

# Measurement of the CKM angle $\gamma$ using $B^0_s o D_s K \pi \pi$ decays

P. d'Argent<sup>1</sup>, E. Gersabeck<sup>1</sup>, M. Kecke<sup>1</sup>, M. Schiller<sup>2</sup>

#### Abstract

We present the first measurement of the weak phase  $2\beta + \gamma$  obtained from a time-dependent (amplitude) analysis of  $B_s^0 \to D_s K \pi \pi$  decays using proton-proton collision data corresponding to an integrated luminosity of xxx fb<sup>-1</sup> recorded by the LHCb detector.

<sup>&</sup>lt;sup>1</sup>Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany <sup>2</sup>School of Physics and Astronomy, University of Glasgow, Glasgow, United Kingdom

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# 1 0 To Do List with Assignment of Tasks

```
1. MC Requests (Urgent!):
2
         Run-2 MC
         Phasespace MC for Dalitz Eff
         (need much higher statistics, filtered request? on what?)
         Ds \rightarrow 3pi MC?
         Part. reco. bkg MC?
         With CPV?
      2. Selection:
         Reoptimize with phasespace cuts (e.g. m(K\pi\pi) < 2GeV)
10
      3. Mass fits (Matthieu):
         Improve part. reco. bkg shape
12
         Save fitted yields in latex table \checkmark
13
      4. Use Meerkat PID resampling ✓
14
         (https://twiki.cern.ch/twiki/bin/view/LHCb/MeerkatPIDResampling)
15
      5. Tagging:
16
         Produce new samples with tagging info (Matthieu, Philippe) \checkmark
17
         Calibration
18
      6. Acceptance: (Matthieu)
19
         Compare data and MC \checkmark
20
      7. Resolution: (Matthieu)
21
         Compare Bs \to DsK and Bs \to DsK\pi\pi MC \checkmark
22
         Get LTU Bs \to DsK data sample?
23
      8. TD-MINT: (Philippe)
24
         Resolution integrals \checkmark
25
         per-event tagging
26
         change to MINUIT2
27
         add blinding
28
```

#### 1 Introduction

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The weak phase  $\gamma$  is the least well known angle of the CKM unitary triangle. A key channel to measure  $\gamma$  is the time-dependent analysis of  $B_s^0 \to D_s K$  decays [1], [2].

The  $B_s^0 \to D_s K \pi \pi$  proceeds at tree level via the transitions shown in Fig. 1.1 a) and b).

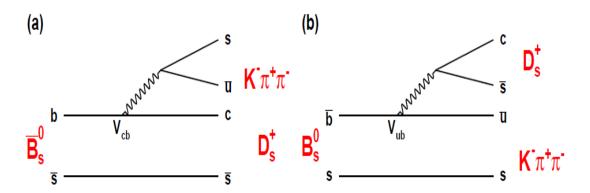


Figure 1.1: Feynman diagram of the  $B_s^0 \to D_s K \pi \pi$  decay, proceeding via a)  $b \to c$  transitions or b)  $b \to u$  transitions.

To measure the weak CKM phase  $\gamma \equiv arg[-(V_{ud}V_{ub}^*)/(V_{cd}V_{cb}^*)]$ , a decay with inter-33 ference between  $b \to c$  and  $b \to u$  transitions at tree level is needed [1]. As illustrated 34 in Fig. 1.1, this is the case for the presented decay mode. A measurement of  $\gamma$  using 35  $B_s^0 \to D_s K \pi \pi$  decays, where the  $K \pi \pi$  subsystem is dominated by excited kaon states such 36 as the  $K_1(1270)$  and  $K_1(1400)$  resonances, will succeed the branching ratio measurement 37 presented in this note. It is complementary to the above mentioned analysis of  $B_s^0 \to D_s K$ , making use of a fully charged final state, where every track is detected in the vertex 39 locator. To account for the non-constant strong phase across the Dalitz plot, one can 40 either develop a time-dependent amplitude model or select a suitable phase-space region 41 and introduce a coherence factor as additional hadronic parameter to the fit. This analysis is based on the first observation of the  $B_s^0 \to D_s K \pi \pi$  decay presented in [3] and [4], where its branching ratio is measured relative to  $B_s^0 \to D_s \pi \pi \pi$ . The result 44 obtained by the previous analysis is  $0.052 \pm 0.005 \, 0.003$ , where the uncertainties are 45 statistical and systematical, respectively. The branching ratio measurement is updated, exploiting the full Run 1 data sample, corresponding to 3 fb<sup>-1</sup> of integrated luminosity.

## <sup>48</sup> 2 Sensitivity studies

#### <sup>49</sup> **2.1 PDF**

First, I define the purely hadronic amplitudes for a given phasespace point x. The weak phase dependence is written latter explicitly in the pdf.

$$A(B_s^0 \to D_s^- K^+ \pi \pi) \equiv A(x) = \sum_i a_i A_i(x)$$
 (2.1)

$$A(B_s^0 \to D_s^+ K^- \pi \pi) \equiv \bar{A}(\bar{x}) = \sum_i \bar{a}_i \,\bar{A}_i(\bar{x})$$
 (2.2)

$$A(\bar{B}_s^0 \to D_s^- K^+ \pi \pi) = \bar{A}(x)$$
 (Assuming no direct CPV) (2.3)

$$A(\bar{B}_s^0 \to D_s^+ K^- \pi \pi) = A(\bar{x})$$
 (Assuming no direct CPV) (2.4)

The full time-dependent amplitude pdf is given by:

$$P(x, t, q_t, q_f) \propto \left[ \left( |A(x)|^2 + |\bar{A}(x)|^2 \right) \cosh \left( \frac{\Delta \Gamma t}{2} \right) + q_t q_f \left( |A(x)|^2 - |\bar{A}(x)|^2 \right) \cos (m_s t) - 2 \operatorname{Re} \left( A(x)^* \bar{A}(x) e^{-iq_f(\gamma - 2\beta_s)} \right) \sinh \left( \frac{\Delta \Gamma t}{2} \right) - 2 q_t q_f \operatorname{Im} \left( A(x)^* \bar{A}(x) e^{-iq_f(\gamma - 2\beta_s)} \right) \sin (m_s t) e^{-\Gamma t}$$

where  $q_t=+1$  (-1)for a  $B_s^0$   $(\bar{B}_s^0)$  tag and  $q_f=+1$  (-1) for  $D_s^-K^+\pi\pi$   $(D_s^+K^-\pi\pi)$  final states.

Integrating over the phasespace, we get

$$\begin{split} \int P(x,t,q_t,q_f) \mathrm{d}x &\propto \left[\cosh\left(\frac{\Delta\Gamma\,t}{2}\right) \\ &+ q_t q_f \left(\frac{1-r^2}{1+r^2}\right) \cos\left(m_s\,t\right) \\ &- 2 \left(\frac{\kappa\,r \cos(\delta - q_f (\gamma - 2\beta_s))}{1+r^2}\right) \sinh\left(\frac{\Delta\Gamma\,t}{2}\right) \\ &- 2 q_t q_f \left(\frac{\kappa\,r \sin(\delta - q_f (\gamma - 2\beta_s))}{1+r^2}\right) \sin\left(m_s\,t\right) \right] e^{-\Gamma t} \\ &= \left[\cosh\left(\frac{\Delta\Gamma\,t}{2}\right) + q_t q_f \,C \cos\left(m_s\,t\right) - \kappa\,D_{q_f} \sinh\left(\frac{\Delta\Gamma\,t}{2}\right) - q_t \,\kappa\,S_{q_f} \sin\left(m_s\,t\right) \right] e^{-\Gamma t} \end{split}$$

where the  $C, D_{q_f}, S_{q_f}$  are defined exactly as for  $D_s K$ . The coherence factor is defined as:

$$\kappa e^{i\delta} \equiv \frac{\int A(x)^* \bar{A}(x) dx}{\sqrt{\int |A(x)|^2 dx} \sqrt{\int |\bar{A}(x)|^2 dx}}$$
(2.5)

$$r \equiv \frac{\sqrt{\int |\bar{A}(x)|^2 dx}}{\sqrt{\int |A(x)|^2 dx}}$$
 (2.6)

and appears in front of the  $D_{q_f}, S_{q_f}$  terms. This means one additional fit parameter for the lifetime fit. In the limit of only one contributing resonance  $\kappa \to 1$ . 59

