

### 3. Methodology

In this section models were created, trying to outperform the buy and hold strategy.

starting by analyzing the data and using simple models, more complex models and combined tools are added step by step in different approaches.

#### 3.1. Data Analysis

As mentioned in section 1.1 We are now going to analyze the data further to gain as much information as possible just by using some simple tools and comparisons.

##### 3.1.1. correlation

One could nearly tell just by looking at the indexes how strong they're correlated. The correlation matrix confirms the assumption, the correlation is nearly 1 for every index to each other.

Table 1: Correlations oft the four indexes

	Index 1	Index 2	Index 3	Index 4
Index 1	1.0000000	0.9899111	0.9788826	0.9672956
Index 2	0.9899111	1.0000000	0.9975499	0.9921171
Index 3	0.9788826	0.9975499	1.0000000	0.9983460
Index 4	0.9672956	0.9921171	0.9983460	1.0000000

##### 3.1.2. transformation, volatility and clusters

Applying the natural logarithm to the series is an approach to cancel out increasing volatility ??.

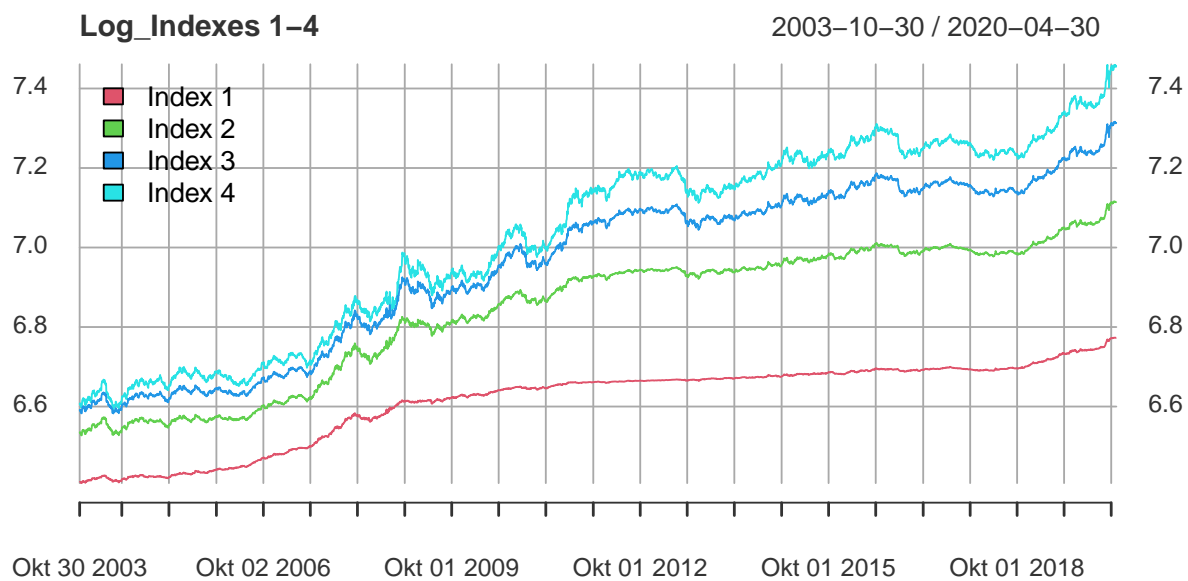
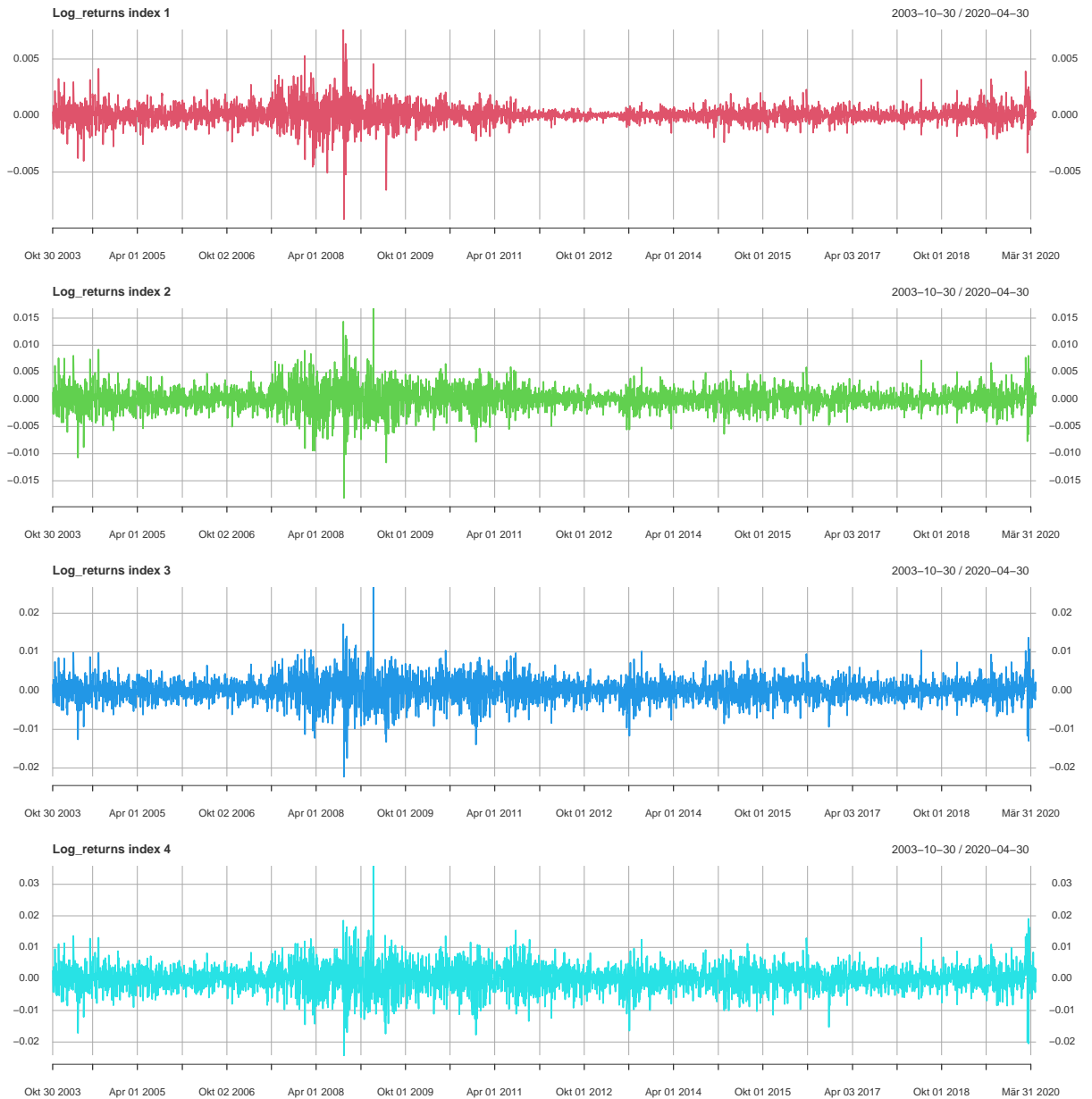
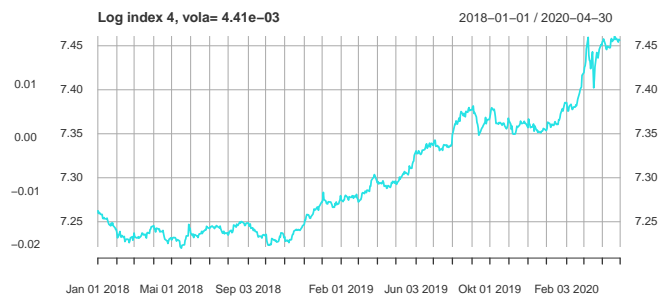
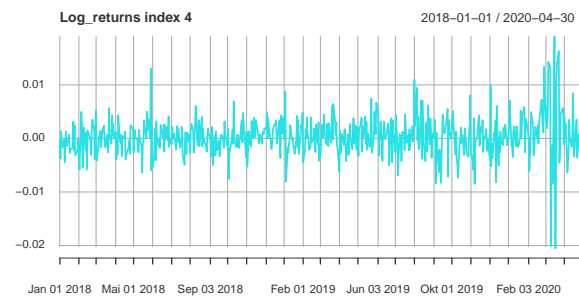
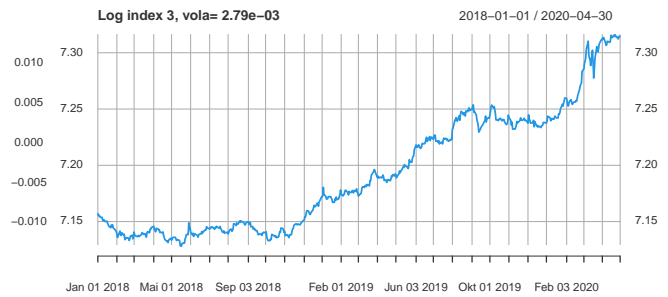
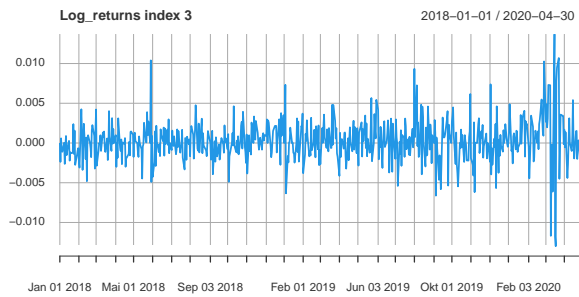
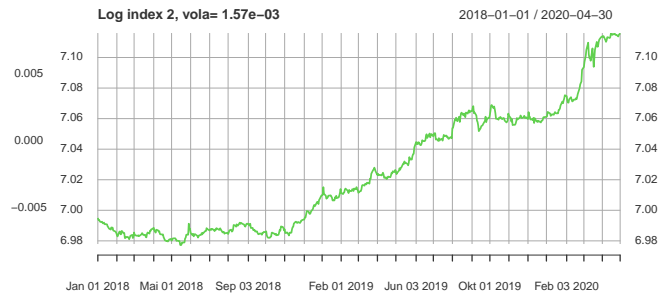
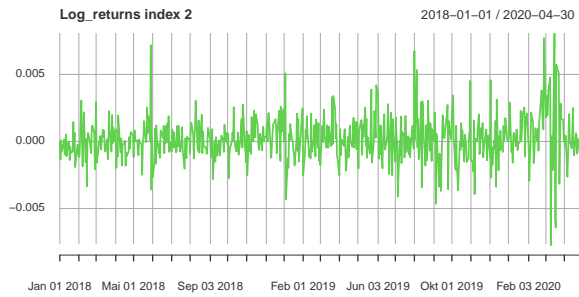
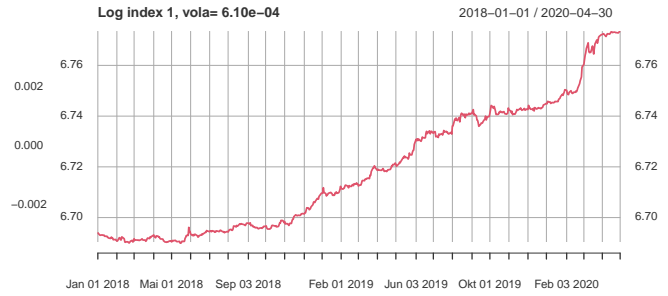
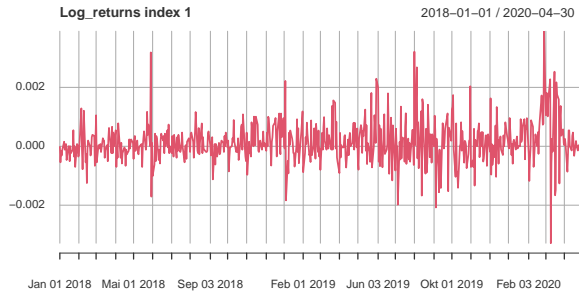


