

# Risk Budgeting

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## Risk Budgeting

$$\sigma(w) = w^T \Sigma w$$

Contribution au risque de l'actif  $i$ :

$$RC_i = \frac{w_i (\Sigma w)_i}{\sqrt{w^T \Sigma w}}$$

## Risk Parity & Budgeting

Parity:

$$RC_i = \frac{1}{N} \sigma(w)$$

Budgeting:

$$RC_i = b_i \sigma(w)$$

Cas Particulier:  $\Sigma$  diagonal

$$\Omega = \sqrt{\text{diag}(\Sigma)}$$

$$w = \frac{\Omega^{-1}}{1^T \Omega^{-1}}$$

## Risk Parity & Budgeting: Exemple.

```

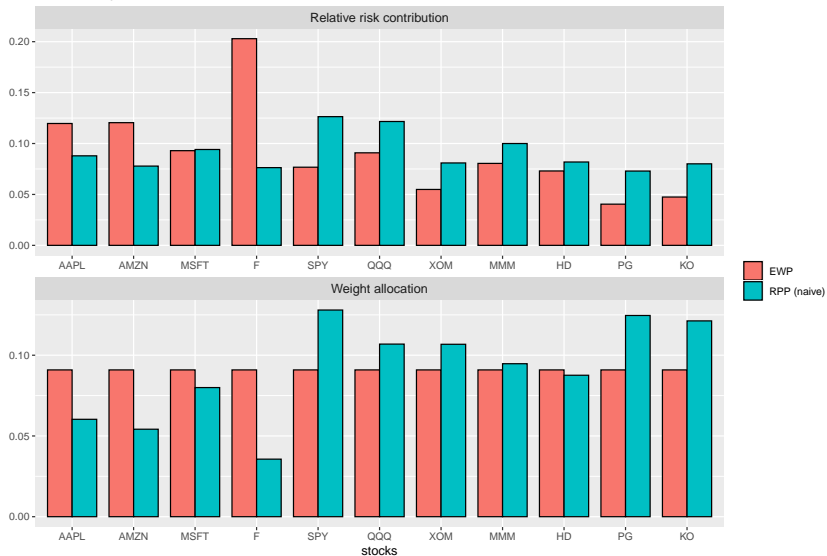
Sigma <- cov(monthly.ret)
mu <- colMeans(monthly.ret)
rpp_naive <- riskParityPortfolio(Sigma, formulation = "diag")
rpp_vanilla <- riskParityPortfolio(Sigma)
rpp_mu <- riskParityPortfolio(Sigma, formulation = "rc-over",
                             mu = mu, lmd_mu = 1e-3,
                             w_ub = 0.16)

w_all <- cbind("EWP" = rep(1/nrow(Sigma), nrow(Sigma)),
              "RPP (naive)" = rpp_naive$w)

```

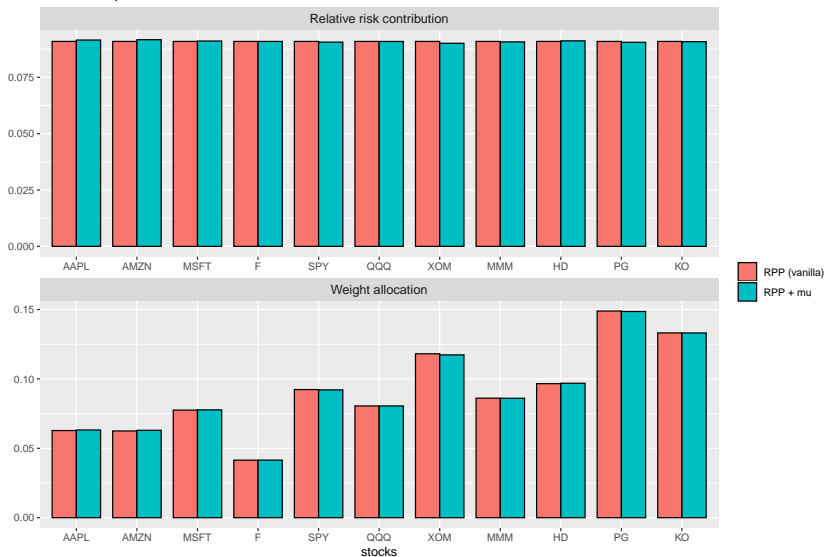
# Risk Budgeting

Portfolio capital and risk distribution



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## Exercice

Utiliser le package “riskParityPortfolio” et le dataset “monthly returns.”

A partir de l'exemple: “A practical example using FAANG price data,” comparer par un backtest les performances et la composition d'un portefeuille tangent et d'un portefeuille “risk parity.”

Ajouter des contraintes au portefeuille tangent:

- ▶ Poids  $\leq 20\%$
- ▶ Secteur Technologie  $\leq 30\%$

<https://cran.r-project.org/web/packages/riskParityPortfolio/vignettes/RiskParityPortfolio.html>