#### 2.2 Estimation of coherence factor 61

To estimate the coherence factor we could generate many toys with random  $a_i$  and  $\bar{a}_i$ 62 values (see https://twiki.cern.ch/twiki/pub/LHCbPhysics/Bu2DKstar/LHCb-ANA-2017-005\_v1.pdf) using the set of amplitudes show in our last talk. However with so many 64 interfering amplitudes, I would be surprised if you couldn't generate every possible value 65 for  $\kappa$ . In any case, this would give us a range where to expect possible values for  $\kappa$ . Worst 66 case would be  $0 \le \kappa \le 1$ . 67

#### Assumptions:

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$$A(x) = \sum_{i} a_i A_i(x)$$
  
 $\bar{A}(x) = \sum_{i} \bar{a}_i \bar{A}_i(x)$ 

- Use amplitudes from flavor-averaged, time-integrated fit
- Draw random  $a_i$  and  $\bar{a}_i$  values
- Constraints:  $\int (|a_i A_i(x)|^2 + |\bar{a}_i \bar{A}_i(x)|^2) \, dx/N = F_i^{eff}$ 75  $r \approx 0.4$  (ration of CKM elements) 76

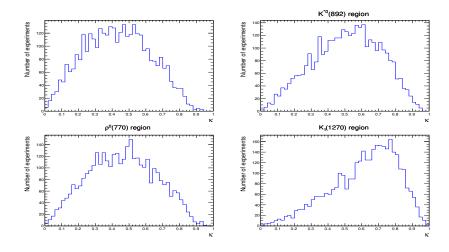


Figure 2.1

Table 2.1

Region	$<\kappa>(\%)$	Cut eff. (%)
Full	43	100
$K^*(892)$	51	43
$\rho^{0}(770)$	46	47
$K_1(1270)$	61	23

#### $_{7}$ 2.3 Results

- 78 Assumptions:
- Use amplitudes from flavor-averaged, time-integrated fit
- r = 0.4 (ratio of CKM elements)
- PDG values for:  $\tau, \Delta m_s, \Delta \Gamma, \beta_s$
- $\epsilon(x,t) = const.$ , perfect resolution
- $\bullet \ \epsilon_{Tag} = 0.66, <\omega> = 0.4$
- $N_{signal} = 3000 \text{ (Run1+15/16 data)}$

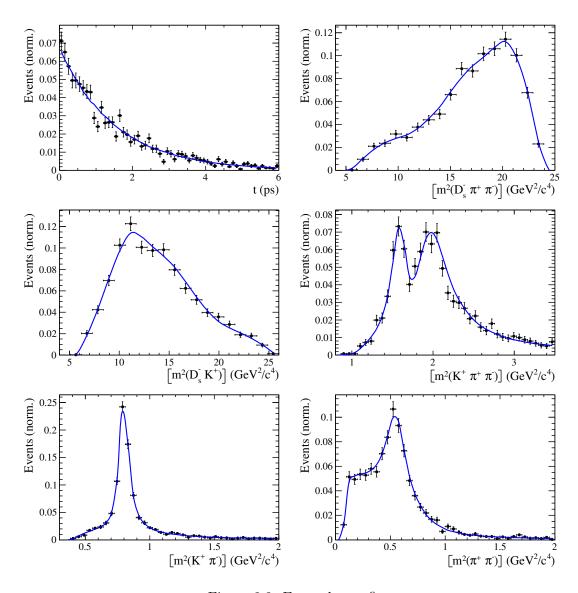


Figure 2.2: Example toy fit

Generated values: 
$$\gamma = 70^{\circ}, \delta = 100^{\circ}$$
 Fit result: 
$$\gamma = 74 \pm 15^{\circ}, \delta = 84 \pm 15^{\circ}$$
 
$$(\gamma = 254 \pm 15^{\circ}, \delta = 264 \pm 15^{\circ})$$

Figure 2.3: Likelihood scan

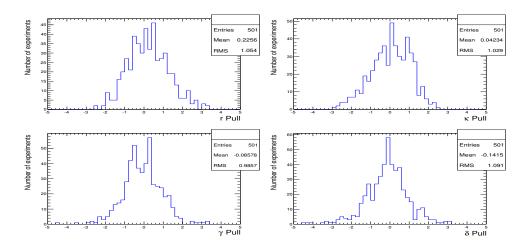


Figure 2.4: Pulls

Table 2.2

	Generated	Full PDF	Phasespace integrated
$\overline{r}$	0.4	$0.38 \pm 0.06$	unstable
$\kappa$	0.2	$0.23 \pm 0.13$	0.2  (fixed)
$\delta$	100	$99 \pm 22$	unstable
$\gamma$	70	$70 \pm 17$	unstable
	Generated	Full PDF	Phasespace integrated
$\overline{r}$	0.4	$0.44 \pm 0.07$	$0.43 \pm 0.11$
$\kappa$	0.4	$0.41 \pm 0.14$	0.4 (fixed)
$\delta$	100	$101 \pm 19$	$95 \pm 41$
$\gamma$	70	$69 \pm 16$	$66 \pm 40$
=			
	Generated	Full PDF	Phasespace integrated
	Generated 0.4	Full PDF $0.41 \pm 0.08$	Phasespace integrated $0.39 \pm 0.11$
$r \kappa$			<u> </u>
	0.4	$0.41 \pm 0.08$	$0.39 \pm 0.11$
$\kappa$	0.4 0.6	$0.41 \pm 0.08$ $0.60 \pm 0.13$	$0.39 \pm 0.11$ 0.6 (fixed)
$\kappa$	0.4 0.6 100	$0.41 \pm 0.08$ $0.60 \pm 0.13$ $98 \pm 17$	$0.39 \pm 0.11$ 0.6 (fixed) $92 \pm 25$
$\kappa$	0.4 0.6 100 70	$0.41 \pm 0.08$ $0.60 \pm 0.13$ $98 \pm 17$ $68 \pm 17$	$0.39 \pm 0.11$ 0.6  (fixed) $92 \pm 25$ $65 \pm 28$
$\begin{array}{c} \kappa \\ \delta \\ \gamma \\ \hline \end{array}$	0.4 0.6 100 70	$0.41 \pm 0.08$ $0.60 \pm 0.13$ $98 \pm 17$ $68 \pm 17$ Full PDF	$0.39 \pm 0.11$ $0.6 \text{ (fixed)}$ $92 \pm 25$ $65 \pm 28$ Phasespace integrated
$ \begin{array}{c} \kappa \\ \delta \\ \gamma \\ \hline  \\ r \end{array} $	0.4 0.6 100 70 Generated 0.4	$0.41 \pm 0.08 \\ 0.60 \pm 0.13 \\ 98 \pm 17 \\ 68 \pm 17$ Full PDF $0.42 \pm 0.09$	$0.39 \pm 0.11$ $0.6 \text{ (fixed)}$ $92 \pm 25$ $65 \pm 28$ Phasespace integrated $0.39 \pm 0.09$

#### 85 3 Selection

For the presented analysis, we reconstruct the  $B_s^0 \to D_s K \pi \pi$  decay through two different 86 final states of the  $D_s$  meson,  $D_s \to KK\pi$  and  $D_s \to \pi\pi\pi$ . Of those two final states 87  $D_s \to KK\pi$  is the most prominent one, while  $\mathcal{BR}(D_s \to \pi\pi\pi) \approx 0.2 \cdot \mathcal{BR}(D_s \to KK\pi)$ holds for the other one. 89 A two-fold approach is used to isolate the  $B_s^0 \to D_s K \pi \pi$  candidates from data passing the stripping line. First, further one-dimensional cuts are applied to reduce the level of 91 combinatorial background and to veto some specific physical background. This stage is 92 specific to the respective final state in which the  $D_s$  meson is reconstructed, since different 93 physical backgrounds, depending on the respective final state, have to be taken into 94 account. After that, a multivariate classifier is trained which combines the information of several input variables, including their correlation, into one powerful discriminator 96 between signal and combinatorial background. For this stage, all possible  $D_s$  final states 97 are treated equally. 98

#### 99 3.1 Cut-based selection

In order to minimize the contribution of combinatorial background to our samples, we apply the following cuts to the b hadron:

• DIRA > 0.99994

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- min IP  $\chi^2 < 20$  to any PV,
- FD  $\chi^2 > 100$  to any PV,
- Vertex  $\chi^2/\text{nDoF} < 8$ ,
- $(Z_{D_s}-Z_{B_s^0})>0$ , where  $Z_M$  is the z-component of the position  $\vec{x}$  of the decay vertex for the  $B_s^0/D_s$  meson.

