Event shapes and jet rates in electron-positron annihilation at NNLO

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Abstract

This article gives the perturbative NNLO results for the most commonly used event shape variables associated to three-jet events in electron-positron annihilation: Thrust, heavy jet mass, wide jet broadening, total jet broadening, C parameter and the Durham three-to-two jet transition variable. In addition the NNLO results for the jet rates corresponding to the Durham, Geneva, Jade-E0 and Cambridge jet algorithms are presented.

1 Introduction

The experiments at LEP (CERN), SLC (SLAC) and PETRA (DESY) have collected a wealth of data from electron-positron annihilation with hadronic final state over a wide range of energies. Of particular interest are three-jet events, which can be used to extract the value of the strong coupling constant. Three-jet events are well suited for this task because the leading term in a perturbative calculation of three-jet observables is already proportional to the strong coupling. In comparing experiments to theory it is important to restrict oneself to infra-red safe observables. For three-jet events in electron-positron annihilation there is a well established set of infra-red safe observables, which is widely used. These are the event shape variables consisting of thrust, heavy jet mass, wide jet broadening, total jet broadening and the *C*-parameter. In addition there are observables related to a specific jet definition. First of all these are the jet rates associated to the different jet definitions. In this paper the following jet algorithms are considered: Durham, Geneva, Jade-E0 and Cambridge. As the Durham jet algorithm is the most popular one, for this jet algorithm also the three-to-two jet transition variable is studied.

All these observables can be calculated in perturbation theory. In this article I present the next-to-next-to-leading order (NNLO) results for these observables. For completeness I also include the next-to-leading order (NLO) and leading order (LO) results.

Another group published results for these observables earlier on in [1–3], but omitted certain subtraction terms related to soft gluons. The present calculation is based on the numerical Monte-Carlo program reported in [4,5]. The additional soft gluon subtraction terms modify the distributions in the peak region. Meanwhile the other group has added the missing subtraction terms and the two programs are now for the main part of the observables in good agreement. A few remaining differences are discussed in the numerical section. A detailed account of the subtraction terms used in this calculation is given in a companion paper [6].

For the thrust distribution there exists an independent calculation of the logarithmic terms based on soft-collinear effective theory [7]. This calculation should agree with the NNLO result for small values of (1-T). For large values of (1-T) the logarithmic terms alone are not sufficient to give an accurate result. On the other hand the perturbative calculation of this paper gives the correct NNLO result for large and intermediate values of (1-T), but has its limitations due to the Monte-Carlo integration method for very small values of (1-T). This gives a region of overlap where the perturbative NNLO result and the one obtained from SCET should agree, and indeed they do.

This article reports the pure perturbative results for the event shapes. Not included are soft-gluon resummations [7–10] nor power corrections [11, 12].

It should be mentioned that the results of this paper rely heavily on research carried out in the past years: Integration techniques for two-loop amplitudes [13–16], the calculation of the relevant tree-, one- and two-loop-amplitudes [17–29], routines for the numerical evaluation of polylogarithms [30–32], methods to handle infrared singularities [33–51] and experience from the NNLO calculations of $e^+e^- \rightarrow 2$ jets and other processes [40,52–68].

This paper is organised as follows: Section 2 gives the definition of the observables related to three-jet events in electron-positron annihilation. Section 3 describes the perturbative calculation of these observables. Section 4 gives the numerical results. Finally, section 5 contains a

summary. In an appendix a useful algorithm for the determination of the thrust axis is described.

2 Definition of the observables

The event shape variable thrust [69, 70] is defined by

$$T = \frac{\max_{\vec{n}} \sum_{j} |\vec{p}_{j} \cdot \vec{n}|}{\sum_{j} |\vec{p}_{j}|}, \tag{1}$$

where \vec{p}_j denotes the three-momentum of particle j and the sum runs over all particles in the final state. The thrust variable maximises the total longitudinal momentum along the unit vector \vec{n} . The value of \vec{n} , for which the maximum is attained is called the thrust axis and denoted by \vec{n}_T . The value of thrust ranges between 1/2 and 1, where T=1 corresponds to an ideal collinear two-jet event and T=1/2 corresponds to a perfectly spherical event. Usually one considers instead of thrust T the variable (1-T), such that the two-jet region corresponds to $(1-T) \to 0$. For three-parton events we have $(1-T) \le 1/3$.

The plane orthogonal to the thrust axis divides the space into two hemispheres H_1 and H_2 . These are used to define the following event shape variables: The hemisphere masses [71] are defined by

$$M_i^2 = \left(\sum_{j \in H_i} p_j\right)^2, \quad i = 1, 2,$$
 (2)

where p_j denotes the four-momentum of particle j. The heavy hemisphere mass M_H and the light hemisphere mass M_L are then defined by

$$M_H^2 = \max(M_1^2, M_2^2), \qquad M_L^2 = \min(M_1^2, M_2^2).$$
 (3)

The light hemisphere mass is a four-jet observable and vanishes for three partons. For the heavy jet mass it is convenient to introduce the dimensionless quantity

$$\rho = \frac{M_H^2}{O^2},\tag{4}$$

where Q is the centre-of-mass energy. For three-parton events we have $\rho \le 1/3$. In leading order the distribution of the heavy jet mass is identical to the distribution of (1-T).

The hemisphere broadenings [72, 73] are defined by

$$B_{i} = \frac{\sum_{j \in H_{i}} |\vec{p}_{j} \times \vec{n}_{T}|}{2\sum_{k} |\vec{p}_{k}|}, \quad i = 1, 2,$$
 (5)

where the sum over j runs over all particles in one of the hemispheres, whereas the sum over k is over all particles in the final state. The wide jet broadening B_W , the narrow jet broadening B_N and the total jet broadening B_T are defined by

$$B_W = \max(B_1, B_2), \quad B_N = \min(B_1, B_2), \quad B_T = B_1 + B_2.$$
 (6)

The narrow jet broadening is a four-jet observable and vanishes for three partons. For three-parton events we have $B_W, B_T \le 1/(2\sqrt{3})$.

The C- and D-parameters [74,75] are obtained from the linearised momentum tensor

$$\theta^{ij} = \frac{1}{\sum_{l} |\vec{p}_{l}|} \sum_{k} \frac{p_{k}^{i} p_{k}^{j}}{|\vec{p}_{k}|}, \quad i, j = 1, 2, 3,$$
(7)

where the sum runs over all final state particles and p_k^i is the *i*-th component of the three-momentum \vec{p}_k of particle k in the c.m. system. The tensor θ is normalised to have unit trace. In terms of the eigenvalues of the θ tensor, λ_1 , λ_2 , λ_3 , with $\lambda_1 + \lambda_2 + \lambda_3 = 1$, one defines

$$C = 3(\lambda_1\lambda_2 + \lambda_2\lambda_3 + \lambda_3\lambda_1),$$

$$D = 27\lambda_1\lambda_2\lambda_3.$$
 (8)

The range of values is $0 \le C, D \le 1$. The *D*-parameter is again a four-jet observable and vanishes for three partons. For three-parton events we have $C \le 3/4$. The *C*-parameter exhibits in perturbation theory a singularity at the three-parton boundary C = 3/4 [76].

The production rate for three-jet events is defined by the ratio of the cross section for three-jet events by the total hadronic cross section

$$R_3 = \frac{\sigma_{3-jet}}{\sigma_{tot}}. (9)$$

This depends on the definition of the jet algorithm, usually specified through a resolution variable and a recombination prescription. The clustering procedure of a jet algorithm in electron-positron annihilation is in most cases defined through the following steps:

- 1. Define a resolution parameter y_{cut}
- 2. For every pair (p_k, p_l) of final-state particles compute the corresponding resolution variable y_{kl} .
- 3. If y_{ij} is the smallest value of y_{kl} computed above and $y_{ij} < y_{cut}$ then combine (p_i, p_j) into a single jet ('pseudo-particle') with momentum p_{ij} according to a recombination prescription.
- 4. Repeat until all pairs of objects (particles and/or pseudo-particles) have $y_{kl} > y_{cut}$.

The various jet algorithms differ in the precise definition of the resolution variable and the recombination prescription. The various recombination prescriptions are:

1. E-scheme:

$$E_{ij} = E_i + E_j, \quad \vec{p}_{ij} = \vec{p}_i + \vec{p}_j.$$
 (10)

The E-scheme conserves energy and momentum, but for massless particles i and j the recombined four-momentum is not massless.

2. E0-scheme:

$$E_{ij} = E_i + E_j, \qquad \vec{p}_{ij} = \frac{E_i + E_j}{|\vec{p}_i + \vec{p}_j|} (\vec{p}_i + \vec{p}_j).$$
 (11)

The E0-scheme conserves energy, but not momentum. For massless particles i and j is the recombined four-momentum again massless.

3. P-scheme:

$$E_{ij} = \frac{\left| \vec{p}_i + \vec{p}_j \right|}{E_i + E_j} \left(E_i + E_j \right) = \left| \vec{p}_i + \vec{p}_j \right|, \qquad \vec{p}_{ij} = \vec{p}_i + \vec{p}_j. \tag{12}$$

The P-scheme conserves momentum, but not energy. For massless particles i and j is the recombined four-momentum again massless, as in the E0-scheme.

For the Durham [77], Geneva [78] and Jade-E0 [79] jet algorithms the resolution variables and the recombination prescriptions are defined as follows:

Durham:
$$y_{ij} = \frac{2\min(E_i^2, E_j^2) \left(1 - \cos \theta_{ij}\right)}{Q^2}, \quad \text{E-scheme,}$$
Geneva:
$$y_{ij} = \frac{8}{9} \cdot \frac{2E_i E_j \left(1 - \cos \theta_{ij}\right)}{\left(E_i + E_j\right)^2}, \quad \text{E-scheme,}$$

$$\text{Jade-E0:} \quad y_{ij} = \frac{2E_i E_j \left(1 - \cos \theta_{ij}\right)}{Q^2}, \quad \text{E0-scheme,}$$

$$(13)$$

where E_i and E_j are the energies of particles i and j, and θ_{ij} is the angle between \vec{p}_i and \vec{p}_j . Q is the centre-of-mass energy. The jet transition variable y_{23} is the value of the jet resolution parameter y_{cut} , for which the event changes from a three-jet to a two-jet configuration. Similar, y_{34} is defined as the value of the resolution parameter, where the event changes from a four-jet to a three-jet configuration. The three-jet rate is related to the jet transition variables y_{23} and y_{34} :

$$R_3(y_{cut}) = \int_{y_{cut}}^1 dy_{23} \frac{d\sigma}{dy_{23}} - \int_{y_{cut}}^1 dy_{34} \frac{d\sigma}{dy_{34}}.$$
 (14)

The Cambridge algorithm [80] distinguishes an ordering variable v_{ij} and a resolution variable y_{ij} . The Cambridge algorithm is defined as follows:

- 1. Select a pair of objects (p_i, p_j) with the minimal value of the ordering variable v_{ij} .
- 2. If $y_{ij} < y_{cut}$ they are combined, one recomputes the relevant values of the ordering variable and goes back to the first step.
- 3. If $y_{ij} \ge y_{cut}$ and $E_i < E_j$ then i is defined as a resolved jet and deleted from the table.
- 4. Repeat until only one object is left in the table. This object is also defined as a jet and clustering is finished.

As ordering variable

$$v_{ij} = 2\left(1 - \cos\theta_{ij}\right) \tag{15}$$

is used. The resolution variable is as in the Durham algorithm

$$y_{ij} = \frac{2\min(E_i^2, E_j^2) \left(1 - \cos \theta_{ij}\right)}{Q^2} \tag{16}$$

and the E-scheme is used as recombination prescription.

3 Perturbative expansion

The perturbative expansion of a differential distribution for any infrared-safe observable O for the process $e^+e^- \rightarrow 3$ jets can be written up to NNLO as

$$\frac{O^n}{\sigma_{tot}(\mu)}\frac{d\sigma(\mu)}{dO} = \frac{\alpha_s(\mu)}{2\pi}\frac{O^n d\bar{A}_O(\mu)}{dO} + \left(\frac{\alpha_s(\mu)}{2\pi}\right)^2 \frac{O^n d\bar{B}_O(\mu)}{dO} + \left(\frac{\alpha_s(\mu)}{2\pi}\right)^3 \frac{O^n d\bar{C}_O(\mu)}{dO}. (17)$$

 \bar{A}_O gives the LO result, \bar{B}_O the NLO correction and \bar{C}_O the NNLO correction. The variable n denotes the moment of the distribution. Unless stated otherwise, the value n=1 is used as default. σ_{tot} denotes the total hadronic cross section calculated up to the relevant order. The arbitrary renormalisation scale is denoted by μ . The n-th moment is given by

$$\langle O^n \rangle = \frac{1}{\sigma_{tot}} \int O^n \frac{d\sigma}{dO} dO.$$
 (18)

In practise the numerical program computes the distribution

$$\frac{O^n}{\sigma_0(\mu)}\frac{d\sigma(\mu)}{dO} = \frac{\alpha_s(\mu)}{2\pi}\frac{O^n dA_O(\mu)}{dO} + \left(\frac{\alpha_s(\mu)}{2\pi}\right)^2\frac{O^n dB_O(\mu)}{dO} + \left(\frac{\alpha_s(\mu)}{2\pi}\right)^3\frac{O^n dC_O(\mu)}{dO}, (19)$$

normalised to σ_0 , which is the LO cross section for $e^+e^- \to \text{hadrons}$, instead of the normalisation to σ_{tot} . There is a simple relation between the two distributions: The functions A_O , B_O and C_O are related to the functions \bar{A}_O , \bar{B}_O and \bar{C}_O by

$$\bar{A}_O = A_O,
\bar{B}_O = B_O - A_{tot}A_O,
\bar{C}_O = C_O - A_{tot}B_O - (B_{tot} - A_{tot}^2)A_O,$$

where

$$A_{tot} = \frac{3(N_c^2 - 1)}{4N_c},$$

$$B_{tot} = \frac{N_c^2 - 1}{8N_c} \left[\left(\frac{243}{4} - 44\zeta_3 \right) N_c + \frac{3}{4N_c} + (8\zeta_3 - 11) N_f \right].$$

 N_c denotes the number of colours and N_f the number of light quark flavours. A_{tot} and B_{tot} are obtained from the perturbative expansion of σ_{tot} [81–83]:

$$\sigma_{tot} = \sigma_0 \left(1 + \frac{\alpha_s}{2\pi} A_{tot} + \left(\frac{\alpha_s}{2\pi} \right)^2 B_{tot} + \mathcal{O}(\alpha_s^3) \right). \tag{20}$$

The perturbative calculation of the inclusive hadronic cross section $\langle \sigma \rangle^{(tot)}$ is actually known to $O(\alpha_s^3)$ [84,85], although we need here only the coefficients up to $O(\alpha_s^3)$.

It is sufficient to calculate the functions \bar{A}_O , \bar{B}_O and \bar{C}_O for a fixed renormalisation scale μ_0 , which can be taken conveniently to be equal to the centre-of-mass energy: $\mu_0 = Q$. The scale variation can be restored from the renormalisation group equation

$$\mu^{2} \frac{d}{d\mu^{2}} \left(\frac{\alpha_{S}}{2\pi}\right) = -\frac{1}{2} \beta_{0} \left(\frac{\alpha_{S}}{2\pi}\right)^{2} - \frac{1}{4} \beta_{1} \left(\frac{\alpha_{S}}{2\pi}\right)^{3} - \frac{1}{8} \beta_{2} \left(\frac{\alpha_{S}}{2\pi}\right)^{4} + O(\alpha_{s}^{5}),$$

$$\beta_{0} = \frac{11}{3} C_{A} - \frac{4}{3} T_{R} N_{f},$$

$$\beta_{1} = \frac{34}{3} C_{A}^{2} - 4 \left(\frac{5}{3} C_{A} + C_{F}\right) T_{R} N_{f},$$

$$\beta_{2} = \frac{2857}{54} C_{A}^{3} - \left(\frac{1415}{27} C_{A}^{2} + \frac{205}{9} C_{A} C_{F} - 2C_{F}^{2}\right) T_{R} N_{f} + \left(\frac{158}{27} C_{A} + \frac{44}{9} C_{F}\right) T_{R}^{2} N_{f}^{2}.$$

$$(21)$$

The colour factors are defined as usual by

$$C_A = N_c, \quad C_F = \frac{N_c^2 - 1}{2N_c}, \quad T_R = \frac{1}{2}.$$
 (22)

The values of the functions \bar{A}_O , \bar{B}_O and \bar{C}_O at a scale μ are then obtained from the ones at the scale μ_0 by

$$\bar{A}_{O}(\mu) = \bar{A}_{O}(\mu_{0}),
\bar{B}_{O}(\mu) = \bar{B}_{O}(\mu_{0}) + \frac{1}{2}\beta_{0}\ln\left(\frac{\mu^{2}}{\mu_{0}^{2}}\right)\bar{A}_{O}(\mu_{0}),
\bar{C}_{O}(\mu) = \bar{C}_{O}(\mu_{0}) + \beta_{0}\ln\left(\frac{\mu^{2}}{\mu_{0}^{2}}\right)\bar{B}_{O}(\mu_{0}) + \frac{1}{4}\left[\beta_{1} + \beta_{0}^{2}\ln\left(\frac{\mu^{2}}{\mu_{0}^{2}}\right)\right]\ln\left(\frac{\mu^{2}}{\mu_{0}^{2}}\right)\bar{A}_{O}(\mu_{0}).$$
(23)

Finally, an approximate solution of eq. (21) for α_s is given by

$$\frac{\alpha_s(\mu)}{2\pi} = \frac{2}{\beta_0 L} \left\{ 1 - \frac{\beta_1}{\beta_0^2} \frac{\ln L}{L} + \frac{\beta_1^2}{\beta_0^4 L^2} \left[\left(\frac{1}{2} - \ln L \right)^2 + \frac{\beta_0 \beta_2}{\beta_1^2} - \frac{5}{4} \right] \right\},\tag{24}$$

where $L = \ln(\mu^2/\Lambda^2)$.

The function C_O can be decomposed into six colour pieces

$$C_O = \frac{(N_c^2 - 1)}{8N_c} \left[N_c^2 C_O^{lc} + C_O^{sc} + \frac{1}{N_c^2} C_O^{ssc} + N_f N_c C_O^{nf} + \frac{N_f}{N_c} C_O^{nfsc} + N_f^2 C_O^{nfnf} \right]. \tag{25}$$

In addition, there are singlet contributions, which arise from interference terms of amplitudes, where the electro-weak boson couples to two different fermion lines. These singlet contributions are expected to be numerically small [28, 86, 87] and neglected in the present calculation. We define

$$C_O|_{lc} = \frac{\left(N_c^2 - 1\right)}{8N_c} N_c^2 C_O^{lc}, \quad C_O|_{sc} = \frac{\left(N_c^2 - 1\right)}{8N_c} C_O^{sc}, \quad C_O|_{ssc} = \frac{\left(N_c^2 - 1\right)}{8N_c} \frac{1}{N_c^2} C_O^{ssc}, \tag{26}$$

$$C_{\mathcal{O}}|_{nf} = \frac{\left(N_c^2 - 1\right)}{8N_c} N_f N_c C_{\mathcal{O}}^{nf}, \quad C_{\mathcal{O}}|_{nfsc} = \frac{\left(N_c^2 - 1\right)}{8N_c} \frac{N_f}{N_c} C_{\mathcal{O}}^{nfsc}, \quad C_{\mathcal{O}}|_{nfnf} = \frac{\left(N_c^2 - 1\right)}{8N_c} N_f^2 C_{\mathcal{O}}^{nfnf},$$

e.g. the function $C_O|_{lc}$ includes the colour factors.

The functions A_O , B_O and C_O are calculated for a fixed renormalisation scale equal to the centre-of-mass energy: $\mu_0 = Q$. They depend only on the value of the observable O. Since only QCD corrections with non-singlet quark couplings are taken into account and singlet contributions to C_O are neglected, the functions A_O , B_O and C_O do not depend on electro-weak couplings.

4 Numerical results

In this section I present the numerical results for the event shape variables and jet rates at next-to-next-to-leading order. All results have been obtained by numerical Monte-Carlo integration. The Monte-Carlo integration introduces a statistical error, which will be quoted with all results. For the infrared singularities a hybrid method between subtraction and slicing has been used. Unless stated otherwise all results have been obtained with the slicing parameter

$$\eta = \frac{s_{min}}{Q^2} = 10^{-5}. (27)$$

It should be noted that the slicing procedure introduces in addition a systematic error. The size of this error can be estimated by varying the slicing parameter η . However, lowering the slicing parameter will increase the statistical error. A practical criteria is to require that the variation due to the slicing parameter is smaller than the statistical error, with the possible exception for the boundaries of the distributions. Imposing this criteria $\eta=10^{-5}$ turns out to be a good compromise between accuracy and efficiency. The boundaries of the distributions close to the two-jet region deserve special attention: There the value of the observable is comparable to η and one expects sizable corrections. I will discuss the dependence on the slicing parameter in the close-to-two-jet region in detail for a few examples.

In a first series of plots I show the comparison of the NNLO results with the NLO and LO

results for the LEP I centre-of-mass energy $\sqrt{Q^2} = m_Z$ with $\alpha_S = 0.118$. The results for the event shape variables thrust, heavy jet mass, wide jet broadening, total jet broadening, C parameter and three-to-two jet transition variable y_{23} are shown in figs. 1 to 6. For each of these observable the distribution weighted by the observable and normalised to the total hadronic cross section is shown, e.g. for thrust the distribution

$$\frac{1-T}{\sigma} \frac{d\sigma}{d(1-T)} \tag{28}$$

is shown. The corresponding plots for the jet rates for the jet algorithms of Durham, Geneva, Jade-E0 and Cambridge are shown in figs. 7 to 10. In all these plots is the leading-order prediction shown in light blue, the next-to-leading-order prediction is shown in pink and the next-to-next-to-leading order prediction is shown in dark blue. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu = Q/2$ to $\mu = 2Q$. In addition the experimental data points [88] from the Aleph experiment (where available) are also shown in these plot. Note that the theory predictions in these plots are the pure perturbative predictions. Power corrections or soft gluon resummation effects are not included in these results.

Numerical results for centre-of-mass energies different from $\sqrt{Q^2} = m_Z$ are also easily obtained. As an example I show in fig. 11 the thrust distribution at centre-of-mass energies of $\sqrt{Q^2} = 91.2 \text{GeV}$, 133GeV, 161GeV, 172GeV, 183GeV, 189GeV, 200GeV, 206GeV, again with experimental data points from the Aleph experiment. As for the LEP II energies the bin size of the experimental data is rather large, I show in fig. 11 the distribution

$$\frac{1}{\sigma} \frac{d\sigma}{d(1-T)} \tag{29}$$

without an additional factor (1-T).

The most important results of this paper are the perturbative coefficients A_O , B_O and C_O . For the six event shape variables (thrust, heavy jet mass, wide jet broadening, total jet broadening, C-parameter and the three-to-two jet transition variable) the numerical values for the LO functions A_O , the NLO functions B_O and the NNLO functions C_O , all weighted by C_O , are given in tables 1 to 7. The corresponding values for the jet rates defined according to the Durham, Geneva, Jade-EO or Cambridge algorithms are given in tables 8 to 11. These values are obtained by Monte-Carlo integration and the statistical Monte-Carlo integration error is indicated in these tables. The systematic error due to the slicing parameter η is not included in these tables, but will be discussed below. The values for the Durham jet rate have already been given in ref. [4]. Due to a typo in the numerical program which was corrected after publication of [4] the corrected values are repeated here.

For the six event shape variables the LO functions A_O , the NLO functions B_O and the NNLO functions C_O are also shown in figs. 12 to 17. The leading-order function A_O and the next-to-leading order function B_O can be computed with high precision and the graphs are shown simply with solid lines in figs. 12-17. For the next-to-next-to-leading order function C_O the Monte-Carlo integration errors are typically at the per cent level, and this function is shown with errorbars corresponding to the Monte-Carlo integration errors in figs. 12-17.

The NNLO function C_O can be split up into the contributions from the individual colour factors

$$C_O|_{lc}, C_O|_{sc}, C_O|_{ssc}, C_O|_{nf}, C_O|_{nfsc}, C_O|_{nfnf}$$
 (30)

defined in eq. (26). For the event shape variables the contributions from the individual colour factors to C_O are given in tables 12 to 18. For the jet rates the contributions from the individual colour factors to C_O are given in tables 19 to 20. In addition the individual colour contributions are plotted for the six event shape variables in figs. 18-23.

In fig. 24-26 the results for the thrust distribution are compared with the calculation of Becher and Schwartz based on soft-collinear effective theory [7]. The leading-order, next-to-leading-order and next-to-next-to-leading order coefficients A_{1-T} , B_{1-T} and C_{1-T} are compared in fig. 24. The individual colour factors of the coefficient C_{1-T} are compared in fig. 25. The effective theory gives a good description of the thrust distribution for small values of (1-T). For values of (1-T) close to 1 the effective theory is not valid and deviations from the perturbative result can be seen. On the other hand the perturbative result obtained from Monte-Carlo integration has its limitation through the slicing parameter introduced to handle the infrared singularities. The deviations of the numerical Monte-Carlo results for the C_{1-T} coefficient from the SCET results for values of (1-T) < 0.003 are an artefact of the slicing parameter. In figs. 24 and 25 the value $\eta = 10^{-5}$ was used for the slicing parameter. To study the situation in more detail, I show in fig. 26 the variation of the numerical result for the leading colour factor of C_{1-T} with the slicing parameter η . The numerical results for $\eta = 10^{-5}$, $\eta = 10^{-7}$ and $\eta = 10^{-9}$ are plotted. For smaller values of η the SCET result is approached.