Figure 1: Visualization log\_indizes

By taking the returns of the transformed series we can visualize volatility clusters as seen in figure ??, clearly visible are the increasing volatility clusters in the financial crisis, due to the high correlation the indexes look pretty similar





### 3.1.5 periodicity

```
## $DFT
## [1] 1.282112e-03+0.000000e+00i -1.347946e-04-3.007434e-04i
## [3] 3.132441e-04-2.603213e-04i 5.288351e-05-4.342329e-04i
## [5] -2.713600e-04-4.652251e-04i -2.551659e-05-2.250935e-04i
## [7] -3.664969e-04-9.217152e-05i -2.717648e-04-1.236588e-04i
## [9] -2.032501e-04+2.702495e-05i -3.338524e-04+9.472463e-05i
## [11] 5.685114e-05-2.204384e-06i -1.782612e-04-7.122921e-06i
## [13] 2.949365e-04+4.335962e-04i 1.884917e-04+1.256230e-05i
## [15] -1.264255e-04-1.184852e-05i 2.365061e-04+2.046574e-04i
## [17] 1.844846e-04-1.492249e-04i -7.585935e-05-4.628853e-04i
## [19] -1.966033e-04-7.023414e-05i 1.805948e-04-7.001699e-05i
```

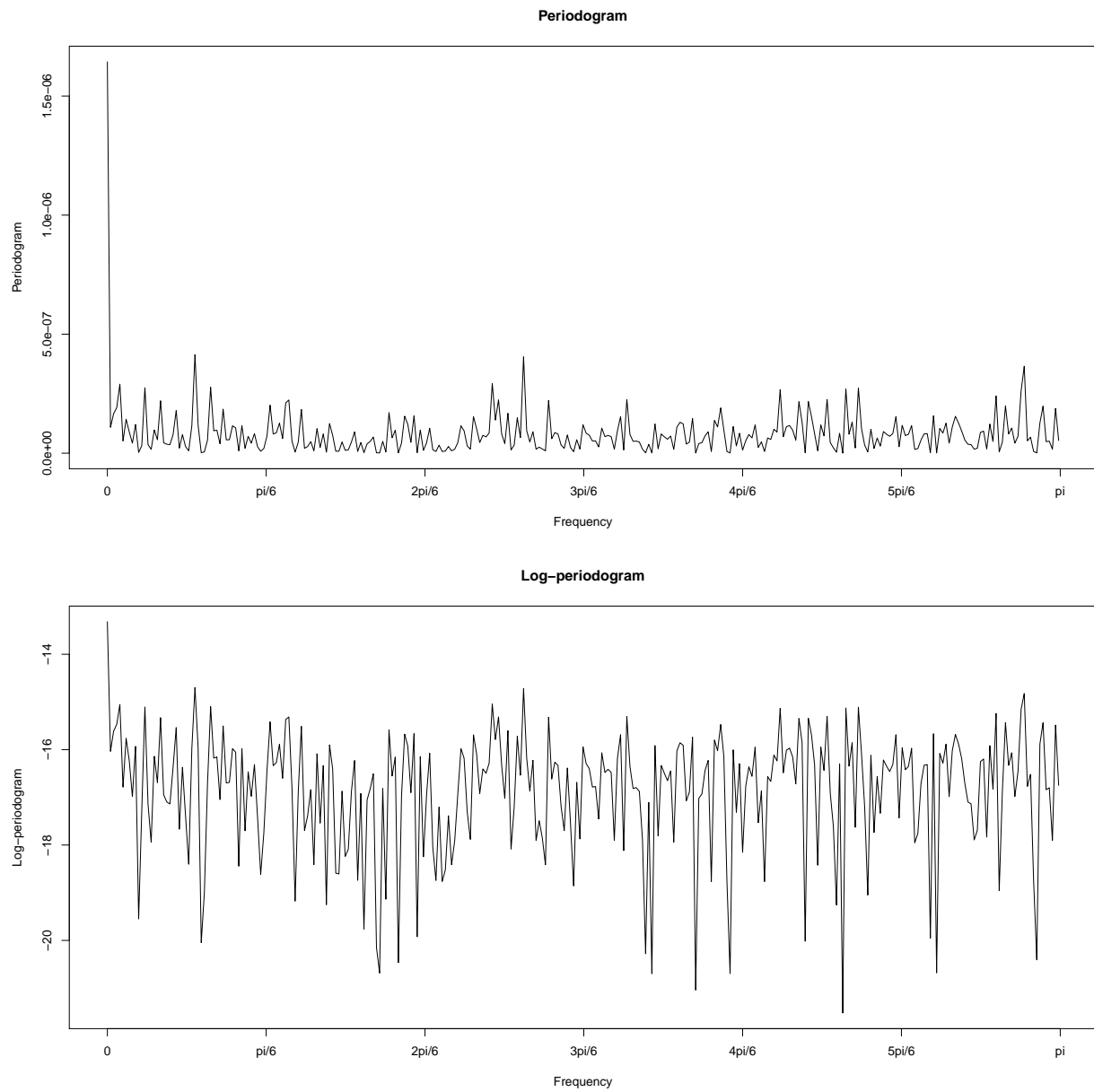


Figure 2: peridodogramm

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## [21] -1.665074e-04+9.137738e-05i -1.492621e-04-2.352690e-04i
## [23] -3.573803e-04+2.259881e-04i 7.457794e-05+1.251010e-04i
## [25] 1.321793e-04+2.455846e-04i 6.237552e-05+1.541902e-04i
## [27] 9.117122e-05+4.322518e-05i 3.131854e-04+1.342511e-04i
## [29] 3.886758e-04-5.131184e-04i 1.730746e-04-2.959691e-04i
## [31] -4.385622e-05-6.637758e-06i -3.379180e-05+6.672512e-05i
## [33] -1.329552e-04-1.921405e-04i -5.108011e-04-1.279647e-04i
## [35] -2.964138e-04-7.988085e-05i 1.916618e-04+2.445270e-04i
## [37] -1.898314e-04-5.883901e-05i -3.946272e-04+1.713199e-04i
## [39] 5.908037e-05+2.291379e-04i -2.296461e-04-6.218111e-05i
## [41] 1.661605e-04+2.955250e-04i 3.263215e-04+4.871442e-06i
## [43] 8.958860e-05-4.188775e-05i 2.552662e-04+2.237736e-04i
## [45] 7.346806e-05-1.230288e-04i 2.150874e-04-1.566635e-04i
## [47] 1.807568e-04-9.810267e-05i -8.118797e-05-2.753855e-04i
## [49] 1.534901e-04+5.937791e-05i -8.980767e-05-1.211315e-05i
## [51] -1.321394e-04+4.585169e-05i 1.644695e-05-2.669810e-04i
## [53] -1.670569e-04+4.168244e-04i 2.395366e-04-1.519419e-04i
## [55] -2.872802e-04+5.652579e-05i -2.329144e-04+2.684688e-04i
## [57] 2.466199e-04+3.021499e-05i 