

# Searching 2



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## Searching 2



### Agenda

1. Advanced Problems Based on Binary Search

## Problems

### 1. Aggressive Cows

There is a new barn with  $N$  stalls and  $C$  cows. The stalls are located on a straight line at positions  $x_1, \dots, x_N$  ( $0 \leq x_i \leq 1,000,000,000$ ). We want to assign the cows to the stalls, such that the minimum distance between any two of them is as large as possible. What is the largest minimum distance?

#### Examples:

Input: No of stalls = 5 Array: {1,2,8,4,9} And number of cows: 3

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After sorting the array, we set a minimum distance, then we keep on increasing until accommodation of all cows is not possible. We stop *just* before that to get our answer, which in this example is 3. For checking if the cows can fit or not, we are simply iterating over our  $n$  stalls, and for every stall with the said minimum distance, we place our cow. After we are done, if all cows have been accommodated, we return true, otherwise false. Let's observe the time complexity of our brute force algorithm here, we are increasing distance in each step (which in the worst case of two cows gets as high as  $m = \text{array}[n-1] - \text{array}[0]$ ), and in that step, we are checking if our cows can "fit", so we are iterating again for each step to check.

### Implementation

```
#include <bits/stdc++.h>

using namespace std;
bool isCompatible(vector<int> inp, int dist)
{
    int n = inp.size();
    int k = inp[0];
    cows--;
    for (int i = 1; i < n; i++)
    {
        if (inp[i] - k >= dist)
        {
            cows--;
            if (!cows)
            {
                return false;
            }
        }
    }
    return true;
}
```

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```

        k = inp[i];
    }
}
return false;
}
int main()
{
    int n, m;
    cin >> n >> m;
    vector<int> inp(n);
    for (int i = 0; i < n; i++)
        cin >> inp[i];
    sort(inp.begin(), inp.end());
    int maxD = inp[n - 1] - inp[0];
    int ans = INT_MIN;
    for (int d = 1; d <= maxD; d++)
    {
        bool possible = isCompatible(inp, c
        if (possible)
        {
            ans = max(ans, d);
        }
    }
    cout << ans << '\n';
}

```

### Optimised Approach

Make sure to sort the array first, because only then it makes sense to use binary search. For the BS approach, we set low = 1 because the minimum distance is 1 and high = array[n-1] - array[0]. because that's the maximum possible distance between two stalls. Let's calculate our mid-value after this.  $mid = low + (high - low) / 2$ .

in brute force, and if it is not possible, this means we can set our upper bound as high-1, and if it is possible, we store it in an answer variable and set our lower bound as mid+1. We keep on doing this until high and low pointers are equal.

## Implementation

```
#include <bits/stdc++.h>

using namespace std;
bool isPossible(int a[], int n, int cows, int minDist)
{
    int cntCows = 1;
    int lastPlacedCow = a[0];
    for (int i = 1; i < n; i++)
    {
        if (a[i] - lastPlacedCow >= minDist)
        {
            cntCows++;
            lastPlacedCow = a[i];
        }
    }
    if (cntCows >= cows)
        return true;
    return false;
}

int main()
{
    int n, cows;
    cin >> n >> cows;
    int a[n];
    for (int i = 0; i < n; i++)
        cin >> a[i];
```

```

int low = 1, high = a[n - 1] - a[0];

while (low <= high)
{
    int mid = (low + high) >> 1;

    if (isPossible(a, n, cows, mid))
    {
        low = mid + 1;
    }
    else
    {
        high = mid - 1;
    }
}
cout << high << endl;

return 0;
}

```

Time Complexity:  $O(N \cdot \log(M))$ .

Space Complexity:  $O(1)$

## 2. Smallest Good Base

Given an integer  $n$  represented as a string, return the smallest good base of  $n$ . We call  $k \geq 2$  a good base of  $n$ , if all digits of  $n$  base  $k$  are 1's.

Example:

Input:  $n = "13"$

Output:  $"3"$

Explanation: 13 base 3 is 111.

### Approach

The input can be stored in a long long int, use

smallest possible base is  $k=2$ , with has the longest possible representation, i.e., largest  $d$ . So, to find the smallest base means to find the longest possible representation "1111...1" based on  $k$ . As  $n \leq 10^{18}$ , so  $n < (1 < 62)$ . We iterate the length of the representation from 62 to 2 (2 can always be valid, with  $base=n-1$ ), and check whether a given length can be valid. For a given length  $d$ , we use binary search to check whether there is a base  $k$  which satisfies  $1+k^1+k^2+\dots+k^d=n$ . The left limit is 1, and the right limit is  $\text{pow}(n, 1/d)+1$ , i.e., the  $d$ -th square root of  $n$ .

## Implementation