As a further example I also show the dependence on the slicing parameter η for the colour factor N_c^2 for the next-to-next-to-leading order coefficient $C_{y_{23}}$ for the three-to-two jet transition distribution in fig. 27. In this plot the numerical results for $\eta = 10^{-5}$, $\eta = 10^{-7}$ and $\eta = 10^{-9}$ are shown.

Fig. 28 compares the results of this calculation to the updated ones from ref. [1]. For the six event shape distributions one observes good agreement with the exception of the three-to-two jet transition distribution at very small values of y_{23} . The discrepancy at small values of y_{23} can be traced back to the colour factor N_c^2 and could have an explanation in terms of a systematic error due to the slicing parameter. The study of the η -dependence in fig. 27 gives hints in this direction, but does not give a conclusive answer. Although in fig. 27 the three results for $\eta = 10^{-5}$, $\eta = 10^{-7}$ and $\eta = 10^{-9}$ are consistent with each other, using $\eta = 10^{-9}$ instead of $\eta = 10^{-5}$ for the comparison with ref. [1] would reduce the discrepancy significantly (but also enlarge the errorbars). Given the complexity of the calculation the agreement of the two numerical programs in all other distributions is remarkable.

5 Conclusions

In this article I reported on the NNLO calculation of observables associated to three-jet events in electron-positron annihilation. I provided NNLO results for the event shape variables thrust,

heavy jet mass, wide jet broadening, total jet broadening, C parameter and the Durham three-totwo jet transition variable. In addition the NNLO results for the jet rates defined in the schemes of Durham, Geneva, Jade-E0 and Cambridge were given. The results of this paper will be useful for an extraction of α_s from three-jet quantities.

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A Calculation of the thrust for a single parton event

For the event shape variable thrust and the ones related to it, it is necessary to determine the maximum

$$\max_{\vec{n}} \sum_{j} \left| \vec{p}_{j} \cdot \vec{n} \right| \tag{31}$$

over all orientations of the unit vector \vec{n} . The sum runs over all final state particles j. For the NNLO calculation we have either 3, 4 or 5 partons in the final state. Of course there are numerical algorithms which can be used to find a local maximum. However the computational cost for such a minimisation/maximisation is comparable to the cost for the matrix elements and therefore not negligible. Furthermore it is non-trivial to ensure that the found maximum is actually the global maximum.

There is a better way to calculate thrust and the thrust axis for a small number of final state particles. This method finds the exact global maximum in $2^{N-1} - 1$ steps for N final state particles. Let us define N signs $s_i \in \{-1, 1\}$ by

$$\vec{p}_j \cdot \vec{n} = s_j \left| \vec{p}_j \cdot \vec{n} \right|. \tag{32}$$

Of course the correct values for the signs s_j are only known once the thrust axis \vec{n} is known. But we know in advance that the *N*-tuple $(s_1, s_2, ..., s_N)$ will be one configuration out of the 2^N possible ones. We can now step over all 2^N possibilities $(s_1, s_2, ..., s_N)$. For a given *N*-tuple $(s_1, s_2, ..., s_N)$ we define

$$\vec{P} = s_1 \vec{p}_1 + s_2 \vec{p}_2 + \dots + s_N \vec{p}_N. \tag{33}$$

We then have

$$\max_{\vec{n}} \sum_{j} |\vec{p}_{j} \cdot \vec{n}| = \max_{\vec{n}} \sum_{j} s_{j} \vec{p}_{j} \cdot \vec{n} = \max_{\vec{n}} \vec{P} \cdot \vec{n}$$
 (34)

This expression is maximised for $\vec{n} = \vec{P}/|\vec{P}|$. Next, one checks if the *N*-tuple $(s_1, s_2, ..., s_N)$ is actually allowed by verifying eq. (32) for all j = 1, ..., N. The maximum is then given by the maximum value obtained from all allowed *N*-tuples. It is actually sufficient to restrict the search to $2^{N-1} - 1$ possibilities, since thrust is invariant under

$$\vec{n} \rightarrow -\vec{n},$$
 (35)

and the two cases where all signs are equal can be excluded due to momentum conservation. With this algorithm we have to check for five-parton final states 15 configurations to find the global maximum, whereas for four-parton final states 7 configurations have to be checked. For the case of three massless particles in the final state the algorithm does not need to be used, since there is a general formula for the thrust axis: The thrust axis is given in this case by the direction of the most energetic particle [89].

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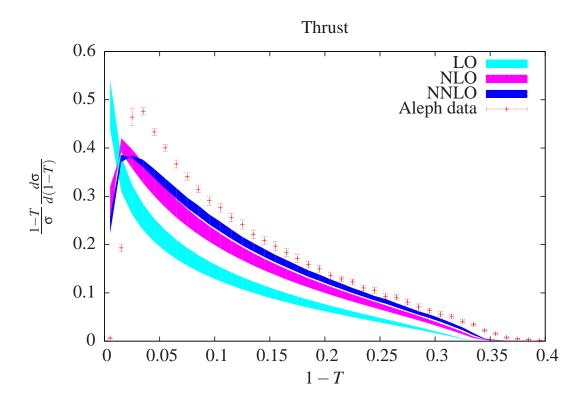


Figure 1: The thrust distribution at LO, NLO and NNLO at $\sqrt{Q^2} = m_Z$ with $\alpha_s(m_Z) = 0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu = m_Z/2$ to $\mu = 2m_Z$. In addition the experimental data points from the Aleph experiment are shown.

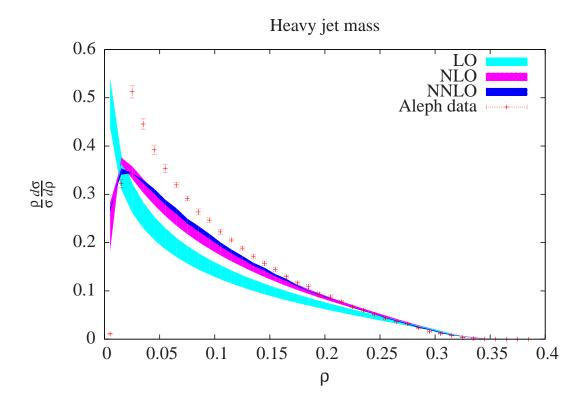


Figure 2: The distribution of the heavy jet mass at LO, NLO and NNLO at $\sqrt{Q^2} = m_Z$ with $\alpha_s(m_Z) = 0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu = m_Z/2$ to $\mu = 2m_Z$. In addition the experimental data points from the Aleph experiment are shown.

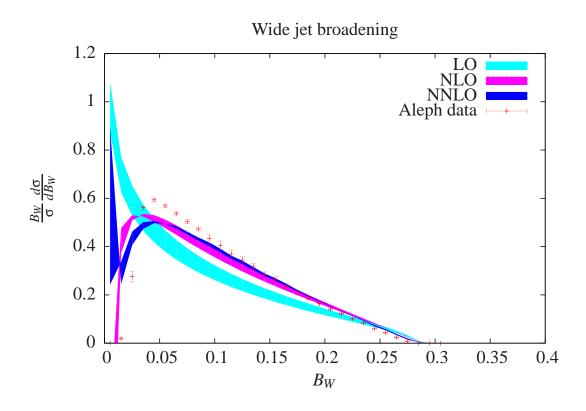


Figure 3: The wide jet broadening distribution at LO, NLO and NNLO at $\sqrt{Q^2} = m_Z$ with $\alpha_s(m_Z) = 0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu = m_Z/2$ to $\mu = 2m_Z$. In addition the experimental data points from the Aleph experiment are shown.

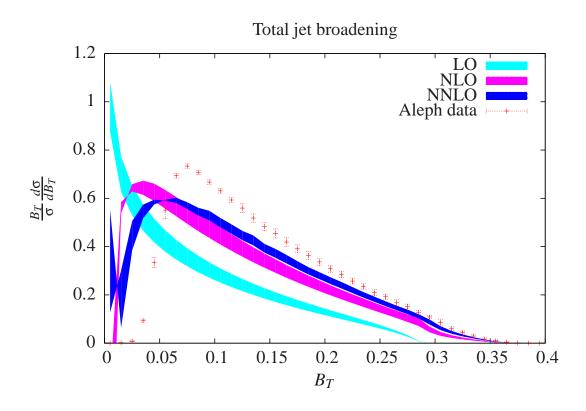


Figure 4: The total jet broadening distribution at LO, NLO and NNLO at $\sqrt{Q^2} = m_Z$ with $\alpha_s(m_Z) = 0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu = m_Z/2$ to $\mu = 2m_Z$. In addition the experimental data points from the Aleph experiment are shown.

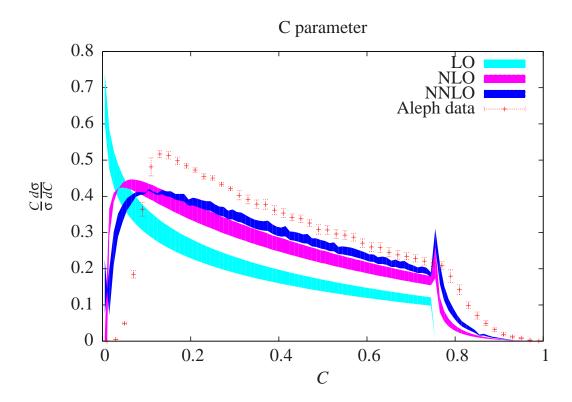


Figure 5: The *C*-parameter distribution at LO, NLO and NNLO at $\sqrt{Q^2} = m_Z$ with $\alpha_s(m_Z) = 0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu = m_Z/2$ to $\mu = 2m_Z$. In addition the experimental data points from the Aleph experiment are shown.

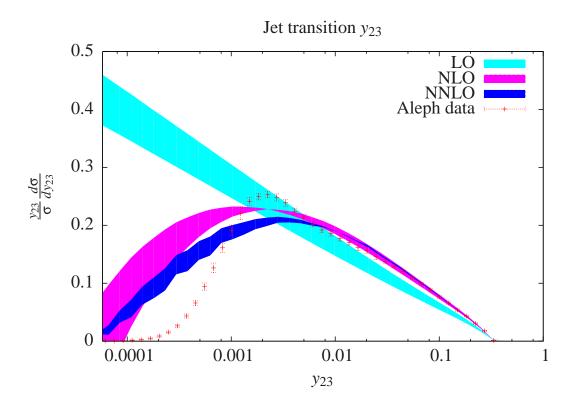


Figure 6: The three-to-two jet transition distribution at LO, NLO and NNLO at $\sqrt{Q^2} = m_Z$ with $\alpha_s(m_Z) = 0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu = m_Z/2$ to $\mu = 2m_Z$. In addition the experimental data points from the Aleph experiment are shown.

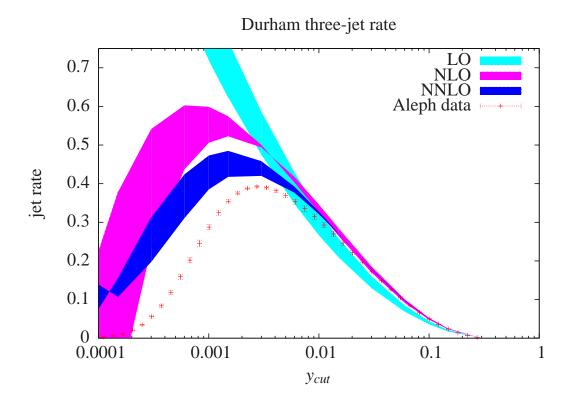


Figure 7: The three jet rate with the Durham jet algorithm at LO, NLO and NNLO at $\sqrt{Q^2} = m_Z$ with $\alpha_s(m_Z) = 0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu = m_Z/2$ to $\mu = 2m_Z$. In addition the experimental data points from the Aleph experiment are shown.

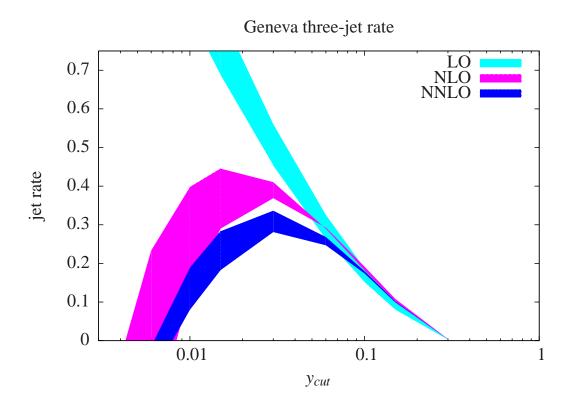


Figure 8: The three jet rate with the Geneva jet algorithm at LO, NLO and NNLO at $\sqrt{Q^2}=m_Z$ with $\alpha_s(m_Z)=0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu=m_Z/2$ to $\mu=2m_Z$.

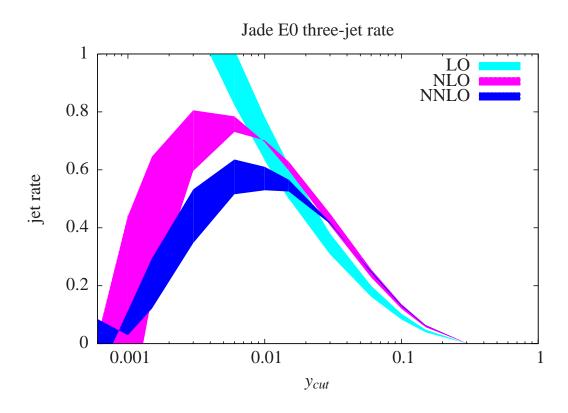


Figure 9: The three jet rate with the Jade E0 jet algorithm at LO, NLO and NNLO at $\sqrt{Q^2}=m_Z$ with $\alpha_s(m_Z)=0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu=m_Z/2$ to $\mu=2m_Z$.

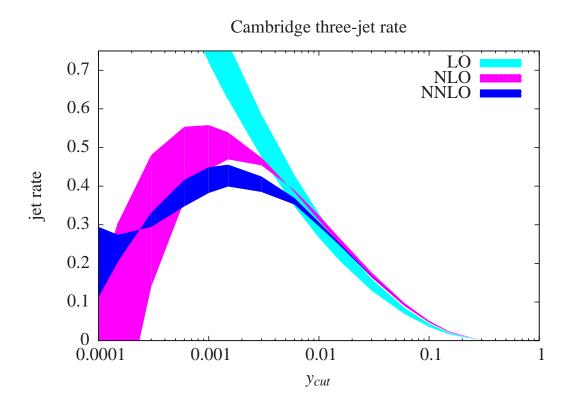


Figure 10: The three jet rate with the Cambridge jet algorithm at LO, NLO and NNLO at $\sqrt{Q^2} = m_Z$ with $\alpha_s(m_Z) = 0.118$. The bands give the range for the theoretical prediction obtained from varying the renormalisation scale from $\mu = m_Z/2$ to $\mu = 2m_Z$.

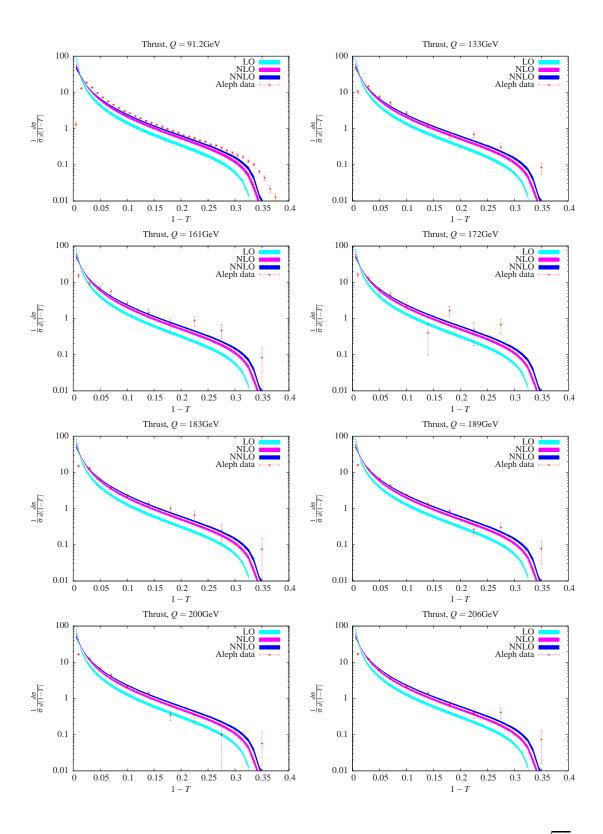


Figure 11: The thrust distribution at LO, NLO and NNLO at various values of $\sqrt{Q^2}$. The bands correspond to a variation of the renormalisation scale from $\mu = m_Z/2$ to $\mu = 2m_Z$. The experimental data points are from the Aleph experiment.

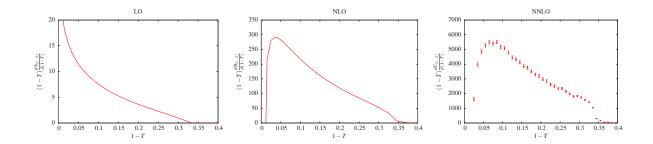


Figure 12: Coefficients of the leading-order $(A_{(1-T)}, \text{ left})$, next-to-leading-order $(B_{(1-T)}, \text{ middle})$ and next-to-next-to-leading order $(C_{(1-T)}, \text{ right})$ contributions to the thrust distribution, all weighted by (1-T). For the coefficient $C_{(1-T)}$ the Monte-Carlo integration errors are also shown.

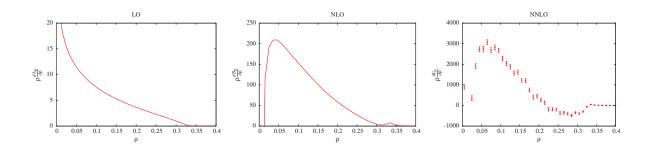


Figure 13: Coefficients of the leading-order $(A_{\rho}, \text{ left})$, next-to-leading-order $(B_{\rho}, \text{ middle})$ and next-to-next-to-leading order $(C_{\rho}, \text{ right})$ contributions to the heavy jet mass distribution, all weighted by ρ . For the coefficient C_{ρ} the Monte-Carlo integration errors are also shown.

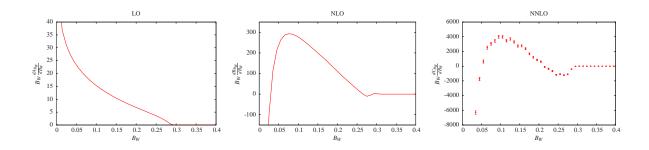


Figure 14: Coefficients of the leading-order (A_{B_W} , left), next-to-leading-order (B_{B_W} , middle) and next-to-next-to-leading order (C_{B_W} , right) contributions to the wide jet broadening distribution, all weighted by B_W . For the coefficient C_{B_W} the Monte-Carlo integration errors are also shown.

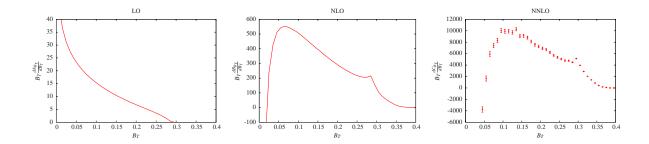


Figure 15: Coefficients of the leading-order (A_{B_T} , left), next-to-leading-order (B_{B_T} , middle) and next-to-next-to-leading order (C_{B_T} , right) contributions to the total jet broadening distribution, all weighted by B_T . For the coefficient C_{B_T} the Monte-Carlo integration errors are also shown.

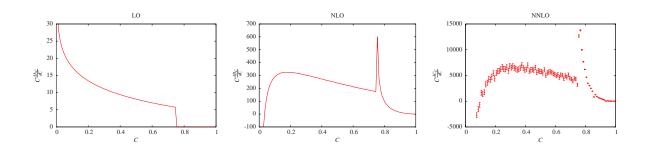


Figure 16: Coefficients of the leading-order (A_C , left), next-to-leading-order (B_C , middle) and next-to-next-to-leading order (C_C , right) contributions to the C-parameter distribution, all weighted by C. For the coefficient C_C the Monte-Carlo integration errors are also shown.

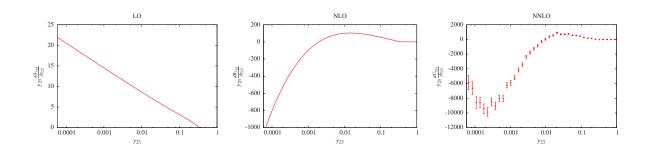


Figure 17: Coefficients of the leading-order ($A_{y_{23}}$, left), next-to-leading-order ($B_{y_{23}}$, middle) and next-to-next-to-leading order ($C_{y_{23}}$, right) contributions to the three-to-two jet transition distribution, all weighted by y_{23} . For the coefficient $C_{y_{23}}$ the Monte-Carlo integration errors are also shown.

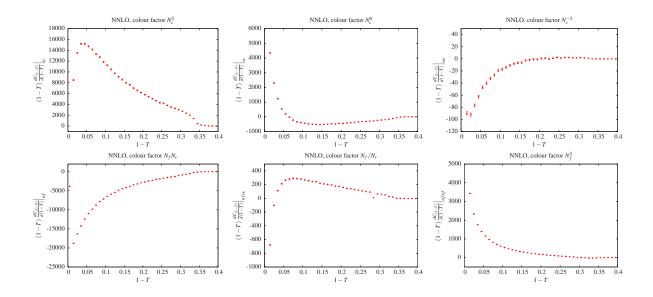


Figure 18: The NNLO coefficient $C_{(1-T)}$ for the thrust distribution split up into individual colour factors.

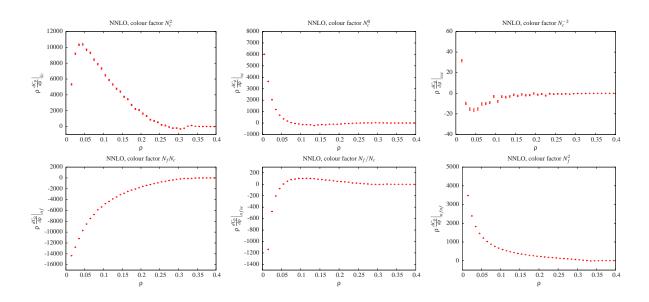


Figure 19: The NNLO coefficient C_{ρ} for the heavy jet mass distribution split up into individual colour factors.

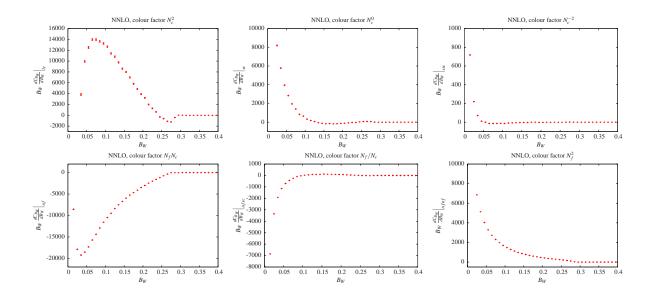


Figure 20: The NNLO coefficient C_{B_W} for the wide jet broadening distribution split up into individual colour factors.

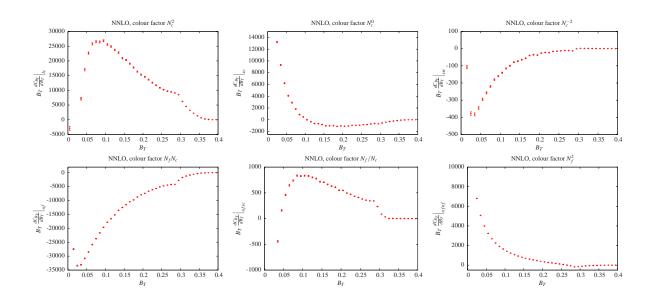


Figure 21: The NNLO coefficient C_{B_T} for the total jet broadening distribution split up into individual colour factors.

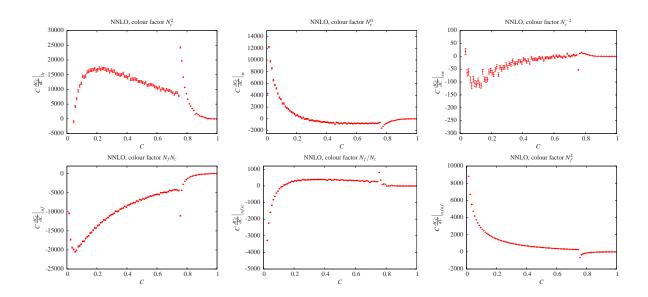


Figure 22: The NNLO coefficient C_C for the C-parameter distribution split up into individual colour factors.

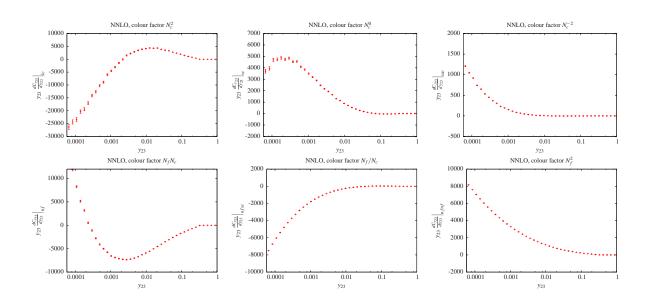


Figure 23: The NNLO coefficient $C_{y_{23}}$ for the three-to-two jet transition distribution split up into individual colour factors.

