

Dataset	5% CS					KMEANS
	PCCC	COPKM	CSC	DILS	LCC	
Appendicitis	0.1	0.0	5.1	501.4	6.4	0.2
Breast Cancer	0.3	–	5.3	1,818.9	104.4	0.2
Bupa	0.4	–	2.6	1,658.8	18.9	0.2
Circles	0.1	–	1.8	1,346.8	8.6	0.1
Ecoli	1.4	0.4	2.0	1,447.1	41.9	0.1
Glass	0.4	0.2	1.7	969.1	28.9	0.2
Haberman	0.4	–	4.4	1,331.1	9.2	0.2
Hayesroth	0.3	0.0	1.7	716.5	7.3	0.2
Heart	0.6	–	4.1	1,391.3	22.4	0.2
Ionosphere	0.4	–	5.8	1,810.6	71.3	0.2
Iris	0.6	0.0	6.4	615.5	6.2	0.3
Led7Digit	1.4	0.4	6.1	1,810.3	–	0.2
Monk2	0.7	–	4.9	1,801.8	23.6	0.1
Moons	0.3	0.0	9.0	1,259.3	6.3	0.2
Movement Libras	2.1	5.9	7.5	1,809.3	853.1	0.3
Newthyroid	0.5	0.0	4.0	980.6	11.0	0.2
Saheart	0.6	–	8.1	1,811.1	39.0	0.2
Sonar	0.5	–	5.8	1,480.5	73.0	0.2
Soybean	0.3	0.0	1.6	229.7	17.2	0.2
Spectfheart	0.4	–	6.8	1,809.9	64.6	0.2
Spiral	0.4	–	4.2	1,280.8	7.7	0.3
Tae	0.4	0.0	2.8	670.0	8.7	0.2
Vehicle	2.2	–	15.3	1,826.6	274.1	0.1
Wine	0.2	0.1	5.3	906.4	17.7	0.2
Zoo	0.5	0.1	1.4	456.4	23.4	0.3
Sum	15.8	21,607.3*	123.5	31,739.7	3,545.2*	5.0

*Nan values (–) are replaced with 1,800 before computing the sum.

Table W12: Average running times (in seconds) of the PCCC algorithm and the four state-of-the-art algorithms (COPKM, CSC, DILS, LCC) for the constraint sets of size 5% CS. The lowest values are stated in bold. The column KMEANS reports the average running time of the unconstrained k-means algorithm. The hyphen indicates that the respective algorithm returned no solution within the time limit of 1,800 seconds.

Dataset	10% CS					KMEANS
	PCCC	COPKM	CSC	DILS	LCC	
Appendicitis	0.2	–	1.5	488.8	7.4	0.2
Breast Cancer	0.2	–	6.9	1,808.1	445.1	0.2
Bupa	0.3	–	4.4	1,795.4	224.0	0.1
Circles	0.2	–	2.9	1,397.8	246.7	0.2
Ecoli	1.5	0.4	5.1	1,525.9	34.6	0.2
Glass	0.8	1.9	5.3	972.2	42.8	0.2
Haberman	0.2	0.1	2.7	1,456.0	176.9	0.2
Hayesroth	0.4	–	2.7	734.2	11.7	0.2
Heart	0.1	–	7.4	1,464.7	117.9	0.3
Ionosphere	0.3	–	4.4	1,809.2	1,815.1	0.2
Iris	0.5	0.0	3.8	647.8	6.8	0.2
Led7Digit	3.4	0.5	4.9	1,808.5	107.0	0.2
Monk2	0.2	3.3	3.3	1,809.3	631.6	0.2
Moons	0.3	–	4.6	1,396.1	46.1	0.2
Movement Libras	5.3	6.3	4.9	1,806.2	1,007.9	0.3
Newthyroid	0.4	0.1	2.2	977.6	21.6	0.2
Saheart	0.2	2.7	7.0	1,812.8	852.4	0.2
Sonar	0.3	–	3.6	1,516.7	269.5	0.2
Soybean	0.2	0.0	1.0	246.6	16.4	0.2
Spectfheart	0.3	–	5.1	1,809.2	267.0	0.2
Spiral	0.2	–	4.7	1,396.3	188.0	0.2
Tae	0.5	–	3.7	696.7	11.5	0.3
Vehicle	0.7	–	14.3	1,811.9	–	0.2
Wine	0.3	0.1	3.5	912.2	19.5	0.2
Zoo	0.4	0.1	1.4	481.9	19.1	0.3
Sum	17.4	23,415.6*	111.5	32,581.7	8,386.6*	5.3

*Nan values (–) are replaced with 1,800 before computing the sum.

Table W13: Average running times (in seconds) of the PCCC algorithm and the four state-of-the-art algorithms (COPKM, CSC, DILS, LCC) for the constraint sets of size 10% CS. The lowest values are stated in bold. The column KMEANS reports the average running time of the unconstrained k-means algorithm. The hyphen indicates that the respective algorithm returned no solution within the time limit of 1,800 seconds.