Additionally, we veto various physical backgrounds, which have either the same final state as our signal decay, or can contribute via a single misidentification of  $K \to \pi$  or  $K \to p$ . In the following, the vetoes are ordered by the reconstructed  $D_s$  final state they apply to:

1. All:

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- (a)  $B_s^0 \to D_s^+ D_s^- : |M(K\pi\pi) m_{D_s}| > 20 \text{ MeV}/c^2$ .
- (b)  $B_s^0 \to D_s^- K^+ K^- \pi^+$ : possible with single missID of  $K^- \to \pi^-$ , rejected by requiring  $\pi^-$  to fulfill  $\mathrm{DLL}_{K\pi} < 5$ .
- 116  $2. D_s \to KK\pi$
- (a)  $B^0 \to D^+(\to K^+\pi^-\pi^+)K\pi\pi$ : possible with single missID of  $\pi^+ \to K^+$ , vetoed by changing particle hypothesis and recompute  $|M(K^+\pi^-\pi^+) m_{Dp}| > 30$  MeV/ $c^2$ , or the  $K^+$  has to fulfill DLL<sub>K $\pi$ </sub> > 10.

- (b)  $\Lambda_b^0 \to \Lambda_c^+(\to pK^-\pi^+)K\pi\pi$ : possible with single missID of  $p \to K^+$ , vetoed by changing particle hypothesis and recompute  $M(pK^-\pi^+) m_{\Lambda_c^+} > 30$  MeV/ $c^2$ , or the  $K^+$  has to fulfill (DLL $_{K\pi}$  DLL $_{p\pi}$ ) > 5.
  - (c)  $D^0 \to KK : D^0$  combined with a random  $\pi$  can fake a  $D_s \to KK\pi$  decay and be a background to our signal, vetoed by requiring  $M(KK) < 1840 \,\text{MeV}/c^2$ .

#### 3. $D_s \to \pi\pi\pi$

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(a)  $D^0 \to \pi\pi$ : combined with a random  $\pi$  can fake a  $D_s \to \pi\pi\pi$  decay and be a background to our signal, vetoed by requiring both possible combinations to have  $M(\pi\pi) < 1700 \,\text{MeV}/c^2$ .

The most prominent final state used in this analysis is  $B_s^0 \to D_s(\to KK\pi)K\pi\pi$ , where the  $D_s$  decay can either proceed via the narrow  $\phi$  resonance, the broader  $K^{*0}$  resonance, or non resonant. Depending on the decay process being resonant or not, we apply additional PID requirements on this final state:

- resonant case:
- $D_s^+ \to \phi \pi^+$ , with  $|M(K^+K^-) m_{\phi}| < 20$  MeV/ $c^2$ : no additional requirements, since  $\phi$  is narrow and almost pure  $K^+K^-$ .
  - $-D_s^+ \to \overline{K}^{*0}K^+$ , with  $|M(K^-\pi^+) m_{K^{*0}}| < 75 \text{ MeV}/c^2$ : DLL<sub>K\pi</sub> > 0 for kaons, since this resonance is more than ten times broader than  $\phi$ .
- non resonant case:  $DLL_{K\pi} > 5$  for kaons, since the non resonant category has significant charmless contributions.

For the  $D_s \to \pi\pi\pi$  final state, we apply global PID requirements:

- DLL $_{K\pi}$  < 10 for all pions.
- DLL<sub> $p\pi$ </sub> < 10 for all pions.

#### 3.2 Multivariate stage

We use TMVA [5] to train a multivariate discriminator, which is used to further improve the signal to background ratio. The 17 variables used for the training are:

- max(ghostProb) over all tracks
- cone $(p_{\rm T})$  asymmetry of every track, which is defined to be the difference between the  $p_{\rm T}$  of the  $\pi/K$  and the sum of all other  $p_{\rm T}$  in a cone of radius  $r = \sqrt{(\Delta\Phi)^2 + (\Delta\eta)^2}$  < 1 rad around the signal  $\pi/K$  track.
  - $\min(\mathrm{IP}\chi^2)$  over the  $X_s$  daughters
- $\max(\text{DOCA})$  over all pairs of  $X_s$  daughters
  - $\min(\mathrm{IP}\chi^2)$  over the  $D_s$  daughters

•  $D_s$  and  $B_s^0$  DIRA

- $D_s$  FD significance
- $\max(\cos(D_s h_i))$ , where  $\cos(D_s h_i)$  is the cosine of the angle between the  $D_s$  and another track i in the plane transverse to the beam
- $B_s^0$  IP $\chi^2$ , FD $\chi^2$  and Vertex  $\chi^2$

Various classifiers were investigated in order to select the best performing discriminator. Consequently, a boosted decision tree with gradient boost (BDTG) is chosen as nominal classifier. We use truth-matched MC as signal input. Simulated signal candidates are required to pass the same trigger, stripping and preselection requirements, that were used to select the data samples. For the background we use events from the high mass sideband  $(m_{B_s^0 candidate} > 5600 \text{ MeV}/c^2)$  of our data samples. As shown in Fig. 3.1, this mass region is sufficiently far away from signal structures and is expected to be dominantly composed of combinatorial background.

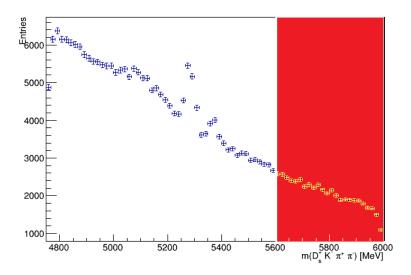


Figure 3.1: Invariant mass distribution of preselected  $B_s^0 \to D_s K \pi \pi$  candidates. The red coloured region with  $m_{B_s^0 candidate} > 5600$  MeV/ $c^2$  is used as background input for the boosted decision tree.

The distributions of the input variables for signal and background are shown in Fig. 3.2.

The relative importance of the input variables for the BDTG training is summarized in Table 3.1.

The BDTG output distribution for test and training samples is shown in Fig 3.3. No sign of overtraining is observed.

We determine the optimal cut value by maximizing the figure of merit  $S/\sqrt{S+B}$  where S is the signal yield and B the background yield in the signal region, defined to be within  $\pm 50~{\rm MeV}/c^2$  of the nominal  $B_s^0$  mass. To avoid a bias in the determination of the branching fraction, we determine S and B using our normalization channel. All trigger,

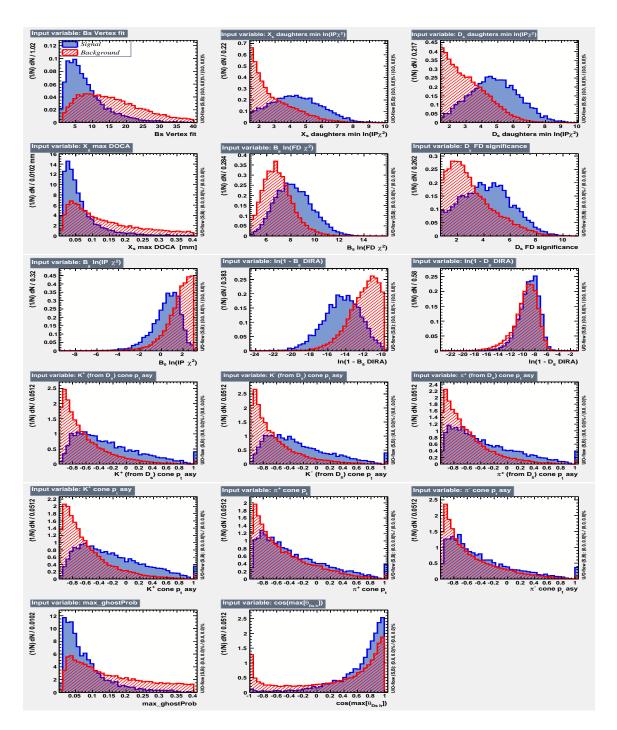


Figure 3.2: Distributions of the input variables used in the BDTG training. The background is shown as red hatched, while the signal is depicted solid blue.

