MATH2: Correction rapide du CC3 du 15 juin 2015.

Exercice 1. Notons a = AB, b = AC et c = BC.

1. Bien évidemment, $c = \sqrt{a^2 + b^2}$ et

$$\frac{\partial c}{\partial a}(a,b) = \frac{2a}{2\sqrt{a^2 + b^2}} = \frac{a}{c}, \qquad \frac{\partial c}{\partial b}(a,b) = \frac{2b}{2\sqrt{a^2 + b^2}} = \frac{b}{c}, \qquad \Delta c = \frac{a}{c}\,\Delta a + \frac{b}{c}\,\Delta b.$$

Les calculs donnent

$$c = 7.9479872$$
, $\Delta c = 0.0223201$, $\frac{\Delta c}{c} = 0.2808273\%$, soit $c = 7.95 \pm 0.02$, $\frac{\Delta c}{c} = 0.28\%$.

2. Puisque S = ab/2, on a

$$\frac{\partial S}{\partial a}(a,b) = \frac{b}{2}, \qquad \frac{\partial S}{\partial b}(a,b) = \frac{a}{2}, \qquad \Delta S = \frac{b}{2}\,\Delta a + \frac{a}{2}\,\Delta b.$$

Les calculs donnent

$$S = 11.4036$$
, $\Delta S = 0.06775$, $\frac{\Delta S}{S} = 0.5941106\%$, soit $S = 11.40 \pm 0.07$, $\frac{\Delta S}{S} = 0.59\%$.

Exercice 2. La masse volumique du béton est $\rho = \frac{M}{c^2 l}$; on a alors

$$\frac{\partial \rho}{\partial M}(M,c,l) = \frac{1}{c^2l} = \frac{\rho}{M}, \qquad \frac{\partial \rho}{\partial c}(M,c,l) = \frac{-2M}{c^3l} = -2\frac{\rho}{c}, \qquad \frac{\partial \rho}{\partial l}(M,c,l) = \frac{-M}{c^2l^2} = -\frac{\rho}{l},$$

ce qui conduit à

$$\Delta \rho = \left|\frac{\rho}{M}\right| \Delta M + \left|-2\frac{\rho}{c}\right| \Delta c + \left|-\frac{\rho}{l}\right| \Delta l = \frac{\rho}{M} \Delta M + 2\frac{\rho}{c} \Delta c + \frac{\rho}{l} \Delta l.$$

Les calculs donnent

$$\rho = 2464.7059, \quad \Delta \rho = 131.21972, \quad \frac{\Delta \rho}{\rho} = 5.3239506\%, \qquad \text{soit} \quad \rho = 2500 \pm 100, \quad \frac{\Delta \rho}{\rho} = 5.3\%.$$