2.338153e-04-3.961002e-04i
## [59] -3.912315e-04-2.650053e-04i 1.179213e-04+1.906206e-04i
## [61] 6.175669e-05+2.973126e-05i 2.016555e-04+7.365904e-05i
## [63] -1.208991e-04-4.106767e-04i 1.381222e-04-3.914986e-05i
## [65] -1.634735e-04+3.651645e-05i 1.728774e-04-1.371881e-04i
## [67] -4.343526e-05-9.059655e-05i -2.614124e-04-1.868144e-04i
## [69] -1.407925e-04+6.566166e-05i 2.835365e-04+1.979102e-05i
## [71] 3.199924e-05-5.774187e-05i -2.855316e-04+2.068250e-04i
## [73] 2.685737e-04+5.163065e-05i -3.151989e-05+8.626919e-05i
## [75] 7.271192e-05-5.494331e-05i 2.138565e-04+3.688100e-05i
## [77] 4.846383e-05-9.828226e-05i -9.264356e-05-7.314445e-05i
## [79] -1.280883e-04+1.749831e-04i 7.559004e-05-2.895953e-04i
## [81] 1.909084e-05-8.307919e-05i 1.391293e-04+1.598646e-04i
## [83] 2.633361e-05-4.387312e-05i -1.956219e-04+3.099775e-05i
## [85] 1.063829e-04+1.956502e-04i 2.089692e-04-1.550278e-04i
## [87] 2.430222e-05-3.443299e-05i 1.822746e-05-2.659161e-05i
## [89] -8.119944e-05+2.080200e-04i -3.171002e-05+6.231099e-05i
## [91] -9.448804e-07-4.127953e-04i -1.199492e-04+2.244780e-04i
## [93] 2.753156e-04-1.431004e-04i -2.543222e-05-2.543865e-05i
## [95] -1.807197e-04-9.872655e-05i 3.582619e-04-1.649696e-04i
## [97] -2.522220e-04-2.404293e-04i 2.130109e-04-1.681823e-05i
## [99] -3.866397e-04+8.903268e-05i -4.460998e-05-1.532942e-05i
## [101] -2.909651e-04+1.129037e-04i -6.251846e-06+1.088816e-04i
## [103] 2.078136e-04-6.943125e-06i 2.639087e-04+1.866032e-04i
## [105] 1.203671e-04+1.676461e-06i 1.887243e-05-8.301302e-05i
## [107] 7.412008e-06+1.836032e-04i 7.929145e-05+2.844645e-05i
## [109] 3.282815e-05+8.914536e-05i 8.230523e-05-1.461563e-04i
## [111] 7.166898e-05-7.031987e-05i -1.292923e-04-3.531206e-06i
## [113] 1.943556e-04+8.403467e-05i 1.158892e-04-3.187031e-04i
## [115] -6.410224e-05-2.995802e-04i -1.309749e-04+1.151394e-04i
## [117] 9.185982e-05-9.336954e-05i -2.947819e-04-2.580718e-04i
## [119] -3.193729e-04-2.920190e-05i -7.915319e-05+1.964278e-04i
## [121] -9.124851e-05+2.586162e-04i 1.474055e-04+2.162984e-04i
## [123] 2.647074e-04+1.204769e-04i 2.052224e-04+5.002838e-04i
## [125] 3.410122e-04+1.512052e-04i 4.711660e-04+4.129143e-05i
## [127] 1.503304e-04-2.425398e-04i 1.919490e-04-5.994501e-05i