stripping and additional selection criteria described in this and the previous chapter are applied to the  $B_s^0 \to D_s \pi \pi \pi$  data samples. After that, we perform a simplified version of the fit to the invariant mass distribution of  $B_s^0 \to D_s \pi \pi \pi$  candidates described in Sec. ??. Here, a Gaussian function to model the signal and an exponential function to model combinatorial background is used. From this fit we estimate the number of signal events in our normalization channel. Multiplying that number with the PDG branching fraction

Variable	relative importance $[\%]$
pi_minus_ptasy_1.00	7.32
$\log_{-}$ Ds_FDCHI2_ORIVX	7.23
$K_{plus_ptasy_1.00}$	7.17
$\log_{-}$ Ds_DIRA	6.96
$Bs\_ENDVERTEX\_CHI2$	6.82
$\max\_ghostProb$	6.76
$pi_plus_ptasy_1.00$	6.57
log_DsDaughters_min_IPCHI2	6.21
$\log_{-}Bs_{-}DIRA$	6.15
$K_{plus\_fromDs\_ptasy\_1.00}$	6.10
log_XsDaughters_min_IPCHI2	5.87
$K_{minus\_fromDs\_ptasy\_1.00}$	5.62
$\cos(\mathrm{Ds}\;\mathrm{h})$	5.58
$\log_{-}Bs_{-}IPCHI2_{-}OWNPV$	5.08
$\log_{\mathrm{Bs\_FDCHI2\_OWNPV}}$	4.04
$Xs_max_DOCA$	3.98
$pi\_minus\_fromDs\_ptasy\_1.00$	2.59

Table 3.1: Summary of the relative importance of each variable in the training of the BDTG.

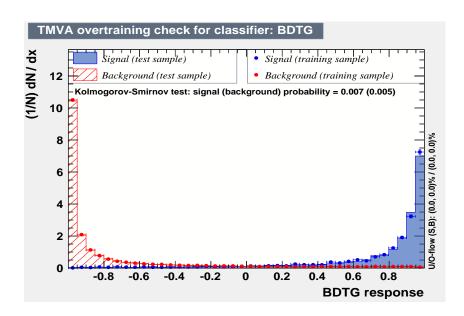


Figure 3.3: BDTG output classifier distribution for (blue) signal and (red) background. The response of an independent test sample (dots) is overlaid.

of  $\frac{\mathcal{B}(B_s^0\to D_sK\pi\pi)}{\mathcal{B}(B_s^0\to D_s\pi\pi\pi)}$  and the ratio of efficiencies discussed in Sec. ?? allows us to estimate the expected number of  $B_s^0\to D_sK\pi\pi$  signal decays. The number of background events can then be computed as

$$N_{bkg} = N_{all} - N_{sig}|_{m_{B_s^0 \pm 50 \,\text{MeV}/c^2}}.$$
(3.1)

The efficiency curves as a function of the cut value are shown in Fig. 3.4. The optimal cut value is found to be BDTG > 0.7012. At this working point the signal efficiency is estimated to be 72.47 %, while the background rejection in the signal region is 97.38 %.

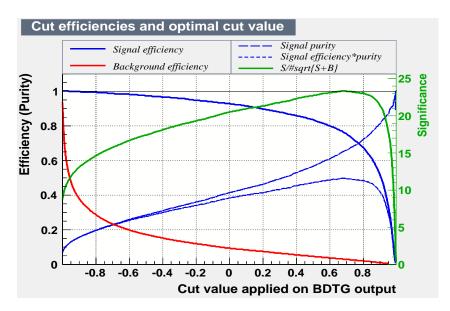
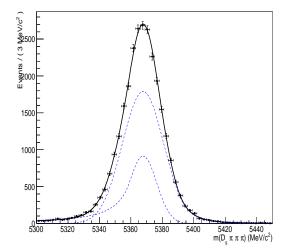


Figure 3.4: Efficiency and purity curves for (blue) signal, (red) background and the (green) FoM curve, as a function of the chosen cut value.

# Fits to invariant mass distributions of signal and normalization channel

In order to properly model the invariant mass distribution of  $B_s^0 \to D_s K \pi \pi$  and  $B_s^0 \to D_s \pi \pi \pi$  candidates, the expected signal shape, as well as the expected shape for the combinatorial and physical background has to be known. This model can then be used to fit the distributions and obtain signal sWeights [6], which are employed to suppress the residual background that is still left in the sample, for the time-dependent amplitude fit.

#### 196 4.1 Signal models for $m(D_s\pi\pi\pi)$ and $m(D_sK\pi\pi)$



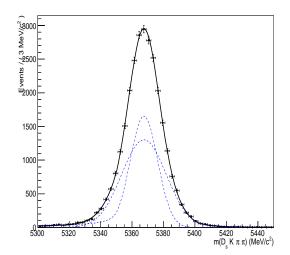


Figure 4.1: Invariant mass distributions of simulated (left)  $B_s^0 \to D_s \pi \pi \pi$  and (right)  $B_s^0 \to D_s K \pi \pi$  events. A fit of the sum of two Crystal Ball functions to each distribution is overlaid. The dotted lines represent the individual Crystal Ball functions.

The mass distribution of  $B_s^0 \to D_s K\pi\pi$  signals is modeled using two Crystal Ball functions, which share the same mean  $\mu$ , but are allowed to have different widths  $\sigma_1$  and  $\sigma_2$ . Another double Crystal Ball function is used to account for the contribution of the  $B^0 \to D_s K\pi\pi$  decay, which is also present in the  $m(D_s K\pi\pi)$  spectrum. The core width, as well as the tail parameters and the ratio of the two individual Crsystal Ball functions are fixed to values obtained by a fit to the invariant mass distribution of simulated events shown in Fig 4.1. The second width  $\sigma_2$  and the shared mean  $\mu$  are floated in the fit to account for possible differences between the simulation and real data. The same approach is used to describe the invariant mass distribution of  $B_s^0 \to D_s \pi\pi\pi$  candidates. A double Crystal Ball function is used to model the signal, the parameters are determined by a fit to the invariant mass of simulated  $B_s^0 \to D_s \pi\pi\pi$  decays, shown in Fig 4.1. The second width and the shared mean are floated to account for differences between data and MC.

#### 4.2 Background models for $m(D_s\pi\pi\pi)$

Different background sources arise in the invariant mass spectrum of candidates in the normalization mode.

213 The following backgrounds have to be accounted for:

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- Combinatorial background: This contribution arises from either a real  $D_s$ , which is paired with random tracks to form the  $B_s^0$  candidates, or via real  $X_d$ 's, which are combined with three tracks that fake a  $D_s$  candidate to form a fake  $B_s^0$ .
- Partially reconstructed  $B_s^0 \to D_s^* \pi \pi \pi$  decays, with  $D_s^* \to D_s \gamma$  or  $D_s^* \to D_s \pi^0$ , where the  $\gamma/\pi^0$  is not reconstructed in the decay chain.

In both cases of combinatorial background, the distribution in the invariant mass of  $B_s^0$  candidates is expected to be smooth and decrease with higher masses. Therefore, one exponential function is used to model these contributions.

The shape of the  $B_s^0 \to D_s^* \pi \pi \pi$  contribution is expected to be peaking in the  $m(D_s \pi \pi \pi)$ 

The shape of the  $B_s^0 \to D_s^*\pi\pi\pi$  contribution is expected to be peaking in the  $m(D_s\pi\pi\pi)$  spectrum, with large tails due to the missing momentum, which is carried away by the  $\pi^0$  or  $\gamma$ . The pion or photon from  $D_s^* \to D_s(\gamma/\pi^0)$  is excluded from the reconstruction. We model the shape of this contribution using the sum of three bifurcated Gaussian functions. The shape parameters, as well as the yield of this contribution, are directly determined on data from a fit to the  $m(D_s\pi\pi\pi)$  invariant mass distribution.

#### 4.3 Background models for $m(D_s K \pi \pi)$

229 For the signal channel, the following background sources have to be considered:

- Combinatorial background: same contributions as discussed in Sec. 4.2.
- Partially reconstructed  $B_s^0 \to D_s^* K \pi \pi$  decays, with  $D_s^* \to D_s \gamma$  or  $D_s^* \to D_s \pi^0$ , where the  $\gamma/\pi^0$  is not reconstructed in the decay chain.
  - Partially reconstructed  $B^0 \to D_s^* K \pi \pi$  decays, with  $D_s^* \to D_s \gamma$  or  $D_s^* \to D_s \pi^0$ , where the  $\gamma/\pi^0$  is not reconstructed in the decay chain.
  - Misidentified  $B_s^0 \to D_s \pi \pi \pi$  decays, where one of the pions is wrongly identified as a kaon  $\pi \to K$ .
  - Misidentified, partially reconstructed  $B_s^0 \to D_s^* \pi \pi \pi$  decays, where one of the pions is wrongly identified as a kaon  $\pi \to K$  and the  $\gamma/\pi^0$  from  $D_s^* \to D_s \gamma/\pi^0$  is not reconstructed.

