

# Some Title

## And Maybe a Subtitle

Peter Illig   Eli Orvis   Yukihiro Segawa   Nick Spinale

Carleton College

February 20<sup>th</sup>, 2018

# Contents

- 1 Introduction
- 2 Simplifying the Problem

# A Title

Contents of the slide

# Roots of $f^n(x)$

$$f(x) = (x - \gamma)^2 + \gamma + m$$

- The roots of  $f(x)$  are  $\gamma \pm \sqrt{-m - \gamma}$
- If  $\alpha$  is a root of  $f^n(x)$ , then  $\gamma \pm \sqrt{\alpha - m - \gamma}$  are roots of  $f^{n+1}(x)$

## Observation

*For  $n > 0$ , the roots of  $f^n(x)$  are, with  $n$  radicals:*

$$\gamma \pm \sqrt{-m \pm \sqrt{-m \pm \sqrt{-m \pm \dots \sqrt{-m - \gamma}}}}$$

# Roots of $f^n(x)$

## Observation

For  $n > 0$ , the roots of  $f^n(x)$  are, with  $n$  radicals:

$$\gamma \pm \sqrt{-m \pm \sqrt{-m \pm \sqrt{-m \pm \dots \sqrt{-m - \gamma}}}}$$

For notational convenience, define  $\beta : \Sigma^* \rightarrow \mathbb{C}$  where

$$\begin{aligned}\beta_\epsilon &= -\gamma \\ \beta_{0s} &= \sqrt{-m + \beta_s} \\ \beta_{1s} &= -\sqrt{-m + \beta_s}\end{aligned}$$

For  $n > 0$ , the roots of  $f^n(x)$  are exactly  $\{ \gamma + \beta_s \mid s \in \Sigma^n \}$ .