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## [129] -2.794451e-04-2.992106e-04i -3.020111e-05-1.144087e-04i
## [131] -7.799012e-08-1.834790e-04i -2.528106e-04-2.914206e-04i
## [133] -2.109885e-04-1.457626e-04i -5.467019e-04-3.252435e-04i
## [135] -2.704841e-04+1.469944e-04i -6.876594e-05-2.062591e-04i
## [137] -1.807500e-04-2.394465e-04i -8.669822e-05+9.618506e-05i
## [139] 2.686666e-05+1.568975e-04i -9.410832e-05+9.371405e-05i
## [141] 8.725697e-06+9.999538e-05i 3.385205e-04+3.277654e-04i
## [143] 2.463291e-04+6.796877e-06i 2.503376e-04+1.546996e-04i
## [145] -4.899055e-06+2.840419e-04i 1.435136e-04+1.159899e-04i
## [147] 1.371209e-04-4.283928e-05i -1.217721e-04-2.485103e-04i
## [149] 2.102409e-05+1.536733e-04i -8.038185e-05-2.470811e-06i
## [151] 2.585009e-05+2.367562e-04i -1.062877e-04-7.734418e-05i
## [153] -1.371781e-04-3.175570e-04i 2.041687e-04+2.056976e-04i
## [155] 1.848510e-04-2.032798e-04i -2.262033e-04-1.348361e-05i
## [157] -1.902534e-04-1.252615e-04i -1.584525e-04+3.463254e-05i
## [159] 1.340819e-04+2.957302e-04i 3.240525e-05-2.619456e-04i
## [161] -1.921929e-04+1.938666e-04i 2.623065e-04+3.037749e-05i
## [163] -4.563004e-07+1.294879e-04i -2.245100e-04-2.080236e-04i
## [165] 3.430891e-04-1.907054e-04i -2.379565e-05+1.139508e-04i
## [167] 4.622817e-04+1.100698e-04i 2.729203e-04-6.770885e-05i
## [169] -1.825291e-04+1.284567e-04i 2.240349e-04-2.452120e-05i
## [171] -3.749370e-05-2.132956e-04i -1.207693e-04-4.976573e-05i
## [173] -2.559895e-05+3.004091e-05i -1.914826e-04+2.388237e-05i
## [175] 2.958360e-05+1.226179e-05i -2.520139e-04-2.431326e-04i
## [177] -1.332879e-04-2.567272e-05i 4.131081e-05+2.810451e-04i
## [179] 2.420275e-04-9.946565e-05i -1.779383e-04-1.645417e-04i
## [181] -2.615986e-04+5.911817e-05i 1.042594e-04-7.291298e-05i
## [183] -2.726994e-04-1.879459e-04i -4.452977e-05+3.578145e-04i
## [185] 3.140481e-04-1.572796e-04i -1.595690e-04+1.141160e-04i
## [187] -5.197568e-05+2.088166e-04i 3.167022e-04+2.136117e-04i
## [189] 2.425364e-05+1.182386e-05i 