The combinatorial background is expected to be non-peaking in the spectrum of the invariant mass of  $B_s^0 \to D_s K \pi \pi$  candidates. An exponential function is used to model this contribution.

The shape of the partially reconstructed background without misID is taken from our normalization channel, where it can be directly fitted by the sum of three bifurcated Gaussian functions as described above. In the signal mass fit, all shape parameters for the  $B_s^0 \to D_s^* K \pi \pi$  background are fixed to the input values from our normalization fit.

For the contribution of the  $B^0 \to D_s^* K \pi \pi$  background, the same shape is used but the means  $\mu_i$  of the bifurcated gaussians are shifted down by  $m_{B_s^0} - m_{B^0}$  [?]. The yields of both contributions are directly determined in the nominal fit.

To determine the shape of misidentified  $B_s^0 \to D_s \pi \pi \pi$  candidates in the  $m(D_s K \pi \pi)$  spectrum, we take a truth-matched signal MC sample of our normalization channel. We then use the PIDCalib package to determine the  $\pi \to K$  fake rate. For every candidate in our MC sample, a (momentum) p and (pseudorapidity)  $\eta$ -dependent event weight is computed and assigned. We flip the particle hypothesis from pion to kaon for the  $\pi$  with the biggest miss-ID weight for each event and recompute the invariant  $B_s^0$  mass. This distribution is then modeled using two Crystal Ball functions. The distribution and the fit are shown in Fig. 4.2(left).

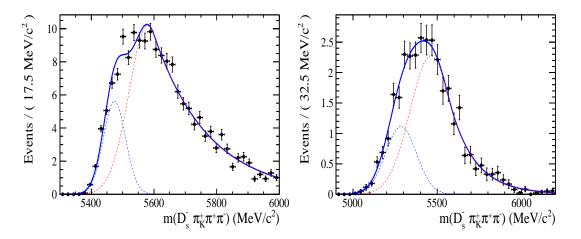


Figure 4.2: Invariant mass distribution of (left) simulated  $B_s^0 \to D_s \pi \pi \pi$  events, where one of the  $\pi$ 's is reconstructed as a K and the misID probability for each event is taken into account. The corresponding distribution for simulated  $B_s^0 \to D_s^* \pi \pi \pi$  events, where the  $\gamma/\pi^0$  from the  $D_s^*$  is excluded from reconstruction, is shown on the right. The solid, black curve on each plot corresponds to the fit consisting of two Crystal Ball functions.

The expected yield of misidentified  $B_s^0 \to D_s \pi \pi \pi$  candidates in the  $m(D_s K \pi \pi)$  spectrum is computed by multiplying the fake probability of  $\propto 3.2\%$ , which is derived from PIDCalib, by the yield of  $B_s^0 \to D_s \pi \pi \pi$  signal candidates, determined in the nominal mass fit of our normalization channel.

In the same way as mentioned above, we can determine the rate of misidentified, partially reconstructed  $B_s^0 \to D_s^*\pi\pi\pi$  decays in our sample of  $B_s^0 \to D_s K\pi\pi$  decays using PIDCalib and a MC sample of  $B_s^0 \to D_s^*\pi\pi\pi$  events. The invariant mass distribution we obtain when we exclude the  $\gamma/\pi^0$ , flip the the particle hypothesis  $\pi \to K$  and apply the event weights given by the fake rate, is shown in Fig. 4.2 (right). The fit of two Crystal Ball functions to this distribution is overlaid. The yield of this contribution is determined from the yield of  $B_s^0 \to D_s^*\pi\pi\pi$  candidates in the nominal mass fit of our normalization channel, multiplied by the misID probability of  $\propto 3.6\%$ .

# 4.4 Fit to $B_s^0 \to D_s \pi \pi \pi$ candidates

An unbinned maximum likelihood fit is performed simultaneously to the invariant mass distribution of  $B_s^0 \to D_s \pi \pi \pi$  candidates. As discussed in Sec. 4.1, the fit is given as the

sum of the double Gaussian signal model, the sum of three bifurcated Gaussian functions to model the partially reconstructed  $B_s^0 \to D_s^*\pi\pi\pi$  background and an Exponential function to account for combinatorial background. The invariant mass distribution and the fit is shown in Fig. 4.3. All simultaneously performed fits to the  $m(D_s\pi\pi\pi)$  distribution, ordered by the respective  $D_s$  final state, can be found in the Appendix A.1. The obtained yields are summarized in Table 4.1.

# <sup>279</sup> 4.5 Fit to $B_s^0 \to D_s K \pi \pi$ candidates

The shape of the invariant mass distribution of  $B_s^0 \to D_s K \pi \pi$  candidates is described by the sum of two double Gaussian functions for the  $B^0$  and  $B_s^0$  signal, two sums of three bifurcated Gaussians for the  $B_s^0/B^0 \to D_s^* K \pi \pi$  partially reconstructed background contributions and two sums of double Crystal Ball functions for the single misID  $B_s^0 \to D_s \pi \pi \pi$  and the partially reconstructed, misidentified  $B_s^0 \to D_s^* \pi \pi \pi$  decays. A simultaneous unbinned maximum likelihood fit is performed and the result is shown in Fig. 4.3. All simultaneously performed fits to the  $m(D_s K \pi \pi)$  distribution, ordered by the respective  $D_s$  final state, can be found in the Appendix A.1. The obtained yields are summarized in Table 4.1.

#### 4.6 Extraction of signal weights

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The sPlot technique [6] is used to extract signal weights from the fits to the invariant mass distributions of our signal and normalization channel. This statistical tool assignes a weight to every event, according to it's position in the respective mass distribution, given the fitted signal and background models. The weights can then be used to suppress the background components in every other observable distribution of interest. Figure 4.4 shows the distribution of weights across the invariant mass spectra of  $B_s^0 \to D_s \pi \pi \pi$  and  $B_s^0 \to D_s K \pi \pi$  candidates.

fit component	yield 2011	yield 2012	yield 2015	yield 2016
$m(D_s K \pi \pi)$				
$B_s^0 \to D_s K \pi \pi$	$426 \pm 57$	$909 \pm 71$	$319 \pm 38$	$2049 \pm 104$
$B^0 \to D_s K \pi \pi$	$345 \pm 58$	$846 \pm 81$	$292 \pm 42$	$1640 \pm 113$
$B^0/B_s^0 \to D_s^* K \pi \pi$	$291 \pm 3215$	$911 \pm 265$	$622 \pm 114$	$3617 \pm 416$
$B_s^0 \to D_s^{(*)} \pi \pi \pi$	$118 \pm 0$	$286 \pm 0$	$97 \pm 0$	$580\pm0$
combinatorial	$2240 \pm 427$	$4372 \pm 330$	$922 \pm 144$	$6723 \pm 499$
$m(D_s\pi\pi\pi)$				
$B_s^0 \to D_s \pi \pi \pi$	$9554 \pm 204$	$22940 \pm 316$	$7839 \pm 185$	$45186 \pm 452$
$B_s^0 \to D_s^* \pi \pi \pi$	$11481 \pm 411$	$27788 \pm 714$	$9670 \pm 380$	$56903 \pm 1372$
combinatorial	$7748 \pm 430$	$17558\pm747$	$6494 \pm 397$	$42523 \pm 1455$

Table 4.1: Summary of yields obtained from the fits to Run1 and Run2 data.

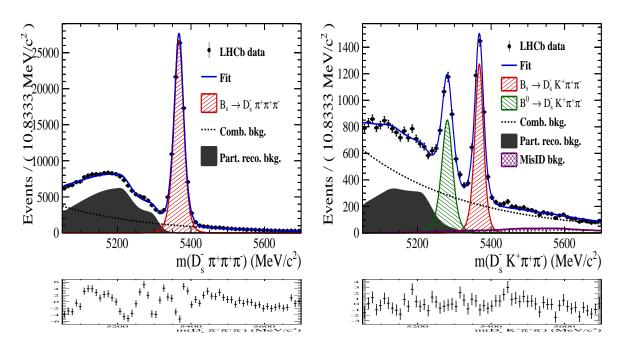


Figure 4.3: Invariant mass distribution of (left)  $B_s^0 \to D_s \pi \pi \pi$  and (right)  $B_s^0 \to D_s K \pi \pi$  candidates for Run1 and Run2 data. The respective fit described in the text is overlaid.

