

# Technische Informatik: Abgabe 6

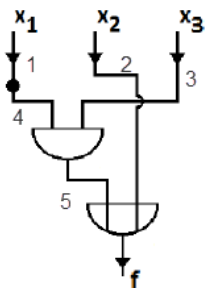
Michael Mardaus

Andrey Tyukin

2. Dezember 2013

## Exercise 6.1 (Circuit jam)

$$f(x_1, x_2, x_3) = \bar{x}_1 x_3 + x_2$$



$f_1, \dots, f_5$  are 0-jams

$$f_1(x_1, x_2, x_3) = \bar{0}x_3 + x_2 = x_3 + x_2$$

$$f_2(x_1, x_2, x_3) = \bar{x}_1 x_3 + 0 = \bar{x}_1 x_3$$

$$f_3(x_1, x_2, x_3) = \bar{x}_1 0 + x_2 = x_2$$

$$f_4(x_1, x_2, x_3) = 0x_3 + x_2 = x_2$$

$$f_5(x_1, x_2, x_3) = 0 + x_2 = x_2$$

$f_6, \dots, f_a$  are 1-jams.

$$f_6(x_1, x_2, x_3) = \bar{1}x_3 + x_2 = x_2$$

$$f_7(x_1, x_2, x_3) = \bar{x}_1 x_3 + 1 = 1$$

$$f_8(x_1, x_2, x_3) = \bar{x}_1 1 + x_2 = \bar{x}_1 + x_2$$

$$f_9(x_1, x_2, x_3) = 1x_3 + x_2 = x_3 + x_2$$

$$f_a(x_1, x_2, x_3) = 1 + x_2 = 1$$

Ausfalltafel:

| # | $x_1$ | $x_2$ | $x_3$ | $f_1$ | $f_2$ | $f_3$ | $f_4$ | $f_5$ | $f_6$ | $f_7$ | $f_8$ | $f_9$ | $f_a$ | $f$ |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-----|
| 0 | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 1     | 1     | 0     | 1     | 0   |
| 1 | 0     | 0     | 1     | 1     | 1     | 0     | 0     | 0     | 0     | 1     | 1     | 1     | 1     | 1   |
| 2 | 0     | 1     | 0     | 1     | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1   |
| 3 | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1   |
| 4 | 1     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 1     | 0     | 0     | 1     | 0   |
| 5 | 1     | 0     | 1     | 1     | 0     | 0     | 0     | 0     | 0     | 1     | 0     | 1     | 1     | 0   |
| 6 | 1     | 1     | 0     | 1     | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1   |
| 7 | 1     | 1     | 1     | 1     | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1   |

$$\Rightarrow f_1 = f_9; f_2; f_3 = f_4 = f_5 = f_6; f_7 = f_a; f_8$$

Ausfallmatrix:

| # | $x_1$ | $x_2$ | $x_3$ | $f_1$ | $f_2$ | $f_3$ | $f_7$ | $f_8$ | $f$ |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-----|
| 0 | 0     | 0     | 0     | 0     | 0     | 0     | 1     | 1     | 0   |
| 1 | 0     | 0     | 1     | 1     | 1     | 0     | 1     | 1     | 1   |
| 2 | 0     | 1     | 0     | 1     | 0     | 1     | 1     | 1     | 1   |
| 3 | 0     | 1     | 1     | 1     | 1     | 1     | 1     | 1     | 1   |
| 4 | 1     | 0     | 0     | 0     | 0     | 0     | 1     | 0     | 0   |
| 5 | 1     | 0     | 1     | 1     | 0     | 0     | 1     | 0     | 0   |
| 6 | 1     | 1     | 0     | 1     | 0     | 1     | 1     | 1     | 1   |
| 7 | 1     | 1     | 1     | 1     | 0     | 1     | 1     | 1     | 1   |

Fehlermatrix:

| # | $x_1$ | $x_2$ | $x_3$ | $f \leftrightarrow f_1$ | $f \leftrightarrow f_2$ | $f \leftrightarrow f_3$ | $f \leftrightarrow f_7$ | $f \leftrightarrow f_8$ | Test |
|---|-------|-------|-------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|------|
| 0 | 0     | 0     | 0     | 0                       | 0                       | 0                       | 1                       | 1                       | ★    |
| 1 | 0     | 0     | 1     | 0                       | 0                       | 1                       | 0                       | 0                       | ★    |
| 2 | 0     | 1     | 0     | 0                       | 1                       | 0                       | 0                       | 0                       | ★    |
| 3 | 0     | 1     | 1     | 0                       | 0                       | 0                       | 0                       | 0                       |      |
| 4 | 1     | 0     | 0     | 0                       | 0                       | 0                       | 1                       | 0                       |      |
| 5 | 1     | 0     | 1     | 1                       | 0                       | 0                       | 1                       | 0                       | ★    |
| 6 | 1     | 1     | 0     | 0                       | 1                       | 0                       | 0                       | 0                       |      |
| 7 | 1     | 1     | 1     | 0                       | 1                       | 0                       | 0                       | 0                       |      |

$\Rightarrow$  Testvector:  $\{(0, 0, 0), (0, 0, 1), (0, 1, 0), (1, 0, 1)\}$

## Exercise 5.2 (Row and Column-Rules are not a function)

todo

## Exercise 6.3 (Hazards)

| $x_1 = 1$ |          |    |    |    |
|-----------|----------|----|----|----|
|           | $x_4x_5$ |    |    |    |
| $x_2x_3$  | 00       | 01 | 11 | 10 |
| 00        |          | 1  |    |    |
| 01        |          | 1  |    | 1  |
| 11        | 1        | 1  |    | 1  |
| 10        | 1        | 1  |    |    |

which yields:  $f = \neg x_1 x_2 \neg x_3 \neg x_4 + \neg x_1 \neg x_2 \neg x_3 \neg x_5 + \neg x_1 x_2 x_3 x_4 x_5 + x_1 x_2 \neg x_4 + x_1 \neg x_4 x_5 + x_1 x_3 x_4 \neg x_5$