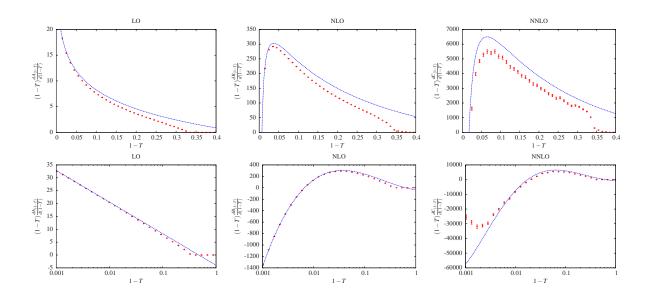


Figure 24: Comparison of the results for the coefficients of the leading-order $(A_{(1-T)}, \text{ left})$, next-to-leading-order $(B_{(1-T)}, \text{ middle})$ and next-to-next-to-leading order $(C_{(1-T)}, \text{ right})$ contributions to the thrust distribution from perturbative QCD (red) and SCET (blue line). The upper row shows the distribution with a linear scale for (1-T), the lower row shows the distribution with a logarithmic scale for (1-T).

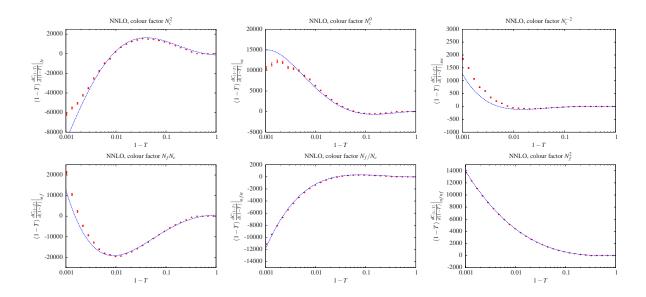


Figure 25: Comparison of the individual colour factors of the next-to-next-to-leading order coefficient $C_{(1-T)}$ for the thrust distribution between perturbative QCD (red) and SCET (blue line). The distributions are shown with a logarithmic scale for (1-T). The deviations of the Monte-Carlo results for small values of (1-T) are due to the slicing procedure.

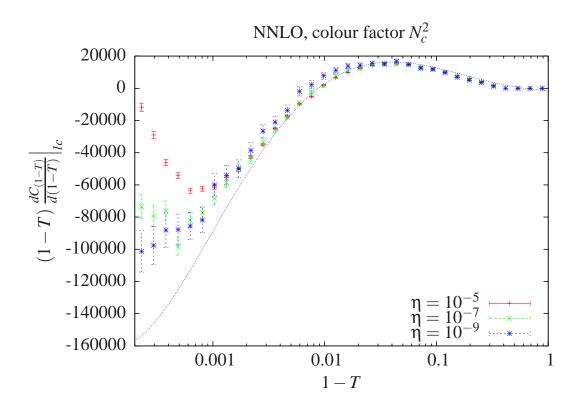


Figure 26: Comparison of the next-to-next-to-leading order coefficient $C_{(1-T)}$ for the colour factor N_c^2 for the thrust distribution between the numerical Monte-Carlo program for various values of η and SCET (blue line).

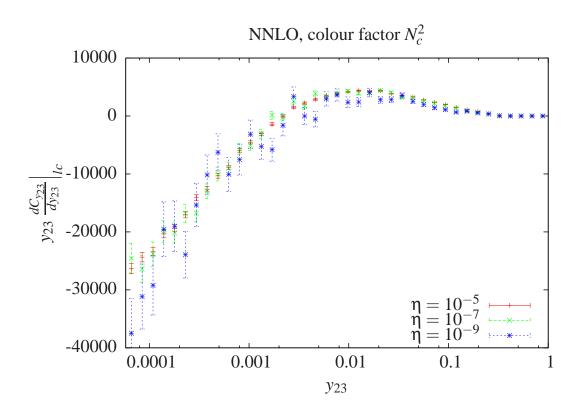


Figure 27: Dependence of the numerical Monte-Carlo result for the next-to-next-to-leading order coefficient $C_{y_{23}}$ for the colour factor N_c^2 for the three-to-two jet transition distribution on the slicing parameter η .

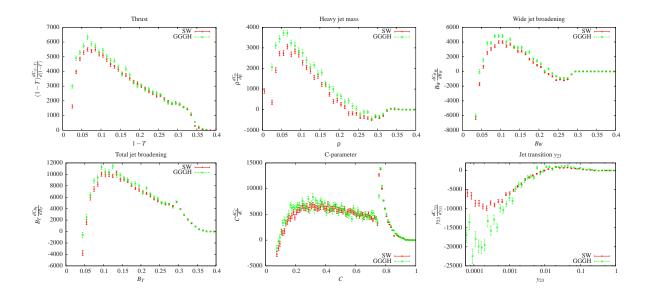


Figure 28: Comparison of the next-to-next-to-leading order coefficient C_O for the six distributions between ref. [1] and the present work.

(1-T)	$(1-T)\frac{dA_{(1-T)}}{d(1-T)}$	$(1-T)\frac{dB_{(1-T)}}{d(1-T)}$	$(1-T)\frac{dC_{(1-T)}}{d(1-T)}$
0.005	$2.5797(2) \cdot 10^{1}$	$-4.957(3) \cdot 10^2$	$-9.0(1) \cdot 10^3$
0.015	$1.8299(1) \cdot 10^{1}$	$2.166(3) \cdot 10^2$	$-3.3(1) \cdot 10^3$
0.025	$1.5411(1) \cdot 10^{1}$	$2.809(3) \cdot 10^2$	$1.6(1) \cdot 10^3$
0.035	$1.35230(9) \cdot 10^{1}$	$2.920(3) \cdot 10^2$	$4.0(1) \cdot 10^3$
0.045	$1.21030(9) \cdot 10^{1}$	$2.877(2) \cdot 10^2$	$4.9(1) \cdot 10^3$
0.055	$1.09692(8) \cdot 10^{1}$	$2.772(2) \cdot 10^2$	$5.3(1) \cdot 10^3$
0.065	$1.00228(8) \cdot 10^{1}$	$2.638(2) \cdot 10^2$	$5.5(1) \cdot 10^3$
0.075	$9.2112(7) \cdot 10^{0}$	$2.505(2) \cdot 10^2$	$5.4(1) \cdot 10^3$
0.085	$8.5022(7) \cdot 10^{0}$	$2.371(2) \cdot 10^2$	$5.5(1) \cdot 10^3$
0.095	$7.8724(7) \cdot 10^{0}$	$2.240(2) \cdot 10^2$	$5.2(1) \cdot 10^3$
0.105	$7.3045(6) \cdot 10^{0}$	$2.113(2) \cdot 10^2$	$5.1(1) \cdot 10^3$
0.115	$6.7891(6) \cdot 10^{0}$	$1.993(2) \cdot 10^2$	$4.8(1) \cdot 10^3$
0.125	$6.3179(6) \cdot 10^{0}$	$1.878(2) \cdot 10^2$	$4.5(1) \cdot 10^3$
0.135	$5.8820(6) \cdot 10^{0}$	$1.768(2) \cdot 10^2$	$4.3(1) \cdot 10^3$
0.145	$5.4791(6) \cdot 10^{0}$	$1.666(2) \cdot 10^2$	$4.1(1) \cdot 10^3$
0.155	$5.1030(5) \cdot 10^{0}$	$1.572(2) \cdot 10^2$	$3.9(1) \cdot 10^3$
0.165	$4.7484(5) \cdot 10^{0}$	$1.475(2) \cdot 10^2$	$3.8(1) \cdot 10^3$
0.175	$4.4141(5) \cdot 10^{0}$	$1.393(2) \cdot 10^2$	$3.5(1) \cdot 10^3$
0.185	$4.0962(5) \cdot 10^{0}$	$1.306(2) \cdot 10^2$	$3.29(9) \cdot 10^3$
0.195	$3.7931(5) \cdot 10^{0}$	$1.231(2) \cdot 10^2$	$3.20(9) \cdot 10^3$
0.205	$3.5028(4) \cdot 10^{0}$	$1.153(2) \cdot 10^2$	$2.98(9) \cdot 10^3$
0.215	$3.2220(4) \cdot 10^{0}$	$1.081(2) \cdot 10^2$	$2.85(9) \cdot 10^3$
0.225	$2.9494(4) \cdot 10^{0}$	$1.011(2) \cdot 10^2$	$2.63(8) \cdot 10^3$
0.235	$2.6826(4) \cdot 10^{0}$	$9.47(1) \cdot 10^{1}$	$2.50(8) \cdot 10^3$
0.245	$2.4223(4) \cdot 10^{0}$	$8.82(1) \cdot 10^{1}$	$2.33(8) \cdot 10^3$
0.255	$2.1634(3) \cdot 10^{0}$	$8.21(1) \cdot 10^{1}$	$2.35(7) \cdot 10^3$
0.265	$1.9062(3) \cdot 10^{0}$	$7.54(1) \cdot 10^{1}$	$2.15(7) \cdot 10^3$
0.275	$1.6470(3) \cdot 10^{0}$	$6.94(1) \cdot 10^{1}$	$1.97(6) \cdot 10^3$
0.285	$1.3841(3) \cdot 10^{0}$	$6.30(1) \cdot 10^{1}$	$1.80(6) \cdot 10^3$
0.295	$1.1169(2) \cdot 10^{0}$	$5.64(1) \cdot 10^{1}$	$1.83(5) \cdot 10^3$
0.305	$8.415(2) \cdot 10^{-1}$	$4.888(9) \cdot 10^{1}$	$1.74(5) \cdot 10^3$
0.315	$5.567(2) \cdot 10^{-1}$	$4.135(8) \cdot 10^{1}$	$1.57(4) \cdot 10^3$
0.325	$2.593(1) \cdot 10^{-1}$	$3.353(5) \cdot 10^{1}$	$1.42(2) \cdot 10^3$
0.335	$1.706(3) \cdot 10^{-2}$	$2.108(3) \cdot 10^{1}$	$1.03(1) \cdot 10^3$
0.345	0	$8.570(8) \cdot 10^{0}$	$2.96(5) \cdot 10^2$
0.355	0	$4.474(5) \cdot 10^0$	$1.55(3) \cdot 10^2$
0.365	0	$2.434(3) \cdot 10^{0}$	$5.3(1) \cdot 10^{1}$
0.375	0	$1.301(2) \cdot 10^{0}$	$3.57(7) \cdot 10^{1}$
0.385	0	$6.44(1) \cdot 10^{-1}$	$1.09(2) \cdot 10^{1}$
0.395	0	$2.818(8) \cdot 10^{-1}$	$1.8(2) \cdot 10^{-1}$
0.405	0	$5.12(3) \cdot 10^{-2}$	$-1.0(1) \cdot 10^{-3}$
0.415	0	$1.45987(8) \cdot 10^{-5}$	$-1.950(2) \cdot 10^{-1}$
0.425	0	$4.66279(3) \cdot 10^{-5}$	$-9(4) \cdot 10^{-3}$
0.435	0	o ´	$-1(1)\cdot 10^{-3}$
0.445	0	0	0

Table 1: Coefficients of the leading-order $(A_{(1-T)})$, next-to-leading-order $(B_{(1-T)})$ and next-to-next-to-leading order $(C_{(1-T)})$ contributions to the thrust distribution.

	44	I AD	dC .
ρ	$\rho \frac{dA_{\rho}}{d\rho}$	$\rho \frac{dB_{\rho}}{d\rho}$	$\rho \frac{dC_{\rho}}{d\rho}$
0.005	$2.5797(2) \cdot 10^{1}$	$-6.243(3) \cdot 10^2$	$9(1) \cdot 10^2$
0.015	$1.8299(1) \cdot 10^{1}$	$1.162(3) \cdot 10^2$	$-3.0(1) \cdot 10^3$
0.025	$1.5411(1) \cdot 10^{1}$	$1.917(3) \cdot 10^2$	$4(1) \cdot 10^2$
0.035	$1.35230(9) \cdot 10^{1}$	$2.088(3) \cdot 10^2$	$1.9(1) \cdot 10^3$
0.045	$1.21030(9) \cdot 10^{1}$	$2.092(2) \cdot 10^2$	$2.7(1) \cdot 10^3$
0.055	$1.09692(8) \cdot 10^{1}$	$2.020(2) \cdot 10^2$	$2.7(1) \cdot 10^3$
0.065	$1.00228(8) \cdot 10^{1}$	$1.918(2) \cdot 10^2$	$3.1(1) \cdot 10^3$
0.075	$9.2112(7) \cdot 10^{0}$	$1.809(2) \cdot 10^2$	$2.7(1) \cdot 10^3$
0.085	$8.5022(7) \cdot 10^0$	$1.695(2) \cdot 10^2$	$2.8(1) \cdot 10^3$
0.095	$7.8724(7) \cdot 10^0$	$1.590(2) \cdot 10^2$	$2.7(1) \cdot 10^3$
0.105	$7.3045(6) \cdot 10^0$	$1.476(2) \cdot 10^2$	$2.3(1) \cdot 10^3$
0.115	$6.7891(6) \cdot 10^0$	$1.370(2) \cdot 10^2$	$2.0(1) \cdot 10^3$
0.125	$6.3179(6) \cdot 10^0$	$1.269(2) \cdot 10^2$	$1.9(1) \cdot 10^3$
0.135	$5.8820(6) \cdot 10^{0}$	$1.161(2) \cdot 10^2$	$1.6(1) \cdot 10^3$
0.145	$5.4791(6) \cdot 10^{0}$	$1.060(2) \cdot 10^2$	$1.6(1) \cdot 10^3$
0.155	$5.1030(5) \cdot 10^0$	$9.63(1) \cdot 10^{1}$	$1.2(1) \cdot 10^3$
0.165	$4.7484(5) \cdot 10^{0}$	$8.67(1) \cdot 10^{1}$	$1.2(1) \cdot 10^3$
0.175	$4.4141(5) \cdot 10^{0}$	$7.81(1) \cdot 10^{1}$	$8(1) \cdot 10^2$
0.185	$4.0962(5) \cdot 10^{0}$	$7.01(1) \cdot 10^{1}$	$4.0(9) \cdot 10^2$
0.195	$3.7931(5) \cdot 10^{0}$	$6.23(1) \cdot 10^{1}$	$4.6(9) \cdot 10^2$
0.205	$3.5028(4) \cdot 10^{0}$	$5.50(1) \cdot 10^{1}$	$2.7(9) \cdot 10^2$
0.215	$3.2220(4) \cdot 10^{0}$	$4.79(1) \cdot 10^1$	$1.4(9) \cdot 10^2$
0.225	$2.9494(4) \cdot 10^{0}$	$4.17(1) \cdot 10^{1}$	$-1.9(8) \cdot 10^2$
0.235	$2.6826(4) \cdot 10^{0}$	$3.55(1) \cdot 10^{1}$	$-1.8(8) \cdot 10^2$
0.245	$2.4223(4) \cdot 10^{0}$	$2.96(1) \cdot 10^{1}$	$-2.0(8) \cdot 10^2$
0.255	$2.1634(3) \cdot 10^{0}$	$2.411(9) \cdot 10^{1}$	$-3.7(7) \cdot 10^2$
0.265	$1.9062(3) \cdot 10^{0}$	$1.871(9) \cdot 10^{1}$	$-3.5(7) \cdot 10^2$
0.275	$1.6470(3) \cdot 10^{0}$	$1.398(8) \cdot 10^{1}$	$-4.1(6) \cdot 10^2$
0.285	$1.3841(3) \cdot 10^{0}$	$9.63(8) \cdot 10^{0}$	$-4.9(6) \cdot 10^2$
0.295	$1.1169(2) \cdot 10^{0}$	$6.11(7) \cdot 10^{0}$	$-3.5(5) \cdot 10^2$
0.305	$8.415(2) \cdot 10^{-1}$	$3.48(6) \cdot 10^{0}$	$-4.0(4) \cdot 10^2$
0.315	$5.567(2) \cdot 10^{-1}$	$2.43(5) \cdot 10^{0}$	$-3.0(3) \cdot 10^2$
0.325	$2.593(1) \cdot 10^{-1}$	$4.67(3) \cdot 10^{0}$	$-6(2) \cdot 10^{1}$
0.335	$1.706(3) \cdot 10^{-2}$	$8.08(2) \cdot 10^{0}$	$4.8(5) \cdot 10^{1}$
0.345	0	$3.189(5) \cdot 10^{0}$	$2.1(1) \cdot 10^{1}$
0.355	0	$1.498(3) \cdot 10^0$	$9.2(6) \cdot 10^{0}$
0.365	0	$7.22(2) \cdot 10^{-1}$	$2.7(2) \cdot 10^{0}$
0.375	0	$3.24(1) \cdot 10^{-1}$	$1.0(2) \cdot 10^{-1}$
0.385	0	$1.154(5) \cdot 10^{-1}$	$-7.0(4) \cdot 10^{-2}$
0.395	0	$1.71(1) \cdot 10^{-2}$	$-2.7(2) \cdot 10^{-3}$
0.405	0	$1.29995(4) \cdot 10^{-6}$	$-3.7(4) \cdot 10^{-3}$
0.415	0	$1.647637(6) \cdot 10^{-5}$	$-1.0(4) \cdot 10^{-1}$
0.425	0	0	0

Table 2: Coefficients of the leading-order (A_{ρ}) , next-to-leading-order (B_{ρ}) and next-to-next-to-leading order (C_{ρ}) contributions to the heavy jet mass distribution.

	44-	dD_	dC-
B_W	$B_W \frac{dA_{B_W}}{dB_W}$	$B_W \frac{dB_{BW}}{dB_W}$	$B_W \frac{dC_{B_W}}{dB_W}$
0.005	$5.146(1) \cdot 10^{1}$	$-4.194(2) \cdot 10^3$	$1.433(7) \cdot 10^5$
0.015	$3.6823(4) \cdot 10^{1}$	$-6.385(7) \cdot 10^2$	$-2.33(3) \cdot 10^4$
0.025	$3.1132(3) \cdot 10^{1}$	$-1.015(5) \cdot 10^2$	$-1.34(2)\cdot 10^4$
0.035	$2.7389(2) \cdot 10^{1}$	$1.126(5) \cdot 10^2$	$-6.3(2)\cdot 10^3$
0.045	$2.4563(2) \cdot 10^{1}$	$2.136(4) \cdot 10^2$	$-1.7(2) \cdot 10^3$
0.055	$2.2291(2) \cdot 10^{1}$	$2.634(4) \cdot 10^2$	$6(2) \cdot 10^2$
0.065	$2.0389(2) \cdot 10^{1}$	$2.867(4) \cdot 10^2$	$2.5(2) \cdot 10^3$
0.075	$1.8734(1) \cdot 10^{1}$	$2.931(3) \cdot 10^2$	$3.1(2) \cdot 10^3$
0.085	$1.7273(1) \cdot 10^{1}$	$2.910(3) \cdot 10^2$	$3.4(2) \cdot 10^3$
0.095	$1.5966(1) \cdot 10^{1}$	$2.827(3) \cdot 10^2$	$4.0(2) \cdot 10^3$
0.105	$1.4778(1) \cdot 10^{1}$	$2.709(3) \cdot 10^2$	$4.0(2) \cdot 10^3$
0.115	$1.3686(1) \cdot 10^{1}$	$2.565(3) \cdot 10^2$	$3.5(2) \cdot 10^3$
0.125	$1.2685(1) \cdot 10^{1}$	$2.413(3) \cdot 10^2$	$3.7(2) \cdot 10^3$
0.135	$1.17528(9) \cdot 10^{1}$	$2.246(2) \cdot 10^2$	$3.3(2) \cdot 10^3$
0.145	$1.08786(9) \cdot 10^{1}$	$2.083(2) \cdot 10^2$	$2.7(1) \cdot 10^3$
0.155	$1.00548(8) \cdot 10^{1}$	$1.911(2) \cdot 10^2$	$2.8(1) \cdot 10^3$
0.165	$9.2782(8) \cdot 10^{0}$	$1.744(2) \cdot 10^2$	$2.4(1) \cdot 10^3$
0.175	$8.5406(7) \cdot 10^{0}$	$1.567(2) \cdot 10^2$	$1.7(1) \cdot 10^3$
0.185	$7.8351(7) \cdot 10^0$	$1.379(2) \cdot 10^2$	$1.2(1) \cdot 10^3$
0.195	$7.1576(6) \cdot 10^{0}$	$1.191(2) \cdot 10^2$	$9(1) \cdot 10^2$
0.205	$6.4999(6) \cdot 10^0$	$1.009(2) \cdot 10^2$	$6(1) \cdot 10^2$
0.215	$5.8549(6) \cdot 10^{0}$	$8.29(2) \cdot 10^{1}$	$-1(1)\cdot 10^2$
0.225	$5.2173(5) \cdot 10^{0}$	$6.57(1) \cdot 10^1$	$-4(1) \cdot 10^2$
0.235	$4.5744(5) \cdot 10^{0}$	$4.89(1) \cdot 10^{1}$	$-6.6(9) \cdot 10^2$
0.245	$3.9151(4) \cdot 10^{0}$	$3.19(1) \cdot 10^1$	$-1.18(8) \cdot 10^3$
0.255	$3.2206(4) \cdot 10^{0}$	$1.57(1) \cdot 10^{1}$	$-1.08(7) \cdot 10^3$
0.265	$2.4584(3) \cdot 10^{0}$	$4.8(9) \cdot 10^{-1}$	$-1.22(6) \cdot 10^3$
0.275	$1.5815(3) \cdot 10^{0}$	$-1.062(7) \cdot 10^{1}$	$-1.10(4) \cdot 10^3$
0.285	$4.942(2) \cdot 10^{-1}$	$-4.38(4) \cdot 10^{0}$	$-4.0(2) \cdot 10^2$
0.295	0	$3.961(6) \cdot 10^0$	$-2.1(1) \cdot 10^{1}$
0.305	0	$6.95(1) \cdot 10^{-1}$	$1.41(9) \cdot 10^0$
0.315	0	$4.06(2) \cdot 10^{-2}$	$-9(7) \cdot 10^{-4}$
0.325	0	$3.88459(5) \cdot 10^{-6}$	$-6(3) \cdot 10^{-2}$
0.335	0	0	0

Table 3: Coefficients of the leading-order (A_{B_W}) , next-to-leading-order (B_{B_W}) and next-to-next-to-leading order (C_{B_W}) contributions to the wide jet broadening distribution.

		TD.	
B_T	$B_T \frac{dA_{B_T}}{dB_T}$	$B_T \frac{dB_{B_T}}{dB_T}$	$B_T \frac{dC_{B_T}}{dB_T}$
0.005	$5.146(1) \cdot 10^{1}$	$-3.776(2) \cdot 10^3$	$9.16(8) \cdot 10^4$
0.015	$3.6823(4) \cdot 10^{1}$	$-2.65(2)\cdot 10^2$	$-5.59(5) \cdot 10^4$
0.025	$3.1132(3) \cdot 10^{1}$	$2.40(2) \cdot 10^2$	$-2.77(5) \cdot 10^4$
0.035	$2.7389(2) \cdot 10^{1}$	$4.24(2) \cdot 10^2$	$-1.24(5) \cdot 10^4$
0.045	$2.4563(2) \cdot 10^{1}$	$5.11(1) \cdot 10^2$	$-3.8(5) \cdot 10^3$
0.055	$2.2291(2) \cdot 10^{1}$	$5.42(1) \cdot 10^2$	$1.6(4) \cdot 10^3$
0.065	$2.0389(2) \cdot 10^{1}$	$5.53(1) \cdot 10^2$	$5.9(4) \cdot 10^3$
0.075	$1.8734(1) \cdot 10^{1}$	$5.46(1) \cdot 10^2$	$7.4(4) \cdot 10^3$
0.085	$1.7273(1) \cdot 10^{1}$	$5.32(1) \cdot 10^2$	$8.3(4) \cdot 10^3$
0.095	$1.5966(1) \cdot 10^{1}$	$5.164(9) \cdot 10^2$	$1.00(4) \cdot 10^4$
0.105	$1.4778(1) \cdot 10^{1}$	$4.960(8) \cdot 10^2$	$9.9(3) \cdot 10^3$
0.115	$1.3686(1) \cdot 10^{1}$	$4.744(8) \cdot 10^2$	$9.9(3) \cdot 10^3$
0.125	$1.2685(1) \cdot 10^{1}$	$4.515(7) \cdot 10^2$	$9.7(3) \cdot 10^3$
0.135	$1.17528(9) \cdot 10^{1}$	$4.288(7) \cdot 10^2$	$1.03(3) \cdot 10^4$
0.145	$1.08786(9) \cdot 10^{1}$	$4.056(6) \cdot 10^2$	$9.1(3) \cdot 10^3$
0.155	$1.00548(8) \cdot 10^{1}$	$3.850(6) \cdot 10^2$	$9.1(3) \cdot 10^3$
0.165	$9.2782(8) \cdot 10^{0}$	$3.615(6) \cdot 10^2$	$8.8(3) \cdot 10^3$
0.175	$8.5406(7) \cdot 10^{0}$	$3.409(6) \cdot 10^2$	$8.1(3) \cdot 10^3$
0.185	$7.8351(7) \cdot 10^{0}$	$3.203(5) \cdot 10^2$	$7.6(2) \cdot 10^3$
0.195	$7.1576(6) \cdot 10^{0}$	$3.016(5) \cdot 10^2$	$7.3(2) \cdot 10^3$
0.205	$6.4999(6) \cdot 10^{0}$	$2.825(5) \cdot 10^2$	$6.9(2) \cdot 10^3$
0.215	$5.8549(6) \cdot 10^{0}$	$2.654(5) \cdot 10^2$	$6.7(2) \cdot 10^3$
0.225	$5.2173(5) \cdot 10^{0}$	$2.496(4) \cdot 10^2$	$6.2(2) \cdot 10^3$
0.235	$4.5744(5) \cdot 10^{0}$	$2.353(4) \cdot 10^2$	$5.7(2) \cdot 10^3$
0.245	$3.9151(4) \cdot 10^{0}$	$2.228(4) \cdot 10^2$	$5.4(2) \cdot 10^3$
0.255	$3.2206(4) \cdot 10^{0}$	$2.124(4) \cdot 10^2$	$5.1(2) \cdot 10^3$
0.265	$2.4584(3) \cdot 10^{0}$	$2.067(3) \cdot 10^2$	$4.8(1) \cdot 10^3$
0.275	$1.5815(3) \cdot 10^{0}$	$2.057(3) \cdot 10^2$	$4.8(1) \cdot 10^3$
0.285	$4.942(2) \cdot 10^{-1}$	$2.158(2) \cdot 10^2$	$4.48(8) \cdot 10^3$
0.295	0	$1.5624(7) \cdot 10^2$	$5.13(4) \cdot 10^3$
0.305	0	$1.0481(4) \cdot 10^2$	$3.95(3) \cdot 10^3$
0.315	0	$7.527(3) \cdot 10^{1}$	$2.88(2) \cdot 10^3$
0.325	0	$5.412(2) \cdot 10^{1}$	$2.04(2) \cdot 10^3$
0.335	0	$3.710(2) \cdot 10^{1}$	$1.42(1) \cdot 10^3$
0.345	0	$2.203(1) \cdot 10^{1}$	$8.57(9) \cdot 10^2$
0.355	0	$1.1206(7) \cdot 10^{1}$	$4.15(6) \cdot 10^2$
0.365	0	$5.581(4) \cdot 10^{0}$	$1.81(3) \cdot 10^2$
0.375	0	$2.611(3) \cdot 10^{0}$	$7.0(1) \cdot 10^{1}$
0.385	0	$1.018(2) \cdot 10^{0}$	$4.0(2) \cdot 10^{0}$
0.395	0	$2.247(7) \cdot 10^{-1}$	$9(1) \cdot 10^{-2}$
0.405	0 0	$1.70679(8) \cdot 10^{-5}$	$-7.35(5) \cdot 10^{-2}$
0.415	U	0	0

Table 4: Coefficients of the leading-order (A_{B_T}) , next-to-leading-order (B_{B_T}) and next-to-next-to-leading order (C_{B_T}) contributions to the total jet broadening distribution.