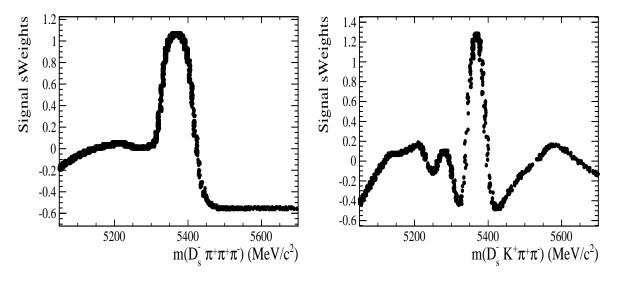


Figure 4.4: Distribution of sWeights across the invariant mass of (left)  $B_s^0 \to D_s \pi \pi \pi$  and (right)  $B_s^0 \to D_s K \pi \pi$  candidates for Run1 and Run2 data.

# 5 Decay-time Acceptance

The decay-time distribution of the  $B_s^0$  mesons is sculpted due to the geometry of the LHCb detector and the applied selection cuts, which are described in Section 3. In particular, any requirement on the flight distance (FD), the impact parameter (IP) or the direction angle (DIRA) of the  $B_s^0$  mesons, as well as the direct cut on the lifetime, will lead to a decay-time dependent efficiency a(t). This efficiency will distort the theoretically expected, time-dependent decay rate

$$\frac{\Gamma(t)^{observed}}{dt} = \frac{\Gamma(t)^{theory}}{dt} \cdot a(t), \tag{5.1}$$

and has to be modelled correctly, in order to describe the observed decay rate. We use our control channel for this measurement, because for  $B_s^0 \to D_s K \pi \pi$  decays the decay-time acceptance is correlated with the CP-observables which we aim to measure. Therefore, floating the CP-observables and the acceptance shape at the same time is not possible. Hence, a fit to the decay-time distribution of  $B_s^0 \to D_s \pi \pi \pi$  candidates is performed and the obtained acceptance shape is corrected by the difference in shape found for the  $B_s^0 \to D_s K \pi \pi$  and  $B_s^0 \to D_s \pi \pi \pi$  MC.

is fit to the decay time distribution of  $B_s^0 \to D_s \pi \pi \pi$  candidates in data. Since the

A PDF of the form

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$$\mathcal{P}(t', \vec{\lambda}) = \left[ (e^{\Gamma_s t} \cdot cosh(\frac{\Delta \Gamma_s t}{2}) \times \mathcal{R}(t - t') \right] \cdot \epsilon(t', \vec{\lambda}), \tag{5.2}$$

fit is performed untagged, the PDF shown in Eq. 5.2 contains no terms proportional to 312  $\Delta m_s$ . The values for  $\Gamma_s$  and  $\Delta \Gamma_s$  are fixed to the latest HFAG results [7]. The decaytime acceptance  $\epsilon(t', \vec{\lambda})$  is modelled using the sum of cubic polynomials  $v_i(t)$ , so called 314 Splines [8]. The polynomials are parametrised by so-called knots which determine their 315 boundaries. Knots can be set across the fitted distribution to account for local changes in 316 the acceptance shape. Using more knots is equivalent to using more base splines which are defined on a smaller sub-range. In total, n+2 base splines  $v_i(t)$  are needed to describe 318 an acceptance shape which is parametrised using n knots. 319 fits shown in the following, the knots have been placed at t320 [0.5, 1.0, 1.5, 2.0, 3.0, 9.5]ps. To accommodate these 6 knot positions, 8 basic splines  $v_i$ , 321 i = [1, ..., 8] are used. Since a rapid change of the decay time acceptance at low decay 322 times due to the turn-on effect generated by the lifetime and other selection cuts is 323 expected, more knots are placed in that regime. At higher decay times we expect linear behaviour, with a possible small effect due to the VELO reconstruction. Therefore fewer 325 knots are used. Furthermore,  $v_7$  is fixed to 1 in order to normalize the overall acceptance 326 function. To stabilise the last spline,  $v_8$  is fixed by a linear extrapolation from the two 327 previous splines:

$$v_N = v_{N-1} + \frac{v_{N-2} - v_{N-1}}{t_{N-2} - t_{N-1}} \cdot (t_N - t_{N-1}). \tag{5.3}$$

Here, N=8 and  $t_{N-1}$  corresponds to the knot position associated with  $v_{N-1}$ . The nominal fit to  $B_s^0 \to D_s \pi \pi \pi$  data using this configuration is shown in Figure 5.1. Note that the normalization of the splines in the following figures is not in scale.

The fits to  $B_s^0 \to D_s \pi \pi \pi$  and  $B_s^0 \to D_s K \pi \pi$  simulation are shown in Figure 5.2.

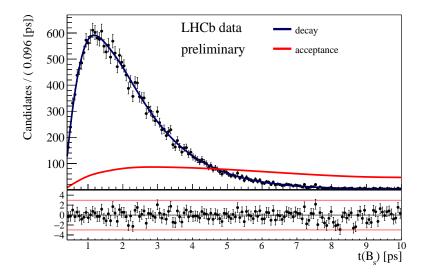


Figure 5.1: Decay-time distribution of  $B_s^0 \to D_s \pi \pi \pi$  candidates for the Run 1 data sample. The fit described in the text is overlaid. The red line shows the spline function describing the acceptance and the blue line depicts the total fit function.

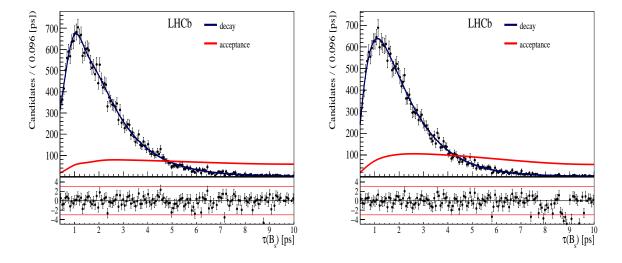


Figure 5.2: Decay-time distribution of (left)  $B_s^0 \to D_s \pi \pi \pi$  and (right)  $B_s^0 \to D_s K \pi \pi$  candidates in MC using truth information. The fit described in the text is overlaid. The red line shows the spline function describing the acceptance and the blue line depicts the total fit function.

The fit parameters obtained from the described fits to data and simulation are summarised in Table 5.1.

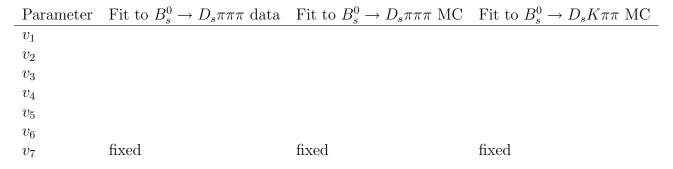


Table 5.1: Summary of the obtained parameters from the acceptance fits described above.

## 6 Decay-time Resoution

The observed oscillation of B mesons is prone to dilution, if the detector resolution is of similar magnitude as the oscillation period. In the  $B_s^0$  system, considering that the measured oscillation frequency of the  $B_s^0$  [9] and the average LHCb detector resolution [10] are both  $\mathcal{O}(50\,\mathrm{fs}^{-1})$ , this is the case. Therefore, it is crucial to correctly describe the decay time resolution in order to avoid a bias on the measurement of time dependent CP parameters.

In the presented analysis, we assume a gaussian resolution function with different widths for each event. This gives rise to a per-event decay time error  $\sigma_t$ , which is computed separately for every event along with the proper time t, by the decay time fitter. Furthermore, the per-event decay time error  $\sigma_t$  is usually underestimated by the decay time fitter, making it necessary to derive a scaling function, which matches the per-event error to the actually measured decay time resolution.

Due to the lack of a decay time unbiased sample of real  $B_s^0 \to D_s K \pi \pi$  decays, this analysis relies on simulation to describe the time resolution. The obtained results will be compared to those found in the closely related  $B_s^0 \to D_s K$  analysis and systematic uncertainties will be assigned conservatively. In the following, we investigate the Run1 and Run2 MC samples to find the proper decay time resolution in bins of the per-event decay time error and derive a scaling function from that.

