

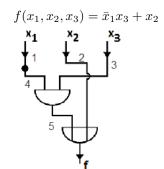
## **Technische Informatik: Abgabe 6**

Michael Mardaus

Andrey Tyukin

4. Dezember 2013

## Exercise 6.1 (Circuit jam)



| $f_1,\ldots,f_5$ are 0-jams                              | $f_6,\ldots,f_a$ are 1-jams.                             |
|----------------------------------------------------------|----------------------------------------------------------|
| $f_1(x_1, x_2, x_3) = \bar{0}x_3 + x_2 = x_3 + x_2$      | $f_6(x_1, x_2, x_3) = \bar{1}x_3 + x_2 = x_2$            |
| $f_2(x_1, x_2, x_3) = \bar{x}_1 x_3 + 0 = \bar{x}_1 x_3$ | $f_7(x_1, x_2, x_3) = \bar{x}_1 x_3 + 1 = 1$             |
| $f_3(x_1, x_2, x_3) = \bar{x}_1 0 + x_2 = x_2$           | $f_8(x_1, x_2, x_3) = \bar{x}_1 + x_2 = \bar{x}_1 + x_2$ |
| $f_4(x_1, x_2, x_3) = 0x_3 + x_2 = x_2$                  | $f_9(x_1, x_2, x_3) = 1x_3 + x_2 = x_3 + x_2$            |
| $f_5(x_1, x_2, x_3) = 0 + x_2 = x_2$                     | $f_a(x_1, x_2, x_3) = 1 + x_2 = 1$                       |

|               | # | $x_1$ | $x_2$ | $x_3$ | $f_1$ | $f_2$ | $f_3$ | $f_4$ | $f_5$ | $f_6$ | $f_7$ | $f_8$ | $f_9$ | $f_a$ | f |  |
|---------------|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|--|
|               | 0 | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 1     | 1     | 0     | 1     | 0 |  |
|               | 1 | 0     | 0     | 1     | 1     | 1     | 0     | 0     | 0     | 0     | 1     | 1     | 1     | 1     | 1 |  |
|               | 2 | 0     | 1     | 0     | 1     | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1 |  |
| Ausfalltafel: | 3 | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1 |  |
|               | 4 | 1     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 1     | 0     | 0     | 1     | 0 |  |
|               | 5 | 1     | 0     | 1     | 1     | 0     | 0     | 0     | 0     | 0     | 1     | 0     | 1     | 1     | 0 |  |
|               | 6 | 1     | 1     | 0     | 1     | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1 |  |
|               | 7 | 1     | 1     | 1     | 1     | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1 |  |

 $\implies f_1 = f_9; f_2; f_3 = f_4 = f_5 = f_6; f_7 = f_a; f_8$ 

|                | #             | $x_1$ | $x_2$ | $x_3$ | $f_1$ | $f_2$ | $f_3$ | $f_7$ | $f_8$ | f |
|----------------|---------------|-------|-------|-------|-------|-------|-------|-------|-------|---|
|                | 0             | 0     | 0     | 0     | 0     | 0     | 0     | 1     | 1     | 0 |
|                | 1             | 0     | 0     | 1     | 1     | 1     | 0     | 1     | 1     | 1 |
|                | 2             | 0     | 1     | 0     | 1     | 0     | 1     | 1     | 1     | 1 |
| Ausfallmatrix: | 3             | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1 |
|                | $\mid 4 \mid$ | 1     | 0     | 0     | 0     | 0     | 0     | 1     | 0     | 0 |
|                | 5             | 1     | 0     | 1     | 1     | 0     | 0     | 1     | 0     | 0 |
|                | 6             | 1     | 1     | 0     | 1     | 0     | 1     | 1     | 1     | 1 |
|                | 7             | 1     | 1     | 1     | 1     | 0     | 1     | 1     | 1     | 1 |
|                |               | -     | -     | -     | -     |       | -     | -     | -     | - |

Fehlermatrix:

|    | # | $x_1$ | $x_2$ | $x_3$ | $f \nleftrightarrow f_1$ | $f \nleftrightarrow f_2$ | $f \nleftrightarrow f_3$ | $f \nleftrightarrow f_7$ | $f \nleftrightarrow f_8$ | Test |
|----|---|-------|-------|-------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|------|
| ĺ  | 0 | 0     | 0     | 0     | 0                        | 0                        | 0                        | 1                        | 1                        | *    |
|    | 1 | 0     | 0     | 1     | 0                        | 0                        | 1                        | 0                        | 0                        | *    |
|    | 2 | 0     | 1     | 0     | 0                        | 1                        | 0                        | 0                        | 0                        | *    |
| ζ: | 3 | 0     | 1     | 1     | 0                        | 0                        | 0                        | 0                        | 0                        |      |
|    | 4 | 1     | 0     | 0     | 0                        | 0                        | 0                        | 1                        | 0                        |      |
|    | 5 | 1     | 0     | 1     | 1                        | 0                        | 0                        | 1                        | 0                        | *    |
|    | 6 | 1     | 1     | 0     | 0                        | 1                        | 0                        | 0                        | 0                        |      |
|    | 7 | 1     | 1     | 1     | 0                        | 1                        | 0                        | 0                        | 0                        |      |

 $\implies$  Testvector:  $\{(0,0,0),(0,0,1),(0,1,0),(1,0,1)\}$ 

## **Exercise 5.2 (Row and Column-Rules are not a function)**

todo

## **Exercise 6.3 (Hazards)**

| $x_1 = 1$ |              |    |    |    |  |  |  |  |  |
|-----------|--------------|----|----|----|--|--|--|--|--|
|           | $x_{4}x_{5}$ |    |    |    |  |  |  |  |  |
| $x_2x_3$  | 00           | 01 | 11 | 10 |  |  |  |  |  |
| 00        |              | 1  |    |    |  |  |  |  |  |
| 01        |              | 1  |    | 1  |  |  |  |  |  |
| 11        | 1            | 1  |    | 1  |  |  |  |  |  |
| 10        | 1            | 1  |    |    |  |  |  |  |  |

which yields:  $f = \neg x_1 x_2 \neg x_3 \neg x_4 + \neg x_1 \neg x_2 \neg x_3 \neg x_5 + \neg x_1 x_2 x_3 x_4 x_5 + x_1 x_2 \neg x_4 + x_1 \neg x_4 x_5 + x_1 x_3 x_4 \neg x_5$