С	$C\frac{dA_C}{dC}$	$C\frac{dB_C}{dC}$	$C\frac{dC_C}{dC}$
0.005	$3.5327(6) \cdot 10^{1}$	$-2.151(1) \cdot 10^3$	$3.06(4) \cdot 10^4$
0.015	$2.7963(3) \cdot 10^{1}$	$-4.75(1) \cdot 10^2$	$-3.04(4) \cdot 10^4$
0.025	$2.5124(3) \cdot 10^{1}$	$-1.45(1) \cdot 10^2$	$-2.15(4)\cdot 10^4$
0.035	$2.3269(2) \cdot 10^{1}$	$1.3(1) \cdot 10^{1}$	$-1.48(4) \cdot 10^4$
0.045	$2.1887(2) \cdot 10^{1}$	$1.09(1) \cdot 10^2$	$-1.12(5) \cdot 10^4$
0.055	$2.0774(2) \cdot 10^{1}$	$1.71(1) \cdot 10^2$	$-7.6(5) \cdot 10^3$
0.065	$1.9831(2) \cdot 10^{1}$	$2.15(1) \cdot 10^2$	$-5.3(5) \cdot 10^3$
0.075	$1.9042(2) \cdot 10^{1}$	$2.44(1) \cdot 10^2$	$-2.7(5) \cdot 10^3$
0.085	$1.8340(2) \cdot 10^{1}$	$2.67(1) \cdot 10^2$	$-1.5(5) \cdot 10^3$
0.095	$1.7710(2) \cdot 10^{1}$	$2.83(1) \cdot 10^2$	$-7(5) \cdot 10^2$
0.105	$1.7152(2) \cdot 10^{1}$	$2.95(1) \cdot 10^2$	$1.6(5) \cdot 10^3$
0.115	$1.6637(2) \cdot 10^{1}$	$3.06(1) \cdot 10^2$	$1.4(5) \cdot 10^3$
0.125	$1.6154(2) \cdot 10^{1}$	$3.10(1) \cdot 10^2$	$1.7(5) \cdot 10^3$
0.135	$1.5713(2) \cdot 10^{1}$	$3.18(1) \cdot 10^2$	$3.3(5) \cdot 10^3$
0.145	$1.5312(2) \cdot 10^{1}$	$3.21(1) \cdot 10^2$	$3.6(5) \cdot 10^3$
0.155	$1.4933(2) \cdot 10^{1}$	$3.23(1) \cdot 10^2$	$4.3(5) \cdot 10^3$
0.165	$1.4572(2) \cdot 10^{1}$	$3.24(1) \cdot 10^2$	$4.2(5) \cdot 10^3$
0.175	$1.4228(2) \cdot 10^{1}$	$3.26(1) \cdot 10^2$	$4.8(5) \cdot 10^3$
0.185	$1.3915(2) \cdot 10^{1}$	$3.241(9) \cdot 10^2$	$5.4(5) \cdot 10^3$
0.195	$1.3609(2) \cdot 10^{1}$	$3.227(9) \cdot 10^2$	$4.4(5) \cdot 10^3$
0.205	$1.3321(2) \cdot 10^{1}$	$3.242(9) \cdot 10^2$	$5.5(5) \cdot 10^3$
0.215	$1.3039(2) \cdot 10^{1}$	$3.214(9) \cdot 10^2$	$5.8(5) \cdot 10^3$
0.225	$1.2779(2) \cdot 10^{1}$	$3.208(9) \cdot 10^2$	$5.9(5) \cdot 10^3$
0.235	$1.2524(2) \cdot 10^{1}$	$3.184(9) \cdot 10^2$	$6.2(5) \cdot 10^3$
0.245	$1.2281(2) \cdot 10^{1}$	$3.179(9) \cdot 10^2$	$6.7(5) \cdot 10^3$
0.255	$1.2046(2) \cdot 10^{1}$	$3.156(9) \cdot 10^2$	$6.3(5) \cdot 10^3$
0.265	$1.1823(2) \cdot 10^{1}$	$3.113(9) \cdot 10^2$	$6.2(5) \cdot 10^3$
0.275	$1.1608(2) \cdot 10^{1}$	$3.079(9) \cdot 10^2$	$6.6(5) \cdot 10^3$
0.285	$1.1392(2) \cdot 10^{1}$	$3.078(9) \cdot 10^2$	$5.9(5) \cdot 10^3$
0.295	$1.1197(2) \cdot 10^{1}$	$3.029(8) \cdot 10^2$	$6.8(5) \cdot 10^3$
0.305	$1.1000(2) \cdot 10^{1}$	$3.008(8) \cdot 10^2$	$6.5(5) \cdot 10^3$
0.315	$1.0812(2) \cdot 10^{1}$	$2.980(8) \cdot 10^2$	$6.8(5) \cdot 10^3$
0.325	$1.0627(2) \cdot 10^{1}$	$2.964(8) \cdot 10^2$	$6.5(5) \cdot 10^3$
0.335	$1.0451(1) \cdot 10^{1}$	$2.908(8) \cdot 10^2$	$6.3(5) \cdot 10^3$
0.345	$1.0273(1) \cdot 10^{1}$	$2.897(8) \cdot 10^2$	$6.1(5) \cdot 10^3$
0.355	$1.0110(1) \cdot 10^{1}$	$2.856(8) \cdot 10^2$	$6.2(5) \cdot 10^3$
0.365	$9.946(1) \cdot 10^0$	$2.843(8) \cdot 10^2$	$6.4(5) \cdot 10^3$
0.375	$9.787(1) \cdot 10^0$	$2.804(8) \cdot 10^2$	$7.0(5) \cdot 10^3$
0.385	$9.628(1) \cdot 10^{0}$	$2.752(8) \cdot 10^2$	$6.5(5) \cdot 10^3$
0.395	$9.484(1) \cdot 10^{0}$	$2.732(8) \cdot 10^2$	$6.1(5) \cdot 10^3$
0.405	$9.332(1) \cdot 10^{0}$	$2.711(8) \cdot 10^2$	$6.2(5) \cdot 10^3$
0.415	$9.190(1) \cdot 10^0$	$2.685(7) \cdot 10^2$	$7.0(5) \cdot 10^3$
0.425	$9.049(1) \cdot 10^0$	$2.636(7) \cdot 10^2$	$5.8(4) \cdot 10^3$
0.435	$8.914(1) \cdot 10^0$	$2.616(7) \cdot 10^2$	$6.1(4) \cdot 10^3$
0.445	$8.779(1) \cdot 10^0$	$2.580(7) \cdot 10^2$	$6.2(4) \cdot 10^3$
0.455	$8.645(1) \cdot 10^0$	$2.555(7) \cdot 10^2$	$6.0(4) \cdot 10^3$
0.465	$8.518(1) \cdot 10^{0}$	$2.518(7) \cdot 10^2$	$6.5(4) \cdot 10^3$
0.475	$8.392(1) \cdot 10^{0}$	$2.491(7) \cdot 10^2$	$5.6(4) \cdot 10^3$
0.485	$8.269(1) \cdot 10^0$	$2.465(7) \cdot 10^2$	$5.9(4) \cdot 10^3$
0.495	$8.152(1) \cdot 10^0$	$2.415(7) \cdot 10^2$	$5.8(4) \cdot 10^3$

Table 5: Coefficients of the leading-order (A_C) , next-to-leading-order (B_C) and next-to-next-to-leading order (C_C) contributions to the C-parameter distribution.

С	$C\frac{dA_C}{dC}$	$C\frac{dB_C}{dC}$	$C\frac{dC_C}{dC}$
0.505	$8.033(1) \cdot 10^{0}$	$2.417(7) \cdot 10^2$	$5.8(4) \cdot 10^3$
0.515	$7.918(1) \cdot 10^{0}$	$2.376(7) \cdot 10^2$	$5.5(4) \cdot 10^3$
0.525	$7.804(1) \cdot 10^{0}$	$2.326(7) \cdot 10^2$	$6.1(4) \cdot 10^3$
0.535	$7.691(1) \cdot 10^0$	$2.312(7) \cdot 10^2$	$5.0(4) \cdot 10^3$
0.545	$7.589(1) \cdot 10^{0}$	$2.285(7) \cdot 10^2$	$5.5(4) \cdot 10^3$
0.555	$7.476(1) \cdot 10^0$	$2.247(7) \cdot 10^2$	$5.7(4) \cdot 10^3$
0.565	$7.377(1) \cdot 10^0$	$2.227(7) \cdot 10^2$	$5.7(4) \cdot 10^3$
0.575	$7.271(1) \cdot 10^0$	$2.190(7) \cdot 10^2$	$5.6(4) \cdot 10^3$
0.585	$7.172(1) \cdot 10^0$	$2.180(7) \cdot 10^2$	$5.4(4) \cdot 10^3$
0.595	$7.073(1) \cdot 10^0$	$2.143(7) \cdot 10^2$	$5.2(4) \cdot 10^3$
0.605	$6.976(1) \cdot 10^0$	$2.105(7) \cdot 10^2$	$4.9(4) \cdot 10^3$
0.615	$6.880(1) \cdot 10^0$	$2.084(7) \cdot 10^2$	$5.2(4) \cdot 10^3$
0.625	$6.788(1) \cdot 10^0$	$2.046(7) \cdot 10^2$	$4.6(4) \cdot 10^3$
0.635	$6.692(1) \cdot 10^0$	$2.025(7) \cdot 10^2$	$5.1(4) \cdot 10^3$
0.645	$6.600(1) \cdot 10^0$	$2.009(7) \cdot 10^2$	$5.1(4) \cdot 10^3$
0.655	$6.515(1) \cdot 10^0$	$1.977(7) \cdot 10^2$	$4.4(4) \cdot 10^3$
0.665	$6.426(1) \cdot 10^0$	$1.947(7) \cdot 10^2$	$5.0(4) \cdot 10^3$
0.675	$6.337(1) \cdot 10^0$	$1.924(7) \cdot 10^2$	$4.7(4) \cdot 10^3$
0.685	$6.253(1) \cdot 10^0$	$1.892(7) \cdot 10^2$	$5.1(4) \cdot 10^3$
0.695	$6.171(1) \cdot 10^0$	$1.877(7) \cdot 10^2$	$4.5(4) \cdot 10^3$
0.705	$6.0874(9) \cdot 10^0$	$1.840(7) \cdot 10^2$	$4.3(3) \cdot 10^3$
0.715	$6.0103(9) \cdot 10^0$	$1.826(7) \cdot 10^2$	$3.9(3) \cdot 10^3$
0.725	$5.9266(9) \cdot 10^0$	$1.800(7) \cdot 10^2$	$4.4(3) \cdot 10^3$
0.735	$5.8474(9) \cdot 10^0$	$1.775(7) \cdot 10^2$	$4.3(3) \cdot 10^3$
0.745	$5.7695(9) \cdot 10^0$	$1.745(8) \cdot 10^2$	$3.2(3) \cdot 10^3$
0.755	0	$6.011(5) \cdot 10^2$	$1.27(2) \cdot 10^4$
0.765	0	$2.771(2) \cdot 10^2$	$1.38(1) \cdot 10^4$
0.775	0	$1.905(1) \cdot 10^2$	$9.99(9) \cdot 10^3$
0.785	0	$1.4246(7) \cdot 10^2$	$7.66(7) \cdot 10^3$
0.795	0	$1.1124(6) \cdot 10^2$	$6.17(6) \cdot 10^3$
0.805	0	$8.895(5) \cdot 10^{1}$	$4.65(5) \cdot 10^3$
0.815	0	$7.228(4) \cdot 10^{1}$	$3.49(4) \cdot 10^3$
0.825	0	$5.913(3) \cdot 10^{1}$	$3.02(4) \cdot 10^3$
0.835	0	$4.876(3) \cdot 10^{1}$	$2.50(3) \cdot 10^3$
0.845	0	$4.037(2) \cdot 10^{1}$	$1.93(3) \cdot 10^3$
0.855	0	$3.336(2) \cdot 10^{1}$	$8.2(2) \cdot 10^2$
0.865	0	$2.754(2) \cdot 10^{1}$	$1.26(2) \cdot 10^3$
0.875	0	$2.270(2) \cdot 10^{1}$	$9.4(2) \cdot 10^2$
0.885	0	$1.856(1) \cdot 10^{1}$	$6.8(1) \cdot 10^2$
0.895	0	$1.506(1) \cdot 10^{1}$	$5.9(1) \cdot 10^2$
0.905	0	$1.212(1) \cdot 10^{1}$	$4.57(9) \cdot 10^2$
0.915	0	$9.587(9) \cdot 10^{0}$	$3.50(7) \cdot 10^2$
0.925	0	$7.458(8) \cdot 10^{0}$	$2.19(5) \cdot 10^2$
0.935	0	$5.645(7) \cdot 10^0$	$1.0(2) \cdot 10^{1}$
0.945	0	$4.125(6) \cdot 10^0$	$1.01(2) \cdot 10^2$
0.955	0	$2.875(5) \cdot 10^{0}$	$2.59(8) \cdot 10^{1}$
0.965	0	$1.835(4) \cdot 10^{0}$	$2.26(5) \cdot 10^{1}$
0.975	0	$1.008(3) \cdot 10^0$	$3.9(1) \cdot 10^0$
0.985	0	$3.99(1) \cdot 10^{-1}$	$-4.886(1) \cdot 10^{-1}$
0.995	0	$1.8841(2) \cdot 10^{-2}$	$-1.443(2) \cdot 10^{-1}$
0.775	, , ,	(2) 13	(2) 10

Table 6: Coefficients of the leading-order (A_C) , next-to-leading-order (B_C) and next-to-next-to-leading order (C_C) contributions to the C-parameter distribution.

$ln y_{23}$	$y_{23} \frac{dA_{y_{23}}}{dy_{23}}$	$y_{23} \frac{dB_{y_{23}}}{dy_{23}}$	$y_{23} \frac{dC_{y_{23}}}{dy_{23}}$
-9.875	$2.222(1) \cdot 10^{1}$	$-1.133(3) \cdot 10^3$	$-2(1)\cdot 10^3$
-9.625	$2.157(1) \cdot 10^{1}$	$-1.004(3) \cdot 10^3$	$-6(1) \cdot 10^3$
-9.375	$2.094(1) \cdot 10^{1}$	$-8.81(3) \cdot 10^2$	$-6.6(9) \cdot 10^3$
-9.125	$2.031(1) \cdot 10^{1}$	$-7.63(2) \cdot 10^2$	$-8.6(8) \cdot 10^3$
-8.875	$1.9650(8) \cdot 10^{1}$	$-6.58(2) \cdot 10^2$	$-8.6(7) \cdot 10^3$
-8.625	$1.8987(7) \cdot 10^{1}$	$-5.63(2) \cdot 10^2$	$-9.4(7) \cdot 10^3$
-8.375	$1.8361(6) \cdot 10^{1}$	$-4.74(2) \cdot 10^2$	$-9.9(6) \cdot 10^3$
-8.125	$1.7707(6) \cdot 10^{1}$	$-3.90(1) \cdot 10^2$	$-8.5(5) \cdot 10^3$
-7.875	$1.7061(5) \cdot 10^{1}$	$-3.21(1) \cdot 10^2$	$-9.1(5) \cdot 10^3$
-7.625	$1.6405(4) \cdot 10^{1}$	$-2.54(1) \cdot 10^2$	$-8.0(4) \cdot 10^3$
-7.375	$1.5758(4) \cdot 10^{1}$	$-1.94(1) \cdot 10^2$	$-8.1(4) \cdot 10^3$
-7.125	$1.5099(3) \cdot 10^{1}$	$-1.415(9) \cdot 10^2$	$-6.2(4) \cdot 10^3$
-6.875	$1.4457(3) \cdot 10^{1}$	$-9.45(8) \cdot 10^{1}$	$-5.9(3) \cdot 10^3$
-6.625	$1.3806(2) \cdot 10^{1}$	$-5.56(7) \cdot 10^{1}$	$-5.2(3) \cdot 10^3$
-6.375	$1.3163(2) \cdot 10^{1}$	$-2.00(6) \cdot 10^{1}$	$-4.1(3) \cdot 10^3$
-6.125	$1.2520(2) \cdot 10^{1}$	$1.21(5) \cdot 10^{1}$	$-3.4(2) \cdot 10^3$
-5.875	$1.1876(2) \cdot 10^{1}$	$3.61(5) \cdot 10^{1}$	$-2.4(2)\cdot 10^3$
-5.625	$1.1235(1) \cdot 10^{1}$	$5.67(4) \cdot 10^{1}$	$-1.8(2) \cdot 10^3$
-5.375	$1.0598(1) \cdot 10^{1}$	$7.36(4) \cdot 10^{1}$	$-1.3(2) \cdot 10^3$
-5.125	$9.965(1) \cdot 10^0$	$8.47(3) \cdot 10^{1}$	$-9(2) \cdot 10^2$
-4.875	$9.3336(9) \cdot 10^0$	$9.48(3) \cdot 10^{1}$	$-3(1)\cdot 10^2$
-4.625	$8.7098(8) \cdot 10^{0}$	$1.005(2) \cdot 10^2$	$0(1) \cdot 10^{1}$
-4.375	$8.0890(7) \cdot 10^0$	$1.027(2) \cdot 10^2$	$4(1) \cdot 10^2$
-4.125	$7.4721(6) \cdot 10^{0}$	$1.033(2) \cdot 10^2$	$5(1) \cdot 10^2$
-3.875	$6.8622(5) \cdot 10^{0}$	$1.009(2) \cdot 10^2$	$9.1(9) \cdot 10^2$
-3.625	$6.2583(5) \cdot 10^{0}$	$9.70(1) \cdot 10^1$	$7.0(8) \cdot 10^2$
-3.375	$5.6606(4) \cdot 10^{0}$	$9.10(1) \cdot 10^{1}$	$7.0(7) \cdot 10^2$
-3.125	$5.0728(4) \cdot 10^{0}$	$8.39(1) \cdot 10^{1}$	$7.6(6) \cdot 10^2$
-2.875	$4.4922(3) \cdot 10^{0}$	$7.551(8) \cdot 10^{1}$	$5.7(5) \cdot 10^2$
-2.625	$3.9202(3) \cdot 10^{0}$	$6.652(7) \cdot 10^{1}$	$5.2(4) \cdot 10^2$
-2.375	$3.3538(2) \cdot 10^{0}$	$5.674(6) \cdot 10^{1}$	$4.5(3) \cdot 10^2$
-2.125	$2.7894(2) \cdot 10^{0}$	$4.676(4) \cdot 10^{1}$	$2.6(3) \cdot 10^2$
-1.875	$2.2184(2) \cdot 10^{0}$	$3.635(3) \cdot 10^{1}$	$1.8(2) \cdot 10^2$
-1.625	$1.6189(1) \cdot 10^{0}$	$2.590(2) \cdot 10^{1}$	$1.4(2) \cdot 10^2$
-1.375	$9.4172(8) \cdot 10^{-1}$	$1.479(2) \cdot 10^{1}$	$3(1) \cdot 10^{1}$
-1.125	$1.6678(3) \cdot 10^{-1}$	$1.704(6) \cdot 10^{0}$	$-4.0(4) \cdot 10^{1}$
-0.875	0	0	0

Table 7: Coefficients of the leading-order $(A_{y_{23}})$, next-to-leading-order $(B_{y_{23}})$ and next-to-next-to-leading order $(C_{y_{23}})$ contributions to the three-to-two jet transition distribution.

y_{cut}	$A_{3-jet,Durham}$	$B_{3-jet,Durham}$	$C_{3-jet,Durham}$
0.3	$2.2301(9) \cdot 10^{-2}$	$1.35(2) \cdot 10^{-1}$	$-6(3) \cdot 10^{0}$
0.15	$1.0028(3) \cdot 10^{0}$	$1.582(3) \cdot 10^{1}$	$5(1) \cdot 10^{1}$
0.1	$2.1150(6) \cdot 10^{0}$	$3.415(7) \cdot 10^{1}$	$1.7(2) \cdot 10^2$
0.06	$4.046(1) \cdot 10^{0}$	$6.57(1) \cdot 10^{1}$	$4.1(3) \cdot 10^2$
0.03	$7.627(2) \cdot 10^{0}$	$1.141(2) \cdot 10^2$	$5.0(6) \cdot 10^2$
0.015	$1.2359(3) \cdot 10^{1}$	$1.495(3) \cdot 10^2$	$-1.2(9) \cdot 10^2$
0.01	$1.5671(4) \cdot 10^{1}$	$1.531(4) \cdot 10^2$	$-1.3(1) \cdot 10^3$
0.006	$2.0430(5) \cdot 10^{1}$	$1.238(5) \cdot 10^2$	$-3.6(2) \cdot 10^3$
0.003	$2.7947(7) \cdot 10^{1}$	$-5.5(7) \cdot 10^{0}$	$-9.0(3) \cdot 10^3$
0.0015	$3.6694(8) \cdot 10^{1}$	$-2.93(1) \cdot 10^2$	$-1.63(5) \cdot 10^4$
0.001	$4.2386(9) \cdot 10^{1}$	$-5.62(1) \cdot 10^2$	$-2.16(6) \cdot 10^4$
0.0006	$5.016(1) \cdot 10^{1}$	$-1.032(2)\cdot 10^3$	$-2.84(8) \cdot 10^4$
0.0003	$6.181(1) \cdot 10^{1}$	$-1.967(2)\cdot 10^3$	$-3.1(1) \cdot 10^4$
0.00015	$7.471(2) \cdot 10^{1}$	$-3.333(2)\cdot 10^3$	$-1.8(3) \cdot 10^4$
0.0001	$8.285(2) \cdot 10^{1}$	$-4.368(3) \cdot 10^3$	$6(4) \cdot 10^3$

Table 8: Coefficients of the leading-order $(A_{3-jet,Durham})$, next-to-leading-order $(B_{3-jet,Durham})$ and next-to-next-to-leading order $(C_{3-jet,Durham})$ contributions to the Durham three-jet rate for various values of y_{cut} .

