# Output tables for the test of Multiple comparisons.

#### September 24, 2018

## 1 Average rankings of Friedman test

Average ranks obtained by applying the Friedman procedure

Conf 4 Conf 5 Conf 6 Conf 7

Table 1: Average Rankings of the algorithms

Friedman statistic considering reduction performance (distributed according to chi-square with 6 degrees of freedom: 4.971429. P-value computed by Friedman Test: 0.5474828246699731. Iman and Davenport statistic considering reduction performance (distributed according to F-distribution with 6 and 24 degrees of freedom: 0.794521.

P-value computed by Iman and Daveport Test: 0.5833663179134587.

### 2 Post hoc comparisons

Results achieved on post hoc comparisons for  $\alpha = 0.05, \alpha = 0.10$  and adjusted p-values.

### 2.1 P-values for $\alpha = 0.05$

i	algorithms	$z = (R_0 - R_i)/SE$	d	$_{ m Holm}$	Shaffer
21	Conf 3 vs. Conf 4	1.903005	0.05704	0.002381	0.002381
20	Conf 1 vs. Conf 3	1.46385	0.143235	0.0025	0.0025
6	Conf 4 vs. Conf 6	1.46385	0.143235	0.002632	0.002632
∞	Conf 4 vs. Conf 5	1.317465	0.187683	0.002778	0.002778
	Conf 4 vs. Conf 7	1.17108	0.241567	0.002941	0.002941
91	Conf 1 vs. Conf 6	1.024695	0.305507	0.003125	0.003125
5	Conf 2 vs. Conf 3	1.024695	0.305507	0.003333	0.003333
4	Conf 1 vs. Conf 5	0.87831	0.379775	0.003571	0.003571
2	Conf 2 vs. Conf 4	0.87831	0.379775	0.003846	0.003846
[2	Conf 1 vs. Conf 7	0.731925	0.464214	0.004167	0.004167
Ξ	Conf 3 vs. Conf 7	0.731925	0.464214	0.004545	0.004545
9	Conf 3 vs. Conf 5	0.58554	0.558185	0.005	0.005
6	Conf 2 vs. Conf 6	0.58554	0.558185	0.005556	0.005556
∞	Conf 1 vs. Conf 2	0.439155	0.660549	0.00625	0.00625
7	Conf 3 vs. Conf 6	0.439155	0.660549	0.007143	0.007143
9	Conf 1 vs. Conf 4	0.439155	0.660549	0.008333	0.008333
ಬ	Conf 2 vs. Conf 5	0.439155	0.660549	0.01	0.01
4	Conf 2 vs. Conf 7	0.29277	0.769698	0.0125	0.0125
33	Conf 6 vs. Conf 7	0.29277	0.769698	0.016667	0.016667
2	Conf 5 vs. Conf 7	0.146385	0.883617	0.025	0.025
	Conf 5 vs. Conf 6	0.146385	0.883617	0.02	0.02

Table 2: P-values Table for  $\alpha = 0.05$ 

Nemenyi's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.002381$ . Holm's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.002381$ . Bergmann's procedure does not reject any hypotheses.

i	algorithms	$z = (R_0 - R_i)/SE$	d	Holm	Shaffer
21	Conf 3 vs. Conf 4	1.903005	0.05704	0.004762	0.004762
20	Conf 1 vs. Conf 3	1.46385	0.143235	0.005	0.005
19	Conf 4 vs. Conf 6	1.46385	0.143235	0.005263	0.005263
18	Conf 4 vs. Conf 5	1.317465	0.187683	0.005556	0.005556
17	Conf 4 vs. Conf 7	1.17108	0.241567	0.005882	0.005882
16	Conf 1 vs. Conf 6	1.024695	0.305507	0.00625	0.00625
15	Conf 2 vs. Conf 3	1.024695	0.305507	0.006667	0.006667
14	Conf 1 vs. Conf 5	0.87831	0.379775	0.007143	0.007143
13	Conf 2 vs. Conf 4	0.87831	0.379775	0.007692	0.007692
12	_	0.731925	0.464214	0.008333	0.008333
11	Conf 3 vs. Conf 7	0.731925	0.464214	0.009091	0.009091
10	Conf 3 vs. Conf 5	0.58554	0.558185	0.01	0.01
6	Conf 2 vs. Conf 6	0.58554	0.558185	0.0111111	0.011111
œ	Conf 1 vs. Conf 2	0.439155	0.660549	0.0125	0.0125
7	Conf 3 vs. Conf 6	0.439155	0.660549	0.014286	0.014286
9	Conf 1 vs. Conf 4	0.439155	0.660549	0.016667	0.016667
20	Conf 2 vs. Conf 5	0.439155	0.660549	0.02	0.02
4	Conf 2 vs. Conf 7	0.29277	0.769698	0.025	0.025
က	Conf 6 vs. Conf 7	0.29277	0.769698	0.033333	0.033333
2	Conf 5 vs. Conf 7	0.146385	0.883617	0.05	0.05
1	Conf 5 vs. Conf 6	0.146385	0.883617	0.1	0.1

Table 3: P-values Table for  $\alpha = 0.10$ 

Nemenyi's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.004762$ . Holm's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.004762$ . Bergmann's procedure does not reject any hypotheses.

$p_{Berg}$	1.197837	2.148524	2.148524	2.148524	2.174099	3.055071	3.360578	3.360578	3.417979	3.417979	3.417979	3.417979	3.907293	3.907293	3.907293	3.907293	3.907293	3.907293	3.907293	3.907293	3.907293
$p_{Shaf}$	1.197837	2.148524	2.148524	2.815242	3.623499	4.582606	4.582606	4.582606	4.582606	5.106357	5.106357	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846
$p_{Holm}$	1.197837	2.864698	2.864698	3.37829	4.106632	4.888113	4.888113	5.316857	5.316857	5.570572	5.570572	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846	5.581846
$p_{Neme}$	1.197837	3.007933	3.007933	3.941338	5.072898	6.415649	6.415649	7.975285	7.975285	9.748501	9.748501	11.721878	11.721878	13.871533	13.871533	13.871533	13.871533	16.163657	16.163657	18.555967	18.555967
unadjusted $p$	0.05704	0.143235	0.143235	0.187683	0.241567	0.305507	0.305507	0.379775	0.379775	0.464214	0.464214	0.558185	0.558185	0.660549	0.660549	0.660549	0.660549	0.769698	0.769698	0.883617	0.883617
hypothesis	Conf 3 vs .Conf 4	Conf 1 vs .Conf 3	Conf 4 vs .Conf 6	Conf 4 vs .Conf 5	Conf 4 vs .Conf 7	Conf 1 vs .Conf 6	Conf 2 vs .Conf 3	Conf 1 vs .Conf 5	Conf 2 vs .Conf 4	Conf 1 vs .Conf 7	Conf 3 vs .Conf 7	Conf 3 vs .Conf 5	Conf 2 vs .Conf 6	Conf 1 vs .Conf 2	Conf 3 vs. Conf 6	Conf 1 vs .Conf 4	Conf 2 vs .Conf 5	Conf 2 vs .Conf 7	Conf 6 vs .Conf 7	Conf 5 vs .Conf 7	Conf 5 vs .Conf 6
i	1	2	က	4	D	9	۲-	∞	6	10	11	12	13	14	15	16	17	18	19	20	21

Table 4: Adjusted p-values