#### 355 6.1 Formalism

For simulated  $B_s^0 \to D_s K \pi \pi$  events, the information on the true  $B_s^0$  lifetime  $\tau_{true}$  assigned at production of the event, as well as the measured decay time  $\tau_{measured}$ , which is determined after the interaction with the LHCb detector, is stored. In this analysis, the difference  $\Delta t = \tau_{true} - \tau_{measured}$  is obtained for each simulated  $B_s^0 \to D_s K \pi \pi$  candidate. The width of the distribution of  $\Delta t$  is a direct measure of the decay time resolution. To analyse the relation between the per-event decay time error  $\sigma_t$  and the actual resolution, the simulated sample is split into 8 bins of  $\sigma_t$ . A fit is then performed to the distribution of  $\Delta t$  in each bin to determine the decay time resolution in that bin. After that, the correlation between the binned per-event decay time error and the measured decay time resolution is analyzed to determine the scaling function. 

## 6.2 Fits to the decay time distributions

The sum of two Gaussian functions is used to fit the distributions of the decay time difference  $\Delta t$  in each  $\sigma_t$  bin. One Gaussian function is relatively narrow and describes the decay time of the majority of candidates in each bin, while the other, broader Gaussian function describes candidates where the measure decay time differs considerably from  $\tau_{true}$ . Those contributions are shifted to the tails of the distribution. From the two Gaussian functions, the combined, effective width  $\sigma_{eff}$  is quoted as decay time resolution in each bin. Figure 6.1 shows the double Gaussian fit to the distribution of the decay time difference for events where 24 ps  $< \sigma_t < 29$  ps. All fits are shown in the Appendix xxY.

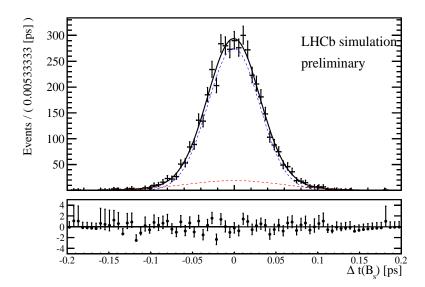


Figure 6.1: Difference of the true and measured decay time of  $B_s^0 \to D_s K \pi \pi$  candidates from MC in the bin 24 ps  $< \sigma_t <$  29 ps. A fit of the sum of two Gaussian functions is overlaid.

For the combination of the two separate widths  $\sigma_1$  and  $\sigma_2$ , a method which takes the damping effect of the finite time resolution on the CP observables into account, is used. The effective damping of the CP amplitudes is described by the dilution  $\mathcal{D}$ , which can take values between 1 and 0. In the case of infinite precision, there would be no damping and therefore  $\mathcal{D} = 1$  would hold, while for a resolution that is much larger than the  $B_s^0$  oscillation frequency,  $\mathcal{D}$  would approach 0. For two Gaussians describing the resolution, the dilution can be defined as [REF TO  $B_s^0 \to D_s K$  HERE]

$$\mathcal{D} = f_1 e^{-\sigma_1^2 \Delta m_s^2/2} + (1 - f_1) e^{-\sigma_2^2 \Delta m_s^2/2}, \tag{6.1}$$

where  $f_1$  is the fraction of events described by the first Gaussian relative to the second and  $\Delta m_s$  is the oscillation period of the  $B_s^0$  meson.

The dilution is computed in every bin of the per-event decay time error and can be converted into the effective resolution

$$\sigma_{eff} = \sqrt{(-2/\Delta m_s^2) \ln \mathcal{D}}.$$
 (6.2)

#### 6.3 Results

The fitted values for the Gaussian widths  $\sigma_1$  and  $\sigma_2$ , the fraction of the first relative to the second Gaussian function  $f_1$ , as well as the effective resolution  $\sigma_{eff}$ , found in each bin  $\sigma_t$ , are shown in Tab. 6.1. Figure 6.2 shows the obtained values for  $\sigma_{eff}$  as a function of the per-event decay time error  $\sigma_t$ . A linear polynom of the form

$$\sigma(\sigma_t)_{mc} = s_0 + s_1 \cdot \sigma_t \tag{6.3}$$

is used to parametrise this distribution. The obtained values are

$$\sigma(\sigma_t)_{mc} = (xx.xxx \pm yy.yyy) + (z.zzz \pm a.aaa)\sigma_t. \tag{6.4}$$

For comparison, the linear scaling functions found for  $\sigma(\sigma_t)$  in the  $B_s^0 \to D_s K$  analysis [REF HERE] for data and MC are also shown in Figure 6.2. We introduce a correction factor to account for possible differences between the decay time resolution found in simulation and data. Motivated by the similarity between the  $B_s^0 \to D_s K \pi \pi$  and  $B_s^0 \to D_s K$  decay, we assume

$$\frac{\sigma(t)_{D_sK\pi\pi,data}}{\sigma(t)_{D_sK\pi\pi,mc}} \approx \frac{\sigma(t)_{D_sK,data}}{\sigma(t)_{D_sK,mc}}.$$
(6.5)

This leads to a correction factor

$$\sigma(t)_{D_sK\pi\pi,data} \approx \frac{\sigma(t)_{D_sK,data}}{\sigma(t)_{D_sK,mc}} \cdot \sigma(t)_{D_sK\pi\pi,mc}, \tag{6.6}$$

where all elements of the right side of the equation are known.

Taking the scaling function found in our simulation, as well as input from the  $B_s^0 \to D_s K$  analysis for  $\sigma(t)_{D_s K, mc/data}$ , we find

$$\sigma(t)_{D_sK\pi\pi,data} = xXx \pm yYy$$

which is the scaling factor used for the per-event decay time error in the nominal timeand amplitude-dependent fit.

$\sigma_t \text{ Bin [fs]}$	$\sigma_1$ [fs]	$\sigma_2$ [fs]	$f_1$	D	$\sigma_{eff}$ [fs]
0to19	$22.57 \pm 0.96$	$45.57 \pm 4.061$	$0.827 \pm 0.057$	$0.89 \pm 0.067$	$27.46 \pm 8.82$
19to24	$24.64 \pm 1.03$	$46.65 \pm 3.109$	$0.768 \pm 0.061$	$0.86 \pm 0.070$	$30.64 \pm 8.48$
24to29	$30.96 \pm 0.90$	$58.76 \pm 5.684$	$0.884 \pm 0.045$	$0.83 \pm 0.05$	$34.66 \pm 5.28$
29to34	$35.28 \pm 1.54$	$57 \pm 6.698$	$0.839 \pm 0.098$	$0.79 \pm 0.10$	$39.09 \pm 10.47$
34 to 39	$37.05 \pm 2.36$	$61.98 \pm 5.769$	$0.707 \pm 0.12$	$0.73 \pm 0.12$	$44.76 \pm 11.78$
39 to 44	$68.38 \pm 8.33$	$42.15 \pm 3.583$	$0.331 \pm 0.18$	$0.66 \pm 0.16$	$50.98 \pm 15.11$
44to49	$199.9 \pm 100.1$	$53.72 \pm 1.419$	$0.020 \pm 0.014$	$0.62 \pm 0.02$	$54.89 \pm 1.60$
49to150	$68.75 \pm 165.3$	$68.92 \pm 4.603$	$0.001 \pm 0.97$	$0.47 \pm 0.65$	$68.92 \pm 63.42$

Table 6.1: Summary of the obtained parameters from the resolution fits described above.

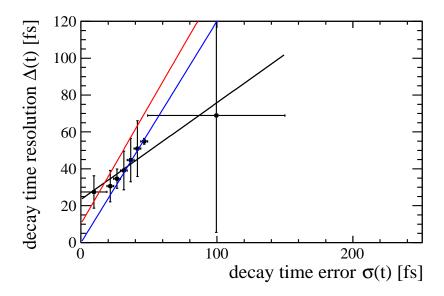


Figure 6.2: Decay-time resolution of  $B_s^0 \to D_s K \pi \pi$  candidates from MC. The scaling functions found in for  $B_s^0 \to D_s K$  (red) data and (blue) MC is also shown for comparison. The fit described in the text is overlaid.