Усиt	A _{3-jet,Geneva}	$B_{3-jet,Geneva}$	$C_{3-jet,Geneva}$
0.3	$1.7615(7) \cdot 10^{-1}$	$2.10(1) \cdot 10^{0}$	$-1.3(6) \cdot 10^{1}$
0.15	$4.7265(9) \cdot 10^{0}$	$5.45(1) \cdot 10^{1}$	$-4.4(6) \cdot 10^2$
0.1	$8.922(1) \cdot 10^{0}$	$7.51(2) \cdot 10^{1}$	$-1.3(1) \cdot 10^3$
0.06	$1.5520(3) \cdot 10^{1}$	$3.87(4) \cdot 10^{1}$	$-5.0(2)\cdot 10^3$
0.03	$2.6717(4) \cdot 10^{1}$	$-2.403(7) \cdot 10^2$	$-1.35(4) \cdot 10^4$
0.015	$4.0440(5) \cdot 10^{1}$	$-9.725(7) \cdot 10^2$	$-2.53(7) \cdot 10^4$
0.01	$4.9627(6) \cdot 10^{1}$	$-1.709(2) \cdot 10^3$	$-2.86(8) \cdot 10^4$
0.006	$6.2446(7) \cdot 10^{1}$	$-3.072(3) \cdot 10^3$	$-2.5(1) \cdot 10^4$
0.003	$8.204(1) \cdot 10^{1}$	$-5.937(5) \cdot 10^3$	$1.4(2) \cdot 10^4$
0.0015	$1.0418(1) \cdot 10^2$	$-1.0300(6) \cdot 10^4$	$1.53(4) \cdot 10^5$
0.001	$1.1833(1) \cdot 10^2$	$-1.3736(9) \cdot 10^4$	$2.81(5) \cdot 10^5$

Table 9: Coefficients of the leading-order $(A_{3-jet,Geneva})$, next-to-leading-order $(B_{3-jet,Geneva})$ and next-to-next-to-leading order $(C_{3-jet,Geneva})$ contributions to the Durham three-jet rate for various values of y_{cut} .

y _{cut}	$A_{3-jet,Jade-E0}$	$B_{3-jet,Jade-E0}$	$C_{3-jet,Jade-E0}$
0.3	$5.393(2) \cdot 10^{-2}$	$1.119(5) \cdot 10^{0}$	$9(8) \cdot 10^{0}$
0.15	$2.3086(5) \cdot 10^{0}$	$5.293(6) \cdot 10^{1}$	$5.3(4) \cdot 10^2$
0.1	$4.9170(9) \cdot 10^{0}$	$1.118(1) \cdot 10^2$	$9(1) \cdot 10^2$
0.06	$9.527(2) \cdot 10^{0}$	$1.994(2) \cdot 10^2$	$1.5(2) \cdot 10^3$
0.03	$1.8137(3) \cdot 10^{1}$	$2.885(4) \cdot 10^2$	$-8(3) \cdot 10^2$
0.015	$2.9425(4) \cdot 10^{1}$	$2.397(8) \cdot 10^2$	$-9.1(6) \cdot 10^3$
0.01	$3.7257(5) \cdot 10^{1}$	$9.1(1) \cdot 10^{1}$	$-1.88(6) \cdot 10^4$
0.006	$4.8389(6) \cdot 10^{1}$	$-2.92(2)\cdot 10^2$	$-2.9(1) \cdot 10^4$
0.003	$6.5768(9) \cdot 10^{1}$	$-1.300(3) \cdot 10^3$	$-4.6(2) \cdot 10^4$
0.0015	$8.572(1) \cdot 10^{1}$	$-3.092(4) \cdot 10^3$	$-4.6(2) \cdot 10^4$
0.001	$9.859(1) \cdot 10^{1}$	$-4.603(5) \cdot 10^3$	$-2.9(4) \cdot 10^4$
0.0006	$1.1607(1) \cdot 10^2$	$-7.143(7) \cdot 10^3$	$3.2(4) \cdot 10^4$
0.0003	$1.4199(2) \cdot 10^2$	$-1.190(1) \cdot 10^4$	$2.30(8) \cdot 10^5$

Table 10: Coefficients of the leading-order $(A_{3-jet,Jade-E0})$, next-to-leading-order $(B_{3-jet,Jade-E0})$ and next-to-next-to-leading order $(C_{3-jet,Jade-E0})$ contributions to the Durham three-jet rate for various values of y_{cut} .

y_{cut}	$A_{3-jet,Cambridge}$	$B_{3-jet,Cambridge}$	$C_{3-jet,Cambridge}$
0.3	$2.2301(9) \cdot 10^{-2}$	$1.35(2) \cdot 10^{-1}$	$-7(3) \cdot 10^{0}$
0.15	$1.0028(3) \cdot 10^{0}$	$1.525(3) \cdot 10^{1}$	$2(3) \cdot 10^{1}$
0.1	$2.1150(6) \cdot 10^{0}$	$3.156(6) \cdot 10^{1}$	$9(6) \cdot 10^{1}$
0.06	$4.046(1) \cdot 10^0$	$5.72(1) \cdot 10^{1}$	$4(9) \cdot 10^{1}$
0.03	$7.627(2) \cdot 10^{0}$	$9.33(2) \cdot 10^{1}$	$-2(2)\cdot 10^2$
0.015	$1.2359(3) \cdot 10^{1}$	$1.127(3) \cdot 10^2$	$-1.1(2) \cdot 10^3$
0.01	$1.5671(4) \cdot 10^{1}$	$1.048(4) \cdot 10^2$	$-2.3(3) \cdot 10^3$
0.006	$2.0430(5) \cdot 10^{1}$	$5.96(6) \cdot 10^{1}$	$-3.9(4) \cdot 10^3$
0.003	$2.7947(7) \cdot 10^{1}$	$-9.66(7) \cdot 10^{1}$	$-9.6(6) \cdot 10^3$
0.0015	$3.6694(8) \cdot 10^{1}$	$-4.15(1) \cdot 10^2$	$-1.41(8) \cdot 10^4$
0.001	$4.2386(9) \cdot 10^{1}$	$-7.03(1) \cdot 10^2$	$-1.7(1) \cdot 10^4$
0.0006	$5.016(1) \cdot 10^1$	$-1.201(2)\cdot 10^3$	$-1.8(1) \cdot 10^4$
0.0003	$6.181(1) \cdot 10^1$	$-2.177(2)\cdot 10^3$	$-1.3(2) \cdot 10^4$
0.00015	$7.471(2) \cdot 10^{1}$	$-3.584(3) \cdot 10^3$	$9(2) \cdot 10^3$
0.0001	$8.285(2) \cdot 10^{1}$	$-4.656(4) \cdot 10^3$	$3.3(3) \cdot 10^4$

Table 11: Coefficients of the leading-order $(A_{3-jet,Cambridge})$, next-to-leading-order $(B_{3-jet,Cambridge})$ and next-to-next-to-leading order $(C_{3-jet,Cambridge})$ contributions to the Durham three-jet rate for various values of y_{cut} .

(1-T)	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.005	$-1.67(1) \cdot 10^4$	$8.14(2) \cdot 10^3$	$5.73(2) \cdot 10^2$	$-3.85(4) \cdot 10^3$	$-5.412(5) \cdot 10^3$	$8.3281(6) \cdot 10^3$
0.015	$8.5(1) \cdot 10^3$	$4.35(3) \cdot 10^3$	$-9.0(3) \cdot 10^{1}$	$-1.880(4) \cdot 10^4$	$-6.80(6)\cdot 10^{2}$	$3.4298(3) \cdot 10^3$
0.025	$1.35(1) \cdot 10^4$	$2.30(3) \cdot 10^3$	$-9.2(3) \cdot 10^{1}$	$-1.632(4) \cdot 10^4$	$-1.02(6) \cdot 10^{2}$	$2.3354(3) \cdot 10^3$
0.035	$1.52(1) \cdot 10^4$	$1.24(3) \cdot 10^3$	$-7.7(2) \cdot 10^{1}$	$-1.425(4) \cdot 10^4$	$1.12(6) \cdot 10^2$	$1.7636(3) \cdot 10^3$
0.045	$1.52(1) \cdot 10^4$	$5.4(3) \cdot 10^2$	$-6.3(2) \cdot 10^{1}$	$-1.243(4) \cdot 10^4$	$2.12(6) \cdot 10^2$	$1.4027(3) \cdot 10^3$
0.055	$1.47(1) \cdot 10^4$	$2.0(2) \cdot 10^{2}$	$-4.7(2) \cdot 10^{1}$	$-1.101(4) \cdot 10^4$	$2.65(6) \cdot 10^2$	$1.1509(3) \cdot 10^3$
0.065	$1.41(1) \cdot 10^4$	$-3(2) \cdot 10^{1}$	$-4.0(2) \cdot 10^{1}$	$-9.83(4)\cdot 10^3$	$2.81(5) \cdot 10^2$	$9.646(3) \cdot 10^2$
0.075	$1.33(1) \cdot 10^4$	$-2.3(2) \cdot 10^2$	$-3.2(2) \cdot 10^{1}$	$-8.76(4) \cdot 10^{3}$	$2.92(5) \cdot 10^2$	$8.209(2) \cdot 10^2$
0.085	$1.27(1) \cdot 10^4$	$-3.4(2) \cdot 10^2$	$-2.7(2) \cdot 10^{1}$	$-7.84(4) \cdot 10^3$	$2.89(5) \cdot 10^{2}$	$7.070(2) \cdot 10^2$
0.095	$1.19(1) \cdot 10^4$	$-3.9(2) \cdot 10^2$	$-1.9(2) \cdot 10^{1}$	$-7.18(3) \cdot 10^3$	$2.81(5) \cdot 10^2$	$6.142(2) \cdot 10^2$
0.105	$1.12(1) \cdot 10^4$	$-4.4(2) \cdot 10^2$	$-1.7(2) \cdot 10^{1}$	$-6.49(3) \cdot 10^3$	$2.69(5) \cdot 10^2$	$5.374(2) \cdot 10^2$
0.115	$1.05(1) \cdot 10^4$	$-4.9(2) \cdot 10^2$	$-1.4(2) \cdot 10^{1}$	$-5.91(3) \cdot 10^3$	$2.59(5) \cdot 10^2$	$4.733(2) \cdot 10^2$
0.125	$9.7(1) \cdot 10^3$	$-5.0(2) \cdot 10^2$	$-1.1(1) \cdot 10^{1}$	$-5.44(3) \cdot 10^3$	$2.46(4) \cdot 10^{2}$	$4.182(2) \cdot 10^{2}$
0.135	$9.1(1) \cdot 10^3$	$-5.2(2)\cdot 10^2$	$-8(1) \cdot 10^{0}$	$-4.88(3) \cdot 10^3$	$2.44(4) \cdot 10^2$	$3.705(2) \cdot 10^2$
0.145	$8.6(1) \cdot 10^3$	$-5.3(2) \cdot 10^2$	$-7(1) \cdot 10^{0}$	$-4.48(3) \cdot 10^3$	$2.21(4) \cdot 10^2$	$3.298(2) \cdot 10^2$
0.155	$8.0(1) \cdot 10^3$	$-5.1(2) \cdot 10^2$	$-6(1) \cdot 10^{0}$	$-4.15(3) \cdot 10^3$	$2.11(4) \cdot 10^2$	$2.937(2) \cdot 10^2$
0.165	$7.64(9) \cdot 10^3$	$-5.0(1) \cdot 10^2$	$-3(1) \cdot 10^{0}$	$-3.85(3) \cdot 10^3$	$2.03(4) \cdot 10^2$	$2.620(2) \cdot 10^2$
0.175	$7.01(9) \cdot 10^3$	$-4.7(1) \cdot 10^2$	$-2(1)\cdot 10^{0}$	$-3.46(3) \cdot 10^3$	$1.96(3) \cdot 10^2$	$2.338(2) \cdot 10^2$
0.185	$6.59(9) \cdot 10^3$	$-4.8(1) \cdot 10^2$	$-1(1) \cdot 10^{0}$	$-3.20(3) \cdot 10^3$	$1.77(3) \cdot 10^2$	$2.079(2) \cdot 10^2$
0.195	$6.19(9) \cdot 10^3$	$-4.4(1) \cdot 10^2$	$-9(9) \cdot 10^{-1}$	$-2.91(3) \cdot 10^3$	$1.75(3) \cdot 10^2$	$1.848(2) \cdot 10^2$
0.205	$5.81(9) \cdot 10^3$	$-4.5(1) \cdot 10^2$	$7(9) \cdot 10^{-1}$	$-2.70(3) \cdot 10^3$	$1.60(3) \cdot 10^2$	$1.639(2) \cdot 10^2$
0.215	$5.44(8) \cdot 10^3$	$-4.2(1) \cdot 10^2$	$1.1(8) \cdot 10^{0}$	$-2.46(2)\cdot 10^3$	$1.47(3) \cdot 10^2$	$1.446(2) \cdot 10^2$
0.225	$5.04(8) \cdot 10^3$	$-4.0(1) \cdot 10^2$	$-3(8) \cdot 10^{-1}$	$-2.28(2)\cdot 10^3$	$1.40(2) \cdot 10^2$	$1.266(2) \cdot 10^2$
0.235	$4.70(8) \cdot 10^3$	$-3.7(1) \cdot 10^2$	$1.0(7) \cdot 10^{0}$	$-2.06(2) \cdot 10^3$	$1.30(2) \cdot 10^2$	$1.097(2) \cdot 10^2$
0.245	$4.33(7) \cdot 10^3$	$-3.49(9) \cdot 10^2$	$2.5(6) \cdot 10^{0}$	$-1.87(2) \cdot 10^3$	$1.20(2) \cdot 10^2$	$9.38(2) \cdot 10^{1}$
0.255	$4.20(7) \cdot 10^3$	$-3.32(9) \cdot 10^2$	$1.4(6) \cdot 10^{0}$	$-1.71(2) \cdot 10^3$	$1.09(2) \cdot 10^2$	$7.88(2) \cdot 10^{1}$
0.265	$3.84(7) \cdot 10^3$	$-3.19(8) \cdot 10^2$	$2.3(5) \cdot 10^{0}$	$-1.53(2) \cdot 10^3$	$9.7(2) \cdot 10^{1}$	$6.41(2) \cdot 10^{1}$
0.275	$3.51(6) \cdot 10^3$	$-2.92(7) \cdot 10^2$	$2.2(5) \cdot 10^{0}$	$-1.39(2) \cdot 10^3$	$9.2(1) \cdot 10^{1}$	$4.94(2) \cdot 10^{1}$
0.285	$3.29(6) \cdot 10^3$	$-2.71(6) \cdot 10^2$	$1.7(4) \cdot 10^{0}$	$-1.26(2)\cdot 10^3$	$8.4(4) \cdot 10^{0}$	$3.53(2) \cdot 10^{1}$
0.295	$3.03(5) \cdot 10^3$	$-2.38(6) \cdot 10^2$	$1.7(3) \cdot 10^{0}$	$-1.05(1) \cdot 10^3$	$6.5(1) \cdot 10^{1}$	$2.14(2) \cdot 10^{1}$
0.305	$2.74(4) \cdot 10^3$	$-2.17(5) \cdot 10^2$	$2.1(3) \cdot 10^{0}$	$-8.6(1) \cdot 10^2$	$5.96(8) \cdot 10^{1}$	$7.3(2) \cdot 10^{0}$
0.315	$2.38(3) \cdot 10^3$	$-1.99(4) \cdot 10^{2}$	$1.5(2) \cdot 10^{0}$	$-6.61(9) \cdot 10^{2}$	$5.03(6) \cdot 10^{1}$	$-6.6(1) \cdot 10^{0}$
0.325	$2.03(2) \cdot 10^3$	$-1.59(2) \cdot 10^2$	$1.1(1) \cdot 10^{0}$	$-4.65(6) \cdot 10^2$	$2.87(3) \cdot 10^{1}$	$-2.14(1) \cdot 10^{1}$
0.335	$1.39(1) \cdot 10^3$	$-1.21(1) \cdot 10^2$	$6(1) \cdot 10^{-2}$	$-2.23(3) \cdot 10^2$	$1.88(2) \cdot 10^{1}$	$-2.570(6) \cdot 10^{1}$
0.345	$4.59(5) \cdot 10^2$	$-5.91(7) \cdot 10^{1}$	$1.0(1) \cdot 10^{-1}$	$-9.2(1) \cdot 10^{1}$	$8.9(6) \cdot 10^{-2}$	$-1.165(3) \cdot 10^{1}$
0.355	$2.20(3) \cdot 10^2$	$-1.92(3) \cdot 10^{1}$	$-1(1) \cdot 10^{-4}$	$-3.99(4) \cdot 10^{1}$	$1.0(1) \cdot 10^{-2}$	$-5.91(2) \cdot 10^{0}$
0.365	$7.4(1) \cdot 10^{1}$	$-1.10(6) \cdot 10^{0}$	$-2(1) \cdot 10^{-4}$	$-1.73(2) \cdot 10^{1}$	$9(9) \cdot 10^{-8}$	$-2.85(1) \cdot 10^{0}$
0.375	$4.50(7) \cdot 10^{1}$	$-2.0(9) \cdot 10^{-2}$	$-8.8(7) \cdot 10^{-3}$	$-7.8(1) \cdot 10^{0}$	$1(1) \cdot 10^{-11}$	$-1.452(7) \cdot 10^{0}$
0.385	$1.17(2) \cdot 10^{1}$	$-1.2(3) \cdot 10^{-2}$	$-2.0(1) \cdot 10^{-3}$	$-8.0(3) \cdot 10^{-1}$	$3(3) \cdot 10^{-13}$	$-1.84(7) \cdot 10^{-2}$
0.395	$2.1(2) \cdot 10^{-1}$	$-3(1) \cdot 10^{-3}$	$-4(4) \cdot 10^{-6}$	$-3(1) \cdot 10^{-5}$	$1.0(7) \cdot 10^{-13}$	$-1.83(6) \cdot 10^{-2}$
0.405	$-1(1) \cdot 10^{-7}$	$4(4) \cdot 10^{-8}$	$-3(2) \cdot 10^{-8}$	$-5(5) \cdot 10^{-12}$	$1.1(7) \cdot 10^{-11}$	$-1.0(1) \cdot 10^{-3}$
0.415	$5(2) \cdot 10^{-5}$	$1.1(4) \cdot 10^{-7}$	$-1(1) \cdot 10^{-11}$	$-1(1) \cdot 10^{-10}$	$4(4) \cdot 10^{-8}$	$-1.951(2) \cdot 10^{-1}$
0.425	$-2(4) \cdot 10^{-3}$	$-7.1(2) \cdot 10^{-3}$	$5(7) \cdot 10^{-7}$	0	0	0
0.435	0	$-1(1)\cdot 10^{-3}$	0	0	0	0
0.445	0	0	0	0	0	0

Table 12: Individual contributions from the different colour factors to $(1-T)\frac{dC_{(1-T)}}{d(1-T)}$ for the thrust distribution.

ρ	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.005	$-1.10(1) \cdot 10^4$	$6.01(2) \cdot 10^3$	$7.83(1) \cdot 10^2$	$2.82(4) \cdot 10^3$	$-6.094(5) \cdot 10^3$	$8.3694(7) \cdot 10^3$
0.015	$5.3(1) \cdot 10^3$	$3.64(3) \cdot 10^3$	$3.2(1) \cdot 10^{1}$	$-1.435(4) \cdot 10^4$	$-1.137(4) \cdot 10^3$	$3.4802(5) \cdot 10^3$
0.025	$9.2(1) \cdot 10^3$	$2.04(2) \cdot 10^3$	$-1.0(1) \cdot 10^{1}$	$-1.278(4) \cdot 10^4$	$-4.76(4) \cdot 10^2$	$2.3914(4) \cdot 10^3$
0.035	$1.03(1) \cdot 10^4$	$1.18(2) \cdot 10^3$	$-1.5(1) \cdot 10^{1}$	$-1.119(4) \cdot 10^4$	$-2.05(4) \cdot 10^2$	$1.8219(4) \cdot 10^3$
0.045	$1.04(1) \cdot 10^4$	$6.9(2) \cdot 10^2$	$-1.6(1) \cdot 10^{1}$	$-9.71(4) \cdot 10^3$	$-7.6(4) \cdot 10^{1}$	$1.4625(3) \cdot 10^3$
0.055	$9.7(1) \cdot 10^3$	$3.6(2) \cdot 10^2$	$-1.5(1) \cdot 10^{1}$	$-8.51(4) \cdot 10^3$	$4(4) \cdot 10^{0}$	$1.2114(3) \cdot 10^3$
0.065	$9.3(1) \cdot 10^3$	$1.7(2) \cdot 10^2$	$-1.0(1) \cdot 10^{1}$	$-7.48(4) \cdot 10^3$	$5.3(4) \cdot 10^{1}$	$1.0256(3) \cdot 10^3$
0.075	$8.4(1) \cdot 10^3$	$4(2) \cdot 10^{1}$	$-1.0(1) \cdot 10^{1}$	$-6.74(3) \cdot 10^3$	$8.0(4) \cdot 10^{1}$	$8.812(3) \cdot 10^2$
0.085	$7.9(1) \cdot 10^3$	$-4(2) \cdot 10^{1}$	$-9(1) \cdot 10^{0}$	$-5.87(3) \cdot 10^3$	$9.1(4) \cdot 10^{1}$	$7.673(3) \cdot 10^2$
0.095	$7.3(1) \cdot 10^3$	$-8(2) \cdot 10^{1}$	$-3(1) \cdot 10^{0}$	$-5.35(3) \cdot 10^3$	$1.03(4) \cdot 10^2$	$6.737(3) \cdot 10^2$
0.105	$6.5(1) \cdot 10^3$	$-1.4(2) \cdot 10^2$	$-8(1) \cdot 10^{0}$	$-4.75(3) \cdot 10^3$	$1.00(4) \cdot 10^2$	$5.964(3) \cdot 10^2$
0.115	$5.9(1) \cdot 10^3$	$-1.4(2) \cdot 10^2$	$-3(1) \cdot 10^{0}$	$-4.32(3) \cdot 10^3$	$1.05(3) \cdot 10^2$	$5.317(3) \cdot 10^2$
0.125	$5.3(1) \cdot 10^3$	$-1.6(2) \cdot 10^2$	$-4(1) \cdot 10^{0}$	$-3.86(3) \cdot 10^3$	$1.00(3) \cdot 10^2$	$4.764(2) \cdot 10^2$
0.135	$4.8(1) \cdot 10^3$	$-2.2(2) \cdot 10^2$	$-3.1(9) \cdot 10^0$	$-3.50(3) \cdot 10^3$	$9.7(3) \cdot 10^{1}$	$4.283(2) \cdot 10^2$
0.145	$4.4(1) \cdot 10^3$	$-1.6(1) \cdot 10^2$	$-1.5(9) \cdot 10^{0}$	$-3.09(3) \cdot 10^3$	$8.8(3) \cdot 10^{1}$	$3.875(2) \cdot 10^2$
0.155	$3.8(1) \cdot 10^3$	$-1.3(1) \cdot 10^2$	$-2.6(9) \cdot 10^{0}$	$-2.82(3) \cdot 10^3$	$8.3(3) \cdot 10^{1}$	$3.517(2) \cdot 10^2$
0.165	$3.45(9) \cdot 10^3$	$-1.6(1) \cdot 10^2$	$-1.1(8) \cdot 10^{0}$	$-2.48(2) \cdot 10^3$	$7.4(3) \cdot 10^{1}$	$3.194(2) \cdot 10^2$
0.175	$2.73(9) \cdot 10^3$	$-1.0(1) \cdot 10^2$	$-1.9(8) \cdot 10^{0}$	$-2.24(2)\cdot 10^3$	$7.1(3) \cdot 10^{1}$	$2.911(2) \cdot 10^2$
0.185	$2.22(9) \cdot 10^3$	$-1.0(1) \cdot 10^2$	$-1.8(8) \cdot 10^{0}$	$-2.04(2) \cdot 10^3$	$6.0(2) \cdot 10^{1}$	$2.649(2) \cdot 10^2$
0.195	$2.09(9) \cdot 10^3$	$-1.1(1) \cdot 10^2$	$-2(7) \cdot 10^{-1}$	$-1.81(2) \cdot 10^3$	$5.2(2) \cdot 10^{1}$	$2.410(2) \cdot 10^2$
0.205	$1.64(9) \cdot 10^3$	$-8(1) \cdot 10^{1}$	$-1.4(7) \cdot 10^{0}$	$-1.55(2)\cdot 10^3$	$4.7(2) \cdot 10^{1}$	$2.198(2) \cdot 10^2$
0.215	$1.33(8) \cdot 10^3$	$-5(1) \cdot 10^{1}$	$-7(7) \cdot 10^{-1}$	$-1.38(2) \cdot 10^3$	$4.2(2) \cdot 10^{1}$	$1.997(2) \cdot 10^2$
0.225	$8.7(8) \cdot 10^2$	$-5(1) \cdot 10^{1}$	$-2.2(6) \cdot 10^{0}$	$-1.22(2) \cdot 10^3$	$3.7(2) \cdot 10^{1}$	$1.814(2) \cdot 10^2$
0.235	$7.2(8) \cdot 10^2$	$-2.2(9) \cdot 10^{1}$	$-5(6) \cdot 10^{-1}$	$-1.06(2) \cdot 10^3$	$2.3(1) \cdot 10^{1}$	$1.632(2) \cdot 10^2$
0.245	$5.4(7) \cdot 10^2$	$-8(9) \cdot 10^{0}$	$-8(5) \cdot 10^{-1}$	$-9.0(2) \cdot 10^{2}$	$2.0(1) \cdot 10^{1}$	$1.469(2) \cdot 10^2$
0.255	$2.1(7) \cdot 10^2$	$-9(8) \cdot 10^{0}$	$-5(5) \cdot 10^{-1}$	$-7.1(2) \cdot 10^2$	$1.6(1) \cdot 10^{1}$	$1.309(2) \cdot 10^2$
0.265	$1.3(7) \cdot 10^2$	$9(8) \cdot 10^{0}$	$-7(4) \cdot 10^{-1}$	$-6.2(2) \cdot 10^2$	$9(1) \cdot 10^{0}$	$1.153(2) \cdot 10^2$
0.275	$-5(6) \cdot 10^{1}$	$1.5(7) \cdot 10^{1}$	$-5(4) \cdot 10^{-1}$	$-4.7(1) \cdot 10^2$	$5.5(9) \cdot 10^{0}$	$9.91(2) \cdot 10^{1}$
0.285	$-2.0(6) \cdot 10^2$	$7(6) \cdot 10^{0}$	$-8(3) \cdot 10^{-1}$	$-3.7(1) \cdot 10^2$	$-1(3) \cdot 10^{-1}$	$8.35(2) \cdot 10^{1}$
0.295	$-2.0(5) \cdot 10^2$	$2.8(5) \cdot 10^{1}$	$-4(2) \cdot 10^{-1}$	$-2.5(1) \cdot 10^2$	$-7(6) \cdot 10^{-1}$	$6.73(2) \cdot 10^{1}$
0.305	$-2.9(4) \cdot 10^{2}$	$1.9(4) \cdot 10^{1}$	$-2(2) \cdot 10^{-1}$	$-1.71(9) \cdot 10^2$	$-1.4(5) \cdot 10^{0}$	$4.94(1) \cdot 10^{1}$
0.315	$-2.1(3) \cdot 10^2$	$1.2(3) \cdot 10^{1}$	$-4(1) \cdot 10^{-1}$	$-1.24(6) \cdot 10^2$	$-5(3) \cdot 10^{-1}$	$2.99(1) \cdot 10^{1}$
0.325	$5(2) \cdot 10^{1}$	$5(2) \cdot 10^{0}$	$-2.5(6) \cdot 10^{-1}$	$-1.24(4) \cdot 10^2$	$3.2(2) \cdot 10^{0}$	$7.12(8) \cdot 10^0$
0.335	$1.34(5) \cdot 10^2$	$-7(7) \cdot 10^{-1}$	$-1.1(6) \cdot 10^{-3}$	$-7.5(1) \cdot 10^{1}$	$5.1(2) \cdot 10^{-1}$	$-1.041(4) \cdot 10^{1}$
0.345	$4.4(1) \cdot 10^{1}$	$-2.4(2) \cdot 10^{0}$	$-4.5(2) \cdot 10^{-2}$	$-1.57(3) \cdot 10^{1}$	$4(3) \cdot 10^{-5}$	$-4.52(1) \cdot 10^{0}$
0.355	$1.86(6) \cdot 10^{1}$	$-3.1(6) \cdot 10^{-1}$	$-1.2(7) \cdot 10^{-5}$	$-7.5(1) \cdot 10^{0}$	$3(3) \cdot 10^{-11}$	$-1.639(5) \cdot 10^{0}$
0.365	$3.7(2) \cdot 10^0$	$-2.4(8) \cdot 10^{-2}$	$-4.0(4) \cdot 10^{-4}$	$-7.5(3) \cdot 10^{-1}$	$1(1) \cdot 10^{-12}$	$-1.62(1) \cdot 10^{-1}$
0.375	$1.4(2) \cdot 10^{-1}$	$-3(3) \cdot 10^{-7}$	$-7(1) \cdot 10^{-5}$	$-5(5) \cdot 10^{-6}$	$4(2) \cdot 10^{-11}$	$-4.38(5) \cdot 10^{-2}$
0.385	$2.1(4) \cdot 10^{-2}$	$1.8(7) \cdot 10^{-6}$	$-3(3) \cdot 10^{-9}$	$-7(7) \cdot 10^{-14}$	$6(4) \cdot 10^{-8}$	$-9.09(2) \cdot 10^{-2}$
0.395	$3(4) \cdot 10^{-5}$	$3(2) \cdot 10^{-9}$	$-2(2) \cdot 10^{-11}$	$-1(1) \cdot 10^{-12}$	$3(2) \cdot 10^{-11}$	$-2.7(2) \cdot 10^{-3}$
0.405	$-3(2) \cdot 10^{-7}$	$9(7) \cdot 10^{-10}$	$-3(1) \cdot 10^{-11}$	$-6(4) \cdot 10^{-12}$	$9(8) \cdot 10^{-9}$	$-3.7(4) \cdot 10^{-3}$
0.415	$2(2) \cdot 10^{-8}$	$1(1) \cdot 10^{-5}$	$-4(4) \cdot 10^{-9}$	$-6(6) \cdot 10^{-4}$	0	$-1.0(4) \cdot 10^{-1}$
0.425	0	0	0	0	0	0

Table 13: Individual contributions from the different colour factors to $\rho \frac{dC_{\rho}}{d\rho}$ for the heavy jet mass distribution.