Dataset	15% CS					KMEANS
	PCCC	COPKM	CSC	DILS	LCC	
Appendicitis	0.2	–	5.3	567.2	16.7	0.2
Breast Cancer	0.1	36.1	5.5	1,815.7	27.6	0.2
Bupa	0.1	6.4	2.2	1,805.8	1,953.1	0.2
Circles	0.1	2.8	5.2	1,552.0	1,850.0	0.3
Ecoli	1.2	–	8.0	1,787.9	238.9	0.2
Glass	0.7	–	1.9	1,090.4	537.3	0.2
Haberman	0.1	1.7	10.7	1,705.6	167.4	0.2
Hayesroth	0.3	–	3.4	782.7	59.2	0.2
Heart	0.3	1.9	5.1	1,625.7	501.0	0.2
Ionosphere	0.2	5.0	2.0	1,807.2	809.4	0.2
Iris	0.6	0.0	7.6	759.5	9.5	0.3
Led7Digit	5.4	–	12.2	1,817.7	–	0.2
Monk2	0.3	15.2	8.3	1,811.8	6.6	0.2
Moons	0.1	2.8	5.4	1,568.5	46.7	0.2
Movement Libras	7.7	8.8	7.9	1,815.2	1,513.9	0.2
Newthyroid	0.1	0.1	6.1	1,114.6	192.6	0.2
Saheart	0.3	15.5	5.9	1,816.4	–	0.2
Sonar	0.4	–	7.3	1,605.9	1,433.7	0.2
Soybean	0.1	0.0	0.9	236.1	19.4	0.2
Spectfheart	0.4	6.5	6.8	1,812.0	531.7	0.2
Spiral	0.1	–	5.5	1,626.3	91.5	0.2
Tae	0.5	–	1.9	797.8	83.3	0.2
Vehicle	0.4	92.7	16.9	1,847.4	–	0.2
Wine	0.4	0.1	3.7	1,027.0	63.1	0.2
Zoo	0.6	0.1	6.0	508.5	20.4	0.2
Sum	20.6	14,595.9*	151.4	34,704.9	15,573.0*	5.2

*Nan values (–) are replaced with 1,800 before computing the sum.

Table W14: Average running times (in seconds) of the PCCC algorithm and the four state-of-the-art algorithms (COPKM, CSC, DILS, LCC) for the constraint sets of size 15% CS. The lowest values are stated in bold. The column KMEANS reports the average running time of the unconstrained k-means algorithm. The hyphen indicates that the respective algorithm returned no solution within the time limit of 1,800 seconds.

Dataset	20% CS					KMEANS
	PCCC	COPKM	CSC	DILS	LCC	
Appendicitis	0.2	–	4.4	606.1	42.8	0.3
Breast Cancer	0.4	65.7	5.4	1,847.9	–	0.2
Bupa	0.2	11.4	3.5	1,811.6	5.5	0.2
Circles	0.3	6.3	4.9	1,807.2	–	0.3
Ecoli	0.7	–	7.3	1,806.4	1,360.9	0.2
Glass	0.4	–	1.7	1,239.5	1,018.3	0.2
Haberman	0.3	4.3	8.7	1,803.4	7.4	0.2
Hayesroth	0.1	–	6.4	865.3	68.4	0.2
Heart	0.2	4.3	7.2	1,810.7	6.2	0.3
Ionosphere	0.3	10.3	2.6	1,815.9	–	0.2
Iris	0.4	0.0	5.4	814.4	16.7	0.3
Led7Digit	2.3	–	5.0	1,826.6	1,843.0	0.3
Monk2	0.5	24.5	5.9	1,818.8	–	0.3
Moons	0.1	6.3	4.0	1,804.3	2.9	0.2
Movement Libras	10.0	–	6.1	1,815.9	1,850.7	0.3
Newthyroid	0.3	0.2	2.8	1,357.8	546.0	0.2
Saheart	0.4	28.1	6.2	1,817.4	–	0.2
Sonar	0.4	1.5	6.6	1,777.1	19.5	0.4
Soybean	0.4	0.0	2.2	243.8	29.0	0.3
Spectfheart	0.3	7.9	5.7	1,815.4	760.2	0.2
Spiral	0.5	–	4.8	1,811.0	7.5	0.2
Tae	0.3	–	5.9	835.5	693.2	0.2
Vehicle	0.4	157.0	14.0	1,840.1	–	0.4
Wine	0.4	0.1	6.5	1,115.9	658.8	0.2
Zoo	0.5	0.1	3.9	539.5	28.5	0.2
Sum	20.1	14,728.0*	137.2	36,647.4	19,765.6*	6.3

*Nan values (–) are replaced with 1,800 before computing the sum.

Table W15: Average running times (in seconds) of the PCCC algorithm and the four state-of-the-art algorithms (COPKM, CSC, DILS, LCC) for the constraint sets of size 20% CS. The lowest values are stated in bold. The column KMEANS reports the average running time of the unconstrained k-means algorithm. The hyphen indicates that the respective algorithm returned no solution within the time limit of 1,800 seconds.