9.123243e-05-1.795789e-04i
## [191] -9.523399e-05+1.881141e-04i 2.698017e-04-4.597442e-06i
## [193] -1.369985e-05-2.992484e-04i -8.344369e-05-1.022853e-05i
## [195] 3.204362e-04-1.870598e-04i -1.269514e-04-3.065871e-04i
## [197] -2.331502e-04+3.690090e-04i -1.456548e-04-2.771942e-04i
## [199] -1.871524e-05-8.146280e-05i -2.925543e-05+1.310489e-05i
## [201] -3.265657e-04+7.288828e-05i 5.032411e-05+1.664874e-04i
## [203] -2.237041e-04+1.837890e-04i 9.333899e-05+6.578667e-05i
## [205] -2.217791e-04+5.534521e-05i 2.495486e-04-1.271789e-04i
## [207] 2.394927e-04-8.331049e-05i 3.339892e-04-8.349369e-05i
## [209] -8.555030e-05-1.302840e-04i 2.160343e-04+2.739338e-05i
## [211] 5.271363e-05+6.559493e-05i 1.450132e-04-2.071756e-04i
## [213] -1.463450e-04-1.906713e-04i -1.563962e-04+2.759924e-04i
## [215] -1.940883e-04-2.260379e-04i -4.174542e-04+3.044267e-04i
## [217] 5.968599e-05+2.562540e-04i 3.331556e-04+1.407870e-05i
## [219] -2.995163e-04+1.628580e-04i 5.369926e-05+3.058734e-04i
## [221] 4.709620e-05+2.297186e-04i 4.644302e-04-2.611218e-05i
## [223] 2.330920e-04-2.752373e-04i 4.498269e-05+1.236850e-06i
## [225] 4.578249e-04-8.804508e-05i -4.014116e-05-3.907209e-04i
## [227] -2.843049e-04-3.819283e-05i -8.301315e-06+9.953559e-05i
## [229] 2.185113e-04-2.662472e-04i -2.685972e-04-2.602937e-05i
## [231] -3.582667e-04+3.121382e-04i -1.755080e-04+1.205529e-04i
## [233] -1.123016e-04+1.003115e-04i -6.354826e-05-1.696353e-05i
## [235] 4.081603e-05+2.862845e-04i 7.519913e-06-1.983573e-05i

```

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## [237] 6.740170e-06+5.191596e-04i -2.294439e-04+1.643241e-04i
## [239] 3.465569e-04-1.001122e-04i 1.177606e-04+9.070272e-05i
## [241] 5.212288e-04+4.759362e-05i -2.045432e-04-2.466952e-04i
## [243] -1.640587e-04-8.351788e-05i 1.682820e-06-7.302932e-05i
## [245] -1.259792e-04-2.899497e-04i 4.240992e-05+1.341758e-04i
## [247] -1.324361e-05-2.522587e-04i -1.550712e-04-7.489535e-05i
## [249] -3.001335e-04-2.402411e-05i 2.115791e-04-1.866074e-04i