B_W	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.005	$3.30(6) \cdot 10^4$	$-8.6(1) \cdot 10^3$	$4.845(5) \cdot 10^3$	$1.192(2) \cdot 10^5$	$-2.799(2) \cdot 10^4$	$2.2782(2) \cdot 10^4$
0.015	$-3.05(2) \cdot 10^4$	$1.169(6) \cdot 10^4$	$7.19(4) \cdot 10^2$	$-8.55(9) \cdot 10^3$	$-6.85(1) \cdot 10^3$	$1.0195(1) \cdot 10^4$
0.025	$-7.5(2) \cdot 10^3$	$8.19(6) \cdot 10^3$	$2.20(3) \cdot 10^2$	$-1.788(8) \cdot 10^4$	$-3.356(9) \cdot 10^3$	$6.8578(7) \cdot 10^3$
0.035	$3.8(2) \cdot 10^3$	$5.78(5) \cdot 10^3$	$7.1(3) \cdot 10^{1}$	$-1.922(7) \cdot 10^4$	$-1.908(8) \cdot 10^3$	$5.1322(6) \cdot 10^3$
0.045	$9.9(2) \cdot 10^3$	$3.95(4) \cdot 10^3$	$1.1(2) \cdot 10^{1}$	$-1.853(6) \cdot 10^4$	$-1.145(7) \cdot 10^3$	$4.0453(6) \cdot 10^3$
0.055	$1.25(2) \cdot 10^4$	$2.84(4) \cdot 10^3$	$0(2) \cdot 10^{-1}$	$-1.731(6) \cdot 10^4$	$-7.03(6) \cdot 10^2$	$3.2925(5) \cdot 10^3$
0.065	$1.40(2) \cdot 10^4$	$1.96(4) \cdot 10^3$	$-1.4(2) \cdot 10^{1}$	$-1.571(6) \cdot 10^4$	$-4.33(6) \cdot 10^2$	$2.7390(5) \cdot 10^3$
0.075	$1.40(2) \cdot 10^4$	$1.41(3) \cdot 10^3$	$-1.4(2) \cdot 10^{1}$	$-1.437(5) \cdot 10^4$	$-2.44(6) \cdot 10^2$	$2.3111(4) \cdot 10^3$
0.085	$1.37(2) \cdot 10^4$	$8.4(3) \cdot 10^2$	$-1.3(2) \cdot 10^{1}$	$-1.292(5) \cdot 10^4$	$-1.07(5) \cdot 10^2$	$1.9746(4) \cdot 10^3$
0.095	$1.33(2) \cdot 10^4$	$6.5(3) \cdot 10^2$	$-1.2(1) \cdot 10^{1}$	$-1.156(5) \cdot 10^4$	$-3.0(5) \cdot 10^{1}$	$1.7000(4) \cdot 10^3$
0.105	$1.26(2) \cdot 10^4$	$3.3(2) \cdot 10^2$	$-1.4(1) \cdot 10^{1}$	$-1.047(4) \cdot 10^4$	$2.2(5) \cdot 10^{1}$	$1.4749(4) \cdot 10^3$
0.115	$1.14(2) \cdot 10^4$	$1.8(2) \cdot 10^2$	$-9(1)\cdot 10^{0}$	$-9.47(4) \cdot 10^3$	$5.6(5) \cdot 10^{1}$	$1.2858(3) \cdot 10^3$
0.125	$1.08(2) \cdot 10^4$	$6(2) \cdot 10^{1}$	$-7(1) \cdot 10^{0}$	$-8.38(4) \cdot 10^3$	$9.5(4) \cdot 10^{1}$	$1.1265(3) \cdot 10^3$
0.135	$9.8(1) \cdot 10^3$	$-5(2) \cdot 10^{1}$	$-6(1) \cdot 10^{0}$	$-7.50(4) \cdot 10^3$	$1.02(4) \cdot 10^2$	$9.905(3) \cdot 10^2$
0.145	$8.6(1) \cdot 10^3$	$-1.2(2)\cdot 10^2$	$-5(1) \cdot 10^{0}$	$-6.70(4) \cdot 10^3$	$1.03(4) \cdot 10^2$	$8.725(3) \cdot 10^2$
0.155	$8.0(1) \cdot 10^3$	$-1.7(2)\cdot 10^2$	$-2.3(9) \cdot 10^{0}$	$-5.95(4) \cdot 10^3$	$1.24(4) \cdot 10^2$	$7.710(3) \cdot 10^2$
0.165	$7.0(1) \cdot 10^3$	$-1.5(2)\cdot 10^2$	$-3.8(8) \cdot 10^{0}$	$-5.25(3) \cdot 10^3$	$1.13(3) \cdot 10^2$	$6.831(3) \cdot 10^2$
0.175	$5.8(1) \cdot 10^3$	$-1.8(2) \cdot 10^2$	$-2(8)\cdot 10^{-1}$	$-4.67(3) \cdot 10^3$	$1.06(3) \cdot 10^2$	$6.068(3) \cdot 10^2$
0.185	$4.8(1) \cdot 10^3$	$-1.7(1) \cdot 10^2$	$-4(7) \cdot 10^{-1}$	$-4.09(3) \cdot 10^3$	$9.8(3) \cdot 10^{1}$	$5.386(2) \cdot 10^2$
0.195	$3.9(1) \cdot 10^3$	$-1.3(1) \cdot 10^2$	$-1.5(7) \cdot 10^0$	$-3.48(3) \cdot 10^3$	$8.3(3) \cdot 10^{1}$	$4.795(2) \cdot 10^2$
0.205	$3.2(1) \cdot 10^3$	$-1.2(1)\cdot 10^2$	$-2.1(6) \cdot 10^{0}$	$-3.00(3) \cdot 10^3$	$7.7(2) \cdot 10^{1}$	$4.269(2) \cdot 10^2$
0.215	$2.0(1) \cdot 10^3$	$-7(1) \cdot 10^{1}$	$-3(6)\cdot 10^{-1}$	$-2.46(3) \cdot 10^3$	$5.6(2) \cdot 10^{1}$	$3.790(2) \cdot 10^2$
0.225	$1.28(9) \cdot 10^3$	$-2(1) \cdot 10^{1}$	$-1.5(5) \cdot 10^{0}$	$-1.99(2) \cdot 10^3$	$4.1(2) \cdot 10^{1}$	$3.348(2) \cdot 10^2$
0.235	$6.2(9) \cdot 10^2$	$-2(1) \cdot 10^{1}$	$-5(5)\cdot 10^{-1}$	$-1.58(2) \cdot 10^3$	$2.3(2) \cdot 10^{1}$	$2.937(2) \cdot 10^2$
0.245	$-3.1(8) \cdot 10^2$	$3.8(9) \cdot 10^{1}$	$-8(4) \cdot 10^{-1}$	$-1.17(2)\cdot 10^3$	$1.3(1) \cdot 10^{1}$	$2.529(2) \cdot 10^2$
0.255	$-6.2(7) \cdot 10^2$	$6.3(8) \cdot 10^{1}$	$-9(3) \cdot 10^{-1}$	$-7.3(2) \cdot 10^2$	$-6(1) \cdot 10^{0}$	$2.123(2) \cdot 10^2$
0.265	$-1.11(6) \cdot 10^3$	$7.4(6) \cdot 10^{1}$	$4(3) \cdot 10^{-1}$	$-3.4(1) \cdot 10^2$	$-1.06(6) \cdot 10^{1}$	$1.678(2) \cdot 10^2$
0.275	$-1.23(4) \cdot 10^3$	$7.0(4) \cdot 10^{1}$	$8(2) \cdot 10^{-1}$	$-3(1) \cdot 10^{1}$	$-2.37(5) \cdot 10^{1}$	$1.136(1) \cdot 10^2$
0.285	$-4.1(2) \cdot 10^2$	$1.2(2) \cdot 10^{1}$	$1.5(6) \cdot 10^{-1}$	$-2.7(5) \cdot 10^{1}$	$-6.7(2) \cdot 10^{0}$	$2.952(8) \cdot 10^{1}$
0.295	$1.9(1) \cdot 10^{1}$	$-2.0(2)\cdot 10^{0}$	$-5.9(2)\cdot 10^{-2}$	$-3.17(4) \cdot 10^{1}$	$3(2) \cdot 10^{-5}$	$-5.73(1) \cdot 10^0$
0.305	$1.53(9) \cdot 10^0$	$-7(7) \cdot 10^{-5}$	$-1.31(8) \cdot 10^{-3}$	$-2(1)\cdot 10^{-3}$	$5(3) \cdot 10^{-12}$	$-1.13(1) \cdot 10^{-1}$
0.315	$1.9(6) \cdot 10^{-3}$	$4(3) \cdot 10^{-8}$	$-5(3) \cdot 10^{-10}$	$-9(9) \cdot 10^{-11}$	$9(5) \cdot 10^{-12}$	$-2.8(2)\cdot 10^{-3}$
0.325	$1.5(8) \cdot 10^{-2}$	$3(3) \cdot 10^{-4}$	$-3(3) \cdot 10^{-9}$	$-4(4) \cdot 10^{-4}$	0	$-7(3) \cdot 10^{-2}$
0.335	0	0	0	0	0	0

Table 14: Individual contributions from the different colour factors to $B_W \frac{dC_{B_W}}{dB_W}$ for the wide jet broadening distribution.

B_T	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.005	$-2.9(7) \cdot 10^3$	$-3.2(1) \cdot 10^3$	$4.480(8) \cdot 10^3$	$9.64(2) \cdot 10^4$	$-2.592(2) \cdot 10^4$	$2.2742(2) \cdot 10^4$
0.015	$-5.33(5) \cdot 10^4$	$1.97(1) \cdot 10^4$	$-1.1(1) \cdot 10^2$	$-2.75(2) \cdot 10^4$	$-4.92(2) \cdot 10^3$	$1.01489(9) \cdot 10^4$
0.025	$-1.23(5) \cdot 10^4$	$1.32(1) \cdot 10^4$	$-3.8(1) \cdot 10^2$	$-3.34(2) \cdot 10^4$	$-1.69(2) \cdot 10^3$	$6.8099(7) \cdot 10^3$
0.035	$7.1(4) \cdot 10^3$	$9.3(1)\cdot 10^3$	$-3.83(9) \cdot 10^2$	$-3.31(2) \cdot 10^4$	$-4.4(2)\cdot 10^2$	$5.0819(6) \cdot 10^3$
0.045	$1.70(4) \cdot 10^4$	$6.2(1) \cdot 10^3$	$-3.46(8) \cdot 10^2$	$-3.08(2) \cdot 10^4$	$1.6(2) \cdot 10^2$	$3.9942(5) \cdot 10^3$
0.055	$2.26(4) \cdot 10^4$	$4.1(1) \cdot 10^3$	$-2.95(7) \cdot 10^2$	$-2.85(1) \cdot 10^4$	$4.6(2) \cdot 10^2$	$3.2413(5) \cdot 10^3$
0.065	$2.58(4) \cdot 10^4$	$2.92(9) \cdot 10^3$	$-2.57(6) \cdot 10^2$	$-2.59(1) \cdot 10^4$	$6.5(2) \cdot 10^2$	$2.6872(5) \cdot 10^3$
0.075	$2.65(4) \cdot 10^4$	$1.82(8) \cdot 10^3$	$-2.20(6)\cdot 10^2$	$-2.37(1) \cdot 10^4$	$7.4(1) \cdot 10^2$	$2.2583(5) \cdot 10^3$
0.085	$2.64(4) \cdot 10^4$	$8.8(7) \cdot 10^2$	$-1.81(5)\cdot 10^2$	$-2.16(1) \cdot 10^4$	$8.3(1) \cdot 10^2$	$1.9214(5) \cdot 10^3$
0.095	$2.69(3) \cdot 10^4$	$4.9(7) \cdot 10^2$	$-1.60(5) \cdot 10^2$	$-1.96(1) \cdot 10^4$	$8.3(1) \cdot 10^2$	$1.6464(5) \cdot 10^3$
0.105	$2.56(3) \cdot 10^4$	$-0(6) \cdot 10^{0}$	$-1.41(4) \cdot 10^2$	$-1.78(1) \cdot 10^4$	$8.3(1) \cdot 10^2$	$1.4206(5) \cdot 10^3$
0.115	$2.49(3) \cdot 10^4$	$-3.3(6) \cdot 10^2$	$-1.15(4)\cdot 10^2$	$-1.66(1) \cdot 10^4$	$8.3(1) \cdot 10^2$	$1.2309(5) \cdot 10^3$
0.125	$2.37(3) \cdot 10^4$	$-6.3(5) \cdot 10^2$	$-9.9(4) \cdot 10^{1}$	$-1.52(1) \cdot 10^4$	$8.0(1) \cdot 10^2$	$1.0699(5) \cdot 10^3$
0.135	$2.28(3) \cdot 10^4$	$-6.7(5) \cdot 10^2$	$-7.9(3) \cdot 10^{1}$	$-1.352(9) \cdot 10^4$	$7.8(1) \cdot 10^2$	$9.316(5) \cdot 10^2$
0.145	$2.09(3) \cdot 10^4$	$-8.3(5) \cdot 10^2$	$-7.3(3) \cdot 10^{1}$	$-1.251(9) \cdot 10^4$	$7.2(1) \cdot 10^2$	$8.118(5) \cdot 10^2$
0.155	$2.03(3) \cdot 10^4$	$-1.03(4) \cdot 10^3$	$-6.4(3) \cdot 10^{1}$	$-1.152(8) \cdot 10^4$	$7.1(1) \cdot 10^2$	$7.091(5) \cdot 10^2$
0.165	$1.90(2) \cdot 10^4$	$-1.03(4) \cdot 10^3$	$-5.6(3) \cdot 10^{1}$	$-1.045(8) \cdot 10^4$	$6.63(9) \cdot 10^2$	$6.171(6) \cdot 10^2$
0.175	$1.78(2) \cdot 10^4$	$-1.01(4) \cdot 10^3$	$-4.0(2) \cdot 10^{1}$	$-9.77(7) \cdot 10^3$	$6.30(8) \cdot 10^2$	$5.373(6) \cdot 10^2$
0.185	$1.64(2) \cdot 10^4$	$-1.12(4) \cdot 10^3$	$-3.5(2) \cdot 10^{1}$	$-8.74(7) \cdot 10^3$	$6.09(8) \cdot 10^2$	$4.632(6) \cdot 10^2$
0.195	$1.53(2) \cdot 10^4$	$-1.05(3) \cdot 10^3$	$-3.8(2) \cdot 10^{1}$	$-7.94(7) \cdot 10^3$	$5.50(7) \cdot 10^2$	$3.985(6) \cdot 10^2$
0.205	$1.46(2) \cdot 10^4$	$-1.09(3) \cdot 10^3$	$-2.6(2) \cdot 10^{1}$	$-7.42(7) \cdot 10^3$	$5.47(7) \cdot 10^2$	$3.382(7) \cdot 10^2$
0.215	$1.36(2) \cdot 10^4$	$-1.05(3) \cdot 10^3$	$-2.2(2) \cdot 10^{1}$	$-6.66(6) \cdot 10^3$	$4.95(6) \cdot 10^2$	$2.827(7) \cdot 10^2$
0.225	$1.26(2) \cdot 10^4$	$-9.4(3) \cdot 10^2$	$-2.4(2) \cdot 10^{1}$	$-6.12(6) \cdot 10^3$	$4.71(6) \cdot 10^2$	$2.304(7) \cdot 10^2$
0.235	$1.17(2) \cdot 10^4$	$-9.4(2) \cdot 10^2$	$-1.6(1) \cdot 10^{1}$	$-5.66(6) \cdot 10^3$	$4.34(5) \cdot 10^2$	$1.774(7) \cdot 10^2$
0.245	$1.09(2) \cdot 10^4$	$-9.2(2) \cdot 10^2$	$-1.4(1) \cdot 10^{1}$	$-5.12(5) \cdot 10^3$	$4.11(5) \cdot 10^2$	$1.263(7) \cdot 10^2$
0.255	$1.02(1) \cdot 10^4$	$-8.4(2) \cdot 10^2$	$-1.3(1) \cdot 10^{1}$	$-4.76(5) \cdot 10^3$	$3.80(4) \cdot 10^2$	$7.01(7) \cdot 10^{1}$
0.265	$9.7(1) \cdot 10^3$	$-8.1(2) \cdot 10^2$	$-1.12(9) \cdot 10^{1}$	$-4.47(4) \cdot 10^3$	$3.58(3) \cdot 10^2$	$7.7(6) \cdot 10^{0}$
0.275	$9.4(1) \cdot 10^3$	$-7.2(1) \cdot 10^2$	$-1.09(7) \cdot 10^{1}$	$-4.24(3) \cdot 10^3$	$3.46(3) \cdot 10^2$	$-6.79(6) \cdot 10^{1}$
0.285	$9.11(7) \cdot 10^3$	$-6.12(9) \cdot 10^2$	$-1.28(5) \cdot 10^{1}$	$-4.17(2) \cdot 10^3$	$3.43(2) \cdot 10^2$	$-1.722(4) \cdot 10^2$
0.295 0.305	$8.52(4) \cdot 10^3$	$-6.91(5) \cdot 10^2$	$-8(3) \cdot 10^{-1}$	$-2.77(1) \cdot 10^3$	$2.35(1) \cdot 10^2$	$-1.570(2) \cdot 10^2$
0.303	$6.26(3) \cdot 10^3$ $4.55(2) \cdot 10^3$	$ \begin{array}{c c} -5.47(3) \cdot 10^2 \\ -4.14(3) \cdot 10^2 \end{array} $	$2.3(2) \cdot 10^0$ $1.9(1) \cdot 10^0$	$-1.741(9) \cdot 10^3$	$8.57(6) \cdot 10^{1}$ $3.32(3) \cdot 10^{1}$	$-1.046(1) \cdot 10^2$ $-7.413(9) \cdot 10^1$
0.313	$3.24(2) \cdot 10^3$	$-3.03(2) \cdot 10^2$	$1.5(1) \cdot 10^{0}$ $1.5(1) \cdot 10^{0}$	$ \begin{array}{r} -1.215(7) \cdot 10^3 \\ -8.52(5) \cdot 10^2 \end{array} $	$3.42(8) \cdot 10^{0}$	$-7.413(9) \cdot 10$ $-5.275(6) \cdot 10^{1}$
0.325	$2.24(1) \cdot 10^3$	$-3.03(2) \cdot 10$ $-2.20(2) \cdot 10^2$	$1.03(7) \cdot 10^{0}$ $1.03(7) \cdot 10^{0}$	$-6.52(3) \cdot 10$ $-5.65(3) \cdot 10^2$	$1.99(5) \cdot 10^0$	$-3.615(5) \cdot 10^{1}$
0.333	$1.337(9) \cdot 10^3$	$-2.20(2) \cdot 10$ $-1.36(1) \cdot 10^2$	$4.5(4) \cdot 10^{-1}$	$-3.03(3) \cdot 10$ $-3.23(2) \cdot 10^2$	$7.7(3) \cdot 10^{-1}$	$-3.013(3) \cdot 10$ $-2.237(3) \cdot 10^{1}$
0.343	$6.37(5) \cdot 10^2$	$-6.24(6) \cdot 10^{1}$	$8(4) \cdot 10^{-3}$	$-3.23(2) \cdot 10$ $-1.470(9) \cdot 10^2$	$2.5(1) \cdot 10^{-1}$	$-2.237(3) \cdot 10$ $-1.226(2) \cdot 10^{1}$
0.365	$2.81(3) \cdot 10^2$	$-0.24(0) \cdot 10^{1}$ $-2.50(3) \cdot 10^{1}$	$-1.3(3) \cdot 10^{-2}$	$-6.80(4) \cdot 10^{1}$	$1.2(2) \cdot 10^{-2}$	$-6.38(2) \cdot 10^{0}$
0.303	$1.01(1) \cdot 10^2$	$-3.0(3) \cdot 10^{-1}$	$-1.6(1) \cdot 10^{-2}$	$-2.75(2) \cdot 10^{1}$	$7(6) \cdot 10^{-12}$	$-0.38(2) \cdot 10$ $-2.90(1) \cdot 10^{0}$
0.375	$4.7(1) \cdot 10^0$	$-3.8(2) \cdot 10^{-1}$	$-2.2(4) \cdot 10^{-4}$	$-2.0(1) \cdot 10^{-1}$	$9(6) \cdot 10^{-14}$	$-1.80(2) \cdot 10^{-1}$
0.395	$1.0(1) \cdot 10^{-1}$	$4(4) \cdot 10^{-8}$	$-2.2(4) \cdot 10^{-9}$	$-2.0(1) \cdot 10^{-7}$	$1.4(8) \cdot 10^{-12}$	$-1.17(5) \cdot 10^{-2}$
0.405	$-1.3(6) \cdot 10^{-5}$	$9(6) \cdot 10^{-10}$	$-3(1) \cdot 10^{-12}$	$-1(1) \cdot 10^{-10}$	$3(2) \cdot 10^{-4}$	$-7.38(4) \cdot 10^{-2}$
0.415	0	0	0	0	0	0
	, ,			, ,	, ,	

Table 15: Individual contributions from the different colour factors to $B_T \frac{dC_{B_T}}{dB_T}$ for the total jet broadening distribution.