# 406 A Appendix

#### of A.1 Detailed mass fits

In this section, all fits to the mass distribution of  $B_s^0 \to D_s \pi \pi \pi$  and  $B_s^0 \to D_s K \pi \pi$  candidates are shown. The fits are performed simultaneously for every year of datataking (2011, 2012, 2015 and 2016) and the  $D_s$  decay ( $D_s \to KK\pi$  non-resonant,  $D_s \to \phi \pi$ ,  $D_s \to K^*K$ , or  $D_s \to \pi \pi \pi$ ) through which the final state is reached.

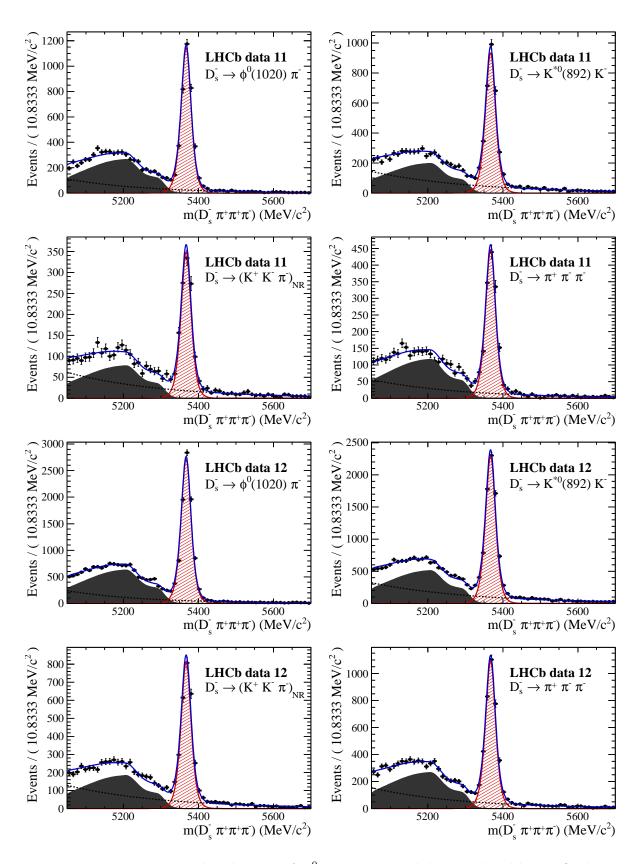


Figure 1.1: Invariant mass distributions of  $B_s^0 \to D_s \pi \pi \pi$  candidates, ordered by  $D_s$  final state, for Run1 data. The fit described in 4.4 is overlaid.

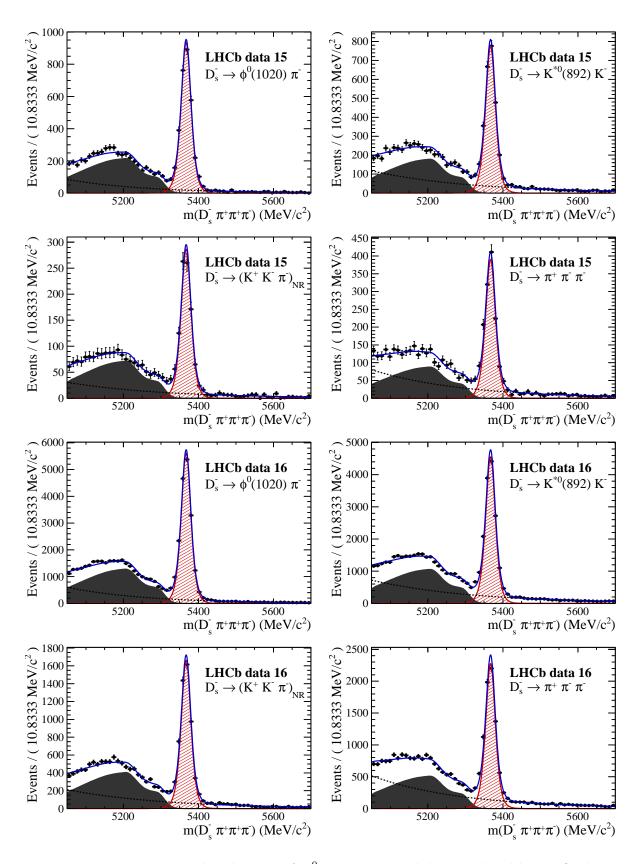


Figure 1.2: Invariant mass distributions of  $B_s^0 \to D_s \pi \pi \pi$  candidates, ordered by  $D_s$  final state, for Run2 data. The fit described in 4.4 is overlaid.

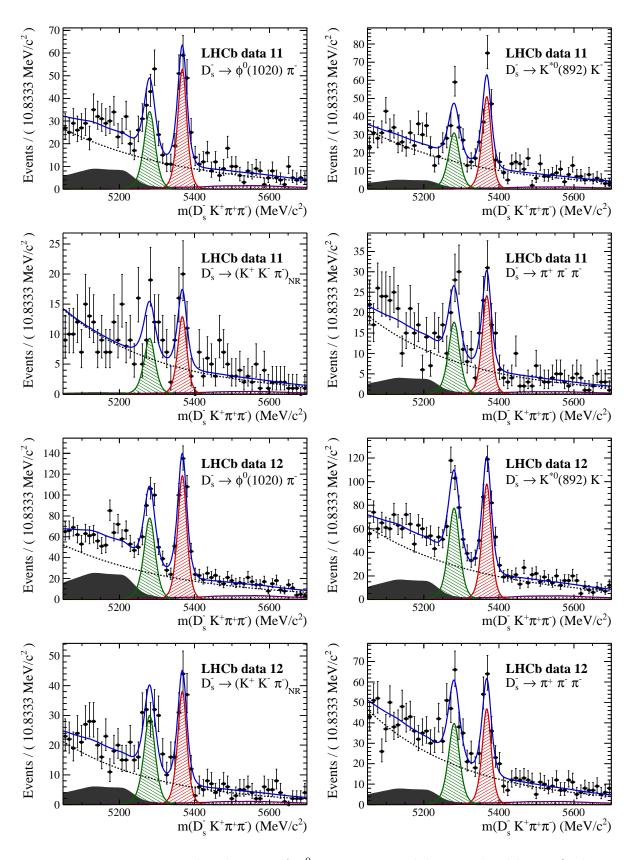


Figure 1.3: Invariant mass distributions of  $B_s^0 \to D_s K \pi \pi$  candidates, ordered by  $D_s$  final state, for Run1 data. The fit described in 4.5 is overlaid.

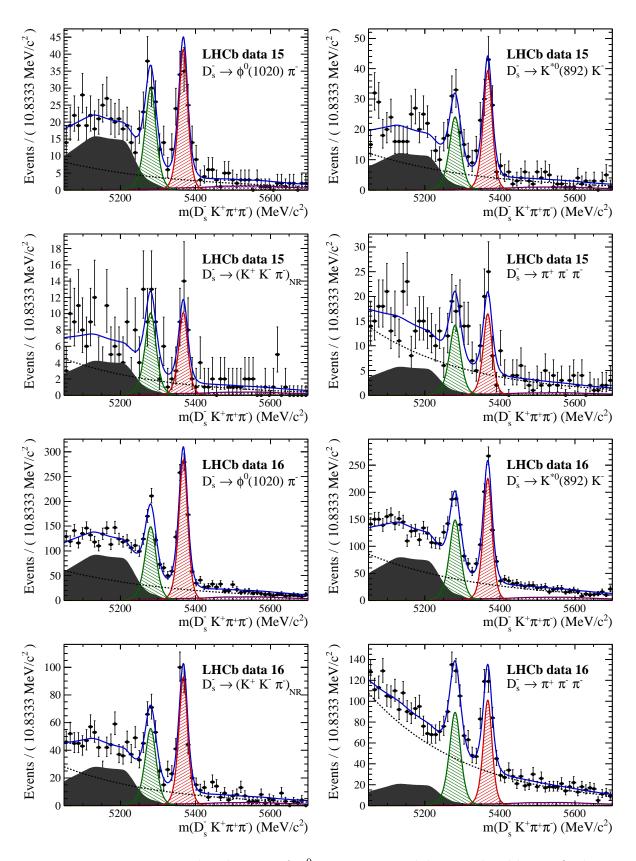


Figure 1.4: Invariant mass distributions of  $B_s^0 \to D_s K \pi \pi$  candidates, ordered by  $D_s$  final state, for Ru2 data. The fit described in 4.5 is overlaid.

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