```
#include <bits/stdc++.h>
using namespace std;

unsigned long long mysolve(unsigned long long n)
{
    double tn = (double)n;
    unsigned long long right = (unsigned long long)tn;
    unsigned long long left = 1;
    while (left <= right)
    {
        unsigned long long mid = left + (right - left) / 2;
        unsigned long long sum = 1, cur = 1;
        for (int i = 1; i <= d; i++)
        {
            cur *= mid;
            sum += cur;
        }
        if (sum == n)
            return mid;
    }
}
```

```

        else
            left = mid + 1;
    }
    return 0;
}

string smallestGoodBase(string n)
{
    unsigned long long tn = (unsigned long
    unsigned long long x = 1;
    for (int i = 62; i >= 1; i--)
    {
        if ((x << i) < tn)
        {
            unsigned long long cur = mysol\
            if (cur != 0)
                return to_string(cur);
        }
    }
    return to_string(tn - 1);
}

int main()
{
    string s;
    cin >> s;
    cout << smallestGoodBase(s);
    return 0;
}

```

Time Complexity:  $O(\log N)$

Space Complexity:  $O(1)$

### 3. [Minimum Size Subarray Sum](#)

Given an array of positive integers `nums` and a positive integer, `target` return the minimal

subarray, return 0 instead.

Example

Input: target = 7, nums = [2,3,1,2,4,3]

Output: 2

Explanation: The subarray [4,3] has a minimal length under the problem constraint.

### **Sliding Window-Based Approach**

We can use a sliding window in this question. Initialise two variables and increment the second one when the sum exceeds the target else increment the first one and find the minimum range for desired subarray sum.

### **Implementation**

```
#include <bits/stdc++.h>
using namespace std;

int minSubArrayLen(int target, vector<int>
{
    int l = 0, h = 0;
    int s = 0, ans = nums.size();
    for (int i : nums)
        s += i;
    if (s < target)
        return 0;
    s = 0;
    for (int i = 0; i < nums.size(); i++)
    {
        s += nums[i];
        while (s - nums[l] >= target)
            s -= nums[l++];
        if (s >= target)
            ans = min(ans, i - l + 1);
    }
}
```



```
int main()  
{  
    int n;  
    cin >> n;  
    int target;  
    cin >> target;  
    vector<int> nums(n);  
    for (int i = 0; i < n; i++)  
    {  
        cin >> nums[i];  
    }  
    cout << minSubArrayLen(target, nums);  
    return 0;  
}
```

### **Binary Search-Based Approach**

So if we clearly see despite not having a sorted array we can do a binary search on the answer because our answer can lie between 1 and n otherwise that will not be a subarray present. So do a binary search from 1 to n and check for each mid if it will give us a subarray having a sum target and continue decreasing it by doing  $hi = mid - 1$ .

### **Implementation**

```
#include <bits/stdc++.h>  
using namespace std;  
  
bool checker(vector<int> &arr, int k, int n  
{  
    int sum = 0;  
    for (int i = 0; i < mid; i++)  
        sum += arr[i];
```

```
while (r < arr.size())
{
    sum -= arr[l++];
    sum += arr[r++];
    maxi = max(sum, maxi);
}
return maxi >= k;
}

int minSubArrayLen(int k, vector<int> &arr)
{
    int n = arr.size();
    int low = 1, high = n;
    int ans = 0;
    while (low <= high)
    {
        int mid = low + (high - low) / 2;
        if (checker(arr, k, mid))
        {
            ans = mid;
            high = mid - 1;
        }
        else
            low = mid + 1;
    }
    return ans;
}

int main()
{
#ifndef ONLINE_JUDGE
    freopen("input.txt", "r", stdin);
    freopen("output.txt", "w", stdout);
#endif
    int n;
    cin >> n;
    int target;
```

```
for (int i = 0; i < n; i++)  
{  
    cin >> nums[i];  
}  
cout << minSubArrayLen(target, nums);  
return 0;  
}
```

Time Complexity:  $O(n \log n)$

Space Complexity:  $O(1)$



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