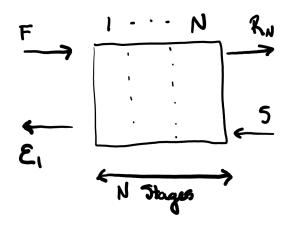
1)

a.



$$x_{EG}^{F} = 0.20$$
  
 $x_{W}^{F} = 0.80$   
 $x_{EG}^{R} \le 0.05$   
 $F = 350 \text{ kg/hr}$   
 $S = 100 \text{ kg/hr}$   
(pure)

## Solve:

Solving for the mixture composition ( $[m_i] = kg/hr$ ),

Comp.	F		S		M	
	$m_{i}$	$X_i$	$m_{i}$	$X_i$	$m_{i}$	$X_i$
EG	70	0.20	0.00	0.00	70	0.156
W	280	0.80	0.00	0.00	280	0.622
f	0	0.00	100	1.00	100	0.222
Tot.	350	1.00	100	1.00	450	1.00

From this, the F, S, and M composition points may be plotted on the Gibbs triangle for the system along with the desired  $R_N$  composition. The material balances around the column dictate that  $E_1$ ,  $R_N$ , and M compositions lie on the same line. Thus, we draw a line through  $R_NM$  and find its intersection with the equilibrium curve ( $E_1$  exits in equilibrium). Additionally, consider the material balance around the entire column,

$$F + S = E_1 + R_N.$$

Meaning,

$$\Delta = F - E_1 = R_N - S = R_i - E_{i+1},$$

for any stage, i. Therefore, all passing streams must intersect at  $\Delta$ . By drawing the lines through  $FE_1$  and  $R_NS$ , we may extract  $\Delta$ . From this, the composition is found by stepping between the tie lines and operating point.

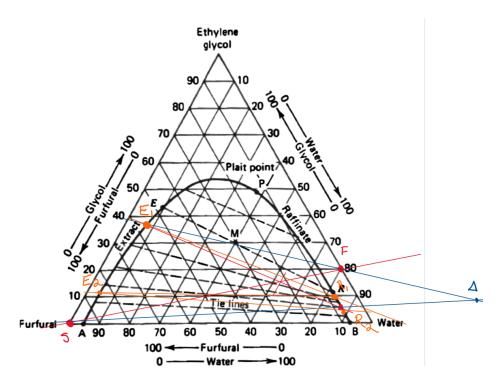


Figure 1: Gibbs triangle for a EG-W-f system

The compositions may be read off the diagram ( $[m_i] = \text{kg/hr}$ ).

Comp.	M		E		R	
	$m_{i}$	$X_i$	$m_{i}$	$X_i$	$m_{i}$	$X_i$
EG	70	0.156	53.7	0.360	9.93	0.033
W	280	0.622	10.4	0.070	268	0.890
f	100	0.222	85.0	0.57	23.5	0.078
Tot.	450	1.00	149	1.00	301	1.00

Since the compositions are known from the Gibbs triangle. We may solve for  $R_N$  and  $E_1$  using any component balance. This forms a linear system,

$$M = E_1 + R_N,$$

$$x_i^M M = x_i^E E_1 + x_i^R R_N,$$

whose solution gives a lever rule like expression,

$$\frac{R_N}{M} = \frac{x_i^M - x_i^E}{x_i^R - x_i^E}.$$

Applying this to all of the components gives 3 different values for  $R_N$ ,

$$({\rm EG,W,f}) \to R_N = (281,303,318)~{\rm kg/hr},$$

Taking the average gives,

$$R_N = 301 \text{ kg/hr}$$

Since  $E_1 = M - R_N$ ,

$$E_1 = 149 \text{ kg/hr}.$$

## b.

From the diagram, there are 2 tie lines, thus, at least N = 2 stages are required.

## c.

Reading from the  $E_2$  point on the diagram,

$$(x_{EG}, x_W, x_f)_{E_2} = (0.11, 0.05, 0.85),$$

which sums to 1.01. By distributing the 0.01 error,

$$(x_{EG}, x_W, x_f)_{E_2} = (0.107, 0.047, 0.846)$$