С	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.005	$-2.82(3) \cdot 10^4$	$4.28(9) \cdot 10^3$	$2.583(6) \cdot 10^3$	$5.10(1) \cdot 10^4$	$-1.578(1) \cdot 10^4$	$1.6764(2) \cdot 10^4$
0.015	$-3.60(3) \cdot 10^4$	$1.22(1) \cdot 10^4$	$4.7(1) \cdot 10^2$	$-1.04(2) \cdot 10^4$	$-5.45(2) \cdot 10^3$	$8.808(1) \cdot 10^3$
0.025	$-1.76(4) \cdot 10^4$	$9.8(1) \cdot 10^3$	$1.6(1) \cdot 10^2$	$-1.73(2) \cdot 10^4$	$-3.27(2) \cdot 10^3$	$6.697(1) \cdot 10^3$
0.035	$-7.3(4) \cdot 10^3$	$8.6(1) \cdot 10^3$	$2(1) \cdot 10^{1}$	$-1.94(2) \cdot 10^4$	$-2.23(2)\cdot 10^3$	$5.522(1) \cdot 10^3$
0.045	$-1.0(4) \cdot 10^3$	$6.6(1) \cdot 10^3$	$-6(1) \cdot 10^{1}$	$-1.99(2) \cdot 10^4$	$-1.59(2) \cdot 10^3$	$4.7388(9) \cdot 10^3$
0.055	$4.2(4) \cdot 10^3$	$5.8(1) \cdot 10^3$	$-6(1) \cdot 10^{1}$	$-2.05(2) \cdot 10^4$	$-1.16(2) \cdot 10^3$	$4.1679(9) \cdot 10^3$
0.065	$6.8(4) \cdot 10^3$	$5.2(1) \cdot 10^3$	$-9(1) \cdot 10^{1}$	$-2.01(2) \cdot 10^4$	$-8.3(2)\cdot 10^2$	$3.7300(9) \cdot 10^3$
0.075	$9.4(4) \cdot 10^3$	$4.3(1) \cdot 10^3$	$-1.1(1) \cdot 10^2$	$-1.91(2) \cdot 10^4$	$-6.2(2)\cdot 10^2$	$3.3755(9) \cdot 10^3$
0.085	$1.12(5) \cdot 10^4$	$3.6(1) \cdot 10^3$	$-9(1) \cdot 10^{1}$	$-1.89(2) \cdot 10^4$	$-4.3(2) \cdot 10^2$	$3.0855(9) \cdot 10^3$
0.095	$1.20(5) \cdot 10^4$	$3.3(1) \cdot 10^3$	$-1.1(1) \cdot 10^2$	$-1.85(2) \cdot 10^4$	$-3.1(2) \cdot 10^2$	$2.8420(8) \cdot 10^3$
0.105	$1.44(5) \cdot 10^4$	$2.6(1) \cdot 10^3$	$-1.1(1)\cdot 10^2$	$-1.78(2) \cdot 10^4$	$-1.7(2) \cdot 10^2$	$2.6327(8) \cdot 10^3$
0.115	$1.42(5) \cdot 10^4$	$2.6(1) \cdot 10^3$	$-9(1)\cdot 10^{1}$	$-1.77(1) \cdot 10^4$	$-7(2)\cdot 10^{1}$	$2.4504(8) \cdot 10^3$
0.125	$1.45(5) \cdot 10^4$	$2.1(1) \cdot 10^3$	$-1.1(1) \cdot 10^2$	$-1.70(1) \cdot 10^4$	$-3(2) \cdot 10^{1}$	$2.2893(8) \cdot 10^3$
0.135	$1.59(5) \cdot 10^4$	$1.9(1) \cdot 10^3$	$-1.1(1)\cdot 10^2$	$-1.66(1) \cdot 10^4$	$7(2) \cdot 10^{1}$	$2.1488(8) \cdot 10^3$
0.145	$1.62(5) \cdot 10^4$	$1.7(1) \cdot 10^3$	$-6(1)\cdot 10^{1}$	$-1.63(1) \cdot 10^4$	$8(2) \cdot 10^{1}$	$2.0234(8) \cdot 10^3$
0.155	$1.65(5) \cdot 10^4$	$1.4(1) \cdot 10^3$	$-9(1) \cdot 10^{1}$	$-1.56(1) \cdot 10^4$	$1.3(2) \cdot 10^2$	$1.9086(8) \cdot 10^3$
0.165	$1.65(5) \cdot 10^4$	$1.2(1) \cdot 10^3$	$-9.2(9) \cdot 10^{1}$	$-1.54(1) \cdot 10^4$	$1.8(2) \cdot 10^2$	$1.8064(8) \cdot 10^3$
0.175	$1.67(5) \cdot 10^4$	$1.0(1) \cdot 10^3$	$-9.0(9) \cdot 10^{1}$	$-1.48(1) \cdot 10^4$	$2.2(2) \cdot 10^{2}$	$1.7110(8) \cdot 10^3$
0.185	$1.70(5) \cdot 10^4$	$8(1) \cdot 10^2$	$-6.0(9) \cdot 10^{1}$	$-1.42(1) \cdot 10^4$	$2.8(2) \cdot 10^2$	$1.6272(8) \cdot 10^3$
0.195	$1.63(5) \cdot 10^4$	$6(1) \cdot 10^2$	$-5.6(9) \cdot 10^{1}$	$-1.43(1) \cdot 10^4$	$2.7(2) \cdot 10^2$	$1.5478(8) \cdot 10^3$
0.205	$1.67(5) \cdot 10^4$	$6(1) \cdot 10^2$	$-6.4(9) \cdot 10^{1}$	$-1.36(1) \cdot 10^4$	$3.2(2) \cdot 10^2$	$1.4751(8) \cdot 10^3$
0.215	$1.72(5) \cdot 10^4$	$4(1) \cdot 10^2$	$-7.1(8) \cdot 10^{1}$	$-1.34(1) \cdot 10^4$	$3.0(2) \cdot 10^2$	$1.4074(8) \cdot 10^3$
0.225	$1.68(5) \cdot 10^4$	$3(1) \cdot 10^2$	$-5.1(8) \cdot 10^{1}$	$-1.29(1) \cdot 10^4$	$3.5(2) \cdot 10^2$	$1.3450(8) \cdot 10^3$
0.235	$1.72(5) \cdot 10^4$	$1(1) \cdot 10^2$	$-4.1(8)\cdot 10^{1}$	$-1.26(1) \cdot 10^4$	$3.4(2) \cdot 10^2$	$1.2865(8) \cdot 10^3$
0.245	$1.71(5) \cdot 10^4$	$2(1) \cdot 10^2$	$-7.2(8) \cdot 10^{1}$	$-1.21(1) \cdot 10^4$	$3.2(2) \cdot 10^2$	$1.2336(8) \cdot 10^3$
0.255	$1.70(5) \cdot 10^4$	$-6(9) \cdot 10^{1}$	$-4.3(7) \cdot 10^{1}$	$-1.22(1) \cdot 10^4$	$3.9(2) \cdot 10^2$	$1.1829(8) \cdot 10^3$
0.265	$1.65(5) \cdot 10^4$	$-1(9) \cdot 10^{1}$	$-5.1(8) \cdot 10^{1}$	$-1.17(1) \cdot 10^4$	$3.7(2) \cdot 10^2$	$1.1354(8) \cdot 10^3$
0.275	$1.67(5) \cdot 10^4$	$-3(9) \cdot 10^{1}$	$-4.3(7) \cdot 10^{1}$	$-1.15(1) \cdot 10^4$	$3.7(2) \cdot 10^2$	$1.0907(8) \cdot 10^3$
0.285	$1.59(5) \cdot 10^4$	$-2.8(9) \cdot 10^{2}$	$-4.3(7) \cdot 10^{1}$	$-1.11(1) \cdot 10^4$	$3.6(2) \cdot 10^2$	$1.0482(8) \cdot 10^3$
0.295	$1.65(5) \cdot 10^4$	$-2.4(9) \cdot 10^{2}$	$-3.1(7) \cdot 10^{1}$	$-1.08(1) \cdot 10^4$	$3.8(2) \cdot 10^2$	$1.0099(8) \cdot 10^3$
0.305	$1.61(5) \cdot 10^4$	$-2.2(9) \cdot 10^{2}$	$-4.3(7) \cdot 10^{1}$	$-1.07(1) \cdot 10^4$	$3.7(2) \cdot 10^2$	$9.723(8) \cdot 10^2$
0.315	$1.63(5) \cdot 10^4$	$-3.6(9) \cdot 10^{2}$	$-2.9(7) \cdot 10^{1}$	$-1.04(1) \cdot 10^4$	$3.9(2) \cdot 10^2$	$9.347(8) \cdot 10^2$
0.325	$1.55(5) \cdot 10^4$	$-3.9(9) \cdot 10^{2}$	$-3.1(7) \cdot 10^{1}$	$-9.8(1) \cdot 10^3$	$3.8(2) \cdot 10^2$	$9.033(8) \cdot 10^2$
0.335	$1.53(5) \cdot 10^4$	$-3.1(8)\cdot 10^{2}$	$-1.7(7) \cdot 10^{1}$	$-9.9(1) \cdot 10^3$	$3.9(2) \cdot 10^2$	$8.704(8) \cdot 10^2$
0.345	$1.51(5) \cdot 10^4$	$-4.2(8) \cdot 10^{2}$	$-2.8(7) \cdot 10^{1}$	$-9.8(1) \cdot 10^3$	$3.9(2) \cdot 10^2$	$8.412(8) \cdot 10^2$
0.355	$1.48(5) \cdot 10^4$	$-4.6(8) \cdot 10^2$	$-2.7(6) \cdot 10^{1}$	$-9.3(1) \cdot 10^3$	$3.8(2) \cdot 10^2$	$8.126(8) \cdot 10^2$
0.365	$1.50(4) \cdot 10^4$	$-5.7(8) \cdot 10^{2}$	$-2.7(6) \cdot 10^{1}$	$-9.2(1) \cdot 10^3$	$3.9(2) \cdot 10^2$	$7.836(8) \cdot 10^2$
0.375	$1.54(4) \cdot 10^4$	$-5.2(8) \cdot 10^{2}$	$-1.8(6) \cdot 10^{1}$	$-9.0(1) \cdot 10^{3}$	$4.0(2) \cdot 10^2$	$7.592(8) \cdot 10^2$
0.385	$1.44(4) \cdot 10^4$	$-5.3(8) \cdot 10^2$	$-2.0(6) \cdot 10^{1}$	$-8.6(1) \cdot 10^3$	$3.9(2) \cdot 10^2$	$7.343(8) \cdot 10^2$
0.395	$1.44(4) \cdot 10^4$	$-5.8(8) \cdot 10^{2}$	$-2.5(6) \cdot 10^{1}$	$-8.8(1) \cdot 10^3$	$3.9(2) \cdot 10^2$	$7.092(8) \cdot 10^2$
0.405	$1.40(4) \cdot 10^4$	$-5.6(8) \cdot 10^2$	$-1.1(6) \cdot 10^{1}$	$-8.3(1) \cdot 10^3$	$3.8(1) \cdot 10^2$	$6.859(8) \cdot 10^2$
0.415	$1.48(4) \cdot 10^4$	$-6.8(7) \cdot 10^2$	$-1.3(6) \cdot 10^{1}$	$-8.1(1) \cdot 10^3$	$3.3(1) \cdot 10^2$	$6.657(8) \cdot 10^2$
0.425	$1.34(4) \cdot 10^4$	$-6.5(7) \cdot 10^2$	$-2.2(5) \cdot 10^{1}$	$-7.9(1) \cdot 10^3$	$3.8(1) \cdot 10^2$	$6.445(8) \cdot 10^2$
0.435	$1.35(4) \cdot 10^4$	$-6.6(7) \cdot 10^2$	$-1.4(5) \cdot 10^{1}$	$-7.8(1) \cdot 10^3$	$4.0(1) \cdot 10^2$	$6.234(8) \cdot 10^2$
0.445	$1.35(4) \cdot 10^4$	$-6.5(7) \cdot 10^{2}$	$-2.6(5) \cdot 10^{1}$	$-7.6(1) \cdot 10^3$	$3.5(1) \cdot 10^2$	$6.052(8) \cdot 10^2$
0.455	$1.36(4) \cdot 10^4$	$-9.0(7) \cdot 10^{2}$	$-6(5)\cdot 10^{0}$	$-7.6(1) \cdot 10^3$	$3.6(1) \cdot 10^2$	$5.859(8) \cdot 10^2$
0.465	$1.33(4) \cdot 10^4$	$-6.2(7) \cdot 10^2$	$-1.3(5) \cdot 10^{1}$	$-7.1(1) \cdot 10^3$	$3.9(1) \cdot 10^2$	$5.683(8) \cdot 10^2$
0.475	$1.27(4) \cdot 10^4$	$-6.7(7) \cdot 10^2$	$-1.1(5) \cdot 10^{1}$	$-7.3(1) \cdot 10^3$	$3.7(1) \cdot 10^2$	$5.506(8) \cdot 10^2$
0.485	$1.27(4) \cdot 10^4$	$-8.4(7) \cdot 10^{2}$	$-1.2(5)\cdot 10^{1}$	$-6.8(1) \cdot 10^3$	$3.6(1) \cdot 10^2$	$5.366(8) \cdot 10^2$
0.495	$1.26(4) \cdot 10^4$	$-7.0(7) \cdot 10^{2}$	$-1.3(5)\cdot 10^{1}$	$-6.9(1) \cdot 10^3$	$3.4(1) \cdot 10^2$	$5.190(8) \cdot 10^{2}$
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Table 16: Individual contributions from the different colour factors to $\rho \frac{dC_C}{dC}$ for the C parameter distribution.

С	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.505	$1.24(4) \cdot 10^4$	$-8.6(7) \cdot 10^2$	$-4(5) \cdot 10^{0}$	$-6.6(1) \cdot 10^3$	$3.6(1) \cdot 10^2$	$5.051(8) \cdot 10^2$
0.515	$1.20(4) \cdot 10^4$	$-6.7(6) \cdot 10^2$	$-9(4) \cdot 10^{0}$	$-6.7(1) \cdot 10^3$	$3.8(1) \cdot 10^2$	$4.909(8) \cdot 10^2$
0.525	$1.24(4) \cdot 10^4$	$-7.0(6) \cdot 10^{2}$	$-5(4) \cdot 10^{0}$	$-6.4(1) \cdot 10^3$	$3.4(1) \cdot 10^2$	$4.762(8) \cdot 10^2$
0.535	$1.13(4) \cdot 10^4$	$-8.5(6) \cdot 10^{2}$	$-1.5(4) \cdot 10^{1}$	$-6.2(1) \cdot 10^3$	$3.5(1) \cdot 10^2$	$4.619(8) \cdot 10^{2}$
0.545	$1.15(4) \cdot 10^4$	$-7.3(6) \cdot 10^2$	$-6(4)\cdot 10^{0}$	$-6.1(1) \cdot 10^3$	$3.3(1) \cdot 10^2$	$4.473(8) \cdot 10^2$
0.555	$1.16(4) \cdot 10^4$	$-7.9(6) \cdot 10^{2}$	$-4(4) \cdot 10^{0}$	$-5.9(1) \cdot 10^3$	$3.2(1) \cdot 10^2$	$4.370(8) \cdot 10^{2}$
0.565	$1.16(4) \cdot 10^4$	$-7.6(6) \cdot 10^2$	$-7(4) \cdot 10^{0}$	$-5.9(1) \cdot 10^3$	$3.5(1) \cdot 10^2$	$4.225(8) \cdot 10^2$
0.575	$1.14(4) \cdot 10^4$	$-8.3(6) \cdot 10^2$	$-6(4) \cdot 10^{0}$	$-5.7(1) \cdot 10^3$	$3.3(1) \cdot 10^2$	$4.109(8) \cdot 10^2$
0.585	$1.09(4) \cdot 10^4$	$-7.6(6) \cdot 10^{2}$	$-4(4) \cdot 10^{0}$	$-5.5(1) \cdot 10^3$	$3.4(1) \cdot 10^2$	$3.997(8) \cdot 10^2$
0.595	$1.07(4) \cdot 10^4$	$-8.1(6) \cdot 10^{2}$	$1(3) \cdot 10^{0}$	$-5.4(1) \cdot 10^3$	$3.2(1) \cdot 10^2$	$3.885(8) \cdot 10^2$
0.605	$1.04(4) \cdot 10^4$	$-7.4(6) \cdot 10^{2}$	$-5(3) \cdot 10^{0}$	$-5.4(1) \cdot 10^3$	$3.3(1) \cdot 10^2$	$3.794(8) \cdot 10^2$
0.615	$1.08(4) \cdot 10^4$	$-7.7(5) \cdot 10^2$	$2(3)\cdot 10^{0}$	$-5.5(1) \cdot 10^3$	$3.2(1) \cdot 10^2$	$3.680(8) \cdot 10^2$
0.625	$9.8(4) \cdot 10^3$	$-8.3(5) \cdot 10^2$	$-2(3) \cdot 10^{0}$	$-5.0(1) \cdot 10^3$	$3.0(1) \cdot 10^2$	$3.573(9) \cdot 10^2$
0.635	$1.02(4) \cdot 10^4$	$-7.3(5) \cdot 10^2$	$3(3) \cdot 10^{0}$	$-5.0(1) \cdot 10^3$	$3.1(1) \cdot 10^2$	$3.484(9) \cdot 10^2$
0.645	$1.01(4) \cdot 10^4$	$-8.0(5) \cdot 10^{2}$	$-2(3) \cdot 10^{0}$	$-4.9(1) \cdot 10^3$	$3.1(1) \cdot 10^2$	$3.392(9) \cdot 10^2$
0.655	$9.4(4) \cdot 10^3$	$-7.8(5) \cdot 10^{2}$	$-5(3) \cdot 10^{0}$	$-4.9(1) \cdot 10^3$	$2.65(9) \cdot 10^2$	$3.293(9) \cdot 10^2$
0.665	$1.00(4) \cdot 10^4$	$-7.5(5) \cdot 10^2$	$0(3) \cdot 10^{-1}$	$-4.9(1) \cdot 10^3$	$2.91(9) \cdot 10^2$	$3.182(9) \cdot 10^2$
0.675	$9.6(3) \cdot 10^3$	$-8.4(5) \cdot 10^{2}$	$-3(3) \cdot 10^{0}$	$-4.7(1) \cdot 10^3$	$3.18(9) \cdot 10^2$	$3.132(9) \cdot 10^2$
0.685	$9.7(3) \cdot 10^3$	$-7.3(5) \cdot 10^2$	$1.0(3) \cdot 10^{1}$	$-4.4(1) \cdot 10^3$	$2.80(9) \cdot 10^2$	$3.012(9) \cdot 10^2$
0.695	$9.2(3) \cdot 10^3$	$-7.7(5) \cdot 10^2$	$2(3) \cdot 10^{0}$	$-4.5(1) \cdot 10^3$	$2.12(7) \cdot 10^{2}$	$2.947(9) \cdot 10^{2}$
0.705	$8.8(3) \cdot 10^3$	$-7.4(5) \cdot 10^2$	$-1(2)\cdot 10^{0}$	$-4.4(1) \cdot 10^3$	$2.75(9) \cdot 10^2$	$2.852(9) \cdot 10^2$
0.715	$8.3(3) \cdot 10^3$	$-7.8(4) \cdot 10^{2}$	$2(2)\cdot 10^{0}$	$-4.2(1) \cdot 10^3$	$2.86(8) \cdot 10^{2}$	$2.78(1) \cdot 10^2$
0.725	$8.9(3) \cdot 10^3$	$-7.7(4) \cdot 10^{2}$	$6(2) \cdot 10^{0}$	$-4.2(1) \cdot 10^3$	$2.71(8) \cdot 10^{2}$	$2.70(1) \cdot 10^2$
0.735	$8.9(3) \cdot 10^3$	$-7.9(4) \cdot 10^2$	$3(2) \cdot 10^{0}$	$-4.3(1) \cdot 10^3$	$2.56(7) \cdot 10^2$	$2.65(1) \cdot 10^2$
0.745	$7.8(3) \cdot 10^3$	$-7.2(4) \cdot 10^2$	$5(2) \cdot 10^{0}$	$-4.4(1) \cdot 10^3$	$2.57(7) \cdot 10^2$	$2.54(1) \cdot 10^2$
0.755	$2.43(2) \cdot 10^4$	$-6.2(3) \cdot 10^2$	$-5.2(1) \cdot 10^{1}$	$-1.106(7) \cdot 10^4$	$8.14(5) \cdot 10^2$	$-6.780(8) \cdot 10^2$
0.765	$1.97(1) \cdot 10^4$	$-1.58(1) \cdot 10^3$	$1.06(7) \cdot 10^{1}$	$-4.36(3) \cdot 10^3$	$3.55(2) \cdot 10^2$	$-3.520(3) \cdot 10^2$
0.775	$1.418(8) \cdot 10^4$	$-1.25(1)\cdot 10^3$	$1.53(6) \cdot 10^{1}$	$-2.78(2) \cdot 10^3$	$7.40(9) \cdot 10^{1}$	$-2.490(2)\cdot 10^2$
0.785	$1.072(7) \cdot 10^4$	$-9.93(9) \cdot 10^2$	$1.01(4) \cdot 10^{1}$	$-2.00(2) \cdot 10^3$	$1.17(1) \cdot 10^2$	$-1.892(2) \cdot 10^2$
0.795	$8.53(6) \cdot 10^3$	$-8.09(7) \cdot 10^2$	$1.07(4) \cdot 10^{1}$	$-1.52(2)\cdot 10^3$	$1.066(8) \cdot 10^2$	$-1.488(2) \cdot 10^2$
0.805	$6.68(5) \cdot 10^3$	$-6.86(6) \cdot 10^2$	$8.7(3) \cdot 10^{0}$	$-1.22(1)\cdot 10^3$	$3.4(4) \cdot 10^{-1}$	$-1.191(1) \cdot 10^2$
0.815	$5.09(4) \cdot 10^3$	$-5.56(5) \cdot 10^2$	$6.7(3) \cdot 10^0$	$-9.6(1) \cdot 10^2$	$1.16(7) \cdot 10^{0}$	$-9.65(1) \cdot 10^{1}$
0.825	$4.34(4) \cdot 10^3$	$-4.54(5) \cdot 10^2$	$4.7(2) \cdot 10^{0}$	$-7.91(8) \cdot 10^2$	$7(1) \cdot 10^{-2}$	$-7.87(1) \cdot 10^{1}$
0.835	$3.52(3) \cdot 10^3$	$-3.59(4) \cdot 10^2$	$2.4(1) \cdot 10^{0}$	$-6.45(6) \cdot 10^2$	$4.62(4) \cdot 10^{1}$	$-6.448(9) \cdot 10^{1}$
0.845	$2.84(3) \cdot 10^3$	$-3.15(3) \cdot 10^2$	$2.3(1) \cdot 10^{0}$	$-5.48(5) \cdot 10^2$	$6.3(1) \cdot 10^0$	$-5.297(8) \cdot 10^{1}$
0.855	$1.56(2) \cdot 10^3$	$-2.58(3) \cdot 10^2$	$1.22(9) \cdot 10^0$	$-4.50(4) \cdot 10^2$	$1.32(2) \cdot 10^{1}$	$-4.356(7) \cdot 10^{1}$
0.865	$1.87(2) \cdot 10^3$	$-2.09(3) \cdot 10^2$	$3.7(5) \cdot 10^{-1}$	$-3.65(3) \cdot 10^2$	$7.6(4) \cdot 10^{-1}$	$-3.551(6) \cdot 10^{1}$
0.875	$1.39(2) \cdot 10^3$	$-1.38(2) \cdot 10^2$	$2.6(4) \cdot 10^{-1}$	$-2.88(3) \cdot 10^2$	$3.63(7) \cdot 10^0$	$-2.904(6) \cdot 10^{1}$
0.885	$1.02(1) \cdot 10^3$	$-9.7(2) \cdot 10^{1}$	$2.1(4) \cdot 10^{-1}$	$-2.18(2) \cdot 10^2$	$2(1) \cdot 10^{-3}$	$-2.343(5) \cdot 10^{1}$
0.895	$8.6(1) \cdot 10^2$	$-7.7(1) \cdot 10^{1}$	$1.7(3) \cdot 10^{-1}$	$-1.74(2) \cdot 10^2$	$2(3) \cdot 10^{-4}$	$-1.880(4) \cdot 10^{1}$
0.905	$6.78(9) \cdot 10^2$	$-6.1(1) \cdot 10^{1}$	$0(2) \cdot 10^{-3}$	$-1.45(1) \cdot 10^2$	$2(2) \cdot 10^{-5}$	$-1.481(4) \cdot 10^{1}$
0.915	$5.05(7) \cdot 10^2$	$-3.33(7) \cdot 10^{1}$	$-1(1) \cdot 10^{-2}$	$-1.106(9) \cdot 10^2$	$2(1) \cdot 10^{-4}$	$-1.149(3) \cdot 10^{1}$
0.925	$3.26(5) \cdot 10^2$	$-2.13(5) \cdot 10^{1}$	$-8(5) \cdot 10^{-4}$	$-7.68(7) \cdot 10^{1}$	$1(1) \cdot 10^{-9}$	$-8.68(3) \cdot 10^{0}$
0.935	$7.3(2) \cdot 10^{1}$	$-6.2(7) \cdot 10^{-1}$	$-1.3(2) \cdot 10^{-2}$	$-5.62(5) \cdot 10^{1}$	$2(1) \cdot 10^{-11}$	$-6.18(2) \cdot 10^{0}$
0.945	$1.40(2) \cdot 10^2$	$-4.8(2) \cdot 10^{0}$	$-1.1(1) \cdot 10^{-2}$	$-2.99(3) \cdot 10^{1}$	$2(1) \cdot 10^{-9}$	$-4.22(2) \cdot 10^{0}$
0.955	$3.19(8) \cdot 10^{1}$	$-8.8(7) \cdot 10^{-1}$	$-3.7(5) \cdot 10^{-3}$	$-2.60(9) \cdot 10^{0}$	$1.3(9) \cdot 10^{-11}$	$-2.51(1) \cdot 10^{0}$
0.965	$2.28(5) \cdot 10^{1}$	$-1.6(6) \cdot 10^{-2}$	$-2(2)\cdot 10^{-5}$	$-1(1)\cdot 10^{-6}$	$1.7(9) \cdot 10^{-11}$	$-1.98(4) \cdot 10^{-1}$
0.975	$4.0(1) \cdot 10^{0}$	$1(1) \cdot 10^{-4}$	$-1.05(9) \cdot 10^{-3}$	$-6(2)\cdot 10^{-3}$	$3(1) \cdot 10^{-13}$	$-1.22(3) \cdot 10^{-1}$
0.985	$1(1) \cdot 10^{-4}$	$1(1) \cdot 10^{-7}$	$2(2) \cdot 10^{-10}$	$-8(7) \cdot 10^{-9}$	$1(1) \cdot 10^{-12}$	$-4.88684(2) \cdot 10^{-1}$
0.995	$-2(1)\cdot 10^{-5}$	$1(1) \cdot 10^{-11}$	$-2(3) \cdot 10^{-10}$	$-2(2)\cdot 10^{-12}$	$6(4) \cdot 10^{-9}$	$-1.443(2) \cdot 10^{-1}$

Table 17: Individual contributions from the different colour factors to $\rho \frac{dC_C}{dC}$ for the C parameter distribution.