## [251] -2.264768e-04-1.405681e-04i -1.979349e-05+2.864389e-04i
## [253] 2.313987e-04+3.167367e-04i -4.700202e-06-1.638496e-04i
## [255] -3.405291e-04+3.310650e-05i 5.089533e-05+2.672930e-04i
## [257] 2.588869e-04-1.104809e-04i -3.034898e-05+3.390678e-04i
## [259] -6.627508e-05+1.076257e-04i 1.378652e-04-1.991130e-05i
## [261] 7.634097e-05-2.219788e-04i 2.275418e-04-1.714935e-04i
## [263] 2.850108e-04+3.195419e-05i 4.243863e-05-1.894555e-05i
## [265] -3.890863e-04-7.458194e-05i 1.046722e-05-3.058013e-05i
## [267] 2.320069e-04-2.238481e-04i -2.534595e-04+1.427819e-04i
## [269] 3.381169e-04+1.090086e-04i -2.002367e-04+4.423808e-05i
## [271] -2.964989e-04+1.481743e-04i -2.522756e-04+3.020921e-04i
## [273] 2.381884e-04-2.645714e-04i -3.029610e-04-3.977400e-05i
## [275] -1.697574e-04+1.644715e-04i 1.837816e-04+6.168018e-05i
## [277] -1.591048e-04+1.039434e-04i 1.189749e-04-5.282830e-05i
## [279] 1.428918e-04-1.655413e-05i 1.253279e-04-2.679445e-04i
## [281] -1.617753e-04+2.576105e-04i 1.146753e-04-6.960150e-05i
## [283] -2.838065e-04-2.044314e-04i -2.210062e-04+1.938058e-05i
## [285] 4.828256e-04-8.611750e-05i 6.654846e-05-3.764722e-05i
## [287] 2.115966e-04-4.127100e-05i -2.688970e-04+3.547699e-04i
## [289] -1.317760e-04+2.519557e-04i 3.205019e-04+5.242191e-05i
## [291] 2.051228e-04-9.030344e-06i 2.645722e-04-3.146360e-05i
## [293] -3.240725e-04-3.971966e-04i -4.095139e-04+4.447124e-04i
## [295] 2.115185e-04-8.563088e-05i 1.903530e-04-1.755484e-04i
## [297] 1.674044e-05-8.238987e-05i -3.595862e-05+8.865995e-06i
## [299] -3.392349e-04+1.066757e-04i -4.363520e-04+8.592792e-05i
## [301] 2.041094e-04-8.343553e-05i -1.547610e-04+1.631643e-04i
## [303] 7.104828e-05+1.084786e-04i 4.151813e-04+1.266292e-04i
## [305] 4.452955e-05-2.262181e-04i
##
## $per
## [1] 1.643811e-06 1.086162e-07 1.658890e-07 1.913549e-07 2.900706e-07
## [6] 5.131820e-08 1.428155e-07 8.914760e-08 4.204096e-08 1.204302e-07
## [11] 3.236912e-09 3.182780e-08 2.749932e-07 3.568693e-08 1.612379e-08
## [16] 