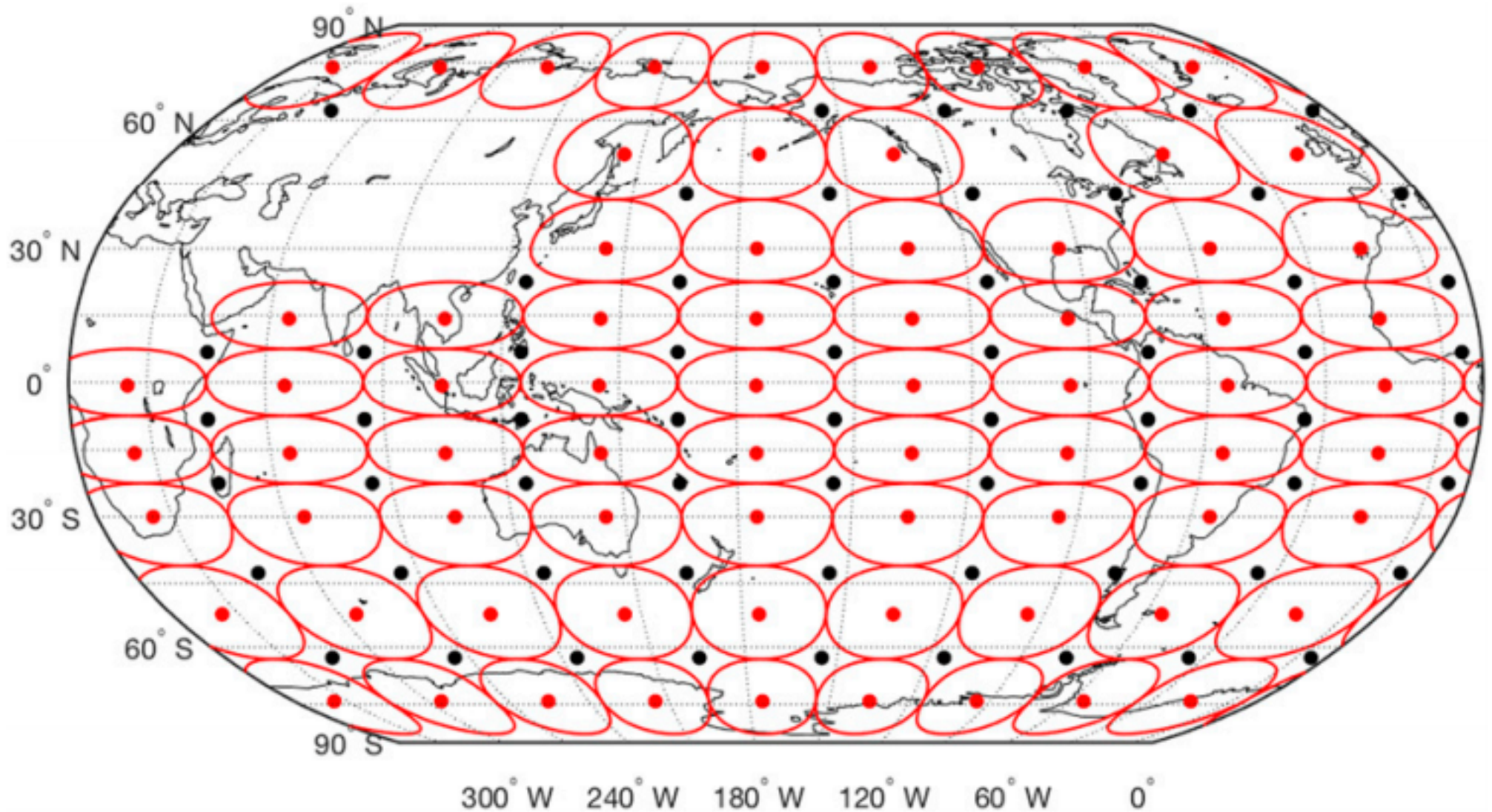
- Run a climate model
- Increase sea surface temperatures by 2K
- Measure changes to  $\Delta R$  due to clouds

$$f_x = \frac{\Delta R}{\Delta T} = \left( \frac{\Delta R}{\Delta climate} \right) \left( \frac{\Delta climate}{\Delta T} \right)$$

Note the long and shortwave feedbacks approximately cancel for deep convection in the tropics