$ln y_{23}$	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
-9.875	$-2.6(1) \cdot 10^4$	$3.1(2) \cdot 10^3$	$1.426(9) \cdot 10^3$	$1.89(3) \cdot 10^4$	$-8.30(2) \cdot 10^3$	$8.762(3) \cdot 10^3$
-9.625	$-2.63(9) \cdot 10^4$	$3.7(2) \cdot 10^3$	$1.208(8) \cdot 10^3$	$1.49(3) \cdot 10^4$	$-7.51(2) \cdot 10^3$	$8.164(2) \cdot 10^3$
-9.375	$-2.44(8) \cdot 10^4$	$3.9(1) \cdot 10^3$	$1.046(7) \cdot 10^3$	$1.19(3) \cdot 10^4$	$-6.74(2) \cdot 10^3$	$7.594(2) \cdot 10^3$
-9.125	$-2.34(7) \cdot 10^4$	$4.7(1) \cdot 10^3$	$9.18(7) \cdot 10^2$	$8.2(2) \cdot 10^3$	$-6.04(1) \cdot 10^3$	$7.048(2) \cdot 10^3$
-8.875	$-2.04(7) \cdot 10^4$	$4.7(1) \cdot 10^3$	$7.41(6) \cdot 10^2$	$5.2(2) \cdot 10^3$	$-5.40(1) \cdot 10^3$	$6.535(2) \cdot 10^3$
-8.625	$-1.94(6) \cdot 10^4$	$4.9(1) \cdot 10^3$	$6.49(5) \cdot 10^2$	$3.2(2) \cdot 10^3$	$-4.79(1) \cdot 10^3$	$6.040(2) \cdot 10^3$
-8.375	$-1.70(6) \cdot 10^4$	$4.7(1) \cdot 10^3$	$5.33(5) \cdot 10^2$	$5(2) \cdot 10^2$	$-4.25(1) \cdot 10^3$	$5.578(1) \cdot 10^3$
-8.125	$-1.41(5) \cdot 10^4$	$4.85(9) \cdot 10^3$	$4.52(4) \cdot 10^2$	$-1.1(2)\cdot 10^3$	$-3.73(1) \cdot 10^3$	$5.137(1) \cdot 10^3$
-7.875	$-1.26(5) \cdot 10^4$	$4.53(8) \cdot 10^3$	$3.68(4) \cdot 10^2$	$-2.8(1) \cdot 10^3$	$-3.268(9) \cdot 10^3$	$4.719(1) \cdot 10^3$
-7.625	$-1.03(4) \cdot 10^4$	$4.56(7) \cdot 10^3$	$3.06(3) \cdot 10^2$	$-4.1(1) \cdot 10^3$	$-2.829(8) \cdot 10^3$	$4.329(1) \cdot 10^3$
-7.375	$-8.9(4) \cdot 10^3$	$4.09(7) \cdot 10^3$	$2.33(3) \cdot 10^2$	$-5.0(1) \cdot 10^3$	$-2.434(8) \cdot 10^3$	$3.9575(9) \cdot 10^3$
-7.125	$-6.0(4) \cdot 10^3$	$3.85(6) \cdot 10^3$	$1.94(3) \cdot 10^2$	$-5.8(1) \cdot 10^3$	$-2.096(7) \cdot 10^3$	$3.6097(8) \cdot 10^3$
-6.875	$-4.5(3) \cdot 10^3$	$3.50(5) \cdot 10^3$	$1.51(2) \cdot 10^2$	$-6.56(9) \cdot 10^3$	$-1.783(6) \cdot 10^3$	$3.2822(7) \cdot 10^3$
-6.625	$-3.1(3) \cdot 10^3$	$3.19(5) \cdot 10^3$	$1.15(2) \cdot 10^2$	$-6.88(8) \cdot 10^3$	$-1.501(5) \cdot 10^3$	$2.9761(6) \cdot 10^3$
-6.375	$-1.4(3) \cdot 10^3$	$2.89(4) \cdot 10^3$	$8.4(2) \cdot 10^{1}$	$-7.13(7) \cdot 10^3$	$-1.261(5) \cdot 10^3$	$2.6907(6) \cdot 10^3$
-6.125	$-1(2)\cdot 10^2$	$2.47(4) \cdot 10^3$	$6.6(2) \cdot 10^{1}$	$-7.28(7) \cdot 10^3$	$-1.052(4) \cdot 10^3$	$2.4229(5) \cdot 10^3$
-5.875	$1.5(2) \cdot 10^3$	$2.17(3) \cdot 10^3$	$4.7(1) \cdot 10^{1}$	$-7.37(6) \cdot 10^3$	$-8.68(4) \cdot 10^2$	$2.1753(5) \cdot 10^3$
-5.625	$2.2(2) \cdot 10^3$	$1.93(3) \cdot 10^3$	$3.3(1) \cdot 10^{1}$	$-7.24(5) \cdot 10^3$	$-6.94(4) \cdot 10^2$	$1.9439(4) \cdot 10^3$
-5.375	$2.9(2) \cdot 10^3$	$1.65(2) \cdot 10^3$	$2.4(1) \cdot 10^{1}$	$-7.03(5) \cdot 10^3$	$-5.50(3) \cdot 10^2$	$1.7302(4) \cdot 10^3$
-5.125	$3.4(2) \cdot 10^3$	$1.30(2) \cdot 10^3$	$1.38(9) \cdot 10^{1}$	$-6.73(4) \cdot 10^3$	$-4.38(3) \cdot 10^{2}$	$1.5330(3) \cdot 10^3$
-4.875	$3.9(1) \cdot 10^3$	$1.14(2) \cdot 10^3$	$8.3(8) \cdot 10^{0}$	$-6.31(4) \cdot 10^3$	$-3.36(3) \cdot 10^2$	$1.3512(3) \cdot 10^3$
-4.625	$4.1(1) \cdot 10^3$	$8.8(2) \cdot 10^2$	$4.6(7) \cdot 10^{0}$	$-5.94(3) \cdot 10^3$	$-2.50(2) \cdot 10^{2}$	$1.1843(3) \cdot 10^3$
-4.375	$4.4(1) \cdot 10^3$	$7.1(1) \cdot 10^2$	$1.7(6) \cdot 10^{0}$	$-5.56(3) \cdot 10^3$	$-1.80(2) \cdot 10^2$	$1.0315(2) \cdot 10^3$
-4.125	$4.27(9) \cdot 10^3$	$5.3(1) \cdot 10^2$	$-5(5)\cdot 10^{-1}$	$-5.03(2) \cdot 10^3$	$-1.23(2) \cdot 10^2$	$8.926(2) \cdot 10^2$
-3.875	$4.35(8) \cdot 10^3$	$4.0(1) \cdot 10^2$	$-1.3(4) \cdot 10^{0}$	$-4.53(2) \cdot 10^3$	$-7.6(2) \cdot 10^{1}$	$7.661(2) \cdot 10^2$
-3.625	$3.87(7) \cdot 10^3$	$2.70(8) \cdot 10^2$	$-1.7(4) \cdot 10^{0}$	$-4.05(2) \cdot 10^3$	$-4.2(1) \cdot 10^{1}$	$6.527(2) \cdot 10^2$
-3.375	$3.52(6) \cdot 10^3$	$1.82(7) \cdot 10^2$	$-2.0(3) \cdot 10^{0}$	$-3.53(2) \cdot 10^3$	$-1.6(1) \cdot 10^{1}$	$5.501(1) \cdot 10^2$
-3.125	$3.29(5) \cdot 10^3$	$1.09(6) \cdot 10^2$	$-2.1(3) \cdot 10^{0}$	$-3.09(1) \cdot 10^3$	$3(1) \cdot 10^0$	$4.586(1) \cdot 10^2$
-2.875	$2.75(5) \cdot 10^3$	$4.5(5) \cdot 10^{1}$	$-1.4(2) \cdot 10^{0}$	$-2.62(1) \cdot 10^3$	$1.72(9) \cdot 10^{1}$	$3.773(1) \cdot 10^2$
-2.625	$2.36(4) \cdot 10^3$	$7(4) \cdot 10^0$	$-1.5(2) \cdot 10^{0}$	$-2.17(1) \cdot 10^3$	$2.31(8) \cdot 10^{1}$	$3.056(1) \cdot 10^2$
-2.375	$1.98(3) \cdot 10^3$	$-2.1(3) \cdot 10^{1}$	$-7(2) \cdot 10^{-1}$	$-1.779(9) \cdot 10^3$	$2.81(6) \cdot 10^{1}$	$2.4251(9) \cdot 10^2$
-2.125	$1.49(3) \cdot 10^3$	$-3.0(3) \cdot 10^{1}$	$-1.0(1) \cdot 10^{0}$	$-1.417(7) \cdot 10^3$	$2.79(5) \cdot 10^{1}$	$1.8729(7) \cdot 10^2$
-1.875	$1.10(2) \cdot 10^3$	$-3.5(2) \cdot 10^{1}$	$-4(1) \cdot 10^{-1}$	$-1.043(6) \cdot 10^3$	$2.44(4) \cdot 10^{1}$	$1.3890(6) \cdot 10^{2}$
-1.625	$7.9(2) \cdot 10^2$	$-3.0(2) \cdot 10^{1}$	$-3.2(8) \cdot 10^{-1}$	$-7.33(4) \cdot 10^{2}$	$1.86(3) \cdot 10^{1}$	$9.514(5) \cdot 10^{1}$
-1.375	$4.0(1) \cdot 10^2$	$-2.0(1) \cdot 10^{1}$	$-2.2(5) \cdot 10^{-1}$	$-4.12(3) \cdot 10^2$	$1.07(2) \cdot 10^{1}$	$5.267(4) \cdot 10^{1}$
-1.125	$7(4) \cdot 10^{0}$	$6(4) \cdot 10^{-1}$	$-0(1) \cdot 10^{-3}$	$-5.80(9) \cdot 10^{1}$	$7.7(5) \cdot 10^{-1}$	$1.028(2) \cdot 10^{1}$
-0.875	0	0	0	0	0	0

Table 18: Individual contributions from the different colour factors to $y_{23} \frac{dC_{y_{23}}}{dy_{23}}$ for the three-to-two jet transition distribution.

Ycut	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.3	$-2(3) \cdot 10^{0}$	$4(2) \cdot 10^{-1}$	$-7(4) \cdot 10^{-3}$	$-5.9(7) \cdot 10^{0}$	$2(4) \cdot 10^{-2}$	$1.48(3) \cdot 10^{0}$
0.15	$4.4(1) \cdot 10^2$	$-1.82(8) \cdot 10^{1}$	$-2.7(3) \cdot 10^{-1}$	$-4.47(4) \cdot 10^2$	$1.13(2) \cdot 10^{1}$	$5.93(2) \cdot 10^{1}$
0.1	$1.05(2) \cdot 10^3$	$-3.1(1) \cdot 10^{1}$	$-4.9(3) \cdot 10^{-1}$	$-1.000(6) \cdot 10^3$	$2.19(3) \cdot 10^{1}$	$1.336(3) \cdot 10^2$
0.06	$2.16(3) \cdot 10^3$	$-2.0(2)\cdot 10^{1}$	$-1.20(6) \cdot 10^{0}$	$-2.048(8) \cdot 10^3$	$3.19(4) \cdot 10^{1}$	$2.843(4) \cdot 10^2$
0.03	$3.84(5) \cdot 10^3$	$1.23(3) \cdot 10^2$	$-2.71(6) \cdot 10^{0}$	$-4.09(2) \cdot 10^3$	$1.08(8) \cdot 10^{1}$	$6.238(9) \cdot 10^2$
0.015	$4.83(8) \cdot 10^3$	$5.78(5) \cdot 10^2$	$-3.1(2) \cdot 10^{0}$	$-6.59(3) \cdot 10^3$	$-1.10(1) \cdot 10^2$	$1.183(2) \cdot 10^3$
0.01	$4.4(1) \cdot 10^3$	$1.060(7) \cdot 10^3$	$2(2) \cdot 10^{-1}$	$-8.12(3) \cdot 10^3$	$-2.66(2) \cdot 10^2$	$1.646(2) \cdot 10^3$
0.006	$2.4(2) \cdot 10^3$	$1.96(1) \cdot 10^3$	$1.35(4) \cdot 10^{1}$	$-9.68(5) \cdot 10^3$	$-6.22(3) \cdot 10^2$	$2.409(3) \cdot 10^3$
0.003	$-4.7(3) \cdot 10^3$	$3.76(2) \cdot 10^3$	$6.54(4) \cdot 10^{1}$	$-1.050(9) \cdot 10^4$	$-1.499(5) \cdot 10^3$	$3.862(5) \cdot 10^3$
0.0015	$-1.74(4) \cdot 10^4$	$6.13(3) \cdot 10^3$	$1.95(2) \cdot 10^2$	$-8.1(1)\cdot 10^3$	$-3.064(9) \cdot 10^3$	$5.899(9) \cdot 10^3$
0.001	$-2.84(6) \cdot 10^4$	$7.61(4) \cdot 10^3$	$3.38(1) \cdot 10^2$	$-4.1(2)\cdot 10^3$	$-4.43(1) \cdot 10^3$	$7.41(1) \cdot 10^3$
0.0006	$-4.60(8) \cdot 10^4$	$9.38(6) \cdot 10^3$	$6.17(3) \cdot 10^2$	$4.7(2) \cdot 10^3$	$-6.79(2) \cdot 10^3$	$9.74(2) \cdot 10^3$
0.0003	$-7.1(1)\cdot 10^4$	$1.070(9) \cdot 10^4$	$1.273(3) \cdot 10^3$	$2.58(3) \cdot 10^4$	$-1.142(3) \cdot 10^4$	$1.380(3) \cdot 10^4$
0.00015	$-9.2(3) \cdot 10^4$	$9.0(2) \cdot 10^3$	$2.406(8) \cdot 10^3$	$6.22(6) \cdot 10^4$	$-1.821(4)\cdot 10^4$	$1.906(5) \cdot 10^4$
0.0001	$-9.4(4) \cdot 10^4$	$5.4(2) \cdot 10^3$	$3.413(7) \cdot 10^3$	$9.13(7) \cdot 10^4$	$-2.341(6) \cdot 10^4$	$2.271(5) \cdot 10^4$

Table 19: Individual contributions from the different colour factors to the NNLO coefficient $C_{3-jet,Durham}$ for the three-jet rate with the Durham jet algorithm for various values of y_{cut} .

y_{cut}	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.3	$4.3(6) \cdot 10^{1}$	$-3(2) \cdot 10^{0}$	$-6(4) \cdot 10^{-2}$	$-6.5(2) \cdot 10^{1}$	$1.68(9) \cdot 10^{0}$	$1.091(1) \cdot 10^{1}$
0.15	$1.17(5) \cdot 10^3$	$6(1) \cdot 10^{1}$	$-4(2)\cdot 10^{-1}$	$-2.05(3) \cdot 10^3$	$2(9) \cdot 10^{-1}$	$3.835(2) \cdot 10^2$
0.1	$1.33(9) \cdot 10^3$	$3.5(2) \cdot 10^2$	$2.0(4) \cdot 10^{0}$	$-3.74(4) \cdot 10^3$	$-9.8(2) \cdot 10^{1}$	$8.788(4) \cdot 10^2$
0.06	$-2.0(2)\cdot 10^3$	$1.16(3) \cdot 10^3$	$1.82(8) \cdot 10^{1}$	$-5.66(8) \cdot 10^3$	$-4.95(5) \cdot 10^2$	$1.9342(9) \cdot 10^3$
0.03	$-1.49(3) \cdot 10^4$	$3.07(5) \cdot 10^3$	$1.20(2) \cdot 10^2$	$-4.2(2)\cdot 10^3$	$-1.94(1) \cdot 10^3$	$4.461(2) \cdot 10^3$
0.015	$-4.24(7) \cdot 10^4$	$5.2(1) \cdot 10^3$	$4.60(2) \cdot 10^2$	$7.8(3) \cdot 10^3$	$-5.17(3) \cdot 10^3$	$8.808(3) \cdot 10^3$
0.01	$-6.44(7) \cdot 10^4$	$6.1(1) \cdot 10^3$	$8.78(3) \cdot 10^2$	$2.47(4) \cdot 10^4$	$-8.34(4) \cdot 10^3$	$1.2472(5) \cdot 10^4$
0.006	$-9.7(1) \cdot 10^4$	$4.3(2) \cdot 10^3$	$1.783(5) \cdot 10^3$	$6.09(6) \cdot 10^4$	$-1.427(6) \cdot 10^4$	$1.8585(8) \cdot 10^4$
0.003	$-1.33(2)\cdot 10^5$	$-6.1(3) \cdot 10^3$	$4.055(9) \cdot 10^3$	$1.46(1) \cdot 10^5$	$-2.68(1) \cdot 10^4$	$3.015(1) \cdot 10^4$
0.0015	$-1.19(3) \cdot 10^5$	$-3.48(5) \cdot 10^4$	$8.18(2) \cdot 10^3$	$2.98(1) \cdot 10^5$	$-4.63(2) \cdot 10^4$	$4.655(2) \cdot 10^4$
0.001	$-8.7(5) \cdot 10^4$	$-6.47(6) \cdot 10^4$	$1.169(2) \cdot 10^4$	$4.24(2) \cdot 10^5$	$-6.16(3) \cdot 10^4$	$5.875(3) \cdot 10^4$

Table 20: Individual contributions from the different colour factors to the NNLO coefficient $C_{3-jet,Geneva}$ for the three-jet rate with the Geneva jet algorithm for various values of y_{cut} .

Ycut	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.3	$3.5(8) \cdot 10^{1}$	$-3(1) \cdot 10^{0}$	$-5(3) \cdot 10^{-2}$	$-2.7(1) \cdot 10^{1}$	$1.0(1) \cdot 10^{0}$	$2.770(5) \cdot 10^{0}$
0.15	$1.85(3) \cdot 10^3$	$-8.9(9) \cdot 10^{1}$	$-2.4(3) \cdot 10^{0}$	$-1.41(1) \cdot 10^3$	$5.4(1) \cdot 10^{1}$	$1.3607(9) \cdot 10^2$
0.1	$3.86(9) \cdot 10^3$	$-1.1(2)\cdot 10^2$	$-8.9(5) \cdot 10^{0}$	$-3.33(2)\cdot 10^3$	$1.10(2) \cdot 10^2$	$3.349(2) \cdot 10^2$
0.06	$7.2(2) \cdot 10^3$	$1.4(3) \cdot 10^2$	$-2.7(1) \cdot 10^{1}$	$-6.83(5) \cdot 10^3$	$1.54(4) \cdot 10^2$	$7.945(4) \cdot 10^2$
0.03	$9.2(3) \cdot 10^3$	$1.48(6) \cdot 10^3$	$-5.8(2) \cdot 10^{1}$	$-1.33(1) \cdot 10^4$	$-3(1) \cdot 10^{1}$	$1.9819(9) \cdot 10^3$
0.015	$2.6(5) \cdot 10^3$	$4.7(2) \cdot 10^3$	$-7.1(3) \cdot 10^{1}$	$-1.95(2) \cdot 10^4$	$-9.4(2) \cdot 10^2$	$4.116(2) \cdot 10^3$
0.01	$-8.9(5) \cdot 10^3$	$7.7(1) \cdot 10^3$	$-2.1(5) \cdot 10^{1}$	$-2.13(3) \cdot 10^4$	$-2.12(3)\cdot 10^3$	$5.947(2) \cdot 10^3$
0.006	$-2.74(9) \cdot 10^4$	$1.18(3) \cdot 10^4$	$1.88(7) \cdot 10^2$	$-1.77(4) \cdot 10^4$	$-4.55(8) \cdot 10^3$	$9.025(4) \cdot 10^3$
0.003	$-6.8(1) \cdot 10^4$	$1.67(6) \cdot 10^4$	$1.02(1) \cdot 10^3$	$3(6) \cdot 10^2$	$-1.08(1) \cdot 10^4$	$1.4875(6) \cdot 10^4$
0.0015	$-1.16(2)\cdot 10^5$	$1.81(6) \cdot 10^4$	$2.99(2) \cdot 10^3$	$4.6(1) \cdot 10^4$	$-2.02(3) \cdot 10^4$	$2.311(1) \cdot 10^4$
0.001	$-1.38(4) \cdot 10^5$	$1.41(7) \cdot 10^4$	$4.84(2) \cdot 10^3$	$9.1(1) \cdot 10^4$	$-2.93(3) \cdot 10^4$	$2.923(1) \cdot 10^4$
0.0006	$-1.45(4) \cdot 10^5$	$0(1) \cdot 10^2$	$8.03(2) \cdot 10^3$	$1.74(2) \cdot 10^5$	$-4.36(3) \cdot 10^4$	$3.855(2) \cdot 10^4$
0.0003	$-7.1(7) \cdot 10^4$	$-4.5(1) \cdot 10^4$	$1.414(4) \cdot 10^4$	$3.47(3) \cdot 10^5$	$-6.93(5) \cdot 10^4$	$5.455(3) \cdot 10^4$

Table 21: Individual contributions from the different colour factors to the NNLO coefficient $C_{3-jet,Jade-E0}$ for the three-jet rate with the Jade-E0 jet algorithm for various values of y_{cut} .

y_{cut}	N_c^2	N_c^0	N_c^{-2}	$N_f N_c$	N_f/N_c	N_f^2
0.3	$-2(3) \cdot 10^{0}$	$3(6) \cdot 10^{-1}$	$-5(2)\cdot 10^{-2}$	$-6.5(6) \cdot 10^{0}$	$-1.5(4) \cdot 10^{-1}$	$1.475(3) \cdot 10^{0}$
0.15	$4.3(3) \cdot 10^2$	$-2.5(4) \cdot 10^{1}$	$0(9) \cdot 10^{-3}$	$-4.48(7) \cdot 10^2$	$1.01(5) \cdot 10^{1}$	$5.986(4) \cdot 10^{1}$
0.1	$9.3(6) \cdot 10^2$	$-2.1(6) \cdot 10^{1}$	$-4(2) \cdot 10^{-1}$	$-9.7(1) \cdot 10^2$	$1.67(7) \cdot 10^{1}$	$1.364(1) \cdot 10^2$
0.06	$1.62(9) \cdot 10^3$	$1(1) \cdot 10^{1}$	$-4(4) \cdot 10^{-1}$	$-1.90(2) \cdot 10^3$	$1.4(1) \cdot 10^{1}$	$2.915(2) \cdot 10^2$
0.03	$2.6(2) \cdot 10^3$	$2.2(2) \cdot 10^2$	$2(6) \cdot 10^{-1}$	$-3.70(5) \cdot 10^3$	$-3.8(2) \cdot 10^{1}$	$6.431(4) \cdot 10^2$
0.015	$2.9(2) \cdot 10^3$	$5.9(3) \cdot 10^2$	$6(1) \cdot 10^{0}$	$-5.61(9) \cdot 10^3$	$-1.98(4) \cdot 10^2$	$1.2207(6) \cdot 10^3$
0.01	$2.1(2) \cdot 10^3$	$1.12(3) \cdot 10^3$	$1.31(9) \cdot 10^{1}$	$-6.8(1) \cdot 10^3$	$-3.82(6) \cdot 10^2$	$1.6975(9) \cdot 10^3$
0.006	$2(4) \cdot 10^2$	$1.91(6) \cdot 10^3$	$3.6(1) \cdot 10^{1}$	$-7.8(2) \cdot 10^3$	$-7.93(8) \cdot 10^2$	$2.485(1) \cdot 10^3$
0.003	$-8.1(5) \cdot 10^3$	$3.53(7) \cdot 10^3$	$1.12(3) \cdot 10^2$	$-7.4(2) \cdot 10^3$	$-1.76(2) \cdot 10^3$	$3.960(2) \cdot 10^3$
0.0015	$-1.89(7) \cdot 10^4$	$5.5(2) \cdot 10^3$	$2.78(4) \cdot 10^{2}$	$-3.5(3) \cdot 10^3$	$-3.42(2)\cdot 10^3$	$6.034(3) \cdot 10^3$
0.001	$-2.79(9) \cdot 10^4$	$6.6(1) \cdot 10^3$	$4.47(3) \cdot 10^2$	$1.3(3) \cdot 10^3$	$-4.89(3) \cdot 10^3$	$7.590(3) \cdot 10^3$
0.0006	$-4.0(1) \cdot 10^4$	$7.9(1) \cdot 10^3$	$7.69(5) \cdot 10^2$	$1.06(4) \cdot 10^4$	$-7.27(6) \cdot 10^3$	$9.959(5) \cdot 10^3$
0.0003	$-5.9(1) \cdot 10^4$	$7.8(3) \cdot 10^3$	$1.505(7) \cdot 10^3$	$3.44(7) \cdot 10^4$	$-1.207(8) \cdot 10^4$	$1.4070(6) \cdot 10^4$
0.00015	$-7.3(2) \cdot 10^4$	$4.6(4) \cdot 10^3$	$2.76(1) \cdot 10^3$	$7.46(8) \cdot 10^4$	$-1.92(1) \cdot 10^4$	$1.9362(9) \cdot 10^4$
0.0001	$-7.5(2) \cdot 10^4$	$-1(4) \cdot 10^2$	$3.81(1) \cdot 10^3$	$1.06(1) \cdot 10^5$	$-2.45(1) \cdot 10^4$	$2.312(1) \cdot 10^4$

Table 22: Individual contributions from the different colour factors to the NNLO coefficient $C_{3-jet,Cambridge}$ for the three-jet rate with the Cambridge jet algorithm for various values of y_{cut} .