9.781978e-08 5.630266e-08 2.200174e-07 4.358569e-08 3.751684e-08
## [21] 3.607453e-08 7.763068e-08 1.787913e-07 2.121214e-08 7.778316e-08
## [26] 2.766534e-08 1.018061e-08 1.161084e-07 4.143594e-07 1.175525e-07
## [31] 1.967428e-09 5.594127e-09 5.459505e-08 2.772927e-07 9.424208e-08
## [36] 9.652769e-08 3.949798e-08 1.850811e-07 5.599469e-08 5.660382e-08
## [41] 1.149443e-07 1.065094e-07 9.780702e-09 1.152355e-07 2.053365e-08
## [46] 7.080604e-08 4.229716e-08 8.242866e-08 2.708495e-08 8.212147e-09
## [51] 1.956319e-08 7.154934e-08 2.016506e-07 8.046412e-08 8.572509e-08
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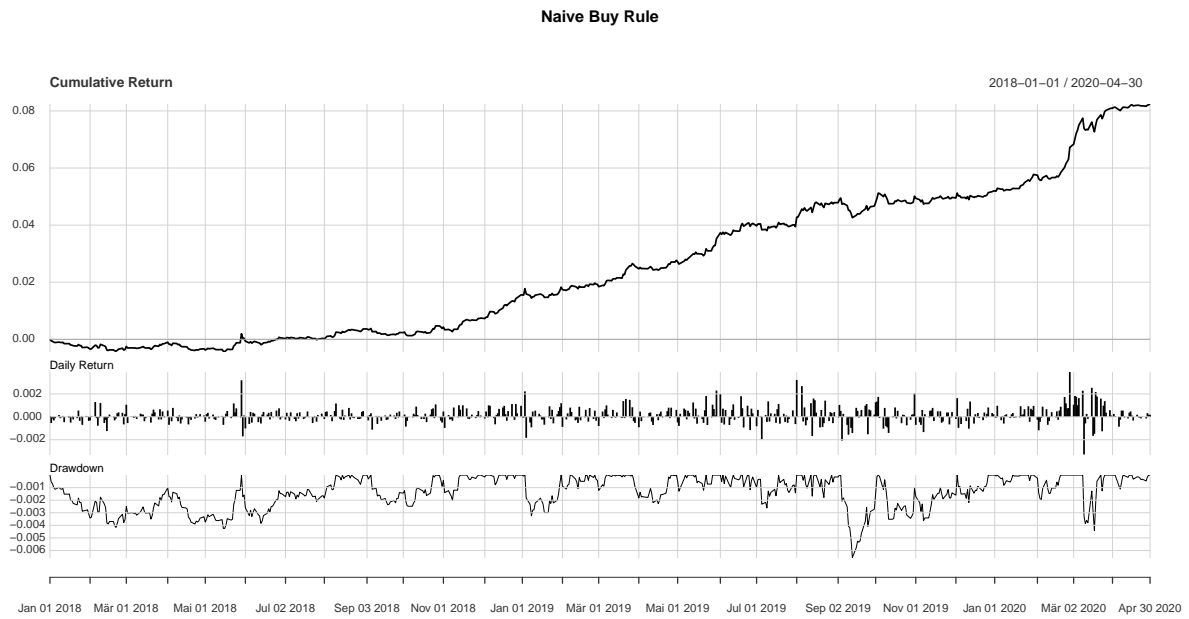


Figure 3: peridodogramm

### 3.2. using simple methods

in Section 2 we have learned different indicators and models for timeseries. these models and indicators are now used to trade the underlying asset. As an example we are taking the MA Crossings, as mentioned 2.3.3. the points where the two MAs cross, are now used to create a trading signal. when the longer MA comes from below to the crossing we are going long the asset and if it approaches the point from above we're shorting the position. Technically we apply a 1 to a vector at each crossing, where we intend to buy and apply a -1 at the points we want to sell.



sna

[2015-10-30/2020-04-30]

Last 1731.67728658523



Okt 30 2015

Apr 03 2017

Apr 02 2018

Apr 01 2019

Mär 3

3.2.1. sma signals to trade

sna

[2015-10-30/2020-04-30]

Last 1731.67728658523



Okt 30 2015

Apr 03 2017

Apr 02 2018

Apr 01 2019

Mär 31 2020

sna

[2015-10-30/2020-04-30]

Last 1731.67728658523



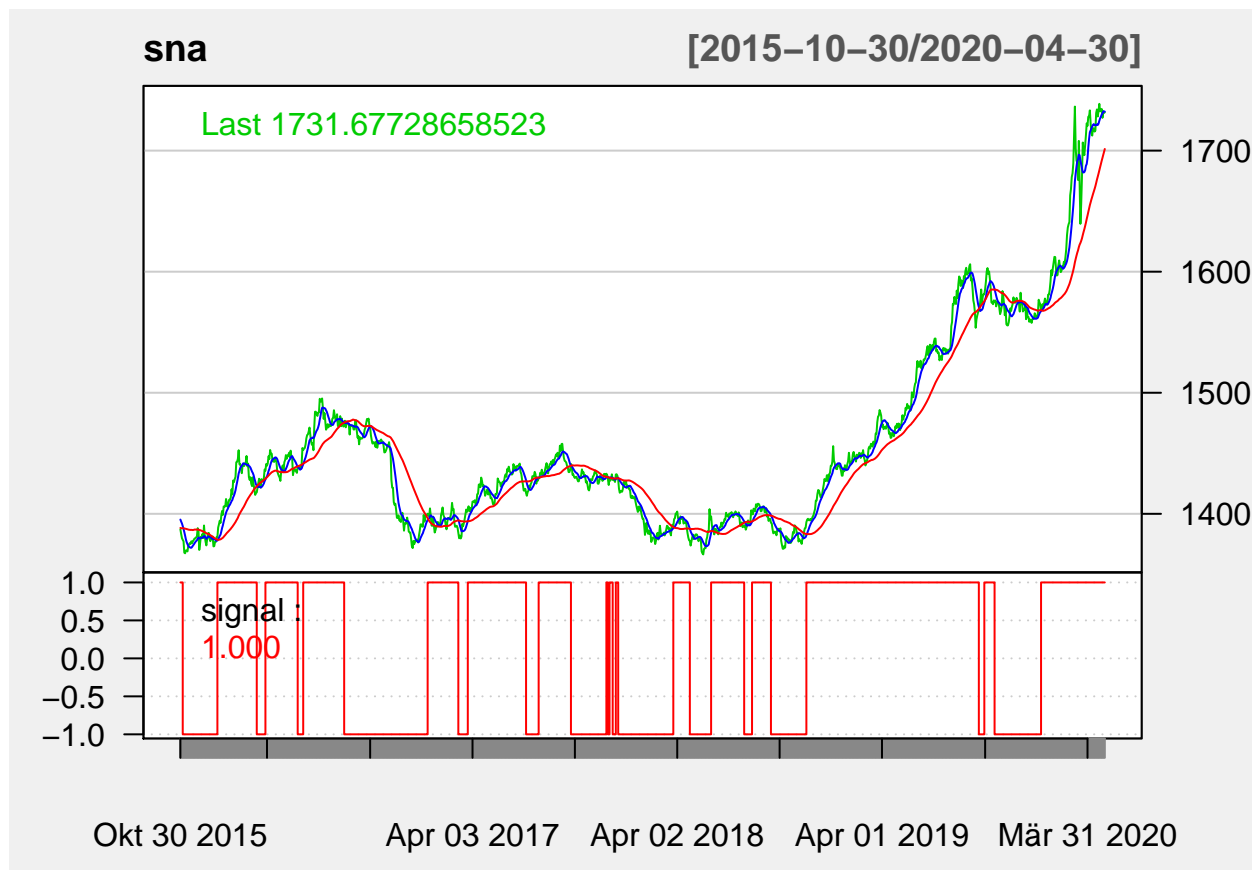
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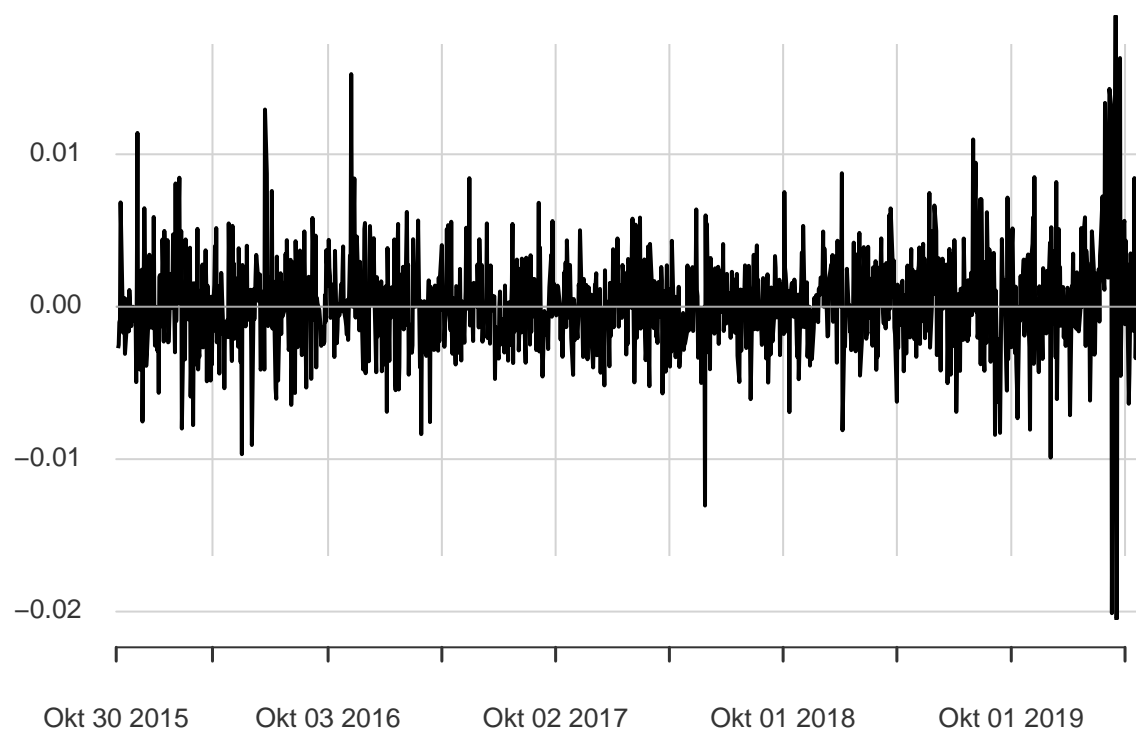
Mär 31 2020



## [1] 0.0001624021

returns daily

2015-10-30 / 2020-04-30



## Naive Rule: Cum Returns

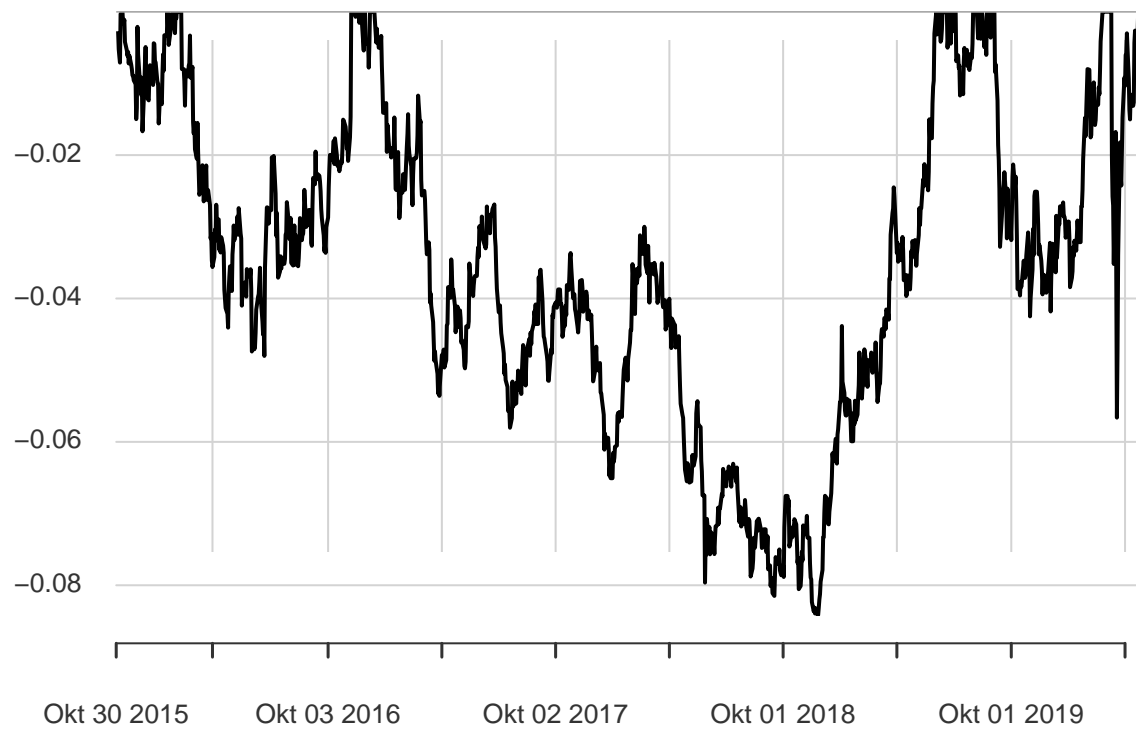
2015-11-02 / 2020-04-30





# Naive Rule: Percentage Drawdown

2015-10-30 / 2020-04-30



## Naive Buy Rule