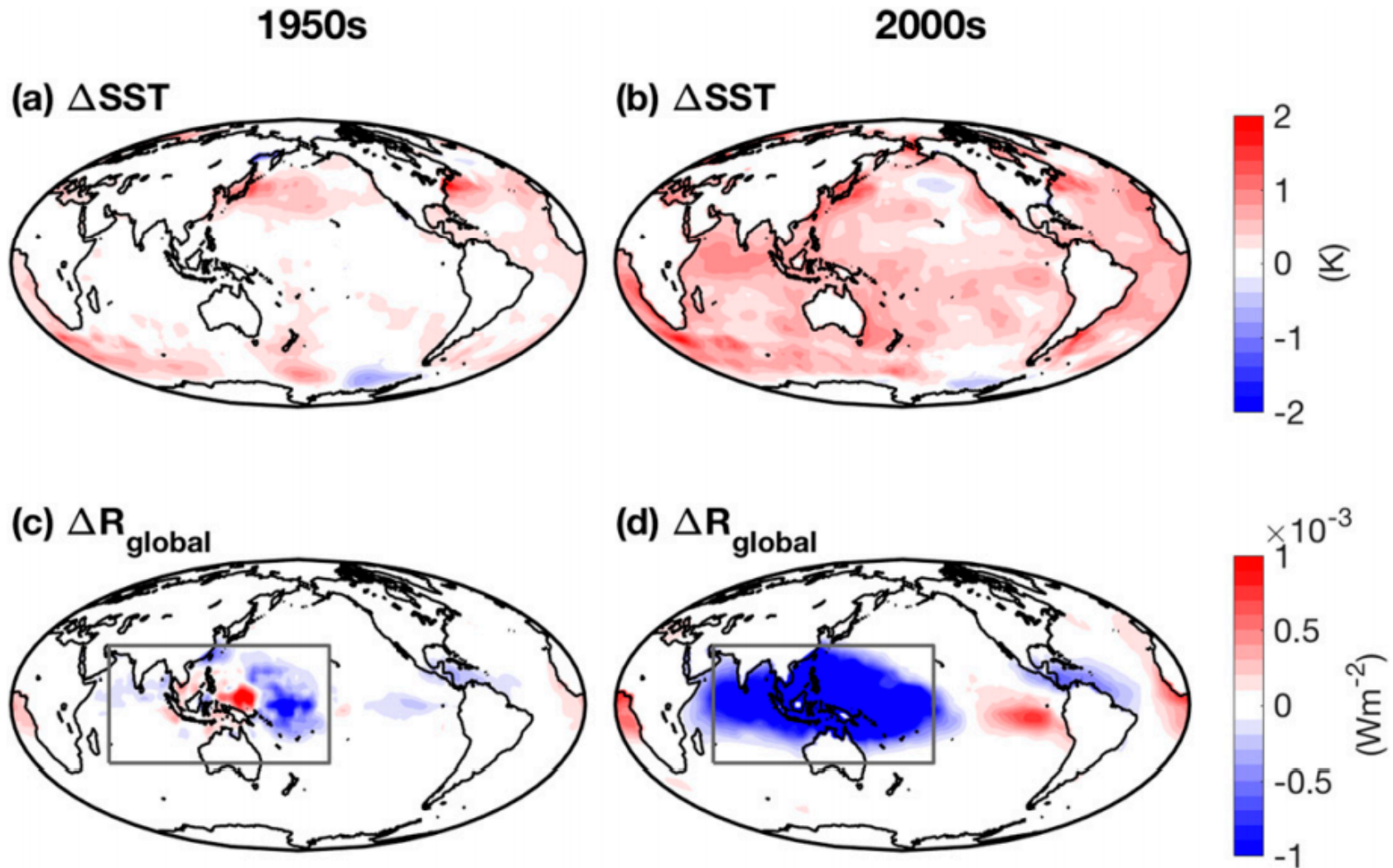


# Next level: Green's functions





# Temperature perturbations in the western Pacific warmpool dominate the radiative response (negative $\Delta R$ is heating)



# 3. Summary

- Long and shortwave cloud feedback estimates differ significantly between models
- Many groups are working on analyses of the physical mechanisms behind the feedback, using a variety of techniques (radiative kernels, patterned SST, Green's functions, high frequency output at specific locations, aquaplanet runs, cloud condensate tendency runs, etc.